

ANALYTIC SOLUTION OF A CLASS-A TRIODE AMPLIFIER

Complete circuit transfer function

$$\begin{aligned}
 H(f) &= \frac{V_{out}(f)}{V_{in}(f)} = \frac{\rho}{\tau\pi + \mu} = \\
 &= \frac{1}{\theta Z_{Cin} R_b} = \\
 &= \frac{\frac{-1}{R_L} - \lambda\sigma}{\frac{-\xi\delta}{\varepsilon} + \gamma} \left(\frac{\xi}{\theta \varepsilon R_b^2} + \frac{-\xi\chi}{\varepsilon} + \frac{1}{Z_{Cgk}} \right) + \lambda \left(\frac{1}{Z_{Cga}} + \eta \left(\frac{-1}{\theta \varepsilon R_b^2} + \frac{\chi}{\varepsilon} \right) \right) \\
 &= \frac{1}{\left(\frac{-1}{Z_{Cin}} + \frac{-1}{R_g} + \frac{-1}{R_b} \right) Z_{Cin} R_b} = \\
 &= \frac{\frac{-1}{R_L} - \left(1 + \frac{Z_{Co}}{R_L} \right) \left(\beta - \frac{\alpha}{R_a} + \frac{\eta\delta}{\varepsilon} \right)}{\frac{-\xi\delta}{\varepsilon} + \gamma} \left(\frac{\xi}{\left(\frac{-1}{Z_{Cin}} + \frac{-1}{R_g} + \frac{-1}{R_b} \right) \varepsilon R_b^2} + \frac{-\xi\chi}{\varepsilon} + \frac{1}{Z_{Cgk}} \right) + \left(1 + \frac{Z_{Co}}{R_L} \right) \left(\frac{1}{Z_{Cga}} + \eta \left(\frac{-1}{\left(\frac{-1}{Z_{Cin}} + \frac{-1}{R_g} + \frac{-1}{R_b} \right) \varepsilon R_b^2} + \frac{\chi}{\varepsilon} \right) \right) \\
 &= \frac{1}{\left(\frac{-1}{Z_{Cin}} + \frac{-1}{R_g} + \frac{-1}{R_b} \right) Z_{Cin} R_b} = \\
 &= \left(\frac{\frac{-1}{R_L} - \left(1 + \frac{Z_{Co}}{R_L} \right) \left(\frac{1}{Z_{Cga}} + \frac{1}{R_i} + \frac{1}{Z_{Cak}} + \frac{1}{R_a} \right) - \frac{1}{R_a R_a \left(\frac{1}{R_{ps}} + \frac{1}{Z_{Cps}} + \frac{1}{R_a} \right)} + \frac{\left(\frac{-1}{R_i} + \frac{-1}{Z_{Cak}} \right) \left(\frac{-1}{Z_{Cga}} + g_m \right)}{\left(\frac{1}{Z_{Cgk}} + g_m \right)}}{\frac{-\left(\frac{-1}{Z_{Cgk}} - g_m + \frac{-1}{R_i} + \frac{-1}{Z_{Cak}} + \frac{-1}{Z_{Ck} // R_k} \right) \left(\frac{-1}{Z_{Cga}} + g_m \right)} + \left(-gm + \frac{-1}{R_i} + \frac{-1}{Z_{Cak}} \right) \left(\frac{1}{Z_{Cgk}} + g_m \right)} \left(\frac{-1}{Z_{Cgk}} - g_m + \frac{-1}{R_i} + \frac{-1}{Z_{Cak}} + \frac{-1}{Z_{Ck} // R_k} \right) + \frac{-\left(\frac{-1}{Z_{Cgk}} - g_m + \frac{-1}{R_i} + \frac{-1}{Z_{Cak}} + \frac{-1}{Z_{Ck} // R_k} \right) \left(\frac{-1}{Z_{Cga}} + \frac{-1}{R_b} + \frac{-1}{Z_{Cgk}} \right)}{\left(\frac{1}{Z_{Cgk}} + g_m \right)} + \frac{1}{Z_{Cgk}} \right) + \\
 &\quad \left(\left(1 + \frac{Z_{Co}}{R_L} \right) \left(\frac{1}{Z_{Cga}} + \left(\frac{-1}{R_i} + \frac{-1}{Z_{Cak}} \right) \left(\frac{-1}{\left(\frac{-1}{Z_{Cin}} + \frac{-1}{R_g} + \frac{-1}{R_b} \right) \left(\frac{1}{Z_{Cgk}} + g_m \right) R_b^2} + \frac{\left(\frac{-1}{Z_{Cga}} + \frac{-1}{R_b} + \frac{-1}{Z_{Cgk}} \right)}{\left(\frac{1}{Z_{Cgk}} + g_m \right)} \right) \right) \right)
 \end{aligned}$$