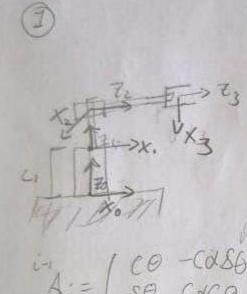


 $X = L_1' Co_2 \theta_1 + L_2 Co_2 (\theta_1' + \theta_2) = L_1' C \theta_1 + L_2 C (\theta_1 + \theta_2)$   $Y = L_1' S \theta_1 + L_2 S (\theta_1 + \theta_2)$   $Z = L_1 - d_3$ 

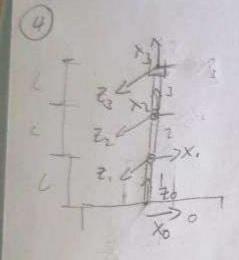


A	0:	di	ai	Vi
1	9	Li	0	0
2	-90	92	0	-90
3	90	93	0	0

$$A_{i} = \begin{cases} c\theta - c\alpha s\theta & s\alpha s\theta & |\alpha c\theta| \\ s\theta & c\alpha c\theta - s\alpha c\theta & |\alpha s\theta| \\ o & s\alpha & |c\alpha| & |\alpha| \\ \hline 0 & s\alpha & |c\alpha| & |\alpha| \\ \hline 0 & 0 & 0 & 1 \end{cases}$$

$${}^{2}A_{1} = \begin{pmatrix} CQ_{1} & -SQ_{1} & 0 & 0 & 0 \\ SQ_{1} & CQ_{1} & 0 & 0 & 0 \\ 0 & 0 & 1 & C_{1} \\ 0 & 0 & 0 & 1 \end{pmatrix} \qquad {}^{2}A_{2} = \begin{pmatrix} 0 & 0 & 1 & 0 \\ -1 & 0 & 0 & 0 \\ 0 & -1 & 0 & q_{2} \\ 0 & 0 & 0 & 1 \end{pmatrix}$$

$$A_3 = \begin{cases} 0 & -1 & 0 & 0 \\ 1 & 0 & 0 & 0 \\ 0 & 0 & 1 & 9_3 \\ \hline 0 & 0 & 0 & 1 \end{cases}$$



IA	O;	di	ai	di
1	9'	4	0	90
2	92	0	1	0
3	93	0	43	0

```
clear, clc
syms q1 q2 q3 px py pz
L1 = 12
L2 = L1
EqX = px == (L2+q3)*cos(q2)*cos(q1)
EqY = py == (L2+q3)*cos(q2)*sin(q1)
EqZ = pz == L1 + (L2 + q3)*sin(q2)
[Sol_q1, Sol_q2, Sol_q3] = solve([EqX EqY EqZ], [q1 q2 q3])%, param, cond],
"ReturnConditions", true);
%disp(Sol_q3)
Sol_q1 = simplify(Sol_q1)
Sol_q2 = simplify(Sol_q2)
Sol_q3 = simplify(Sol_q3)
L1 =
    12
L2 =
    12
EqX =
px == cos(q1)*cos(q2)*(q3 + 12)
EqY =
py == cos(q2)*sin(q1)*(q3 + 12)
EqZ =
pz == sin(q2)*(q3 + 12) + 12
Warning: Solutions are only valid under certain conditions. To include
parameters and conditions in the solution, specify the 'ReturnConditions'
value
as 'true'.
