

Foundation of Cryptography (0368-4162-01), Introduction¹

Adminstration + Introduction

Iftach Haitner

Tel Aviv University.

October 30, 2025

¹Last edited on: 2025/11/05.

Part I

Administration and Course Overview

Section 1

Administration

Important Details

1. Iftach Haitner. Check Point building, room 444, email [iftachh at tauex.tau.ac.il](mailto:iftachh@tauex.tau.ac.il).

Important Details

1. Iftach Haitner. Check Point building, room 444, email [iftachh at tauex.tau.ac.il](mailto:iftachh@tauex.tau.ac.il).
2. Reception: Please coordinate via email.

Important Details

1. Iftach Haitner. Check Point building, room 444, email [iftachh at tauex.tau.ac.il](mailto:iftachh@tauex.tau.ac.il).
2. Reception: Please coordinate via email.
3. Who are you?

Important Details

1. Iftach Haitner. Check Point building, room 444, email [iftachh at tauex.tau.ac.il](mailto:iftachh@tauex.tau.ac.il).
2. Reception: Please coordinate via email.
3. Who are you?
4. Mailing list: 0368-4162-01@listserv.tau.ac.il

Important Details

1. Iftach Haitner. Check Point building, room 444, email [iftachh at tauex.tau.ac.il](mailto:iftachh@tauex.tau.ac.il).
2. Reception: Please coordinate via email.
3. Who are you?
4. Mailing list: 0368-4162-01@listserv.tau.ac.il
 - ▶ Registered students are automatically on the list (need to activate the account by going to <https://www.tau.ac.il/newuser/>)

Important Details

1. Iftach Haitner. Check Point building, room 444, email [iftachh at tauex.tau.ac.il](mailto:iftachh@tauex.tau.ac.il).
2. Reception: Please coordinate via email.
3. Who are you?
4. Mailing list: 0368-4162-01@listserv.tau.ac.il
 - ▶ Registered students are automatically on the list (need to activate the account by going to <https://www.tau.ac.il/newuser/>)
 - ▶ If you're not registered and want to get on the list (or want to get another address on the list), send e-mail to: listserv@listserv.tau.ac.il with the line:
subscribe 0368-3500-34 <Real Name>

Important Details

1. Iftach Haitner. Check Point building, room 444, email [iftachh at tauex.tau.ac.il](mailto:iftachh@tauex.tau.ac.il).
2. Reception: Please coordinate via email.
3. Who are you?
4. Mailing list: 0368-4162-01@listserv.tau.ac.il
 - ▶ Registered students are automatically on the list (need to activate the account by going to <https://www.tau.ac.il/newuser/>)
 - ▶ If you're not registered and want to get on the list (or want to get another address on the list), send e-mail to: listserv@listserv.tau.ac.il with the line:
subscribe 0368-3500-34 <Real Name>
5. Course website:
<http://moodle.tau.ac.il/course/view.php?id=368416201> (or just Google **iftach** and follow the link)

Grades

1. Class exam 80

Grades

1. Class exam 80
2. Homework 20%: 5-6 exercises.

Grades

1. Class exam 80
2. Homework 20%: 5-6 exercises.
 - ▶ Recommended to use \LaTeX ([Overleaf](#) is a great choice)

Grades

1. Class exam 80
2. Homework 20%: 5-6 exercises.
 - ▶ Recommended to use \LaTeX (Overleaf is a great choice)
 - ▶ Exercises should be sent to ? or put in mailbox ?, **in time!**

and..

1. Slides

and..

1. Slides
2. English

Course Prerequisites

1. Some prior knowledge of cryptography (such as 0369.3049) might help, but not necessarily
2. Basic probability.
3. Basic complexity (the classes \mathcal{P} , \mathcal{NP} , \mathcal{BPP})

Course Material

1. Books:

- 1.1 Oded Goldreich. Foundations of Cryptography.
- 1.2 Jonathan Katz and Yehuda Lindell. An Introduction to Modern Cryptography.
- 1.3 Dan Boneh and Victor Shoup. A Graduate Course in Applied Cryptography.

2. Lecture notes

- 2.1 Ran Canetti www.cs.tau.ac.il/~canetti/f08.html
- 2.2 Yehuda Lindell u.cs.biu.ac.il/~lindell/89-856/main-89-856.html
- 2.3 Luca Trevisan www.cs.berkeley.edu/~daw/cs276/
- 2.4 Salil Vadhan people.seas.harvard.edu/~salil/cs120/

Section 2

Course Topics

Course Topics

Basic primitives in cryptography (i.e., one-way functions, pseudorandom generators and zero-knowledge proofs).

