

Foundation of Cryptography, Lecture 8

Secure Multiparty Computation

Iftach Haitner, Tel Aviv University

Tel Aviv University.

May 20, 2014

Section 1

The Model

Multiparty Computation

- Multiparty Computation – computing a functionality f

Multiparty Computation

- Multiparty Computation – computing a functionality f
- Secure Multiparty Computation: compute f in a “secure manner”

Multiparty Computation

- Multiparty Computation – computing a functionality f
- Secure Multiparty Computation: compute f in a “secure manner”
 - ▶ Correctness

Multiparty Computation

- Multiparty Computation – computing a functionality f
- Secure Multiparty Computation: compute f in a “secure manner”
 - ▶ Correctness
 - ▶ Privacy

Multiparty Computation

- Multiparty Computation – computing a functionality f
- Secure Multiparty Computation: compute f in a “secure manner”
 - ▶ Correctness
 - ▶ Privacy
 - ▶ Independence of inputs

Multiparty Computation

- Multiparty Computation – computing a functionality f
- Secure Multiparty Computation: compute f in a “secure manner”
 - ▶ Correctness
 - ▶ Privacy
 - ▶ Independence of inputs
 - ▶ Guaranteed output delivery

Multiparty Computation

- Multiparty Computation – computing a functionality f
- Secure Multiparty Computation: compute f in a “secure manner”
 - ▶ Correctness
 - ▶ Privacy
 - ▶ Independence of inputs
 - ▶ Guaranteed output delivery
 - ▶ Fairness : corrupted parties should get their output iff the honest parties do

Multiparty Computation

- Multiparty Computation – computing a functionality f
- Secure Multiparty Computation: compute f in a “secure manner”
 - ▶ Correctness
 - ▶ Privacy
 - ▶ Independence of inputs
 - ▶ Guaranteed output delivery
 - ▶ Fairness : corrupted parties should get their output iff the honest parties do
 - ▶ and ...

Multiparty Computation

- Multiparty Computation – computing a functionality f
- Secure Multiparty Computation: compute f in a “secure manner”
 - ▶ Correctness
 - ▶ Privacy
 - ▶ Independence of inputs
 - ▶ Guaranteed output delivery
 - ▶ Fairness : corrupted parties should get their output iff the honest parties do
 - ▶ and ...
- Examples: coin-tossing, broadcast, electronic voting, electronic auctions

Multiparty Computation

- Multiparty Computation – computing a functionality f
- Secure Multiparty Computation: compute f in a “secure manner”
 - ▶ Correctness
 - ▶ Privacy
 - ▶ Independence of inputs
 - ▶ Guaranteed output delivery
 - ▶ Fairness : corrupted parties should get their output iff the honest parties do
 - ▶ and ...
- Examples: coin-tossing, broadcast, electronic voting, electronic auctions
- How should we model it?

Multiparty Computation

- Multiparty Computation – computing a functionality f
- Secure Multiparty Computation: compute f in a “secure manner”
 - ▶ Correctness
 - ▶ Privacy
 - ▶ Independence of inputs
 - ▶ Guaranteed output delivery
 - ▶ Fairness : corrupted parties should get their output iff the honest parties do
 - ▶ and ...
- Examples: coin-tossing, broadcast, electronic voting, electronic auctions
- How should we model it?
- Real Vs. Ideal paradigm

Real Model Execution

For a pair of algorithms $\bar{A} = (A_1, A_2)$ and inputs $x_c, x_1, x_2 \in \{0, 1\}^*$, let $\text{REAL}_{\bar{A}}(x_c, x_1, x_2)$ be the joint output of $(A_1(x_c, x_1), A_2(x_c, x_2))$.

Real Model Execution

For a pair of algorithms $\bar{A} = (A_1, A_2)$ and inputs $x_c, x_1, x_2 \in \{0, 1\}^*$, let $\text{REAL}_{\bar{A}}(x_c, x_1, x_2)$ be the joint output of $(A_1(x_c, x_1), A_2(x_c, x_2))$.

Given a two-party protocol π , an algorithm taking the role of one of the parties in π is:

Real Model Execution

For a pair of algorithms $\bar{A} = (A_1, A_2)$ and inputs $x_c, x_1, x_2 \in \{0, 1\}^*$, let $\text{REAL}_{\bar{A}}(x_c, x_1, x_2)$ be the joint output of $(A_1(x_c, x_1), A_2(x_c, x_2))$.

Given a two-party protocol π , an algorithm taking the role of one of the parties in π is:

- **Malicious** — acts arbitrarily.

Real Model Execution

For a pair of algorithms $\bar{A} = (A_1, A_2)$ and inputs $x_c, x_1, x_2 \in \{0, 1\}^*$, let $\text{REAL}_{\bar{A}}(x_c, x_1, x_2)$ be the joint output of $(A_1(x_c, x_1), A_2(x_c, x_2))$.

Given a two-party protocol π , an algorithm taking the role of one of the parties in π is:

- **Malicious** — acts arbitrarily.
- **Honest** — acts exactly according to π .

Real Model Execution

For a pair of algorithms $\bar{A} = (A_1, A_2)$ and inputs $x_c, x_1, x_2 \in \{0, 1\}^*$, let $\text{REAL}_{\bar{A}}(x_c, x_1, x_2)$ be the **joint** output of $(A_1(x_c, x_1), A_2(x_c, x_2))$.

Given a two-party protocol π , an algorithm taking the role of one of the parties in π is:

- **Malicious** — acts **arbitrarily**.
- **Honest** — acts **exactly** according to π .
- **Semi-honest** — acts according to π , but might output **additional information**.

Real Model Execution

For a pair of algorithms $\bar{A} = (A_1, A_2)$ and inputs $x_c, x_1, x_2 \in \{0, 1\}^*$, let $\text{REAL}_{\bar{A}}(x_c, x_1, x_2)$ be the **joint** output of $(A_1(x_c, x_1), A_2(x_c, x_2))$.

Given a two-party protocol π , an algorithm taking the role of one of the parties in π is:

- **Malicious** — acts **arbitrarily**.
- **Honest** — acts **exactly** according to π .
- **Semi-honest** — acts according to π , but might output **additional information**.

Real Model Execution

For a pair of algorithms $\bar{A} = (A_1, A_2)$ and inputs $x_c, x_1, x_2 \in \{0, 1\}^*$, let $\text{REAL}_{\bar{A}}(x_c, x_1, x_2)$ be the **joint** output of $(A_1(x_c, x_1), A_2(x_c, x_2))$.