Sol_q1 =
-2*atan((px - (12*((((px^2 + py^2 + pz^2 - 24*pz + 144)^(1/2) - pz + 12)*(pz + pz^2 - 24*pz + 144)^(1/2))
(px^2 + py^2 + pz^2 - 24*pz + 144)^(1/2) - 12))^(1/2) + (px^2 + py^2 + pz^2)
```

```
-24*pz + 144)^{(1/2)}/(pz - 12) - (px^2 + py^2 + pz^2 - 24*pz + 144)^{(1/2)}
 + (pz*(((px^2 + py^2 + pz^2 - 24*pz + 144)^(1/2) - pz + 12)*(pz + (px^2 + pz^2 + 144)^2))
py^2 + pz^2 - 24*pz + 144)^(1/2) - 12))^(1/2) + (px^2 + py^2 + pz^2 - 24*pz + pz^2)^2
 144)^{(1/2)})/(pz - 12))/py)
-2*atan((px + (12*((((px^2 + py^2 + pz^2 - 24*pz + 144)^(1/2) - pz + 12)*(pz + pz^2 + pz^2 + pz^2))
(px^2 + py^2 + pz^2 - 24*pz + 144)^(1/2) - 12))^(1/2) + (px^2 + py^2 + pz^2)
 -24*pz + 144)^{(1/2)}/(pz - 12) + (px^2 + py^2 + pz^2 - 24*pz + 144)^{(1/2)}
 -(pz^*(((px^2 + py^2 + pz^2 - 24*pz + 144)^(1/2) - pz + 12)^*(pz + (px^2 + pz^2 + 144)^*))
 py^2 + pz^2 - 24*pz + 144)^(1/2) - 12))^(1/2) + (px^2 + py^2 + pz^2 - 24*pz + pz^2)
 144)^{(1/2)})/(pz - 12))/py)
-2*atan((px - (12*((((px^2 + py^2 + pz^2 - 24*pz + 144)^(1/2) - pz + 12)*(pz + pz^2 + pz^2))))
(px^2 + py^2 + pz^2 - 24*pz + 144)^(1/2) - 12))^(1/2) - (px^2 + py^2 + pz^2)
 -24*pz + 144)^{(1/2)}/(pz - 12) + (px^2 + py^2 + pz^2 - 24*pz + 144)^{(1/2)}
 + (pz*(((px^2 + py^2 + pz^2 - 24*pz + 144)^(1/2) - pz + 12)*(pz + (px^2 + pz^2 + 144)^2))
py^2 + pz^2 - 24*pz + 144)^(1/2) - 12))^(1/2) - (px^2 + py^2 + pz^2 - 24*pz + pz^2)
 144)^{(1/2)})/(pz - 12))/py)
-2*atan((px + (12*((((px^2 + py^2 + pz^2 - 24*pz + 144)^*(1/2) - pz + 12)*(pz + pz^2 + pz^2 + pz^2))
(px^2 + py^2 + pz^2 - 24*pz + 144)^(1/2) - 12))^(1/2) - (px^2 + py^2 + pz^2)
 -24*pz + 144)^{(1/2)})/(pz - 12) - (px^2 + py^2 + pz^2 - 24*pz + 144)^{(1/2)}
 -(pz*(((px^2 + py^2 + pz^2 - 24*pz + 144)^(1/2) - pz + 12)*(pz + (px^2 + 144)^2))
py^2 + pz^2 - 24*pz + 144)^(1/2) - 12))^(1/2) - (px^2 + py^2 + pz^2 - 24*pz + pz^2)
 144)^{(1/2)})/(pz - 12))/py)
Sol_q2 =
 2*atan((((px^2 + py^2 + pz^2 - 24*pz + 144)^(1/2) - pz + 12)*(pz + (px^2 + pz^2 + 144)^2)))
py^2 + pz^2 - 24*pz + 144)^(1/2) - 12))^(1/2) + (px^2 + py^2 + pz^2 - 24*pz + pz^2)^2
 144)^{(1/2)}/(pz - 12)
-2*atan((((px^2 + py^2 + pz^2 - 24*pz + 144)^(1/2) - pz + 12)*(pz + (px^2 + pz^2 + 144)^2))
 py^2 + pz^2 - 24*pz + 144)^(1/2) - 12))^(1/2) + (px^2 + py^2 + pz^2 - 24*pz + pz^2)
 144)^{(1/2)}/(pz - 12)
 2*atan(((((px^2 + py^2 + pz^2 - 24*pz + 144)^(1/2) - pz + 12)*(pz + (px^2 + pz^2 + 144)^2))))
py^2 + pz^2 - 24*pz + 144)^(1/2) - 12))^(1/2) - (px^2 + py^2 + pz^2 - 24*pz + pz^2)
