On Designing Distributed Auction Mechanisms for Wireless Spectrum Allocation

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Abstract—Auctions are believed to be effective methods to solve the problem of wireless spectrum allocation. Existing spectrum auction mechanisms are all centralized and suffer from several critical drawbacks of the centralized systems, which motivates the design of distributed spectrum auction mechanisms. However, extending a centralized spectrum auction to a distributed one broadens the strategy space of agents from one dimension (bid) to three dimensions (bid, communication, and computation), and thus cannot be solved by traditional approaches from mechanism design. In this paper, we propose two distributed spectrum auction mechanisms, namely distributed VCG and FAITH. Distributed VCG implements the celebrated Vickrey-Clarke-Groves mechanism in a distributed fashion to achieve optimal social welfare, at the cost of exponential communication overhead. In contrast, FAITH achieves sub-optimal social welfare with tractable computation and communication overhead. We prove that both of the two proposed mechanisms achieve faithfulness, *i.e.*, the agents' individual utilities are maximized, if they follow the intended strategies. Besides, we extend FAITH to adapt to dynamic scenarios where agents can arrive or depart at any time, without violating the property of faithfulness. We implement distributed VCG and FAITH, and evaluate their performance in various setups. Evaluation results show that distributed VCG results in optimal allocation, while FAITH is more efficient in computation and communication.

Index Terms—Wireless Network, Spectrum Allocation, Game Theory, Distributed Algorithmic Mechanism Design, VCG Mechanism, Faithfulness

1 Introduction

The naturally limited radio spectrum is becoming increasingly scarcer due to the fast development of wireless technology. Unfortunately, traditional static spectrum allocation approaches are expensive and inefficient, causing newly emerged wireless services and applications unable to meet their demands for spectrum [1]. To tackle the limitations of traditional spectrum allocations, secondary spectrum market has been widely adopted where spectrum owners (*i.e.*, primary users) can sell or lease idle spectrum to wireless applications (*i.e.*, secondary users). Auctions have become natural choices for the secondary market due to their fairness and efficiency [2].

In recent years, a number of spectrum auction mechanisms (*e.g.*, [2]–[11]) have been proposed. These mechanisms achieve some attractive properties, such as strategy-proofness and approximate social welfare. Here, intuitively, strategy-proofness means that one can maximize her payoff by truthfully revealing her private valuation on the spectrum; social welfare means the sum of auction winners' val-

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uations on the allocated spectrum. However, these existing spectrum auction mechanisms have to rely on a centralized and trusted authority to perform as an auctioneer and to process the auction procedures.

The centralized spectrum auction mechanisms have several critical drawbacks [12]. The first is that the functionality of the centralized mechanisms is based on the assumption that there exists a trusted central authority. But in practice, especially in the secondary spectrum market for wireless networks, a trusted central authority may not always exist. The second drawback is that the scalability of the centralized spectrum auctions can be poor. Since the centralized mechanisms usually need an auctioneer to collect all the bids in order to calculate the auction outcome, the agents need reliable ways to deliver their bids to the auctioneer. Unfortunately, such communication channels may not always exist between the auctioneer and the agents in wireless networks, especially when the wireless network is not fully connected. The third drawback, which is not only limited to spectrum auction mechanisms, but also applies to centralized systems in general, is robustness. Once the central authority breaks down, the entire system collapses.

To tackle the above drawbacks of the centralized spectrum auction mechanisms, we propose to implement distributed spectrum auction mechanisms. However, designing a distributed spectrum auction mechanism is much more challenging due to the following three reasons.

Most of all, without the management of a central authority, the roles of agents are now two-fold. They need not only to compete with each other for the wireless spectrum (as they do in centralized mechanisms), but also to cooperate in determining the outcome of the auction. This greatly broad-

ens the strategy space of the agents from *one dimension* (*i.e.*, bid reporting) to *three dimensions* (*i.e.*, bid reporting, message passing, and computation) [13], and thus are beyond the scope of traditional mechanism design perspective.

Second, unlike conventional goods, wireless spectrum can be spatially reused by multiple agents as long as their transmissions do not reduce each other's Signal to Interference and Noise Ratio (SINR) below a predefined threshold. Such a unique property makes it computationally intractable when calculating an optimal spectrum allocation for a large scale wireless network, even in a centralized manner. Due to lack of global information of inter-agent interferences, optimizing the spectrum allocation with local knowledge in a distributed wireless network is really challenging.

Third, due to wireless devices' limited computation capability and communication bandwidth, traditional secure multiparty computation cannot be directly applied, given its high computation and communication overhead. Therefore, the problem of designing a manipulation-resistant distributed auction mechanism need to be carefully considered.

In this paper, we consider the spectrum allocation problem from the perspective of distributed algorithmic mechanism design (DAMD) [12], and adopt the solution concept of faithfulness to characterize three-dimensional manipulationproofness of distributed mechanisms. We propose two complementary distributed auction mechanisms, i.e., distributed VCG and FAITH. Distributed VCG is an extension of the celebrated Vickrey-Clarke-Groves (VCG) mechanism [14]–[16] to the distributed scenario. It collects bidding information bottom-up based on a carefully constructed pseudo-tree, and disseminates the optimal allocation top-down following the same tree structure. The payment for using the allocated spectrum is determined in the VCG manner. However, the optimal spectrum allocation is achieved at the cost of high communication overhead. Therefore, distributed VCG can only work in sparse secondary spectrum markets. Then, we present FAITH, which achieves sub-optimal spectrum allocation with bounded computation and communication overhead in general cases. We further extend FAITH to adapt dynamic network scenarios where agents may arrive and departure at any time. Our analysis shows that all the three proposed mechanisms are faithfulness.