Given a two-party protocol π , an algorithm taking the role of one of the parties in π is:

- **Malicious** — acts **arbitrarily**.
- **Honest** — acts **exactly** according to π .
- **Semi-honest** — acts according to π , but might output **additional information**.

$\bar{A} = (A_1, A_2)$ is an **admissible** with respect to π , if at least one party is honest.

Ideal Model Execution

Ideal Model Execution

For a pair of oracle-aided algorithms $\overline{B} = (B_1, B_2)$, inputs $x_c, x_1, x_2 \in \{0, 1\}^*$ and a function $f = (f_1, f_2)$, let $\text{IDEAL}_{\overline{B}}^f(x_c, x_1, x_2)$ be the joint output of the parties in the end of the following experiment:

Ideal Model Execution

For a pair of oracle-aided algorithms $\overline{B} = (B_1, B_2)$, inputs $x_c, x_1, x_2 \in \{0, 1\}^*$ and a function $f = (f_1, f_2)$, let $\text{IDEAL}_{\overline{B}}^f(x_c, x_1, x_2)$ be the joint output of the parties in the end of the following experiment:

- 1 The input of B_i is (x_c, x_i) .
- 2 B_i sends value y_i to the trusted party (possibly \perp)
- 3 Trusted party sends $z_i = f_i(y_0, y_1)$ to B_i (sends \perp , if $\perp \in \{y_0, y_1\}$)
- 4 Each party outputs some value.

Ideal Model Execution

For a pair of oracle-aided algorithms $\overline{B} = (B_1, B_2)$, inputs $x_c, x_1, x_2 \in \{0, 1\}^*$ and a function $f = (f_1, f_2)$, let $\text{IDEAL}_{\overline{B}}^f(x_c, x_1, x_2)$ be the joint output of the parties in the end of the following experiment:

- 1 The input of B_i is (x_c, x_i) .
- 2 B_i sends value y_i to the trusted party (possibly \perp)
- 3 Trusted party sends $z_i = f_i(y_0, y_1)$ to B_i (sends \perp , if $\perp \in \{y_0, y_1\}$)
- 4 Each party outputs some value.

An oracle-aided algorithm B taking the role of one of the parties on the above experiment is:

Ideal Model Execution

For a pair of oracle-aided algorithms $\overline{B} = (B_1, B_2)$, inputs $x_c, x_1, x_2 \in \{0, 1\}^*$ and a function $f = (f_1, f_2)$, let $\text{IDEAL}_{\overline{B}}^f(x_c, x_1, x_2)$ be the joint output of the parties in the end of the following experiment:

- 1 The input of B_i is (x_c, x_i) .
- 2 B_i sends value y_i to the trusted party (possibly \perp)
- 3 Trusted party sends $z_i = f_i(y_0, y_1)$ to B_i (sends \perp , if $\perp \in \{y_0, y_1\}$)
- 4 Each party outputs some value.

An oracle-aided algorithm B taking the role of one of the parties on the above experiment is:

- **Malicious** — acts arbitrarily.

Ideal Model Execution

For a pair of oracle-aided algorithms $\bar{B} = (B_1, B_2)$, inputs $x_c, x_1, x_2 \in \{0, 1\}^*$ and a function $f = (f_1, f_2)$, let $\text{IDEAL}_{\bar{B}}^f(x_c, x_1, x_2)$ be the joint output of the parties in the end of the following experiment:

- 1 The input of B_i is (x_c, x_i) .
- 2 B_i sends value y_i to the trusted party (possibly \perp)
- 3 Trusted party sends $z_i = f_i(y_0, y_1)$ to B_i (sends \perp , if $\perp \in \{y_0, y_1\}$)
- 4 Each party outputs some value.

An oracle-aided algorithm B taking the role of one of the parties on the above experiment is:

- **Malicious** — acts arbitrarily.
- **Honest** — sends its private input to the trusted party (i.e., sets $y_i = x_i$), and its only output is the value it gets from the trusted party (i.e., z_i).

Ideal Model Execution

For a pair of oracle-aided algorithms $\bar{B} = (B_1, B_2)$, inputs $x_c, x_1, x_2 \in \{0, 1\}^*$ and a function $f = (f_1, f_2)$, let $\text{IDEAL}_{\bar{B}}^f(x_c, x_1, x_2)$ be the joint output of the parties in the end of the following experiment:

- 1 The input of B_i is (x_c, x_i) .
- 2 B_i sends value y_i to the trusted party (possibly \perp)
- 3 Trusted party sends $z_i = f_i(y_0, y_1)$ to B_i (sends \perp , if $\perp \in \{y_0, y_1\}$)
- 4 Each party outputs some value.

An oracle-aided algorithm B taking the role of one of the parties on the above experiment is:

- **Malicious** — acts arbitrarily.
- **Honest** — sends its private input to the trusted party (i.e., sets $y_i = x_i$), and its only output is the value it gets from the trusted party (i.e., z_i).
- **Semi-honest**, sends its input to the trusted party, outputs z_i plus possibly additional information.

Ideal Model Execution

For a pair of oracle-aided algorithms $\bar{B} = (B_1, B_2)$, inputs $x_c, x_1, x_2 \in \{0, 1\}^*$ and a function $f = (f_1, f_2)$, let $\text{IDEAL}_{\bar{B}}^f(x_c, x_1, x_2)$ be the joint output of the parties in the end of the following experiment:

- 1 The input of B_i is (x_c, x_i) .
- 2 B_i sends value y_i to the trusted party (possibly \perp)
- 3 Trusted party sends $z_i = f_i(y_0, y_1)$ to B_i (sends \perp , if $\perp \in \{y_0, y_1\}$)
- 4 Each party outputs some value.

An oracle-aided algorithm B taking the role of one of the parties on the above experiment is:

- **Malicious** — acts arbitrarily.
- **Honest** — sends its private input to the trusted party (i.e., sets $y_i = x_i$), and its only output is the value it gets from the trusted party (i.e., z_i).
- **Semi-honest**, sends its input to the trusted party, outputs z_i plus possibly additional information.

Ideal Model Execution

For a pair of oracle-aided algorithms $\bar{B} = (B_1, B_2)$, inputs $x_c, x_1, x_2 \in \{0, 1\}^*$ and a function $f = (f_1, f_2)$, let $\text{IDEAL}_{\bar{B}}^f(x_c, x_1, x_2)$ be the joint output of the parties in the end of the following experiment:

- 1 The input of B_i is (x_c, x_i) .
- 2 B_i sends value y_i to the trusted party (possibly \perp)
- 3 Trusted party sends $z_i = f_i(y_0, y_1)$ to B_i (sends \perp , if $\perp \in \{y_0, y_1\}$)
- 4 Each party outputs some value.