 144)^{(1/2)}/(pz - 12)
-2*atan((((px^2 + py^2 + pz^2 - 24*pz + 144)^(1/2) - pz + 12)*(pz + (px^2 + pz^2 + 144)^2))
py^2 + pz^2 - 24*pz + 144)^(1/2) - 12))^(1/2) - (px^2 + py^2 + pz^2 - 24*pz + pz^2)
144)^{(1/2)}/(pz - 12)
Sol q3 =
  (px^2 + py^2 + pz^2 - 24*pz + 144)^(1/2) - 12
-(px^2 + py^2 + pz^2 - 24*pz + 144)^(1/2) - 12
-(px^2 + py^2 + pz^2 - 24*pz + 144)^(1/2) - 12
  (px^2 + py^2 + pz^2 - 24*pz + 144)^(1/2) - 12
Sol_q1 =
-2*atan((px + (px^2 + py^2)^(1/2))/py)
-2*atan((px - (px^2 + py^2)^(1/2))/py)
-2*atan((px + (px^2 + py^2)^(1/2))/py)
-2*atan((px - (px^2 + py^2)^(1/2))/py)
```

```
Sol_{q2} = \\ 2*atan(((px^2 + py^2)^{(1/2)} + (px^2 + py^2 + pz^2 - 24*pz + 144)^{(1/2)})/(pz - 12)) \\ -2*atan(((px^2 + py^2)^{(1/2)} + (px^2 + py^2 + pz^2 - 24*pz + 144)^{(1/2)})/(pz - 12)) \\ 2*atan(((px^2 + py^2)^{(1/2)} - (px^2 + py^2 + pz^2 - 24*pz + 144)^{(1/2)})/(pz - 12)) \\ -2*atan(((px^2 + py^2)^{(1/2)} - (px^2 + py^2 + pz^2 - 24*pz + 144)^{(1/2)})/(pz - 12)) \\ -2*atan(((px^2 + py^2)^{(1/2)} - (px^2 + py^2 + pz^2 - 24*pz + 144)^{(1/2)})/(pz - 12)) \\ Sol_{q3} = \\ (px^2 + py^2 + pz^2 - 24*pz + 144)^{(1/2)} - 12 \\ - (px^2 + py^2 + pz^2 - 24*pz + 144)^{(1/2)} - 12 \\ - (px^2 + py^2 + pz^2 - 24*pz + 144)^{(1/2)} - 12 \\ (px^2 + py^2 + pz^2 - 24*pz + 144)^{(1/2)} - 12 \\ (px^2 + py^2 + pz^2 - 24*pz + 144)^{(1/2)} - 12 \\ (px^2 + py^2 + pz^2 - 24*pz + 144)^{(1/2)} - 12 \\ (px^2 + py^2 + pz^2 - 24*pz + 144)^{(1/2)} - 12 \\ (px^2 + py^2 + pz^2 - 24*pz + 144)^{(1/2)} - 12 \\ (px^2 + py^2 + pz^2 - 24*pz + 144)^{(1/2)} - 12 \\ (px^2 + py^2 + pz^2 - 24*pz + 144)^{(1/2)} - 12 \\ (px^2 + py^2 + pz^2 - 24*pz + 144)^{(1/2)} - 12 \\ (px^2 + py^2 + pz^2 - 24*pz + 144)^{(1/2)} - 12 \\ (px^2 + py^2 + pz^2 - 24*pz + 144)^{(1/2)} - 12 \\ (px^2 + py^2 + pz^2 - 24*pz + 144)^{(1/2)} - 12 \\ (px^2 + py^2 + pz^2 - 24*pz + 144)^{(1/2)} - 12 \\ (px^2 + py^2 + pz^2 - 24*pz + 144)^{(1/2)} - 12 \\ (px^2 + py^2 + pz^2 - 24*pz + 144)^{(1/2)} - 12 \\ (px^2 + py^2 + pz^2 - 24*pz + 144)^{(1/2)} - 12 \\ (px^2 + py^2 + pz^2 - 24*pz + 144)^{(1/2)} - 12 \\ (px^2 + py^2 + pz^2 - 24*pz + 144)^{(1/2)} - 12 \\ (px^2 + py^2 + pz^2 - 24*pz + 144)^{(1/2)} - 12 \\ (px^2 + py^2 + pz^2 - 24*pz + 144)^{(1/2)} - 12 \\ (px^2 + py^2 + pz^2 - 24*pz + 144)^{(1/2)} - 12 \\ (px^2 + py^2 + pz^2 - 24*pz + 144)^{(1/2)} - 12 \\ (px^2 + py^2 + pz^2 - 24*pz + 144)^{(1/2)} - 12 \\ (px^2 + py^2 + pz^2 - 24*pz + 144)^{(1/2)} - 12 \\ (px^2 + py^2 + pz^2 - 24*pz + 144)^{(1/2)} - 12 \\ (px^2 + py^2 + pz^2 - 24*pz + 144)^{(1/2)} - 12 \\ (px^2 + py^2 + pz^2 - 24*pz + 144)^{(1/2)} - 12 \\ (px^2 + py^2 + pz^2 - 24*pz + 144)^{(1/2)} - 12 \\ (px^2 + py^2 + pz^2 - 24*pz + 144)^{(1/2)} - 12 \\ (px^2 + py^2 + p