Our main contributions are listed as follows.

- To the best of our knowledge, we are the first to consider the problem of distributed algorithmic mechanism design for secondary wireless spectrum markets. We extend the celebrated VCG mechanism to a distributed scenario, and prove that our extension is a faithful implementation of spectrum auction mechanism, achieving optimal social welfare.
- Second, we propose a more practical and efficient faithful distributed spectrum auction mechanism, called FAITH, which achieves sub-optimal social welfare with bounded computation and communication overhead.
- Third, we further extend FAITH to adapt to a dynamic network environment, where agents can arrive at and depart from the spectrum market at any time. Extended FAITH also achieves faithfulness with low communication overhead.

 Finally, we implement distributed VCG and FAITH, and extensively evaluate their performance in various topologies. Our evaluation results well demonstrate the properties of distributed VCG and FAITH.

The rest of the paper is organized as follows. In Section 2, we present the technical preliminaries, including the auction model and solution concepts. The distributed VCG and FAITH are presented in Section 3 and Section 4, respectively. Then, we extend FAITH to adapt to a dynamic environment in Section 5. In Section 6, we present further discussions on our proposed mechanisms. In Section 7, we evaluate distributed VCG and FAITH, and present evaluation results. We briefly review related work in Section 8. Finally, we conclude this paper in Section 9.

2 PRELIMINARIES

In this section, we describe our auction model for wireless spectrum allocation, and present related solution concepts.

2.1 Model of Distributed Spectrum Auction

We model the problem of channel allocation in the secondary spectrum market as a distributed auction, in which there are a number of orthogonal channels to be leased out and a set of channel buyers, called *agents*, who want to lease the channels to serve their subscribers and make profits. Multiple agents can share the same channel as long as they do not interfere with each other [17]. Without the control of an auctioneer, a distributed auction is conducted by the autonomous and rational agents themselves in the secondary spectrum market. The objective of this auction is to efficiently select winners among the agents satisfying their interference constraints, and also to prevent the agents from manipulating the auction outcome.

Specifically, we consider a set $\mathbb{C}=\{c_1,c_2,\ldots,c_m\}$ of orthogonal and homogeneous channels. Information of the channels is public and known to the agents. Each channel can be simultaneously allocated to multiple non-conflicting agents, *i.e.*, they can provide services to their subscribers simultaneously with an adequate SINR. Following the conventions of spectrum allocation auction [9], [10], [18], the interference between the agents is represented by a *conflict graph*, where an edge between two nodes/agents represents channel inference between them. An example of conflict graph is shown in Fig. 1(a). We assume that a practical conflict graph has already been measured with techniques such as [10], and the underlying distributed system/application has informed each agent of her neighbors. Other alternative interference models will be discussed in Section 6.3.

We assume that the agents in one auction belong to the same connected component in the conflict graph. For a conflict graph with multiple connected components, each connected component can conduct an independent distributed spectrum auction. We also assume that conflicting agents can communicate with each other through a commonly known control channel, *i.e.*, the communication range of the agents on the control channel is larger than the interference range of them on working channels. This is backed by the existing communication protocols, *e.g.*, the communication

range of IEEE 802.11b at a data rate of 1Mbps is normally larger than the interference range of IEEE 802.11n at 150Mbps.

We also consider a set $\mathbb{A} = \{a_1, a_2, \dots, a_n\}$ of agents. Each agent $a_i \in \mathbb{A}$ has a per-channel valuation v_i , which is commonly known as type in the literature and is private to the agent herself. In a distributed auction, a_i needs to report her per-channel bid b_i to other agents. We note that rational agents a_i may cheat her bid $b_i \neq v_i$ in order to win the spectrum auction. The agent a_i also has a strict demand of d_i channels. Any winning agent a_i has to pay p_i for allocated channel(s). We define the utility of agent a_i to be the difference between her total valuation and payment, i.e., $u_i \triangleq d_i \times v_i - p_i$. Similar to papers [12], [19]–[22], we assume that there is a Credit Clearance Service (CCS), who neither participates in the auction to determine the allocation and payment, nor needs to be always online during the auction. In distributed VCG, the CCS only collects the payments from the agents through an intermittently connected wireless overlay network. In FAITH, the CCS subtly controls agents' manipulated strategies on computation and communication by conducting an audit process.

In this paper, we consider that the agents are rational but helpful, meaning that although self-interested, each of the agents follows the prescriptions of the spectrum auction mechanism, if no unilateral deviation can lead to a better utility. We assume that there is no collusion among the agents, and tend to leave the design of collusion-resistant mechanisms to our future work.

In contrast to the agents' individual objectives, the overall objective of the spectrum auction is to maximize social welfare (SW), which is the sum of each winning agent a_i 's valuation v_i on her allocated channel(s), *i.e.*,

$$SW \triangleq \sum_{a_i \in \mathbb{W}} (d_i \times v_i),$$

where $\mathbb{W} \subseteq \mathbb{A}$ is the set of winners.

2.2 Solution Concepts

Given the auction model, we review some important solution concepts used in this paper. First, we recall the definition of *distributed mechanism*.

Definition 1 (Distributed Mechanism [12], [23]). A distributed mechanism $\mathcal{M} = (\Sigma, \mathbf{s}^M, g)$ defines a feasible strategy space of agents $\Sigma = \Sigma_1 \times \Sigma_2 \times \ldots \times \Sigma_n$, a prescribed strategy profile $\mathbf{s}^M = (s_1^M, s_2^M, \ldots, s_n^M) \in \Sigma$, and a determination rule $g: \Sigma \to \mathcal{K}$ executed by the mechanism, where \mathcal{K} is the set of possible outcomes.