- ▶ Focus on *formal* definitions and *rigorous* proofs.
- ▶ The goal is not studying some list, but to understand cryptography.
- ▶ Get ready to start researching

Part II

Foundation of Cryptography

Section 3

Cryptography and Computational Hardness

Cryptography and Computational Hardness

1. What is Cryptography?

Cryptography and Computational Hardness

1. What is Cryptography?
2. Hardness assumptions, why do we need them?

Cryptography and Computational Hardness

1. What is Cryptography?
2. Hardness assumptions, why do we need them?
3. Does $\mathcal{P} \neq \mathcal{NP}$ suffice?

Cryptography and Computational Hardness

1. What is Cryptography?
2. Hardness assumptions, why do we need them?
3. Does $\mathcal{P} \neq \mathcal{NP}$ suffice?
 \mathcal{NP} : all (languages) $L \subset \{0, 1\}^*$ for which there exists a polynomial-time algorithm V and (a polynomial) $p \in \text{poly}$ such that the following hold:

Cryptography and Computational Hardness

1. What is Cryptography?
2. Hardness assumptions, why do we need them?
3. Does $\mathcal{P} \neq \mathcal{NP}$ suffice?
 - \mathcal{NP} : all (languages) $L \subset \{0, 1\}^*$ for which there exists a polynomial-time algorithm V and (a polynomial) $p \in \text{poly}$ such that the following hold:
 - 3.1 $V(x, w) = 0$ for any $x \notin L$ and $w \in \{0, 1\}^*$

Cryptography and Computational Hardness

1. What is Cryptography?
2. Hardness assumptions, why do we need them?
3. Does $\mathcal{P} \neq \mathcal{NP}$ suffice?
 - \mathcal{NP} : all (languages) $L \subset \{0, 1\}^*$ for which there exists a polynomial-time algorithm V and (a polynomial) $p \in \text{poly}$ such that the following hold:
 - 3.1 $V(x, w) = 0$ for any $x \notin L$ and $w \in \{0, 1\}^*$
 - 3.2 for any $x \in L$, $\exists w \in \{0, 1\}^*$ with $|w| \leq p(|x|)$ and $V(x, w) = 1$

Cryptography and Computational Hardness

1. What is Cryptography?
2. Hardness assumptions, why do we need them?
3. Does $\mathcal{P} \neq \mathcal{NP}$ suffice?

\mathcal{NP} : all (languages) $L \subset \{0, 1\}^*$ for which there exists a polynomial-time algorithm V and (a polynomial) $p \in \text{poly}$ such that the following hold:

3.1 $V(x, w) = 0$ for any $x \notin L$ and $w \in \{0, 1\}^*$

3.2 for any $x \in L$, $\exists w \in \{0, 1\}^*$ with $|w| \leq p(|x|)$ and $V(x, w) = 1$

$\mathcal{P} \neq \mathcal{NP}$: i.e., $\exists L \in \mathcal{NP}$, such that for any polynomial-time algorithm A , $\exists x \in \{0, 1\}^*$ with $A(x) \neq 1_L(x)$

Cryptography and Computational Hardness

1. What is Cryptography?
2. Hardness assumptions, why do we need them?
3. Does $\mathcal{P} \neq \mathcal{NP}$ suffice?

\mathcal{NP} : all (languages) $L \subset \{0, 1\}^*$ for which there exists a polynomial-time algorithm V and (a polynomial) $p \in \text{poly}$ such that the following hold:

3.1 $V(x, w) = 0$ for any $x \notin L$ and $w \in \{0, 1\}^*$

3.2 for any $x \in L$, $\exists w \in \{0, 1\}^*$ with $|w| \leq p(|x|)$ and $V(x, w) = 1$

$\mathcal{P} \neq \mathcal{NP}$: i.e., $\exists L \in \mathcal{NP}$, such that for any polynomial-time algorithm A , $\exists x \in \{0, 1\}^*$ with $A(x) \neq 1_L(x)$

polynomial-time algorithms: an algorithm A runs in polynomial-time, if $\exists p \in \text{poly}$ such that the running time of $A(x)$ is bounded by $p(|x|)$ for any $x \in \{0, 1\}^*$

Cryptography and Computational Hardness

1. What is Cryptography?
2. Hardness assumptions, why do we need them?
3. Does $\mathcal{P} \neq \mathcal{NP}$ suffice?

\mathcal{NP} : all (languages) $L \subset \{0, 1\}^*$ for which there exists a polynomial-time algorithm V and (a polynomial) $p \in \text{poly}$ such that the following hold:

3.1 $V(x, w) = 0$ for any $x \notin L$ and $w \in \{0, 1\}^*$

3.2 for any $x \in L$, $\exists w \in \{0, 1\}^*$ with $|w| \leq p(|x|)$ and $V(x, w) = 1$

