Lansing dataset

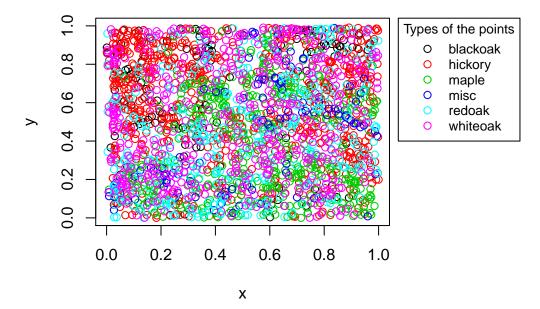
This vignette explains how to use the ppjsdm package with the Lansing dataset from spatstat. We begin by loading the data with all species.

```
data(lansing)
configuration <- as.Configuration(lansing)
window <- Rectangle_window(c(0, 1), c(0, 1))</pre>
```

The point configuration is plotted below.

```
par(mar = c(5, 4, 4, 13) + 0.1)
plot(configuration, window = window)
```

Points in the configuration

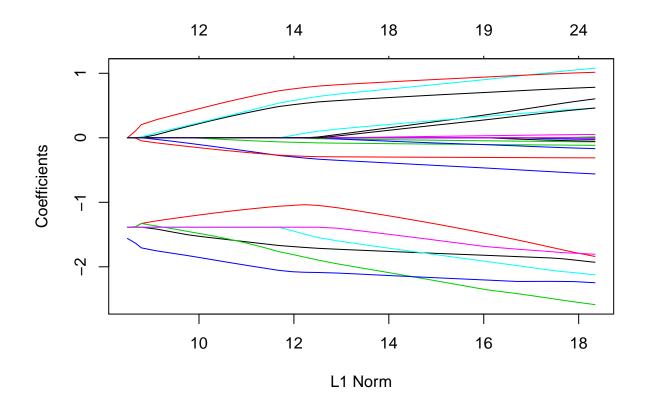


We fit the data with the Geyer model.

```
radii <- matrix(0.05, 6, 6)
```

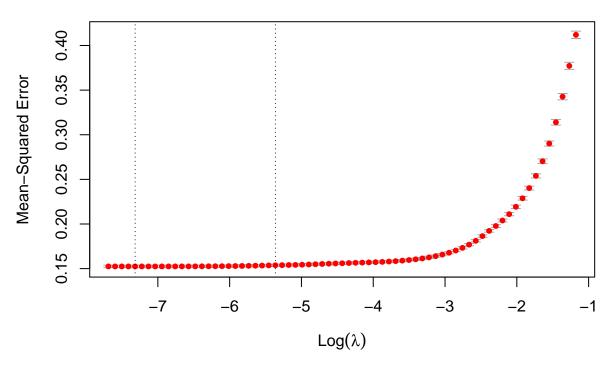
The matrix radii models interaction radii within a species, and between species.