An oracle-aided algorithm B taking the role of one of the parties on the above experiment is:

- **Malicious** — acts arbitrarily.
- **Honest** — sends its private input to the trusted party (i.e., sets $y_i = x_i$), and its only output is the value it gets from the trusted party (i.e., z_i).
- **Semi-honest**, sends its input to the trusted party, outputs z_i plus possibly additional information.

$\bar{B} = (B_1, B_2)$ is **admissible**, if at least one party is honest.

Secure computation

Definition 1 (secure computation)

A protocol π **securely computes** f , if \forall admissible PPT pair $\bar{A} = (A_1, A_2)$ for π , exists admissible oracle-aided PPT pair $\bar{B} = (B_1, B_2)$, s.t.

$$\{\text{REAL}_{\bar{A}}(1^n, x_1, x_2)\}_{x_c, x_1, x_2 \in \{0,1\}^*} \approx_c \{\text{IDEAL}_{\bar{B}}^f(x_1, x_2)\}_{x_c, x_1, x_2 \in \{0,1\}^*}$$

Secure computation

Definition 1 (secure computation)

A protocol π **securely computes** f , if \forall admissible PPT pair $\bar{A} = (A_1, A_2)$ for π , exists admissible oracle-aided PPT pair $\bar{B} = (B_1, B_2)$, s.t.

$$\{\text{REAL}_{\bar{A}}(1^n, x_1, x_2)\}_{x_c, x_1, x_2 \in \{0,1\}^*} \approx_c \{\text{IDEAL}_{\bar{B}}^f(x_1, x_2)\}_{x_c, x_1, x_2 \in \{0,1\}^*}$$

- Recall that the enumeration index (i.e., x_c, x_1, x_2) is given to the distinguisher.

Secure computation

Definition 1 (secure computation)

A protocol π securely computes f , if \forall admissible PPT pair $\bar{A} = (A_1, A_2)$ for π , exists admissible oracle-aided PPT pair $\bar{B} = (B_1, B_2)$, s.t.

$$\{\text{REAL}_{\bar{A}}(1^n, x_1, x_2)\}_{x_c, x_1, x_2 \in \{0,1\}^*} \approx_c \{\text{IDEAL}_{\bar{B}}^f(x_1, x_2)\}_{x_c, x_1, x_2 \in \{0,1\}^*}$$

- Recall that the enumeration index (i.e., x_c, x_1, x_2) is given to the distinguisher.
- π securely computes f implies that π computes f correctly.

Secure computation

Definition 1 (secure computation)

A protocol π **securely computes** f , if \forall admissible PPT pair $\bar{A} = (A_1, A_2)$ for π , exists admissible oracle-aided PPT pair $\bar{B} = (B_1, B_2)$, s.t.

$$\{\text{REAL}_{\bar{A}}(1^n, x_1, x_2)\}_{x_c, x_1, x_2 \in \{0,1\}^*} \approx_c \{\text{IDEAL}_{\bar{B}}^f(x_1, x_2)\}_{x_c, x_1, x_2 \in \{0,1\}^*}$$

- Recall that the enumeration index (i.e., x_c, x_1, x_2) is given to the distinguisher.
- π securely computes f implies that π computes f **correctly**.
- Security parameter

Secure computation

Definition 1 (secure computation)

A protocol π **securely computes** f , if \forall admissible PPT pair $\bar{A} = (A_1, A_2)$ for π , exists admissible oracle-aided PPT pair $\bar{B} = (B_1, B_2)$, s.t.

$$\{\text{REAL}_{\bar{A}}(1^n, x_1, x_2)\}_{x_c, x_1, x_2 \in \{0,1\}^*} \approx_c \{\text{IDEAL}_{\bar{B}}^f(x_1, x_2)\}_{x_c, x_1, x_2 \in \{0,1\}^*}$$

- Recall that the enumeration index (i.e., x_c, x_1, x_2) is given to the distinguisher.
- π securely computes f implies that π computes f **correctly**.
- Security parameter
- Auxiliary inputs

Secure computation

Definition 1 (secure computation)

A protocol π **securely computes** f , if \forall admissible PPT pair $\bar{A} = (A_1, A_2)$ for π , exists admissible oracle-aided PPT pair $\bar{B} = (B_1, B_2)$, s.t.

$$\{\text{REAL}_{\bar{A}}(1^n, x_1, x_2)\}_{x_c, x_1, x_2 \in \{0,1\}^*} \approx_c \{\text{IDEAL}_{\bar{B}}^f(x_1, x_2)\}_{x_c, x_1, x_2 \in \{0,1\}^*}$$

- Recall that the enumeration index (i.e., x_c, x_1, x_2) is given to the distinguisher.
- π securely computes f implies that π computes f **correctly**.
- Security parameter
- Auxiliary inputs
- We focus on semi-honest adversaries.

Section 2

Oblivious Transfer

Oblivious transfer

An (one-out-of-two) OT protocol **securely computes** the functionality $\text{OT} = (\text{OT}_S, \text{OT}_R)$ over $(\{0, 1\}^* \times \{0, 1\}^*) \times \{0, 1\}$, where $\text{OT}_S(\cdot) = \perp$ and $\text{OT}_R((\sigma_0, \sigma_1), i) = \sigma_i$.

Oblivious transfer

An (one-out-of-two) OT protocol **securely computes** the functionality $\text{OT} = (\text{OT}_S, \text{OT}_R)$ over $(\{0, 1\}^* \times \{0, 1\}^*) \times \{0, 1\}$, where $\text{OT}_S(\cdot) = \perp$ and $\text{OT}_R((\sigma_0, \sigma_1), i) = \sigma_i$.

- “Complete” for multiparty computation

Oblivious transfer

An (one-out-of-two) OT protocol **securely computes** the functionality $\text{OT} = (\text{OT}_S, \text{OT}_R)$ over $(\{0, 1\}^* \times \{0, 1\}^*) \times \{0, 1\}$, where $\text{OT}_S(\cdot) = \perp$ and $\text{OT}_R((\sigma_0, \sigma_1), i) = \sigma_i$.

- “Complete” for multiparty computation
- We show how to construct for bit inputs.

Oblivious transfer from trapdoor permutations

Let (G, f, Inv) be a TDP and let b be an hardcore predicate for f .

Oblivious transfer from trapdoor permutations

Let (G, f, Inv) be a TDP and let b be an hardcore predicate for f .

Protocol 2 $((S, R))$

Common input: 1^n

S's input: $\sigma_0, \sigma_1 \in \{0, 1\}$.