```

```
syms q1 q2 q3 px py pz
L1 = 12
L2 = L1
EqX = px == L1*cos(q1) + L2*cos(q1+q2)
EqY = py == L1*sin(q1) + L2*sin(q1+q2)
EqZ = pz == L1 - q3
[Sol_q1 Sol_q2 Sol_q3] = solve([EqX EqY EqZ], [q1 q2 q3]);
Sol_q1 = simplify(Sol_q1)
Sol_q2 = simplify(Sol_q2)
Sol_q3 = simplify(Sol_q3)
L1 =
    12
L2 =
    12
EqX =
px == 12*cos(q1 + q2) + 12*cos(q1)
EqY =
py == 12*sin(q1 + q2) + 12*sin(q1)
EqZ =
pz == 12 - q3
Sol_q1 =
2*atan((24*py + (-px^4 - 2*px^2*py^2 + 576*px^2 - py^4 + 576*py^2)^{(1/2)})/
(px^2 + 24*px + py^2))
2*atan((24*py - (-px^4 - 2*px^2*py^2 + 576*px^2 - py^4 + 576*py^2)^{(1/2)})/
(px^2 + 24*px + py^2))
Sol q2 =
-2*atan((-(px^2 + py^2)*(px^2 + py^2 - 576))^(1/2)/(px^2 + py^2))
```

```
clear, clc
syms px py pz az ax ay
syms q1 q2 q3
L1 = 12
L2 = L1
L3 = L1
DHParam = [q1 L1 0 0; -pi/2 q2 0 -pi/2; pi/2 q3 0 0];
[A, T, Q, Rot, Tra] = DH(DHParam, px, py, pz, az);
    EqX = px == (Tra(1));
    EqY = py == (Tra(2));
    EqZ = pz == (Tra(3));
    Eqs = [EqX; EqY; EqZ];
    % n, s, a
    EqAux = az == Rot(2,3);
    EqAux = az == Rot(3,3);
   EqAux = az == Rot(3,1);
    jointVar = symvar(T);
Q = solve([EqX EqY EqZ], jointVar, "Real", true)%, "PrincipalValue", false)
888888885
L1 =
    12
L2 =
   12
L3 =
    12
     3
[q1, 12, 0, 0]
[-pi/2, q2, 0, -pi/2]
[pi/2, q3, 0, 0]
```

```
(:,:,1) =
[\cos(q1), -\sin(q1), 0, 0]
[\sin(q1), \cos(q1), 0, 0]
      0,
               0, 1, 12]
       0,
                 0, 0, 1]
[
(:,:,2) =
                0, 1, 0]
      0,
                0,0,0]
      -1,
                -1, 0, q2]
       0,
       0,
                0, 0, 1]
(:,:,3) =
       0,
                -1, 0, 0]
                0,0,0]
[
       1,
                 0, 1, q3]
[
       0,
                 0,0,1]
       0,
[0, -\sin(q1), \cos(q1), q3*\cos(q1)]
[ 0, cos(q1), sin(q1), q3*sin(q1)]
[-1,
            0,
                   0, q2 + 12
[ 0,
            0,
                     0,
                                 1]
Warning: Solutions are only valid under certain conditions. To include
parameters and conditions in the solution, specify the 'ReturnConditions'
value
as 'true'.