For any agent a_i , her prescribed strategy $s_i^M \in \Sigma_i$ is composed of three sub-strategies, i.e., information-revelation strategy, message-passing strategy, and computation strategy [23].

Definition 2 (IC, CC, AC [23]). A distributed mechanism achieves IC (resp. CC, AC) if no agent can gain higher utility by deviating from her prescribed information-revelation strategy (resp. message-passing strategy and computation strategy) in an equilibrium.

Definition 3 (Dominant Strategy Equilibrium [24]). A strategy profile s^* is a dominant strategy equilibrium, if for any agent

i, any strategy $s_i' \neq s_i^*$, and any other agents' strategy profile s_{-i} , we have

$$u_i(g(s_i^*, s_{-i})) \ge u_i(g(s_i', s_{-i})).$$

Dominant strategy equilibrium is a strong solution concept achieved in some traditional centralized auction mechanisms, *e.g.*, Vickrey-Clarke-Groves (VCG) mechanism [14]–[16]. However, it may not be achieved in distributed settings due to the agents' three-dimensional manipulations. Therefore, we turn to seek for ex-post Nash equilibrium, which is a weaker but effective solution concept in game theory.

Definition 4 (Ex-Post Nash Equilibrium [12], [13]). A strategy profile s^* is an ex-post Nash equilibrium of a distributed mechanism, if for any agent a_i , any $s_i' \neq s_i^*$, we have

$$u_i(g(s_i^*, \mathbf{s}_{-i}^*)) \ge u_i(g(s_i', \mathbf{s}_{-i}^*)).$$

We now introduce the concept of faithful implementation.

Definition 5 (Faithful Implementation [13], [23]). A distributed mechanism $\mathcal{M} = (\Sigma, \mathbf{s}^M, g)$ is a faithful implementation of outcome $g(\mathbf{s}^M)$ when prescribed strategy profile \mathbf{s}^M is an ex-post Nash equilibrium.

Intuitively, under a faithful distributed mechanism, the agents' individual utilities are maximized, if they follow the prescribed strategies.

3 DISTRIBUTED VCG

In this section, we present a distributed implementation of the celebrated VCG auction mechanism. We first briefly review the concept of VCG mechanism.

Definition 6 (VCG mechanism [14]–[16]). A mechanism (f, p_1, \ldots, p_n) is a Vickrey-Clarke-Groves (VCG) mechanism if

- Outcome function $f:(v_1,\ldots,v_n)\to\mathcal{K}$, ends up with $\mathbf{k}^*=argmax_{\mathbf{k}\in\mathcal{K}}\sum_i v_i(\mathbf{k})$, where \mathcal{K} is the set of possible outcomes.
- Payment function $p_i(v_1,\ldots,v_n)=h_i(\boldsymbol{v}_{-i})-\sum_{j\neq i}v_j(\boldsymbol{k}^*)$, where $h_i:V_{-i}\to\mathcal{R}$ (i.e., h_i does not depend on v_i).

We note that the outcome function of VCG outputs the optimal channel allocation k^* , and the payment of each agent a_i is calculated independent of a_i .

3.1 Design Rationale

To prevent the agents' manipulations, our distributed VCG mechanism is based on the *partition principle* proposed by [23]. Intuitively, the calculation process of each agent's payment is separated from the agent, s.t., each agent cannot influence the calculation of her payment. Thus, it is in the best interest of every agent to follow the suggested protocol to calculate the optimal channel allocation outcome k^* (detailed proof is in Section 3.5).

To implement the VCG mechanism in a distributed manner, we also need a distributed algorithm to calculate the optimal spectrum allocation. One possible approach is to employ the algorithm of Distributed Pseudo-tree Optimization Procedure (DPOP) [25], which is the state-ofthe-art solution to the distributed constrained optimization problem [26]. However, the original DPOP algorithm cannot

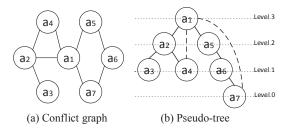


Fig. 1: Pseudo-Tree Construction

handle the agents' multi-channel requests and does not take the spatial reusability of spectrum into consideration, thus it cannot be directly applied to the spectrum allocation scenarios. To address the limitations of the original DPOP algorithm, we extend the original DPOP algorithm by (1) proposing a concept of "constraint view" to handle the agents' multi-channel requests, and (2) reconstructing the conflicting graph into a pseudo-three to facilitate the search of optimal channel assignment. After that, the payment calculation of every agent can be implemented using our extended DPOP algorithm on a modified graph.

In this section, we propose the design of our distributed VCG mechanism, which has three phases: pseudo-tree construction, channel assignment, and payment determination.

3.2 Pseudo-Tree Construction

Before running the channel assignment algorithm, we first construct a pseudo-tree from the conflict graph, *s.t.*, we can exploit the problem structure of channel allocation to detect independent subproblems that can be solved separately. A pseudo-tree [27] of a graph is an arrangement of the graph with the property that adjacent vertices fall in the same branch of the tree. The relative independence of nodes lying in different branches of the pseudo-tree facilitates parallel searches for global optimal result [28], [29]. It is known that a Depth-First Search (DFS) tree is a pseudo-tree (though the inverse may not hold [25]). Fig. 1 shows an example of the pseudo-tree construction, where Fig. 1(b) is a pseudo-tree constructed from the conflict graph shown in Fig. 1(a).