R's input: $i \in \{0, 1\}$.

- ➊ S chooses $(e, d) \leftarrow G(1^n)$, and sends e to R .
- ➋ R chooses $x_0, x_1 \leftarrow \{0, 1\}^n$, sets $y_i = f_e(x_i)$ and $y_{1-i} = x_{1-i}$, and sends y_0, y_1 to S .
- ➌ S sets $c_j = b(\text{Inv}_d(y_j)) \oplus \sigma_j$, for $j \in \{0, 1\}$, and sends (c_0, c_1) to R .
- ➍ R outputs $c_i \oplus b(x_i)$.

Oblivious transfer from trapdoor permutations

Let (G, f, Inv) be a TDP and let b be an hardcore predicate for f .

Protocol 2 $((S, R))$

Common input: 1^n

S's input: $\sigma_0, \sigma_1 \in \{0, 1\}$.

R's input: $i \in \{0, 1\}$.

- 1 S chooses $(e, d) \leftarrow G(1^n)$, and sends e to R.
- 2 R chooses $x_0, x_1 \leftarrow \{0, 1\}^n$, sets $y_i = f_e(x_i)$ and $y_{1-i} = x_{1-i}$, and sends y_0, y_1 to S.
- 3 S sets $c_j = b(\text{Inv}_d(y_j)) \oplus \sigma_j$, for $j \in \{0, 1\}$, and sends (c_0, c_1) to R.
- 4 R outputs $c_i \oplus b(x_i)$.

Claim 3

Protocol 2 securely computes OT (in the semi-honest model).

Proving Claim 3

We need to prove that \forall semi-honest admissible PPT pair $\bar{A} = (A_1, A_2)$ for (S, R) , exists admissible oracle-aided PPT pair $\bar{B} = (B_1, B_2)$ s.t.

$$\{\text{REAL}_{\bar{A}}(1^n, (\sigma_0, \sigma_1), i)\} \approx_c \{\text{IDEAL}_{\bar{B}}^{\text{OT}}(1^n, (\sigma_0, \sigma_1), i)\}, \quad (1)$$

where the enumeration is over $n \in \mathbb{N}$ and $\sigma_0, \sigma_1, i \in \{0, 1\}$.

R's privacy

For a semi-honest implementation S' of S , define the oracle-aided semi-honest strategy S'_I as follows.

R's privacy

For a semi-honest implementation S' of S , define the oracle-aided semi-honest strategy S'_I as follows.

Algorithm 4 (S'_I)

input: $1^n, \sigma_0, \sigma_1$

- 1 Send (σ_0, σ_1) to the trusted party.
- 2 Emulate $(S'(1^n, \sigma_0, \sigma_1), R(1^n, 0))$.
- 3 Output the output that S' does.

R's privacy

For a semi-honest implementation S' of S , define the oracle-aided semi-honest strategy S'_I as follows.

Algorithm 4 (S'_I)

input: $1^n, \sigma_0, \sigma_1$

- 1 Send (σ_0, σ_1) to the trusted party.
- 2 Emulate $(S'(1^n, \sigma_0, \sigma_1), R(1^n, 0))$.
- 3 Output the output that S' does.

Let $\bar{A} = (S', R)$ and $\bar{B} = (S'_I, R_I)$, where R_I is honest.

R's privacy

For a semi-honest implementation S' of S , define the oracle-aided semi-honest strategy S'_I as follows.

Algorithm 4 (S'_I)

input: $1^n, \sigma_0, \sigma_1$

- ➊ Send (σ_0, σ_1) to the trusted party.
- ➋ Emulate $(S'(1^n, \sigma_0, \sigma_1), R(1^n, 0))$.
- ➌ Output the output that S' does.

Let $\bar{A} = (S', R)$ and $\bar{B} = (S'_I, R_I)$, where R_I is honest.

Claim 5

$$\{\text{REAL}_{\bar{A}}(1^n, (\sigma_0, \sigma_1), i)\} \equiv \{\text{IDEAL}_{\bar{B}}^{\text{OT}}(1^n, (\sigma_0, \sigma_1), i)\}.$$

R's privacy

For a semi-honest implementation S' of S , define the oracle-aided semi-honest strategy S'_I as follows.

Algorithm 4 (S'_I)

input: $1^n, \sigma_0, \sigma_1$

- 1 Send (σ_0, σ_1) to the trusted party.
- 2 Emulate $(S'(1^n, \sigma_0, \sigma_1), R(1^n, 0))$.
- 3 Output the output that S' does.

Let $\bar{A} = (S', R)$ and $\bar{B} = (S'_I, R_I)$, where R_I is honest.

Claim 5

$$\{\text{REAL}_{\bar{A}}(1^n, (\sigma_0, \sigma_1), i)\} \equiv \{\text{IDEAL}_{\bar{B}}^{\text{OT}}(1^n, (\sigma_0, \sigma_1), i)\}.$$

Proof?

S's privacy

For a semi-honest implementation R' of R , define the oracle-aided semi-honest strategy R'_I as follows.

S's privacy

For a semi-honest implementation R' of R , define the oracle-aided semi-honest strategy R'_I as follows.

Algorithm 6 (R'_I)

input: $1^n, i \in \{0, 1\}$,

- 1 Send i to the trusted party, and let σ be its answer.
- 2 Emulate $(S(1^n, \sigma_0, \sigma_1), R'(1^n, i))$, for $\sigma_i = \sigma$ and $\sigma_{1-i} = 0$.
- 3 Output the output that R' does.

S's privacy

For a semi-honest implementation R' of R , define the oracle-aided semi-honest strategy R'_I as follows.

Algorithm 6 (R'_I)

input: $1^n, i \in \{0, 1\}$,

- 1 Send i to the trusted party, and let σ be its answer.
- 2 Emulate $(S(1^n, \sigma_0, \sigma_1), R'(1^n, i))$, for $\sigma_i = \sigma$ and $\sigma_{1-i} = 0$.
- 3 Output the output that R' does.

Let $\bar{A} = (S, R')$ and $\bar{B} = (S_I, R'_I)$, where S_I is honest.

S's privacy

For a semi-honest implementation R' of R , define the oracle-aided semi-honest strategy R'_I as follows.

Algorithm 6 (R'_I)

input: $1^n, i \in \{0, 1\}$,

- 1 Send i to the trusted party, and let σ be its answer.
- 2 Emulate $(S(1^n, \sigma_0, \sigma_1), R'(1^n, i))$, for $\sigma_i = \sigma$ and $\sigma_{1-i} = 0$.
- 3 Output the output that R' does.