```
fit <- ppjsdm::gibbsm(configuration,</pre>
                     window = window,
                     model = "Geyer",
                     radius = radii,
                     use_glmnet = TRUE)
#> 28 x 1 sparse Matrix of class "dgCMatrix"
#>
#> (Intercept)
#> log_lambda1 4.362448697
#> log_lambda2 6.102477812
#> log_lambda3 5.042221358
#> log_lambda4 3.967071845
#> log_lambda5 5.108543141
#> log_lambda6 5.684656013
#> alpha_1_1 0.783225895
#> alpha_1_2 -0.000340953
#> alpha_1_3 -0.116948070
#> alpha_1_4
             -0.560425485
#> alpha_1_5
              0.017151731
#> alpha_1_6
             0.011622290
#> alpha_2_2
             0.603679361
             -0.311224865
#> alpha_2_3
#> alpha_2_4
              -0.063374025
#> alpha_2_5
#> alpha_2_6
             -0.167808324
#> alpha_3_3
              1.079311454
#> alpha_3_4
              0.052032502
#> alpha_3_5
#> alpha_3_6
             -0.053830404
#> alpha_4_4
             1.015970724
#> alpha_4_5
              0.011096244
#> alpha_4_6
             -0.025865592
#> alpha_5_5
              0.460942997
#> alpha_5_6
              -0.014691249
#> alpha_6_6
              0.461365850
plot(fit$complete)
```



plot(fit\$cv)

21 20 20 19 19 17 13 11 8 8 8 9 9 6 4 3



```
print(coefficients(fit$complete))
#> 28 x 48 sparse Matrix of class "dgCMatrix"
                  [[ suppressing 48 column names 's0', 's1', 's2' ... ]]
#>
#> (Intercept)
#> shifted_log_lambda1 -1.386294 -1.386294361 -1.38629436 -1.41492719 -1.46074227
#> shifted_log_lambda2 -1.386294 -1.379903614 -1.32778795 -1.28835740 -1.25234431
#> shifted_log_lambda3 -1.386294 -1.377642454 -1.32838931 -1.36744917 -1.40886417
#> shifted_log_lambda4 -1.560648 -1.634949302 -1.70610755 -1.75202957 -1.79030805
 \texttt{\#>} \ shifted\_log\_lambda5 \ -1.386294 \ -1.386294361 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.386294436 \ -1.386294436 \ -1.386294436 \ -1.386294436 \ -1.386294436 \ -1.38629444 \ -1.3862
#> shifted_log_lambda6 -1.386294 -1.386294361 -1.38629436 -1.38629436 -1.38629436
#> alpha_1_1
                                                                                                                                                                                     0.04702823 0.11446758
#> alpha_1_2
#> alpha_1_3
                                                                                                                                                                                  -0.02401194 -0.05373081
#> alpha_1_4
#> alpha_1_5
#> alpha_1_6
#> alpha 2 2
                                                                                                     -0.005171702 -0.04645433 -0.07836064 -0.10761912
#> alpha_2_3
#> alpha_2_4
#> alpha_2_5
#> alpha_2_6
                                                                                                                                                0.01398425 0.07566664 0.13464475
#> alpha_3_3
#> alpha_3_4
#> alpha_3_5
#> alpha_3_6
```

```
#> alpha_4_4
                                                  0.108022019 0.20389894 0.28022920 0.34641722
#> alpha_4_5
#> alpha_4_6
#> alpha 5 5
#> alpha_5_6
#> alpha_6_6
#>
#> (Intercept)
#> shifted_log_lambda1 -1.50323910 -1.531540445 -1.55442019 -1.57592298
#> shifted_log_lambda2 -1.22025542 -1.192307925 -1.16703636 -1.14435630
#> shifted_log_lambda3 -1.45183381 -1.488956526 -1.52476136 -1.56172478
#> shifted_loq_lambda4 -1.82629422 -1.861069912 -1.89425877 -1.92548805
#> shifted_log_lambda5 -1.38629436 -1.386294361 -1.38629436 -1.38629436
#> shifted_log_lambda6 -1.38629436 -1.386294361 -1.38629436 -1.38629436
#> alpha_1_1
                                         0.17508274 0.227731574 0.27498369 0.31800745
#> alpha_1_2
#> alpha_1_3
                                                              -0.007630117 -0.01772626 -0.02711546
                                       . -0.007630117 -0.01772626 -0.02711546
-0.08278564 -0.110056043 -0.13591823 -0.16102463
#> alpha_1_4
#> alpha_1_5
#> alpha_1_6
#> alpha_2_2
                         .
-0.13395193 -0.157187983 -0.17827374 -0.19734404
#> alpha 2 3
#> alpha_2_4
#> alpha_2_5
#> alpha_2_6
                                         0.19049733 0.241315018 0.28910994 0.33463976
#> alpha 3 3
#> alpha_3_4
#> alpha_3_5
#> alpha_3_6
                                     #> alpha_4_4
#> alpha_4_5
#> alpha_4_6
#> alpha_5_5
#> alpha_5_6
#> alpha_6_6
#>
#> (Intercept)
#> shifted_log_lambda1 -1.59702842 -1.6164440 -1.63535263 -1.65276092 -1.66957559
#> shifted_log_lambda2 -1.12381537 -1.1055804 -1.08908984 -1.07434119 -1.06100493
#> shifted_log_lambda3 -1.60078120 -1.6405366 -1.68187802 -1.72301142 -1.76508842
#> shifted_log_lambda4 -1.95489480 -1.9824010 -2.00820701 -2.03229805 -2.05482721
#> shifted_log_lambda5 -1.38629436 -1.3862944 -1.38629436 -1.38629436 -1.38629436
 \texttt{\#>} \ shifted\_log\_lambda6 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629436 \ -1.38629440 \ -1.3862948 \ -1.3862948 \ -1.3862948 \ -1.3862948 \ -1.3862948 \ -1.3862948 \ -1.