$\mathcal{P} \neq \mathcal{NP}$: i.e., $\exists L \in \mathcal{NP}$, such that for any polynomial-time algorithm A , $\exists x \in \{0, 1\}^*$ with $A(x) \neq 1_L(x)$

polynomial-time algorithms: an algorithm A runs in polynomial-time, if $\exists p \in \text{poly}$ such that the running time of $A(x)$ is bounded by $p(|x|)$ for any $x \in \{0, 1\}^*$

4. Problems: hard on the average. No known solution

Cryptography and Computational Hardness

1. What is Cryptography?
2. Hardness assumptions, why do we need them?
3. Does $\mathcal{P} \neq \mathcal{NP}$ suffice?

\mathcal{NP} : all (languages) $L \subset \{0, 1\}^*$ for which there exists a polynomial-time algorithm V and (a polynomial) $p \in \text{poly}$ such that the following hold:

3.1 $V(x, w) = 0$ for any $x \notin L$ and $w \in \{0, 1\}^*$

3.2 for any $x \in L$, $\exists w \in \{0, 1\}^*$ with $|w| \leq p(|x|)$ and $V(x, w) = 1$

$\mathcal{P} \neq \mathcal{NP}$: i.e., $\exists L \in \mathcal{NP}$, such that for any polynomial-time algorithm A , $\exists x \in \{0, 1\}^*$ with $A(x) \neq 1_L(x)$

polynomial-time algorithms: an algorithm A runs in polynomial-time, if $\exists p \in \text{poly}$ such that the running time of $A(x)$ is bounded by $p(|x|)$ for any $x \in \{0, 1\}^*$

4. Problems: hard on the average. No known solution
5. One-way functions: an efficiently computable function that no efficient algorithm can invert.

Part III

Notation

Notation I

- ▶ For $t \in \mathbb{N}$, let $[t] := \{1, \dots, t\}$.
- ▶ Given a string $x \in \{0, 1\}^*$ and $0 \leq i < j \leq |x|$, let $x_{i, \dots, j}$ stands for the substring induced by taking the i, \dots, j bit of x (i.e., $x[i] \dots x[j]$).
- ▶ Given a function f defined over a set \mathcal{U} , and a set $\mathcal{S} \subseteq \mathcal{U}$, let $f(\mathcal{S}) := \{f(x) : x \in \mathcal{S}\}$, and for $y \in f(\mathcal{U})$ let $f^{-1}(y) := \{x \in \mathcal{U} : f(x) = y\}$.
- ▶ **poly** stands for the set of all polynomials.
- ▶ The worst-case running-time of a *polynomial-time algorithm* on input x , is bounded by $p(|x|)$ for some $p \in \text{poly}$.
- ▶ A function is *polynomial-time computable*, if there exists a polynomial-time algorithm to compute it.
- ▶ PPT stands for probabilistic polynomial-time algorithms.
- ▶ A function $\mu : \mathbb{N} \mapsto [0, 1]$ is negligible, denoted $\mu(n) = \text{neg}(n)$, if for any $p \in \text{poly}$ there exists $n' \in \mathbb{N}$ with $\mu(n) \leq 1/p(n)$ for any $n > n'$.

Distribution and random variables I

- ▶ The support of a distribution P over a finite set \mathcal{U} , denoted $\text{Supp}(P)$, is defined as $\{u \in \mathcal{U} : P(u) > 0\}$.
- ▶ Given a distribution P and an event E with $\Pr_P[E] > 0$, we let $(P \mid E)$ denote the conditional distribution P given E (i.e., $(P \mid E)(x) = \frac{P(x) \wedge E}{\Pr_P[E]}$).
- ▶ For $t \in \mathbb{N}$, let U_t denote a random variable uniformly distributed over $\{0, 1\}^t$.
- ▶ Given a random variable X , we let $x \leftarrow X$ denote that x is distributed according to X (e.g., $\Pr_{x \leftarrow X}[x = 7]$).
- ▶ Given a finite set S , we let $x \leftarrow S$ denote that x is uniformly distributed in S .
- ▶ We use the convention that when a random variable appears twice in the same expression, it refers to a *single* instance of this random variable. For instance, $\Pr[X = X] = 1$ (regardless of the definition of X).

Distribution and random variables II

- ▶ Given distribution P over \mathcal{U} and $t \in \mathbb{N}$, we let P^t over \mathcal{U}^t be defined by $D^t(x_1, \dots, x_t) = \prod_{i \in [t]} D(x_i)$.
- ▶ Similarly, given a random variable X , we let X^t denote the random variable induced by t independent samples from X .