Let $\bar{A} = (S, R')$ and $\bar{B} = (S_I, R'_I)$, where S_I is honest.

Claim 7

$$\{\text{REAL}_{\bar{A}}(1^n, (\sigma_0, \sigma_1), i)\} \approx_c \{\text{IDEAL}_{\bar{B}}^{\text{OT}}(1^n, (\sigma_0, \sigma_1), i)\}.$$

S's privacy

For a semi-honest implementation R' of R , define the oracle-aided semi-honest strategy R'_I as follows.

Algorithm 6 (R'_I)

input: $1^n, i \in \{0, 1\}$,

- ➊ Send i to the trusted party, and let σ be its answer.
- ➋ Emulate $(S(1^n, \sigma_0, \sigma_1), R'(1^n, i))$, for $\sigma_i = \sigma$ and $\sigma_{1-i} = 0$.
- ➌ Output the output that R' does.

Let $\bar{A} = (S, R')$ and $\bar{B} = (S_I, R'_I)$, where S_I is honest.

Claim 7

$$\{\text{REAL}_{\bar{A}}(1^n, (\sigma_0, \sigma_1), i)\} \approx_c \{\text{IDEAL}_{\bar{B}}^{\text{OT}}(1^n, (\sigma_0, \sigma_1), i)\}.$$

Proof?

Section 3

Yao Garbled Circuit

Before we start

- Fix a (multiple message) semantically-secure private-key encryption scheme (G, E, D) with
 - 1 $G(1^n) = U_n$.
 - 2 For any $m \in \{0, 1\}^*$
 $\Pr_{d, d' \leftarrow \{0, 1\}^n} [D_d(E_{d'}(m)) \neq \perp] = \text{neg}(n)$.

Before we start

- Fix a (multiple message) semantically-secure private-key encryption scheme (G, E, D) with
 - 1 $G(1^n) = U_n$.
 - 2 For any $m \in \{0, 1\}^*$
 $\Pr_{d, d' \leftarrow \{0, 1\}^n} [D_d(E_{d'}(m)) \neq \perp] = \text{neg}(n)$.

Can we construct such a scheme?

Before we start

- Fix a (multiple message) semantically-secure private-key encryption scheme (G, E, D) with
 - 1 $G(1^n) = U_n$.
 - 2 For any $m \in \{0, 1\}^*$
 $\Pr_{d, d' \leftarrow \{0, 1\}^n} [D_d(E_{d'}(m)) \neq \perp] = \text{neg}(n)$.

Can we construct such a scheme?

- Boolean circuits: gates, wires, inputs, outputs, values, computation

The Garbled Circuit

The Garbled Circuit

Fix a Boolean circuit C and $n \in \mathbb{N}$.

The Garbled Circuit

Fix a Boolean circuit C and $n \in \mathbb{N}$.

- Let \mathcal{W} and \mathcal{G} be the (indices) of **wires** and **gates** of C , respectively.

The Garbled Circuit

Fix a Boolean circuit C and $n \in \mathbb{N}$.

- Let \mathcal{W} and \mathcal{G} be the (indices) of **wires** and **gates** of C , respectively.
- For $w \in \mathcal{W}$, associate a pair of random 'keys' $k_w = (k_w^0, k_w^1) \in (\{0, 1\}^n)^2$.

The Garbled Circuit

Fix a Boolean circuit C and $n \in \mathbb{N}$.

- Let \mathcal{W} and \mathcal{G} be the (indices) of **wires** and **gates** of C , respectively.
- For $w \in \mathcal{W}$, associate a pair of random 'keys' $k_w = (k_w^0, k_w^1) \in (\{0, 1\}^n)^2$.
- For $g \in \mathcal{G}$ with input wires i and j , and output wire h , let $T(g)$ be the following table:

The Garbled Circuit

Fix a Boolean circuit C and $n \in \mathbb{N}$.

- Let \mathcal{W} and \mathcal{G} be the (indices) of **wires** and **gates** of C , respectively.
- For $w \in \mathcal{W}$, associate a pair of random 'keys' $k_w = (k_w^0, k_w^1) \in (\{0, 1\}^n)^2$.
- For $g \in \mathcal{G}$ with input wires i and j , and output wire h , let $T(g)$ be the following table:

The Garbled Circuit

Fix a Boolean circuit C and $n \in \mathbb{N}$.

- Let \mathcal{W} and \mathcal{G} be the (indices) of **wires** and **gates** of C , respectively.
- For $w \in \mathcal{W}$, associate a pair of random ‘keys’ $k_w = (k_w^0, k_w^1) \in (\{0, 1\}^n)^2$.
- For $g \in \mathcal{G}$ with input wires i and j , and output wire h , let $T(g)$ be the following table:

input wire i	input wire j	output wire h	hidden output wire
k_i^0	k_j^0	$k_h^{g(0,0)}$	$E_{k_i^0}(E_{k_j^0}(k_h^{g(0,0)}))$
k_i^0	k_j^1	$k_h^{g(0,1)}$	$E_{k_i^0}(E_{k_j^1}(k_h^{g(0,1)}))$
k_i^1	k_j^0	$k_h^{g(1,0)}$	$E_{k_i^1}(E_{k_j^0}(k_h^{g(1,0)}))$
k_i^1	k_j^1	$k_h^{g(1,1)}$	$E_{k_i^1}(E_{k_j^1}(k_h^{g(1,1)}))$

Figure: Table for gate g , with input wires i and j , and output wire h .

The Garbled Circuit, cont.

input wire i	input wire j	output wire h	hidden output wire
k_i^0	k_j^0	$k_h^{g(0,0)}$	$E_{k_i^0}(E_{k_j^0}(k_h^{g(0,0)}))$
k_i^0	k_j^1	$k_h^{g(0,1)}$	$E_{k_i^0}(E_{k_j^1}(k_h^{g(0,1)}))$
k_i^1	k_j^0	$k_h^{g(1,0)}$	$E_{k_i^1}(E_{k_j^0}(k_h^{g(1,0)}))$
k_i^1	k_j^1	$k_h^{g(1,1)}$	$E_{k_i^1}(E_{k_j^1}(k_h^{g(1,1)}))$

The Garbled Circuit, cont.

input wire i	input wire j	output wire h	hidden output wire
k_i^0	k_j^0	$k_h^{g(0,0)}$	$E_{k_i^0}(E_{k_j^0}(k_h^{g(0,0)}))$
k_i^0	k_j^1	$k_h^{g(0,1)}$	$E_{k_i^0}(E_{k_j^1}(k_h^{g(0,1)}))$
k_i^1	k_j^0	$k_h^{g(1,0)}$	$E_{k_i^1}(E_{k_j^0}(k_h^{g(1,0)}))$
k_i^1	k_j^1	$k_h^{g(1,1)}$	$E_{k_i^1}(E_{k_j^1}(k_h^{g(1,1)}))$

Let \mathcal{I} and \mathcal{O} be the input and outputs wires of \mathcal{C} .