The pseudo-tree consists of tree edges, shown as solid lines, and back edges, shown as dashed lines. For each agent a_i in the pseudo-tree, her parent $P(a_i)$ and children $C(a_i)$ are the set of agent(s) that are located in higher and lower levels than a_i respectively and directly connected to a_i through tree edges. We further define $PP(a_i)$ and $PC(a_i)$ as the set of pseudo parents and pseudo children of agent a_i , respectively. In contrast, an agent is connected to her pseudo parents and pseudo children through back edges. For example, in Fig. 1(b), agent a_1 has 2 children and 2 pseudo children, i.e., $C(a_1) = \{a_2, a_5\}$ and $PC(a_1) = \{a_4, a_7\}$. Agent a_7 has a parent and a pseudo parent, i.e., $P(a_7) = \{a_6\}$ and $PP(a_7) = \{a_1\}$.

To construct a pseudo-tree in a distributed manner, we can employ a distributed DFS tree construction protocol (e.g., [30], [31] with polynomial time and space complexity). We note that there are multiple pseudo-trees that can be constructed by applying a given distributed DFS tree construction protocol. However, no matter which pseudo-tree is constructed, our following algorithm for channel assignment can derive an allocation profile with optimal

```
Algorithm 1: Social Welfare Aggregation (a_i)
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```
1 if C(a_i) = \emptyset and P(a_i) \neq \emptyset then
          CV(a_i) \leftarrow P(a_i) \cup PP(a_i);
 2
 3
          foreach k_{CV(a_i)} \in \Pi_{j \in CV(a_i)} D_j do
                SW_i(CV(a_i): \boldsymbol{k}_{CV(a_i)}) \leftarrow
                max_{k_i \in D_i} \left( v_i(a_i : k_i, CV(a_i) : \mathbf{k}_{CV(a_i)}) \right);
          Send SW_i to P(a_i);
 5
   else
 6
          if C(a_i) \neq \emptyset and P(a_i) \neq \emptyset then
                Collect aggregation messages \{SW_j|j \in C(a_i)\};
                Extract CV(a_i) from received SW messages;
 9
                foreach k_{CV(a_i)} \in \prod_{j \in CV(a_i)} D_j do
10
                      SW_i(CV(a_i): \boldsymbol{k}_{CV(a_i)}) \leftarrow
11
                     \max_{k_i \in D_i} \left( v_i(a_i : k_i, CV(a_i) : \boldsymbol{k}_{CV(a_i)}) + \sum_{a_j \in C(a_i)} SW_j(a_i : k_i, CV(a_i) : \boldsymbol{k}_{CV(a_i)}) \right);
                Send SW_i to agents in P(a_i);
```

social welfare. Due to limitations of space, we do not present here a detailed algorithm for constructing a pseudo-tree. We assume that the pseudo-tree has already been constructed and every agent has known her parent, children, pseudo parents, pseudo children, and their levels in the pseudo-tree.

3.3 Channel Assignment

Our channel assignment algorithm consists of two phases: a bottom-up *social welfare aggregation* and a top-down *channel choice propagation*. The former one aggregates the social welfare achieved by each subtree to calculate the optimal social welfare, while the latter let each agent select her channel allocation based on her parent's and pseudo-parents' channel selections. Our algorithm supports both single-channel demands and multi-channel demands. For clarity of presentation, we only discuss single-channel demands here, *i.e.*, $\forall a_i \in \mathbb{A}, d_i = 1$. In this case, agents' selection domains are the same, *i.e.*, $\forall a_i \in \mathbb{A}, D_i = \{c_1, c_2, \dots, c_m, NULL\}$. We put NULL in agents' selection domains, *s.t.*, agents can choose nothing when they do not want to lease any channel.

Here, we define agent a_i 's constraint view $CV(a_i)$ to be the set of a_i 's parent, a_i 's pseudo parents, and any other agent satisfying the following two conditions: (1) having higher level than a_i and (2) having a pseudo child located in the subtree rooted at a_i (e.g., $CV(a_4) = \{a_1, a_2\}$ and $CV(a_6) = \{a_1, a_5\}$). The constraint view of each agent will be obtained in the follow-up social welfare aggregation phase. In our algorithm, " $a_i: k_i$ " means "when a_i is allocated k_i " and $v_i(a_i: k_i, a_j: k_j)$ is a_i 's valuation over the channel allocation that a_i is allocated k_i and a_j is allocated k_j , where $k_i \in D_i$ and $k_j \in D_j$. Note that a_i 's valuation function equals a_i 's per-channel valuation v_i when and only when a_i is allocated a channel and none of a_i 's neighbors are allocated the same channel.

3.3.1 Social Welfare Aggregation

The bottom-up social welfare (SW) aggregation, as shown in Algorithm 1, starts from leaf agents of the pseudo-tree and goes up towards the root following tree edges. For

Algorithm 2: Choice Propagation (a_i)

```
1 if P(a_i) = \emptyset then
         k_i^* \leftarrow argmax_{k_i \in D_i} \sum_{a_x \in C(a_i)} SW_x(a_i : k_i);
Send choice message \langle a_i, k_i^* \rangle to agents in C(a_i);
3
4
   else
         Collect choice message from P(a_i);
5
         Extract CV(a_i)'s channel assignment k_{CV(a_i)}^*;
6
         k_i^* \leftarrow argmax_{k_i \in D_i} SW_i(a_i : k_i, CV(a_i) : k_{CV(a_i)}^*);
7
         foreach a_j \in C(a_i) do
8
               Extract CV(a_j)'s channel assignment k_{CV(a_j)}^*;
               Send choice message \langle CV(a_j), \boldsymbol{k}_{CV(a_j)}^* \rangle to a_j;
10
```

agent a_i , SW_i is the set of possible optimal social welfare that can be achieved by the subtree rooted at a_i , under each possible channel assignment of $CV(a_i)$. After collecting social welfare messages from her children, an agent can compose her aggregation message, and, if she is not the root, send it to her parent.