#> alpha_1_2
                                  -0.03551999 -0.0434207 -0.05048857 -0.05712441 -0.06306811
#> alpha_1_3
                                        -0.18526840 -0.2087917 -0.23144026 -0.25329858 -0.27426085
#> alpha_1_4
#> alpha_1_5
#> alpha_1_6
#> alpha_2_2
                                    -0.21467838 -0.2302249 -0.24433189 -0.25705032 -0.26858555
#> alpha_2_3
#> alpha_2_4
#> alpha_2_5
```

```
#> alpha_2_6
#> alpha_3_3
                                                                   0.37867435 \quad 0.4206736 \quad 0.46139420 \quad 0.50012847 \quad 0.53764598
#> alpha 3 4
#> alpha 3 5
#> alpha_3_6
#> alpha_4_4
                                                             0.59591260 0.6336035 0.66815943 0.69983264 0.72891283
#> alpha_4_5
#> alpha_4_6
#> alpha 5 5
#> alpha_5_6
#> alpha_6_6
#>
#> (Intercept)
#> shifted_log_lambda1 -1.68504417 -1.699688611 -1.7134394468 -1.72723999
#> shifted_log_lambda2 -1.04901097 -1.036847387 -1.0484534492 -1.08293856
#> shifted_log_lambda3 -1.80625891 -1.849403517 -1.8956927793 -1.95289248
#> shifted_log_lambda4 -2.07581664 -2.084897888 -2.0882427405 -2.09659680
 \verb| #> shifted_log_lambda5   -1.43896935   -1.493854475   -1.5460267096   -1.59606889   | +1.5460267096   -1.59606889   | +1.5460267096   -1.5460267096   -1.59606889   | +1.5460267096   -1.5460267096   | +1.5460267096   | +1.5460267096   | +1.5460267096   | +1.5460267096   | +1.5460267096   | +1.5460267096   | +1.5460267096   | +1.5460267096   | +1.5460267096   | +1.5460267096   | +1.5460267096   | +1.5460267096   | +1.5460267096   | +1.5460267096   | +1.5460267096   | +1.5460267096   | +1.5460267096   | +1.5460267096   | +1.5460267096   | +1.5460267096   | +1.5460267096   | +1.5460267096   | +1.5460267096   | +1.5460267096   | +1.5460267096   | +1.5460267096   | +1.5460267096   | +1.5460267096   | +1.5460267096   | +1.5460267096   | +1.5460267096   | +1.5460267096   | +1.5460267096   | +1.5460267096   | +1.5460267096   | +1.5460267096   | +1.5460267096   | +1.5460267096   | +1.5460267096   | +1.5460267096   | +1.5460267096   | +1.5460267096   | +1.5460267096   | +1.5460267096   | +1.5460267096   | +1.5460267096   | +1.5460267096   | +1.5460267096   | +1.5460267096   | +1.5460267096   | +1.5460267096   | +1.5460267096   | +1.5460267096   | +1.5460267096   | +1.5460267096   | +1.5460267096   | +1.5460267096   | +1.5460267096   | +1.5460267096   | +1.5460267096   | +1.5460267096   | +1.5460267096   | +1.5460267096   | +1.5460267096   | +1.5460267096   | +1.5460267096   | +1.5460267096   | +1.5460267096   | +1.5460267096   | +1.5460267096   | +1.5460267096   | +1.5460267096   | +1.5460267096   | +1.5460267096   | +1.5460267096   | +1.5460267096   | +1.5460267096   | +1.5460267096   | +1.5460267096   | +1.5460267096   | +1.5460267096   | +1.5460267096   | +1.5460267096   | +1.5460267096   | +1.5460267096   | +1.5460267096   | +1.5460267096   | +1.5460267096   | +1.5460267096   | +1.5460267096   | +1.5460267096   | +1.5460267096   | +1.5460267096   | +1.5460267096   | +1.5460267096   | +1.5460267096   | +1.5460267096   | +1.5460267096   | +1.5460267096   | +1.5460267096   | +1.5460267096   | +1.5460267096   | +1.5
#> shifted_log_lambda6 -1.38629436 -1.386294361 -1.3862193032 -1.40134542
#> alpha_1_2
