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In [1]: import sympy as smp
import math
from IPython.display import display
from IPython.display import Markdown as md
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In [2]: display(md('../theorems/fundamental_theorem_of_calculus.md'))
display(md('../md/derivatives.md'))
```

# Fundamental Theorem Of Calculus:

If  $f$  is continuous on  $[a, b]$  then the function  $g$  defined by:

$$g(x) = \int_a^x f(t) dt \quad a \leq x \leq b$$

is continuous on  $[a, b]$  and differentiable on  $(a, b)$ , and  $g'(x) = f(x)$

## Derivatives

### Definition of Derivative:

$$\frac{d}{dx}(f(x)) = f'(x) = \lim_{h \rightarrow 0} \frac{f(x+h) - f(x)}{h}$$

### Derivative Rules:

``{admonition}Constant Rule: :class: note

$$\frac{d}{dx}[c] = 0$$

\$\$
\begin{gathered}
\frac{d}{dx} \pi = 0 \quad \frac{d}{dx} \pi = 0 \\
\end{gathered}
\$\$

``{admonition}Power Rule: :class: note

\$\$
\begin{aligned}
\frac{d}{dx} x^n &= nx^{n-1} \\
\end{aligned}
\$\$

$$\frac{d}{dx} n^2 = 2n \quad \frac{d}{dx} \varphi^3 = 3\varphi^2$$

``{admonition}Product Rule: :class: note

$$\frac{d}{dx}[f(x)g(x)] = f'(x)g(x) + f(x)g'(x)$$

```\admonition\Quotient Rule:  
:class: note

\$\$  
\begin{aligned}  
\frac{d}{dx}\left[\frac{f(x)}{g(x)}\right] &= \frac{g(x)f'(x) - f(x)g'(x)}{g(x)^2}  
\end{aligned}  
\$\$  
```\admonition\Chain Rule: :class: note

$$\frac{d}{dx}[f(g(x))] = f'(g(x))g'(x)$$

...