For a leaf agent a_i , if $P(a_i) = \{a_j\}$ and $PP(a_i) = \varnothing$, then $CV(a_i) = \{a_j\}$ and the social welfare that can be achieved at a_i would only depend on her parent a_j . Thus the SW_i sent from a_i to a_j would be a vector of the optimal social welfare that can be achieved at a_i , under each possible channel assignment of a_j . However, if $PP(a_i) \neq \varnothing$, then $CV(a_i) = \{a_j\} \cup PP(a_i)$ and the social welfare that can be achieved at a_i , would depend on both her parent and pseudo parents. Thus, the SW_i would be a hypercube of $1 + |PP(a_i)|$ dimensions (one dimension for parent and the other $|PP(a_i)|$ for pseudo parents) of the tuple $\langle P(a_i), PP(a_i) \rangle$.

For an intermediate agent a_i , the social welfare that can be achieved by the subtree rooted at a_i would be constrained by agents in her constraint view. After receiving all the SW messages from her children, an intermediate agent can examine the SW messages and get her children's constraint views and then extract her own constraint view $CV(a_i)$. After that, under each possible channel assignment of $CV(a_i)$, say $\mathbf{k}_{CV(a_i)}$, a_i calculates the optimal social welfare that can be achieved by the subtree rooted at a_i , which is $SW_i(CV(a_i): \mathbf{k}_{CV(a_i)})$.

3.3.2 Choice Propagation

The top-down choice propagation, as shown in Algorithm 2, starts from root agent and moves towards the leaves. After receiving all the SW messages, the root agent calculates the overall social welfare under each of her own channel choices, then picks the optimal choice, and sends her choice message down to her children. For any non-root agent a_i , based on the received choice message from her parent, a_i picks her own channel choice k_i^* that maximizes the social welfare for the subtree rooted at a_i , and sends the decision down to her children. The choice message received by a_i from $P(a_i)$, contains not only her parent's choice, but also the choices of other agents in $CV(a_i)$.

When all the leaf agents have made their choices, the algorithm terminates. The channel assignment outcome $\mathbf{k}^* = (k_1^*, k_2^*, \dots, k_n^*)$, where $k_i^* \in D_i$, is the one that maximizes the overall social welfare.

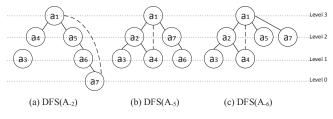


Fig. 2: DFS (A_{-i})

3.4 Payment Determination

After determining the optimal channel assignment k^* , we calculate the payment for each winner. We set $h_i(v_{-i})$ in VCG payment function to $\max_{k \in \mathcal{K}} \sum_{j \neq i} v_j(k)$, then the payment of agent a_i is

$$p_i = max_{\mathbf{k} \in \mathcal{K}} \sum_{j \neq i} v_j(\mathbf{k}) - \sum_{j \neq i} v_j(\mathbf{k}^*).$$

We define ${m k}_{-i}^* = argmax_{{m k} \in \mathcal{K}} \sum_{j \neq i} v_j({m k})$, then

$$p_i = \sum_{j \neq i} v_j(\mathbf{k}_{-i}^*) - \sum_{j \neq i} v_j(\mathbf{k}^*) = \sum_{j \neq i} (v_j(\mathbf{k}_{-i}^*) - v_j(\mathbf{k}^*)).$$

From the above payment scheme, we observe that the agent a_i 's payment can be calculated without a_i . We define DFS(A) as the DFS tree constructed from the conflict graph with all the agents A, and DFS(A_{-i}) as the DFS tree with the agent a_i being removed from the original conflict graph. To calculate payment for a_i , we first exclude a_i from the conflict graph and create DFS(\mathbb{A}_{-i}) by modifying DFS(\mathbb{A}): the highest descendant of a_i that has a back edge with an ancestor of a_i turns the back edge into a tree edge. If such descendant does not exist, we exclude a_i and her adjacent edges. For example, Fig. 2 shows the DFS(A_{-2}), $\mathrm{DFS}(A_{-5})$ and $\mathrm{DFS}(A_{-6})$ after agent a_2 , a_5 and a_6 are removed respectively from Fig. 1(b). Then, we run channel assignment algorithm on modified DFS(\mathbb{A}_{-i}) to get k_{-i}^* . If excluding a_i causes more connected components, then we run channel assignment algorithm on each connected component once. Afterwards, each agent $a_i \neq a_i$ is asked to report $v_j(\mathbf{k}_{-i}^*) - v_j(\mathbf{k}^*)$ to the CCS, who then extracts payments from agents' accounts. We run this procedure for each $a_i \in W$, where W is the set of winners, thus |W| times, to calculate payments for all agents.

3.5 Mechanism Analysis

Theorem 1. The proposed distributed VCG mechanism is a faithful implementation.