The Garbled Circuit, cont.

input wire i	input wire j	output wire h	hidden output wire
k_i^0	k_j^0	$k_h^{g(0,0)}$	$E_{k_i^0}(E_{k_j^0}(k_h^{g(0,0)}))$
k_i^0	k_j^1	$k_h^{g(0,1)}$	$E_{k_i^0}(E_{k_j^1}(k_h^{g(0,1)}))$
k_i^1	k_j^0	$k_h^{g(1,0)}$	$E_{k_i^1}(E_{k_j^0}(k_h^{g(1,0)}))$
k_i^1	k_j^1	$k_h^{g(1,1)}$	$E_{k_i^1}(E_{k_j^1}(k_h^{g(1,1)}))$

Let \mathcal{I} and \mathcal{O} be the input and outputs wires of \mathcal{C} .

- For $g \in \mathcal{G}$, let $\tilde{T}(g)$ be a random permutation of the fourth column of $T(g)$.

The Garbled Circuit, cont.

input wire i	input wire j	output wire h	hidden output wire
k_i^0	k_j^0	$k_h^{g(0,0)}$	$E_{k_i^0}(E_{k_j^0}(k_h^{g(0,0)}))$
k_i^0	k_j^1	$k_h^{g(0,1)}$	$E_{k_i^0}(E_{k_j^1}(k_h^{g(0,1)}))$
k_i^1	k_j^0	$k_h^{g(1,0)}$	$E_{k_i^1}(E_{k_j^0}(k_h^{g(1,0)}))$
k_i^1	k_j^1	$k_h^{g(1,1)}$	$E_{k_i^1}(E_{k_j^1}(k_h^{g(1,1)}))$

Let \mathcal{I} and \mathcal{O} be the input and outputs wires of \mathcal{C} .

- For $g \in \mathcal{G}$, let $\tilde{T}(g)$ be a **random permutation** of the fourth column of $T(g)$.
- Let $\mathcal{C}(x)_w$ be the **bit-value** the computation of $\mathcal{C}(x)$ assigns to w .

The Garbled Circuit, cont.

input wire i	input wire j	output wire h	hidden output wire
k_i^0	k_j^0	$k_h^{g(0,0)}$	$E_{k_i^0}(E_{k_j^0}(k_h^{g(0,0)}))$
k_i^0	k_j^1	$k_h^{g(0,1)}$	$E_{k_i^0}(E_{k_j^1}(k_h^{g(0,1)}))$
k_i^1	k_j^0	$k_h^{g(1,0)}$	$E_{k_i^1}(E_{k_j^0}(k_h^{g(1,0)}))$
k_i^1	k_j^1	$k_h^{g(1,1)}$	$E_{k_i^1}(E_{k_j^1}(k_h^{g(1,1)}))$

Let \mathcal{I} and \mathcal{O} be the input and outputs wires of \mathcal{C} .

- For $g \in \mathcal{G}$, let $\tilde{T}(g)$ be a **random permutation** of the fourth column of $T(g)$.
- Let $\mathcal{C}(x)_w$ be the **bit-value** the computation of $\mathcal{C}(x)$ assigns to w .
- Given

The Garbled Circuit, cont.

input wire i	input wire j	output wire h	hidden output wire
k_i^0	k_j^0	$k_h^{g(0,0)}$	$E_{k_i^0}(E_{k_j^0}(k_h^{g(0,0)}))$
k_i^0	k_j^1	$k_h^{g(0,1)}$	$E_{k_i^0}(E_{k_j^1}(k_h^{g(0,1)}))$
k_i^1	k_j^0	$k_h^{g(1,0)}$	$E_{k_i^1}(E_{k_j^0}(k_h^{g(1,0)}))$
k_i^1	k_j^1	$k_h^{g(1,1)}$	$E_{k_i^1}(E_{k_j^1}(k_h^{g(1,1)}))$

Let \mathcal{I} and \mathcal{O} be the input and outputs wires of \mathcal{C} .

- For $g \in \mathcal{G}$, let $\tilde{T}(g)$ be a **random permutation** of the fourth column of $T(g)$.
- Let $\mathcal{C}(x)_w$ be the **bit-value** the computation of $\mathcal{C}(x)$ assigns to w .
- Given
 - $\tilde{T} = \{(g, \tilde{T}(g))\}_{g \in \mathcal{G}}$.

The Garbled Circuit, cont.

input wire i	input wire j	output wire h	hidden output wire
k_i^0	k_j^0	$k_h^{g(0,0)}$	$E_{k_i^0}(E_{k_j^0}(k_h^{g(0,0)}))$
k_i^0	k_j^1	$k_h^{g(0,1)}$	$E_{k_i^0}(E_{k_j^1}(k_h^{g(0,1)}))$
k_i^1	k_j^0	$k_h^{g(1,0)}$	$E_{k_i^1}(E_{k_j^0}(k_h^{g(1,0)}))$
k_i^1	k_j^1	$k_h^{g(1,1)}$	$E_{k_i^1}(E_{k_j^1}(k_h^{g(1,1)}))$

Let \mathcal{I} and \mathcal{O} be the input and outputs wires of \mathcal{C} .

- For $g \in \mathcal{G}$, let $\tilde{T}(g)$ be a **random permutation** of the fourth column of $T(g)$.
- Let $\mathcal{C}(x)_w$ be the **bit-value** the computation of $\mathcal{C}(x)$ assigns to w .
- Given
 - $\tilde{T} = \{(g, \tilde{T}(g))\}_{g \in \mathcal{G}}$.
 - $\{k_w^{\mathcal{C}(x)_w}\}_{w \in \mathcal{I}}$ for some x .

The Garbled Circuit, cont.

input wire i	input wire j	output wire h	hidden output wire
k_i^0	k_j^0	$k_h^{g(0,0)}$	$E_{k_i^0}(E_{k_j^0}(k_h^{g(0,0)}))$
k_i^0	k_j^1	$k_h^{g(0,1)}$	$E_{k_i^0}(E_{k_j^1}(k_h^{g(0,1)}))$
k_i^1	k_j^0	$k_h^{g(1,0)}$	$E_{k_i^1}(E_{k_j^0}(k_h^{g(1,0)}))$
k_i^1	k_j^1	$k_h^{g(1,1)}$	$E_{k_i^1}(E_{k_j^1}(k_h^{g(1,1)}))$

Let \mathcal{I} and \mathcal{O} be the input and outputs wires of \mathcal{C} .