0 =
  struct with fields:
    q1: [2×1 sym]
    q2: [2×1 sym]
    q3: [2\times 1 \text{ sym}]
assume(q1>-pi & q1<pi & q2>0 & q3>0)
   EqX = px == expand(Tra(1));
   EqY = py == expand(Tra(2));
   EqZ = pz == expand(Tra(3));
   EqAux = az == Rot(3,1);
   EqAux2 = ay == Rot(2,1);
   EqAux3 = ax == Rot(1,1);
   jointVar = symvar(T);
   %Q = solve([EqX EqY EqZ EqAux1 EqAux1b EqAux2 EqAux2b EqAux3 EqAux3b], jointVar, "Real"
```

```
Q = solve([EqX EqY EqZ EqAux EqAux2 EqAux3], jointVar(2:end), "Real",true) % Se puede j
  Q2 = solve([EqX EqY EqZ EqAux EqAux2 EqAux3], jointVar, "Real", true) % Se puede jugar c
    Q.q1 = solve
    888888888855
% A es el arreglo conteniendo las matrices de transformación de i = 1 a i =
% n. T es la matriz de transformación simplificada, la matriz de cinemática
% directa. Q es un vector conteniendo los resultados para las variables de
% q1 a qn. Rot es la matriz de rotación extraída de T. Y Tra es el ventor
% posición extraído de T.
% syms n_x s_x a_x p_x n_y s_y a_y p_y n_z s_z a_z p_z
T_syms = [n_x s_x a_x p_x; n_y s_y a_y p_y; n_z s_z a_z p_z; 0 0 0 1];
T1 = (A(:,:,1)) \setminus T_{syms} == A(:,:,2) *A(:,:,3)
%inverseKinematics()
      ia = inv(A(:, :, 1));
응
      ter2 = A(:, :, 2) * A(:, :, 3);
응
      eq1 = ter2(3,4) == ia (3,1)*px + ia(3,2) *py;
응
      %q1 = solve(eq1,q1, 'real',true);
응
응
      ib = inv(A(:, :, 2))*ia;
응
      ter1 = A(:, :, 3);
응
응
      eq2 = ter1(2,4) == ib(2,1)*px + ib(2,2)*py + ib(2,3)*pz + ib(2,4)*1;
응
      eq3 = ter1(1,4) == ib(1,1)*px + ib(1,2)*py + ib(1,3)*pz + ib(1,4)*1;
응
%
      [q2,q3] = solve([eq2,eq3],[q2 q3], 'real', true);
%
응
      q1 = atan2(py,px);
응
응
      q2 = eval(q2(1));
응
      q3 = eval(q3(1));
응
%
응
      th = [q1, q2, q3];
응
      th2 = rad2deg(th);
ે
%
      th2(1)
%
      th2(2)
응
      th2(3)
```

```
clear, clc
syms px py pz az ax ay
syms q1 q2 q3
L1 = 12
T_12 = T_11
L3 = L1
DHParam = [q1 L1 0 pi/2; q2 0 L2 0; q3 0 L3 0];
[A, T, Q, Rot, Tra] = DH(DHParam, px, py, pz, az);
%assume(q1>-pi & q1<pi & q2>-pi & q2<pi & q3>-pi & q3<pi)
assume(pz>0 & q1<0 & q1 > -pi)% & q2>0 & q3>0)
    EqX = px == simplify(Tra(1));
    EqY = py == simplify(Tra(2));
    EqZ = pz == simplify(Tra(3));
    jointVar = symvar(T);
      Q3 = solve([EqZ], jointVar(3), 'real',true) % Se puede jugar con las
variables a resolver y a partir de ahí sacar la última solución. Usando la
primera variable como parámetro. Dado el caso de que las ecuaciones no son
 linealmente indemendientes entre sí
     Q3b = Q3(1) %== q3
     %q3 = Q3(1)
     EqX = simplify(subs(EqX, q3, Q3b))
      EqY = simplify(subs(EqY, q3, Q3b))
      Q12 = solve([EqX EqY], jointVar(1:2)) % Se puede jugar con las
variables a resolver y a partir de ahí sacar la última solución. Usando la
primera variable como parámetro. Dado el caso de que las ecuaciones no son
 linealmente indemendientes entre sí
      Q1 = solve([EqX], jointVar(1), 'real', true) % Se puede jugar con las
variables a resolver y a partir de ahí sacar la última solución. Usando la
primera variable como parámetro. Dado el caso de que las ecuaciones no son
linealmente indemendientes entre sí
      Q1b = Q1(2) \% = = q3
     %q3 = Q3(1)
     EqY = simplify(subs(EqY, jointVar(1), Q1b))
     EqZ = simplify(subs(EqZ, jointVar(1), Q1b))
      Q23 = solve([EqX EqY], jointVar(2:3)) % Se puede jugar con las
variables a resolver y a partir de ahí sacar la última solución. Usando la
primera variable como parámetro. Dado el caso de que las ecuaciones no son
linealmente indemendientes entre sí
    %%%%%%%%%%55
% A es el arreglo conteniendo las matrices de transformación de i = 1 a i =
```

```
% n. T es la matriz de transformación simplificada, la matriz de cinemática
% directa. Q es un vector conteniendo los resultados para las variables de
% q1 a qn. Rot es la matriz de rotación extraída de T. Y Tra es el ventor
% posición extraído de T.