                                                        -0.06864520 -0.073845857 -0.0786719407 -0.08265822
#> alpha_1_3
                                                             -0.29438040 -0.313338271 -0.3312515847 -0.34839149
#> alpha_1_4
#> alpha_1_5
#> alpha_1_6
#> alpha 2 2
                                                                                                                                        0.0123862371 0.05024052
                                                     -0.27902539 -0.287205998 -0.2929565261 -0.29502627
#> alpha_2_3
#> alpha_2_4
                                                                                          -0.005875714 -0.0143560713 -0.01927741
#> alpha_2_5
#> alpha_2_6
                                                                                                                                      -0.0001015625 -0.01805297
                                                             0.57320420 0.607397887 0.6407418740 0.67615150
#> alpha_3_3
#> alpha_3_4
#> alpha_3_5
#> alpha_3_6
#> alpha_4_4
                                                          0.75560163 0.779549950 0.8013893396 0.82170428
#> alpha_4_5
#> alpha_4_6
                                                            0.03445016 0.069570210 0.1026493613 0.13405989
#> alpha 5 5
#> alpha_5_6
                                                                                                                                                                               0.02720445
#> alpha_6_6
#> (Intercept)
#> shifted_loq_lambda1 -1.74051047 -1.752998968 -1.76451577 -1.77523768
#> shifted_log_lambda2 -1.13003194 -1.176633649 -1.22129446 -1.26567003
#> shifted_log_lambda3 -2.00563493 -2.055339974 -2.10224853 -2.14712824
#> shifted_log_lambda4 -2.11102724 -2.125448553 -2.13871969 -2.15110979
#> shifted_log_lambda5 -1.64079670 -1.682388235 -1.72107667 -1.75707746
 \verb| #> shifted_log_lambda6   -1.43593706   -1.470986574   -1.50449175   -1.53665950   | +1.50449175   -1.53665950   | +1.50449175   -1.53665950   | +1.50449175   -1.53665950   | +1.50449175   -1.53665950   | +1.50449175   -1.53665950   | +1.50449175   -1.53665950   | +1.50449175   -1.53665950   | +1.50449175   -1.53665950   | +1.50449175   -1.53665950   | +1.50449175   -1.53665950   | +1.50449175   -1.53665950   | +1.50449175   -1.53665950   | +1.50449175   -1.53665950   | +1.50449175   -1.53665950   | +1.50449175   -1.50449175   -1.50449175   -1.50449175   | +1.50449175   -1.50449175   | +1.50449175   -1.50449175   | +1.50449175   | +1.50449175   | +1.50449175   | +1.50449175   | +1.50449175   | +1.50449175   | +1.50449175   | +1.50449175   | +1.50449175   | +1.50449175   | +1.50449175   | +1.50449175   | +1.50449175   | +1.50449175   | +1.50449175   | +1.50449175   | +1.50449175   | +1.50449175   | +1.50449175   | +1.50449175   | +1.50449175   | +1.50449175   | +1.50449175   | +1.50449175   | +1.50449175   | +1.50449175   | +1.50449175   | +1.50449175   | +1.50449175   | +1.50449175   | +1.50449175   | +1.50449175   | +1.50449175   | +1.50449175   | +1.50449175   | +1.50449175   | +1.50449175   | +1.50449175   | +1.50449175   | +1.50449175   | +1.50449175   | +1.50449175   | +1.50449175   | +1.50449175   | +1.50449175   | +1.50449175   | +1.50449175   | +1.50449175   | +1.50449175   | +1.50449175   | +1.50449175   | +1.50449175   | +1.50449175   | +1.50449175   | +1.50449175   | +1.50449175   | +1.50449175   | +1.50449175   | +1.50449175   | +1.50449175   | +1.50449175   | +1.50449175   | +1.50449175   | +1.50449175   | +1.50449175   | +1.50449175   | +1.50449175   | +1.50449175   | +1.50449175   | +1.50449175   | +1.50449175   | +1.50449175   | +1.50449175   | +1.50449175   | +1.50449175   | +1.50449175   | +1.50449175   | +1.50449175   | +1.50449175   | +1.50449175   | +1.50449175   | +1.50449175   | +1.50449175   | +1.50449175   | +1.50449175   | +1.50449175   | +1.50449175   | +1.50449175   | +1.5044917
#> alpha_1_2
                                                -0.08588385 -0.088755545 -0.09142383 -0.09384665
-0.36439359 -0.379481587 -0.39374704 -0.40720185
#> alpha_1_3
#> alpha_1_4
                                                              -0.36439359 -0.379481587 -0.39374704 -0.40720185
#> alpha_1_5
```

```
#> alpha_1_6
#> alpha_2_2
                    0.09001672 0.127911059 0.16356059 0.19770933
#> alpha 2 3
                   -0.29655341 -0.297928387 -0.29921276 -0.30031654
                   -0.02322887 -0.026849805 -0.03021460 -0.03326071
#> alpha 2 4
#> alpha 2 5
#> alpha_2_6
                   -0.03174078 -0.044003718 -0.05518960 -0.06521858
#> alpha_3_3
                   0.70674611 0.735144076 0.76186569 0.78721989
                   0.00418853 0.008655218 0.01271541 0.01644541
#> alpha_3_4
#> alpha 3 5
#> alpha_3_6
#> alpha_4_4
                   0.83930089 0.855393707 0.87019454 0.88379705
#> alpha_4_5
#> alpha_4_6
                    #> alpha_5_5
#> alpha_5_6
#> alpha_6_6
                    #> (Intercept)
#> shifted_log_lambda1 -1.78511204 -1.79423492 -1.80271993 -1.81050267 -1.81767134
#> shifted_log_lambda2 -1.30793651 -1.34857939 -1.38873352 -1.42655634 -1.46251186
#> shifted_log_lambda3 -2.18935980 -2.22924153 -2.26727193 -2.30277174 -2.33607263
\#> shifted_log_lambda4 -2.16249370 -2.17300469 -2.18282103 -2.19180940 -2.20008385
#> shifted_log_lambda5 -1.79047488 -1.82144437 -1.85017948 -1.87672575 -1.90125851
 \texttt{\#>} \ \textit{shifted\_log\_lambda6} \ -1.56714182 \ -1.59599301 \ -1.62350024 \ -1.64933176 \ -1.67356891 
                   0.65509156  0.66721047  0.67833571  0.68852172  0.69785306
#> alpha_1_1
#> alpha 1 2
                  -0.09609094 -0.09815071 -0.10000842 -0.10173169 -0.10331199
#> alpha_1_3
#> alpha_1_4
                   -0.41986435 -0.43175425 -0.44289538 -0.45331497 -0.46304079
#> alpha_1_5
#> alpha_1_6
#> alpha_2_2
                   0.22976666 0.26001312 0.28898778 0.31603876 0.34142537
                   -0.30134675 -0.30227802 -0.30306037 -0.30379745 -0.30446603
#> alpha_2_3
#> alpha_2_4
                   -0.03608619 -0.03868177 -0.04101281 -0.04317361 -0.04515684
#> alpha_2_5
#> alpha_2_6
                  -0.07437402 -0.08268773 -0.09012861 -0.09693251 -0.10312403
                   0.81102001 0.83340252 0.85457944 0.87432758 0.89279822
#> alpha_3_3
                    #> alpha_3_4
#> alpha 3 5
#> alpha_3_6
                    0.89629569 0.90777467 0.91830975 0.92797813 0.93684644
#> alpha_4_4
#> alpha_4_5
#> alpha_4_6
                    #> alpha_5_5
#> alpha_5_6
                    #> alpha_6_6
#>
#> (Intercept)