- For $g \in \mathcal{G}$, let $\tilde{T}(g)$ be a **random permutation** of the fourth column of $T(g)$.
- Let $\mathcal{C}(x)_w$ be the **bit-value** the computation of $\mathcal{C}(x)$ assigns to w .
- Given
 - $\tilde{T} = \{(g, \tilde{T}(g))\}_{g \in \mathcal{G}}$.
 - $\{k_w^{\mathcal{C}(x)_w}\}_{w \in \mathcal{I}}$ for some x .
 - $\{(w, k_w = (k_w^0, k_w^1))\}_{w \in \mathcal{O}}$.

The Garbled Circuit, cont.

input wire i	input wire j	output wire h	hidden output wire
k_i^0	k_j^0	$k_h^{g(0,0)}$	$E_{k_i^0}(E_{k_j^0}(k_h^{g(0,0)}))$
k_i^0	k_j^1	$k_h^{g(0,1)}$	$E_{k_i^0}(E_{k_j^1}(k_h^{g(0,1)}))$
k_i^1	k_j^0	$k_h^{g(1,0)}$	$E_{k_i^1}(E_{k_j^0}(k_h^{g(1,0)}))$
k_i^1	k_j^1	$k_h^{g(1,1)}$	$E_{k_i^1}(E_{k_j^1}(k_h^{g(1,1)}))$

Let \mathcal{I} and \mathcal{O} be the input and outputs wires of \mathcal{C} .

- For $g \in \mathcal{G}$, let $\tilde{T}(g)$ be a **random permutation** of the fourth column of $T(g)$.
- Let $\mathcal{C}(x)_w$ be the **bit-value** the computation of $\mathcal{C}(x)$ assigns to w .
- Given
 - $\tilde{T} = \{(g, \tilde{T}(g))\}_{g \in \mathcal{G}}$.
 - $\{k_w^{\mathcal{C}(x)_w}\}_{w \in \mathcal{I}}$ for some x .
 - $\{(w, k_w = (k_w^0, k_w^1))\}_{w \in \mathcal{O}}$.

The Garbled Circuit, cont.

input wire i	input wire j	output wire h	hidden output wire
k_i^0	k_j^0	$k_h^{g(0,0)}$	$E_{k_i^0}(E_{k_j^0}(k_h^{g(0,0)}))$
k_i^0	k_j^1	$k_h^{g(0,1)}$	$E_{k_i^0}(E_{k_j^1}(k_h^{g(0,1)}))$
k_i^1	k_j^0	$k_h^{g(1,0)}$	$E_{k_i^1}(E_{k_j^0}(k_h^{g(1,0)}))$
k_i^1	k_j^1	$k_h^{g(1,1)}$	$E_{k_i^1}(E_{k_j^1}(k_h^{g(1,1)}))$

Let \mathcal{I} and \mathcal{O} be the input and outputs wires of C .

- For $g \in \mathcal{G}$, let $\tilde{T}(g)$ be a **random permutation** of the fourth column of $T(g)$.
- Let $C(x)_w$ be the **bit-value** the computation of $C(x)$ assigns to w .
- Given
 - $\tilde{T} = \{(g, \tilde{T}(g))\}_{g \in \mathcal{G}}$.
 - $\{k_w^{C(x)_w}\}_{w \in \mathcal{I}}$ for some x .
 - $\{(w, k_w = (k_w^0, k_w^1))\}_{w \in \mathcal{O}}$.

One can efficiently compute $C(x)$.

The Garbled Circuit, cont.

input wire i	input wire j	output wire h	hidden output wire
k_i^0	k_j^0	$k_h^{g(0,0)}$	$E_{k_i^0}(E_{k_j^0}(k_h^{g(0,0)}))$
k_i^0	k_j^1	$k_h^{g(0,1)}$	$E_{k_i^0}(E_{k_j^1}(k_h^{g(0,1)}))$
k_i^1	k_j^0	$k_h^{g(1,0)}$	$E_{k_i^1}(E_{k_j^0}(k_h^{g(1,0)}))$
k_i^1	k_j^1	$k_h^{g(1,1)}$	$E_{k_i^1}(E_{k_j^1}(k_h^{g(1,1)}))$

Let \mathcal{I} and \mathcal{O} be the input and outputs wires of C .

- For $g \in \mathcal{G}$, let $\tilde{T}(g)$ be a **random permutation** of the fourth column of $T(g)$.
- Let $C(x)_w$ be the **bit-value** the computation of $C(x)$ assigns to w .
- Given
 - $\tilde{T} = \{(g, \tilde{T}(g))\}_{g \in \mathcal{G}}$.
 - $\{k_w^{C(x)_w}\}_{w \in \mathcal{I}}$ for some x .
 - $\{(w, k_w = (k_w^0, k_w^1))\}_{w \in \mathcal{O}}$.

One can efficiently compute $C(x)$.

- (essentially) No additional information about x leaks.

The Protocol

- Let $f(x_A, x_B) = (f_A(x_A, x_B), f_B(x_A, x_B))$ be function and let C be a circuit that computes f .

The Protocol

- Let $f(x_A, x_B) = (f_A(x_A, x_B), f_B(x_A, x_B))$ be function and let C be a circuit that computes f .
- Let \mathcal{I}_A and \mathcal{I}_B be the input wires corresponds to x_A and x_B respectively in C , and let \mathcal{O}_A and \mathcal{O}_B be the output wires corresponds to f_A and f_B outputs respectively in C .

The Protocol

- Let $f(x_A, x_B) = (f_A(x_A, x_B), f_B(x_A, x_B))$ be function and let C be a circuit that computes f .
- Let \mathcal{I}_A and \mathcal{I}_B be the input wires corresponds to x_A and x_B respectively in C , and let \mathcal{O}_A and \mathcal{O}_B be the output wires corresponds to f_A and f_B outputs respectively in C .
- Recall that $C(x)_w$ is the bit-value the computation of $C(x)$ assigns to w .

The Protocol

- Let $f(x_A, x_B) = (f_A(x_A, x_B), f_B(x_A, x_B))$ be function and let C be a circuit that computes f .
- Let \mathcal{I}_A and \mathcal{I}_B be the input wires corresponds to x_A and x_B respectively in C , and let \mathcal{O}_A and \mathcal{O}_B be the output wires corresponds to f_A and f_B outputs respectively in C .
- Recall that $C(x)_w$ is the bit-value the computation of $C(x)$ assigns to w .
- Let (S, R) be a secure protocol for OT .