Proof. When agents follow the prescribed strategies $s^* = (s_1^*, \ldots, s_n^*)$, the optimal allocation k^* can be achieved, then for any agent a_i , a_i 's utility is

$$\begin{split} u_i(g(s_i^*, \boldsymbol{s}_{-i}^*)) &= v_i(\boldsymbol{k}^*) - p_i \\ &= v_i(\boldsymbol{k}^*) - \sum_{j \neq i} v_j(\boldsymbol{k}_{-i}^*) + \sum_{j \neq i} v_j(\boldsymbol{k}^*) \\ &= \sum_{j \in \mathbb{A}} v_j(\boldsymbol{k}^*) - \sum_{j \neq i} v_j(\boldsymbol{k}_{-i}^*). \end{split}$$

If agent a_i personally chose to deviate from s_i^* to $s_i' \neq s_i^*$, then the channel assignment outcome may change to \mathbf{k}' . Since \mathbf{k}^* maximizes social welfare, then $\sum_{i \in \mathbb{A}} v_i(\mathbf{k}') \leq$

 $\sum_{j\in\mathbb{A}} v_j(\boldsymbol{k}^*)$. We also note that a_i 's payment would not be influenced by her manipulation, then a_i 's utility under this situation is

$$u_{i}(g(s'_{i}, \boldsymbol{s}_{-i}^{*})) = \sum_{j \in \mathbb{A}} v_{j}(\boldsymbol{k}') - \sum_{j \neq i} v_{j}(\boldsymbol{k}_{-i}^{*})$$

$$\leq \sum_{j \in \mathbb{A}} v_{j}(\boldsymbol{k}^{*}) - \sum_{j \neq i} v_{j}(\boldsymbol{k}_{-i}^{*}) = u_{i}(g(s_{i}^{*}, \boldsymbol{s}_{-i}^{*}))$$

which means that under the prescribed strategy profile, following the prescribed strategy maximizes one's utility. Thus the strategy profile is an ex-post Nash equilibrium and the distributed VCG is a faithful distributed mechanism.

We also note that the number of messages that distributed VCG produces is polynomial but the size of the largest message produced is exponential to the largest $|CV(a_i)|, \forall a_i \in \mathbb{A}$.

4 FAITH

In this section, we propose a more practical distributed spectrum auction, namely FAITH, to incentivize the rational agents towards an efficient spectrum allocation in expost Nash equilibrium. FAITH overcomes the computation and communication intractability of the distributed VCG spectrum auction, and thus can be extended to large scale spectrum markets.

4.1 Design Rationale

In most of the strategy-proof centralized spectrum auctions, an auctioneer sorts the agents in a non-increasing order of bids, greedily allocates channels to agents without violating the conflict constraints, and charges each winning agent with *critical price* [32]. The greedy allocation guarantees the feasibility of the algorithm, while the critical price-based payment schemes ensures the strategy-proofness. Based on this rationale, for each agent a_i , we divide the set of her neighbors \mathbb{N}_i into *preemptive neighbor* set $\mathbb{PN}_i = \{a_j | a_j \succ a_i, a_j \in \mathbb{N}_i\}$ and *feedback neighbor* set $\mathbb{FN}_i = \{a_j | a_i \succ a_j, a_j \in \mathbb{N}_i\}$. We note that \succ defines a priority order, *i.e.*, $a_i \succ a_j$, if $b_i > b_j$, or $b_i = b_j$ and a_i has a smaller index than a_j , where b_i is a_i 's per-channel bid.

The greedy allocation strategy of the centralized spectrum auctions indicates that in distributed scenarios, an agent's channel allocation is only affected by her preemptive neighbors, and her allocation will directly influence the channel selections of her feedback neighbors. Thus propagating and gathering information in a well-designed order can enable the agents to determine their channel allocations in a fully distributed way.

Although the property of incentive compatibility can be achieved by enforcing the critical price-based payment scheme, simply allowing the agents themselves to handle the whole auction decision process may give them opportunities to manipulate the auction outcome by deviating from their prescribed computation and communication actions. Therefore, besides incentive compatibility, a distributed auction should also resist agents' manipulations in communication and computation. We observe that in a distributed spectrum auction, the computation and communication of an agent can be responded and confirmed by at least one of

her neighbors, *i.e.*, every agent acts both as a principal for herself, and as a witness for all of her neighbors. Exploiting agents' dual roles can provide necessary information for the CCS to verify agents' behaviors and to enable a "catch and punish" scheme (*i.e.*, check the consistency of the information and penalize a deviation with a fine much heavier than what one can gain).

4.2 Design Details

FAITH has two phases: (1) Bid Exchange and (2) Channel Selection and Payment Calculation. Agents carry out the two phases autonomously and independently without the participation of any centralized party.

4.2.1 Bid Exchange

In this phase, the agents exchange bid statement messages (MSGBs) with neighbors to get local bidding information. Each agent $a_i \in \mathbb{A}$ sends her bid statement message, which is formatted as

$$MSGB_i = \langle BID, i, b_i, d_i \rangle$$

to all of her neighbors \mathbb{N}_i . Upon receiving a bid statement message MSGB_j from a neighbor a_j , agent a_i adds agent a_j into her preemptive neighbor set \mathbb{PN}_i , if $a_j \succ a_i$; otherwise, a_i adds a_j into her feedback neighbor set \mathbb{FN}_i . After the bid exchange phase, each of the agents gets her preemptive neighbor set and feedback neighbor set.

4.2.2 Channel Selection and Payment Calculation

Although logically separated, the processes of channel selection and payment calculation can be integrated together in order to reduce the number of messages involved in the distributed spectrum auction mechanism. The pseudo-code of this integrated process is shown in Algorithm 3.

We start from describing the distributed channel selection algorithm based on the locally collected bidding information, and then specify how to combine information needed for payment calculation.