#> shifted_log_lambda1 -1.824378428 -1.830612693 -1.83645436 -1.8417227929
\#> shifted_log_lambda2 -1.495969417 -1.525936446 -1.55590437 -1.5828159876
#> shifted_log_lambda3 -2.362756873 -2.380984221 -2.39919120 -2.4154661275
#> shifted_log_lambda4 -2.207774614 -2.214825772 -2.22147429 -2.2272966480
#> shifted_log_lambda6 -1.692322354 -1.704329623 -1.71586980 -1.7264012314
```

```
#> alpha_1_1
               0.706420771 0.714273538 0.72148732 0.7280641804
#> alpha_1_2
#> alpha 1 3
                     -0.104686551 -0.105880371 -0.10691818 -0.1079136795
#> alpha 1 4
                     -0.472113215 -0.480570637 -0.48842465 -0.4957083508
#> alpha_1_5
#> alpha_1_6
#> alpha_2_2
                      -0.305114677 -0.305815129 -0.30636283 -0.3069339669
#> alpha_2_3
#> alpha_2_4
                     -0.046947783 -0.048596999 -0.05004025 -0.0514147380
#> alpha_2_5
                    -0.109143527 -0.115093609 -0.12043323 -0.1253648897
#> alpha_2_6
#> alpha_3_3
                    0.910085926 0.926074309 0.94127780 0.9551291844
                     0.032928903 0.034925012 0.03678563 0.0384505374
#> alpha_3_4
#> alpha_3_5
                   -0.002641043 -0.008970064 -0.01465657 -0.0199259149
#> alpha_3_6
#> alpha_4_4
                     0.944973566 0.952415505 0.95922834 0.9654705170
#> alpha_4_5
#> alpha_4_6
                                                         -0.0001235012
#> alpha_5_5
                    0.336883059 0.349521876 0.36122406 0.3718893953
#> alpha_5_6
                 0.286195343 0.303638919 0.31969756 0.3344838648
#> alpha_6_6
#> (Intercept)
#> shifted_log_lambda1 -1.846604276 -1.851019852 -1.85518987 -1.85881765
#> shifted_log_lambda2 -1.608073073 -1.630891165 -1.65395516 -1.67314120
#> shifted_log_lambda3 -2.432305929 -2.447419360 -2.46263680 -2.47518621
#> shifted_log_lambda4 -2.226802481 -2.226517687 -2.22641442 -2.22612218
#> shifted_log_lambda5 -1.997951870 -2.012788813 -2.02665816 -2.03895010
#> shifted_log_lambda6 -1.735059107 -1.742807381 -1.75051011 -1.75709925
#> alpha_1_1
                      0.734098510 0.739600323 0.74465999 0.74923506
#> alpha_1_2
                     -0.108826854 -0.109689326 -0.11041960 -0.11117679
#> alpha_1_3
#> alpha_1_4
                     -0.502370830 -0.508537935 -0.51423243 -0.51949390
#> alpha_1_5
#> alpha_1_6
                    0.445355087 0.461708699 0.47766007 0.49135837
#> alpha_2_2
#> alpha_2_3
                     -0.307390993 -0.307854718 -0.30818634 -0.30861860
#> alpha_2_4
                    -0.052712435 -0.053932459 -0.05498330 -0.05603740
#> alpha_2_5
#> alpha_2_6
                     -0.130133550 -0.134507176 -0.13843150 -0.14204601
                    0.968077228 0.979900242 0.99121255 1.00111082
#> alpha_3_3
#> alpha_3_4
                    0.039990972 0.041375244 0.04267971 0.04380568
#> alpha_3_5
                     -0.023996316 -0.027805812 -0.03117735 -0.03437332
#> alpha_3_6
#> alpha_4_4
                    0.971102428 0.976262867 0.98098064 0.98529784
#> alpha_4_5
                   -0.003502447 -0.006505082 -0.00927081 -0.01175979
#> alpha_4_6
                     0.381721726 0.390675883 0.39901576 0.40643044
#> alpha_5_5
#> alpha_5_6
                    #> alpha_6_6
#>
#> (Intercept)
\#> shifted_log_lambda1 -1.86238814 -1.867616888 -1.872845866 -1.8787357819
```

```