The Protocol

- Let $f(x_A, x_B) = (f_A(x_A, x_B), f_B(x_A, x_B))$ be function and let C be a circuit that computes f .
- Let \mathcal{I}_A and \mathcal{I}_B be the input wires corresponds to x_A and x_B respectively in C , and let \mathcal{O}_A and \mathcal{O}_B be the output wires corresponds to f_A and f_B outputs respectively in C .
- Recall that $C(x)_w$ is the bit-value the computation of $C(x)$ assigns to w .
- Let (S, R) be a secure protocol for OT .

The Protocol

- Let $f(x_A, x_B) = (f_A(x_A, x_B), f_B(x_A, x_B))$ be function and let C be a circuit that computes f .
- Let \mathcal{I}_A and \mathcal{I}_B be the input wires corresponds to x_A and x_B respectively in C , and let \mathcal{O}_A and \mathcal{O}_B be the output wires corresponds to f_A and f_B outputs respectively in C .
- Recall that $C(x)_w$ is the bit-value the computation of $C(x)$ assigns to w .
- Let (S, R) be a secure protocol for OT.

Protocol 8 $((A, B))$

Common input: 1^n . **A/B's input:** x_A/x_B

- 1 A samples at random $\{k_w = (k_w^0, k_w^1)\}_{w \in \mathcal{W}}$, and generate \tilde{T} .
- 2 A sends \tilde{T} and $\{(w, k_w^{C(x_1, \cdot)_w})\}_{w \in \mathcal{I}_A}$ to B .
- 3 $\forall w \in \mathcal{I}_B$, A and B interact in $(S(k_w), R(C(\cdot, x_2)_w))(1^n)$.
- 4 B computes the (garbled) circuit, and sends $\{(w, k_w^{C(x_1, x_2)_w})\}_{w \in \mathcal{O}_A}$ to A .
- 5 A sends $\{(w, k_w)\}_{w \in \mathcal{O}_B}$ to B .
- 6 The parties compute $f_A(x_1, x_2)$ and $f_B(x_1, x_2)$ respectively.

Claim 9

Protocol 8 securely computes f (in the semi-honest model)

Claim 9

Protocol 8 securely computes f (in the semi-honest model)

Proof:

Claim 9

Protocol 8 securely computes f (in the semi-honest model)

Proof: We focus on A 's privacy.

Claim 9

Protocol 8 securely computes f (in the semi-honest model)

Proof: We focus on A 's privacy. For a semi-honest B' , define

Algorithm 10 (B'_I)

input: 1^n and x_B .

- 1 Send x_B to the trusted party, and let o_B be its answer.
- 2 Emulate the first 4 steps of $(A(1^{|x_A|}), B'(x_B)(1^n))$.
- 3 For each $w \in \mathcal{O}_B$: permute the order of the pair k_w according to o_B , and the key of w computed in the emulation.
- 4 Complete the emulation, and output the output that B' does.

Claim 9

Protocol 8 securely computes f (in the semi-honest model)

Proof: We focus on A 's privacy. For a semi-honest B' , define

Algorithm 10 (B'_I)

input: 1^n and x_B .

- 1 Send x_B to the trusted party, and let o_B be its answer.
- 2 Emulate the first 4 steps of $(A(1^{|x_A|}), B'(x_B)(1^n))$.
- 3 For each $w \in \mathcal{O}_B$: permute the order of the pair k_w according to o_B , and the key of w computed in the emulation.
- 4 Complete the emulation, and output the output that B' does.

Claim: B'_I is a good “simulator” for B' .

Extensions

Extensions

- Efficiently computable f

Both parties first compute C_f – a circuit that compute f for inputs of the right length

Extensions

- Efficiently computable f

Both parties first compute C_f – a circuit that compute f for inputs of the right length

- Hiding C ?

Extensions

- Efficiently computable f

Both parties first compute C_f – a circuit that compute f for inputs of the right length

- Hiding C ?

Extensions

- Efficiently computable f

Both parties first compute C_f – a circuit that compute f for inputs of the right length

- Hiding C ? All but its size

Malicious model

The parties prove that they act “honestly”

Malicious model

The parties prove that they act “honestly”

- 1 Forces the parties to chose their random coin properly

Malicious model

The parties prove that they act “honestly”

- 1 Forces the parties to choose their random coin properly
- 2 Before each step, the parties prove in \mathcal{ZK} that they followed the prescribed protocol (with respect to the random-coins chosen above)

Malicious model

The parties prove that they act “honestly”

- 1 Forces the parties to choose their random coin properly
- 2 Before each step, the parties prove in \mathcal{ZK} that they followed the prescribed protocol (with respect to the random-coins chosen above)

Malicious model

The parties prove that they act “honestly”

- 1 Forces the parties to choose their random coin properly
- 2 Before each step, the parties prove in \mathcal{ZK} that they followed the prescribed protocol (with respect to the random-coins chosen above)

More efficient alternatives: “cut and choose”

Course Summary

See diagram

What we did not cover

- “Few” reductions

What we did not cover

- “Few” reductions
- Environment security (e.g., UC)

What we did not cover

- “Few” reductions
- Environment security (e.g., UC)
- Information theoretic crypto

What we did not cover

- “Few” reductions
- Environment security (e.g., UC)
- Information theoretic crypto
- Non-generic constructions : number theory, lattices

What we did not cover

- “Few” reductions
- Environment security (e.g., UC)
- Information theoretic crypto
- Non-generic constructions : number theory, lattices
- Impossibility results

What we did not cover

- “Few” reductions
- Environment security (e.g., UC)
- Information theoretic crypto
- Non-generic constructions : number theory, lattices
- Impossibility results
- “Real life cryptography” (e.g., Random oracle model)

What we did not cover

- "Few" reductions
- Environment security (e.g., UC)
- Information theoretic crypto
- Non-generic constructions : number theory, lattices
- Impossibility results
- "Real life cryptography" (e.g., Random oracle model)
- Security

What we did not cover

- "Few" reductions
- Environment security (e.g., UC)
- Information theoretic crypto
- Non-generic constructions : number theory, lattices
- Impossibility results
- "Real life cryptography" (e.g., Random oracle model)
- Security
- Differential Privacy

What we did not cover

- “Few” reductions
- Environment security (e.g., UC)
- Information theoretic crypto
- Non-generic constructions : number theory, lattices
- Impossibility results
- “Real life cryptography” (e.g., Random oracle model)
- Security
- Differential Privacy
- and....