In the process of channel selection, each agent a_i uses channel selection message (MSGC) to inform neighbors of her selected channel set \mathbb{C}_i^* , in the format as

$$MSGC_i = \langle CHL, i, \mathbb{C}_i^* \rangle$$
.

As discussed in Section 4.1, the channel selection of one agent is only affected by the selection of her preemptive neighbors. Thus, agent a_i first collects MSGCs from her preemptive neighbors in \mathbb{PN}_i , and updates her available channel set \mathbb{AC}_i by deactivating the channels that are already selected by her preemptive neighbors (Lines 2 to 7). Then, if there are enough channels left, she selects the first d_i channel(s) from \mathbb{AC}_i as her own selected channel set

$$\mathbb{C}_i^* \leftarrow \operatorname{First}(\mathbb{AC}_i, d_i).$$

If $\mathbb{C}_i^* \neq \emptyset$, then a_i is a winning agent (Lines 8 to 11).

The next step is to calculate each winning agent's payment. We employ the critical price as winning agent a_i 's payment, *i.e.*, the minimum price for a_i to win in the spectrum auction. In our cases, a_i 's critical price is the bid of her critical neighbor a_j , where if a_i bids lower than a_j , a_i will

Algorithm 3: Channel Selection and Payment Calculation (a_i)

```
1 \mathbb{N}'_i \leftarrow \emptyset, \mathbb{AC}_i \leftarrow \mathbb{C}, p_i = 0;
 2 foreach a_j \in \mathbb{PN}_i do
            Receive MSG_j from agent a_j;
            foreach MSGP_k = \langle PAY, k \rangle in MSG_i do
              \mid \mathbb{N}'_i \leftarrow \mathbb{N}'_i \cup \{a_k\};
            Extract MSGC_j = \langle CHL, j, \mathbb{C}_i^* \rangle from MSG_j;
           \mathbb{AC}_i \leftarrow \mathbb{AC}_i \backslash \mathbb{C}_i^*;
 s if |\mathbb{AC}_i| \geq d_i then
            \mathbb{C}_i^* \leftarrow \operatorname{First}(\mathbb{AC}_i, d_i);
           MSGC_i \leftarrow < CHL, i, \mathbb{C}_i^* >, MSGP_i \leftarrow < PAY, i >;
11 else \mathbb{C}_i^* \leftarrow \emptyset;
12 foreach a_k \in \mathbb{N}_i' do
            \mathbb{AC}_{i|-k} \leftarrow \mathbb{C};
13
            foreach a_j \in \mathbb{PN}_i do
14
                   Extract MSGR_{j,k} = \langle RPY, j, k, \mathbb{C}_{j|-k} \rangle from
15
                   MSG_j
                   if MSGR_{j,k} exists then \mathbb{AC}_{i|-k} \leftarrow \mathbb{AC}_{i|-k} \setminus \mathbb{C}_{j|-k};
16
                  else \mathbb{AC}_{i|-k} \leftarrow \mathbb{AC}_{i|-k} \setminus \mathbb{C}_{j}^{*};
17
            if |\mathbb{AC}_{i|-k}| \geq d_i then \mathbb{C}_{i|-k} \leftarrow \mathrm{First}(\mathbb{AC}_{i|-k}, d_i);
18
            else \mathbb{C}_{i|-k} \leftarrow \emptyset;
19
            MSGR_{i,k} \leftarrow < \overrightarrow{RPY}, i, k, \mathbb{C}_{i|-k} >;
20
            MSGR_i \leftarrow MSGR_i \mid\mid MSGR_{i,k}
21
           MSGP_i \leftarrow MSGP_i \parallel MSGP_k;
22
     Send MSG_i \leftarrow MSGC_i \parallel MSGP_i \parallel MSGR_i to \mathbb{N}_i;
     if \mathbb{C}_i^* \neq \emptyset then
24
            Sort agents in \mathbb{F}\mathbb{N}_i in decreasing order of bids as \overline{\mathbb{F}\mathbb{N}}_i;
25
            foreach a_i \in \overline{\mathbb{FN}}_i do
                   Receive MSG_j from agent a_j;
27
                   Extract < RPY, j, i, \mathbb{C}_{j|-i}^- > from MSG_j;
28
                   \mathbb{AC}_i \leftarrow \mathbb{AC}_i \setminus \mathbb{C}_{j|-i};
29
                   if |\mathbb{AC}_i| < d_i then p_i \leftarrow b_j \times d_i; break;
31 Return \mathbb{C}_i^* and p_i;
```

not be allocated, and if a_i bids higher than a_j , a_i will be allocated. Since a_i cannot influence the channel selection of her preemptive neighbors, a_i 's critical neighbor (if exists) must be one of her feedback neighbors. Thus, to calculate a_i 's payment, a_i 's feedback neighbors are required to provide necessary information, which is their channel selection if the agent a_i does not participate in the spectrum auction. Each winning agent a_i sends a payment determination request message

$$MSGP_i = < PAY, i >$$

to her feedback neighbors (Line 10). Since the channel selection of a_i 's feedback neighbors can be affected by those agents that do not directly connect to a_i , the payment determination request message $MSGP_i$ may need to be further forwarded (Line 21). We note that the total number of forwarding is bounded by the number of agents.