% syms n_x s_x a_x p_x n_y s_y a_y p_y n_z s_z a_z p_z
% T_syms = [n_x s_x a_x p_x;n_y s_y a_y p_y;n_z s_z a_z p_z;0 0 0 1];
T1 = (A(:,:,1)) T_syms == A(:,:,2)*A(:,:,3)
%inverseKinematics()
    ia = inv(A(:, :, 1));
    ter2 = A(:, :, 2) * A(:, :, 3);
    eq1 = ter2(3,4) == ia(3,1)*px + <math>ia(3,2)*py;
    %q1 = solve(eq1,q1, 'real',true);
    ib = inv(A(:, :, 2))*ia;
    ter1 = A(:, :, 3);
    eq2 = ter1(2,4) = ib(2,1)*px + ib(2,2)*py + ib(2,3)*pz + ib(2,4)*1;
    eq3 = ter1(1,4) == ib(1,1)*px + ib(1,2)*py + ib(1,3)*pz + ib(1,4)*1;
    [q2,q3] = solve([eq2,eq3],[q2 q3], 'real', true);
    q1 = atan2(py,px);
    q2 = eval(q2(1));
    q3 = eval(q3(1));
    th = [q1,q2,q3];
    th2 = rad2deq(th);
    th2(1);
    th2(2);
    th2(3);
% fun = @(q) norm([Tra(1);Tra(2);Tra(3)]);
L1 =
    12
L2 =
    12
```

```
L3 =
    12
     3
[q1, 12, 0, pi/2]
[q2, 0, 12, 0]
[q3, 0, 12, 0]
(:,:,1) =
[cos(q1),
                 0, sin(q1),
                                           0]
[sin(q1),
                 0, -\cos(q1),
                                            0]
[ 0,
                   1,
                        0,
                                            12]
                   0,
      0,
                              0,
                                            1]
(:,:,2) =
                          0, 12*cos(q2)]
[\cos(q2), -\sin(q2),
[\sin(q2), \cos(q2),
                             0, 12*sin(q2)
[ 0,
               0,
                              1,
                                             0]
      0,
                  0,
                               0,
                                            1]
(:,:,3) =
                       0, 12*cos(q3)]
[\cos(q3), -\sin(q3),
[sin(q3), cos(q3),
                             0, 12*sin(q3)]
    0,
              0,
                              1,
                                             0]
       0,
                   0,
                                             1]
                               0,
[\cos(q2 + q3)*\cos(q1), -\sin(q2 + q3)*\cos(q1), \sin(q1), 12*\cos(q1)*(\cos(q2 + q3))*\cos(q1), \sin(q1), \sin(q1), \sin(q1), \sin(q1)
q3) + cos(q2))]
[\cos(q2 + q3)*\sin(q1), -\sin(q2 + q3)*\sin(q1), -\cos(q1), 12*\sin(q1)*(\cos(q2 + q3)*\sin(q1), -\cos(q1), 12*\sin(q1)*(\cos(q2 + q3)*\sin(q1), -\cos(q1), 12*\sin(q1))]
q3) + cos(q2))]
[
         sin(q2 + q3),
                                  cos(q2 + q3),
                                                       0, 12*sin(q2 + q3) +
 12*sin(q2) + 12
                       0,
                                                 0,
                                                             0,
Γ
              1]
```

Warning: Solutions are only valid under certain conditions. To include parameters and conditions in the solution, specify the 'ReturnConditions' value as 'true'.