#> shifted_log_lambda2 -1.69394387 -1.711605579 -1.728123636 -1.7446792255
#> shifted_log_lambda3 -2.48889868 -2.500635733 -2.511689181 -2.5228444784
#> shifted_log_lambda4 -2.22612185 -2.226430573 -2.226985575 -2.2277795412
#> shifted log lambda5 -2.05081513 -2.061259141 -2.070927086 -2.0773207026
#> shifted_log_lambda6 -1.76392328 -1.770851919 -1.777808352 -1.7820704507
                       0.75347894 0.757318626 0.760811746 0.7640470653
#> alpha_1_1
#> alpha_1_2
                     -0.11175414 -0.112325190 -0.112888592 -0.1133825879
#> alpha_1_3
#> alpha_1_4
                      -0.52433484 -0.528850176 -0.533021692 -0.5368835267
#> alpha_1_5
                                                              0.0008420666
#> alpha_1_6
                                    #> alpha_2_2
                      0.50543080 0.517683447 0.529055819 0.5401259533
                    0.50543080 0.517683447 0.529055819 0.5401259533
-0.30884806 -0.309252620 -0.309518093 -0.3096910324
-0.05688561 -0.057739536 -0.058497916 -0.0591433633
#> alpha_2_3
#> alpha_2_4
#> alpha_2_5
                     -0.14532362 -0.148300249 -0.151074825 -0.1535820483
#> alpha_2_6
#> alpha_3_3
                       1.01096961 1.019651444 1.027655523 1.0353079325
                      0.04491434 0.045870576 0.046743827 0.0475653975
#> alpha_3_4
#> alpha_3_5
#> alpha_3_6
                     -0.03714688 -0.039546585 -0.041719577 -0.0435612086
                      0.98924418 0.992818582 0.996112618 0.9991248705
#> alpha_4_4
#> alpha_4_5
#> alpha_4_6
                     -0.01408797 -0.015837963 -0.017345733 -0.0186357642
                      0.41353395 0.419811567 0.425609737 0.4309643342
#> alpha_5_5
#> alpha_5_6
                                                             -0.0018408448
#> alpha_6_6
                      0.39232929 0.400933832 0.409027705 0.4166265049
#>
#> (Intercept)
#> shifted_log_lambda1 -1.885936265 -1.892767725 -1.899569765 -1.905941766
#> shifted_log_lambda2 -1.758682679 -1.772711404 -1.785488449 -1.797051081
#> shifted_log_lambda3 -2.532194063 -2.541600235 -2.550069692 -2.557705439
#> shifted_log_lambda4 -2.228353182 -2.229012596 -2.232083489 -2.235328238
\#> shifted_log_lambda5 -2.083256080 -2.089268446 -2.095553697 -2.101478755
#> shifted_log_lambda6 -1.785195655 -1.788477264 -1.791483364 -1.794251286
#> alpha_1_1 0.767009588 0.769750311 0.772255810 0.774542762
#> alpha_1_2
                     -0.113923852 -0.114371844 -0.114810895 -0.115223723
#> alpha_1_3
#> alpha_1_4
                     -0.540492888 -0.543800878 -0.546820338 -0.549594895
                      0.002922982 0.004860086 0.007079018 0.009198880
#> alpha_1_5
                      0.005218783 0.006297844 0.007260814 0.008155911
#> alpha_1_6
                      0.549666292 0.559021269 0.567503178 0.575195346
#> alpha_2_2
                    -0.309929733 -0.310078334 -0.310232286 -0.310385821
-0.059788223 -0.060330721 -0.060841231 -0.061316731
#> alpha_2_3
#> alpha_2_4
#> alpha_2_5
                       -0.155829574 -0.157934765 -0.159800229 -0.161498603
#> alpha_2_6
#> alpha_3_3
                       1.041968730 1.048402848 1.054215640 1.059490481
#> alpha_3_4
                      0.048264840 0.048936344 0.049526556 0.050055399
#> alpha_3_5
#> alpha_3_6
                     -0.045239569 -0.046759744 -0.048114091 -0.049354936
                      1.001855415 1.004360075 1.006527696 1.008476129
#> alpha_4_4
                                                  0.001880328 0.003790177
#> alpha_4_5
#> alpha_4_6
                       -0.019764611 -0.020814965 -0.021821380 -0.022677175
                       0.435755777 0.440408465 0.444281710 0.447815414
#> alpha_5_5
```

```
#> alpha_5_6
                     -0.003948522 -0.005849693 -0.007573185 -0.009143491
#> alpha_6_6
                      #> (Intercept)
#> shifted_log_lambda1 -1.911745495 -1.917023410 -1.921820113 -1.926919075
#> shifted_log_lambda2 -1.807483670 -1.816855825 -1.825219587 -1.834430916
#> shifted_log_lambda3 -2.564604886 -2.570831251 -2.576427071 -2.582751764
#> shifted_log_lambda4 -2.238275715 -2.240948527 -2.243370525 -2.245983272
#> shifted_log_lambda5 -2.106912316 -2.111859643 -2.116347579 -2.121197017
#> shifted_log_lambda6 -1.796806035 -1.799171588 -1.801377525 -1.804586315
                    0.776625533 0.778521249 0.780245297 0.781913873
#> alpha_1_1
#> alpha_1_2
                     -0.115606879 -0.115962349 -0.116292738 -0.116506599
#> alpha_1_3
#> alpha_1_4
                     -0.552139564 -0.554471853 -0.556608607 -0.558546512
#> alpha_1_5
                    0.011131911 0.012890703 0.014489169 0.016064162
#> alpha_1_6
                    0.008973830 0.009721682 0.010407233 0.011158276
#> alpha_2_2
                     #> alpha_2_3
                     -0.310538365 -0.310691181 -0.310846796 -0.310966761
                    -0.061759243 -0.062171817 -0.062557846 -0.062844403
#> alpha_2_4
#> alpha_2_5
                     -0.163048720 -0.164461856 -0.165747785 -0.166958786
#> alpha 2 6
#> alpha 3 3
                     1.064279699 1.068620466 1.072541658 1.076581438
#> alpha_3_4
                     0.050533071 0.050964758 0.051354514 0.051752064
#> alpha_3_5
                   -0.050486418 -0.051512793 -0.052439173 -0.053174177
#> alpha_3_6
#> alpha_4_4
                    1.010253431 1.011875662 1.013356399 1.014718795
#> alpha_4_5
                    0.005533964 0.007123607 0.008572216 0.009966875
#> alpha_4_6
                   -0.023455194 -0.024162290 -0.024803478 -0.025367772
                     0.451032864 0.453947674 0.456576214 0.459252303
#> alpha_5_5
                     -0.010556773 -0.011830151 -0.012973133 -0.013951988
#> alpha_5_6
#> alpha_6_6
                     0.445860934 0.450270301 0.454289454 0.458427694
#>
#> (Intercept)
#> shifted_log_lambda1 -1.929120443
#> shifted_log_lambda2 -1.839173441
#> shifted_log_lambda3 -2.586296269
#> shifted_log_lambda4 -2.247536254
#> shifted_log_lambda5 -2.124189995
#> shifted_log_lambda6 -1.806431580
#> alpha_1_1
                     0.783225895
                     -0.000340953
#> alpha_1_2
#> alpha_1_3
                    -0.116948070
#> alpha_1_4
                     -0.560425485
#> alpha_1_5
                     0.017151731
#> alpha_1_6
                     0.011622290
#> alpha_2_2
                     0.603679361
#> alpha_2_3
                     -0.311224865
                     -0.063374025
#> alpha_2_4
#> alpha_2_5
#> alpha_2_6
                     -0.167808324
#> alpha_3_3
                     1.079311454
#> alpha_3_4
                      0.052032502
#> alpha_3_5
```