```
clear, clc
tic
syms px py pz az ax ay
syms q1 q2 q3
L1 = 13.5
T_12 = 15
L3 = 20
DHParam = [q1 L1 0 pi/2; (pi/2+q2) 0 L2 0; q3 0 L3 0];
[A, T, Q, Rot, Tra] = DH(DHParam, px, py, pz, az);
%assume(q1>-pi & q1<pi & q2>-pi & q2<pi & q3>-pi & q3<pi)
assume(pz>0 & q1<0 & q1 > -pi)% & q2>0 & q3>0)
    EqX = px == simplify(Tra(1));
    EqY = py == simplify(Tra(2));
    EqZ = pz == simplify(Tra(3));
    jointVar = symvar(T);
    %%%%%%%%%%55
% A es el arreglo conteniendo las matrices de transformación de i = 1 a i =
% n. T es la matriz de transformación simplificada, la matriz de cinemática
% directa. Q es un vector conteniendo los resultados para las variables de
% q1 a qn. Rot es la matriz de rotación extraída de T. Y Tra es el ventor
% posición extraído de T.
% syms n_x s_x a_x p_x n_y s_y a_y p_y n_z s_z a_z p_z
% T_syms = [n_x s_x a_x p_x;n_y s_y a_y p_y;n_z s_z a_z p_z;0 0 0 1];
% T1 = (A(:,:,1)) \  \  = A(:,:,2) \  \  A(:,:,3)
    ia = inv(A(:, :, 1));
    ter2 = A(:, :, 2) * A(:, :, 3);
    eq1 = ter2(3,4) == ia(3,1)*px + <math>ia(3,2)*py;
    %q1 = solve(eq1,q1, 'real',true);
    ib = inv(A(:, :, 2))*ia;
    ter1 = A(:, :, 3);
    eq2 = ter1(2,4) == ib(2,1)*px + ib(2,2)*py + ib(2,3)*pz + ib(2,4)*1;
    eq3 = ter1(1,4) == ib(1,1)*px + <math>ib(1,2)*py + ib(1,3)*pz + ib(1,4)*1;
    assume(q2>0 \& q3>0)
    [q2,q3] = solve([eq2,eq3],[q2 q3], 'real', true);
```

```
q1 = atan2(-py,-px); %ajustado a mano para dar órdenes de valores
 negativos
    q2a = eval(q2(1));
    q3a = eval(q3(1));
    q2b = eval(q2(2));
    q3b = eval(q3(2));
    toc
응
     th = [q1,q2,q3];
왕
      th2 = rad2deq(th);
응
응
      th2(1);
응
      th2(2);
      th2(3);
% fun = @(q) norm([Tra(1);Tra(2);Tra(3)]);
L1 =
   13.5000
L2 =
    15
L3 =
    20
     3
[q1, 27/2, 0, pi/2]
[q2 + pi/2, 0, 15, 0]
[q3, 0, 20, 0]
(:,:,1) =
                              0, sin(q1),
                                                             0]
        cos(q1),
                              0, -cos(q1),
        sin(q1),
                                                             0]
                                                          27/2]
[
              0,
                               1,
                                         0,
              0,
                               0,
                                         0,
                                                             1]
(:,:,2) =
```

```
0, 15*cos(q2 + pi/2)]
[\cos(q2 + pi/2), -\sin(q2 + pi/2),
                                       0, 15*sin(q2 + pi/2)]
[\sin(q2 + pi/2), \cos(q2 + pi/2),
[
             0,
                             0,
                                       1,
                                                           0]
[
             0,
                              0,
                                        0,
                                                           1]
(:,:,3) =
                                                20*cos(q3)1
       cos(q3),
                      -sin(q3),
                                       0,
[
                                       0,
                                                  20*sin(q3)]
       sin(q3),
                       cos(q3),
                              0,
[
                                                           01
             0,
                                       1,
[
             0,
                              0,
                                       0,
                                                           1]
[-\sin(q2 + q3)*\cos(q1), -\cos(q2 + q3)*\cos(q1), \sin(q1), -5*\cos(q1)*(4*\sin(q2))]
+ q3) + 3*sin(q2))]
[-\sin(q2 + q3)*\sin(q1), -\cos(q2 + q3)*\sin(q1), -\cos(q1), -5*\sin(q1)*(4*\sin(q2))]
+ q3) + 3*sin(q2))]
[
         cos(q2 + q3),
                             -sin(q2 + q3),
                                                    0, 	 20*cos(q2 + q3) +
15*cos(q2) + 27/2
Γ
                    0,
                                           0,
                                                   0,
                1]
```

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Elapsed time is 44.052097 seconds.