Upon receiving a payment determination request message $MSGP_k$, agent a_i first checks whether there are sufficient channels left, given her preemptive neighbors' selection if agent a_k does not participate in the spectrum auction, *i.e.*,

$$\mathbb{AC}_{i|-k} \leftarrow \mathbb{C} - \bigcup_{j \in \mathbb{PN}_i} \mathbb{C}_{j|-k},$$

where $\mathbb{C}_{j|-k}$ denotes agent a_j 's channel selection if agent a_k

is absent from the auction (Lines 14 to 17). If $|\mathbb{AC}_{i|-k}| \geq d_i$, agent a_i sets $\mathbb{C}_{i|-k} \leftarrow \mathrm{First}(\mathbb{AC}_{i|-k}, d_i)$; otherwise, $\mathbb{C}_{i|-k} \leftarrow \varnothing$ (Line 18 and 19). The agent a_i encapsulates this selection into her reply message MSGR_i (Line 21), *i.e.*,

$$MSGR_i \leftarrow MSGR_i \mid\mid MSGR_{i,k}$$

where

$$MSGR_{i,k} = \langle RPY, i, k, \mathbb{C}_{i|-k} \rangle$$
.

We note that sending the three different kinds of messages (*i.e.*, $MSGC_i$, $MSGP_i$, and $MSGR_i$) separately may introduce extra overhead for MAC layer coordination, we combine all of these three kinds of messages together

$$MSG_i \leftarrow MSGC_i \mid\mid MSGP_i \mid\mid MSGR_i$$

and utilize the broadcast of the wireless communication media to send the integrated messages in a single shot (Line 23).

After collecting replies from all her feedback neighbors (Lines 23 to 29), agent a_i can calculate her payment, if she is a winning agent. Here, she sorts her feedback neighbors in a decreasing order of bids as $\overline{\mathbb{FN}}_i$ (Line 25), and then follows the order to determine her critical price b_j , if it exists (Lines 26 to 30). The payment is $p_i \leftarrow b_j \times d_i$ (Line 30).

4.2.3 A Toy Example

Figure 3 shows a toy example for channel selection and payment calculation. In this example, we consider four agents $\mathbb{A}=\{a_1,a_2,a_3,a_4\}$, and 2 channels $\mathbb{C}=\{c_1,c_2\}$ for sale. The per-channel valuation for each agent is 7,8,9, and 6 respectively. For clarity, we assume that each of the agents demands one channel.

Each agent keeps a local ranking of agents (e.g., a_1 gets $a_3 \succ a_1 \succ a_4$, and a_3 gets $a_3 \succ a_2 \succ a_1 > a_4$) after the bid exchange phase. Based on the ranking, each agent sequentially selects one channel. For agent a_3 , she does not need to consider any preemptive selections, since she ranks the highest in her neighborhood. So she selects a channel c_1 , broadcasts her message $MSG_3 = MSGC_3 ||MSGP_3|$, and waits for feedback neighbors' replies to calculate her payment. Upon receiving MSG₃, agents a_1 and a_2 can run Algorithm 3 concurrently, since they are out of conflict. Agent a_1 then updates her available channel set, selects a channel c_2 , selects a payment determining channel c_1 assuming that a_3 is absent, and broadcasts her message MSG₁ = $MSGC_1||MSGP_1||MSGR_1$. Agent a_2 runs the same process. Finally, agent a_4 collects messages from all her preemptive neighbors and responds her own message MSG₄. Thereafter, winning agents extract critical price from feedback messages and calculate payment (i.e., $p_1 = 0, p_2 = 0, p_3 = 6$). Table 1 lists the contents of corresponding messages.

4.2.4 Consistency Check

To guarantee faithfulness, the consistency of the communication and computation should be checked. Note that each message sent in the spectrum auction has at least two copies (*i.e.*, one at the sender and the other at the receiver) in the network. We require each of the agents to submit the messages she sent and received to the CCS, when a transaction is cleared. After collecting all the messages, the CCS can check the messages, authorize the channel allocations, and collect

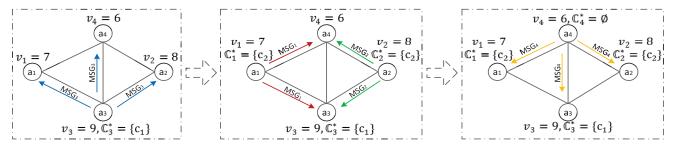


Fig. 3: Message Flow for Channel Selection and Payment Calculation with 4 Agents and 2 Channels.

Agent	a_1	a_2	a_3	a_4
Ranking	$a_3 \succ a_1 \succ a_4$	$a_3 \succ a_2 \succ a_4$	$a_3 \succ a_2 \succ a_1 \succ a_4$	$a_3 \succ a_2 \succ a_1 \succ a_4$
MSGB	< BID, 1, 7, 1 >	< BID, 2, 8, 1 >	< BID, 3, 9, 1 >	< BID, 4, 6, 1 >
MSGC	$< CHL, 1, \{c_2\} >$	$< CHL, 2, \{c_2\} >$	$< CHL, 3, \{c_1\} >$	< CHL, 4, ∅ >
MSGP	< PAY, 3 > < PAY, 1 >	< PAY, 3 > < PAY, 2 >	< PAY, 3 >	< PAY, 3 > < PAY, 1 > < PAY, 2 >
MSGR	$< \text{RPY}, 1, 3, \{c_1\} >$	$<$ RPY, 2, 3, $\{c_1\}$ $>$		$<$ RPY, 4, 3, $\{c_2\}$ $><$ RPY, 4, 2, \varnothing $>$ $<$ RPY, 4, 1, \varnothing $>$

TABLE 1: Messages Transmitted in The Network.

the payments. If a mismatch is detected, the involved agents have to pay a penalty which is much higher than the largest possible utility one can gain by cheating. We note that the CCS does not always need to have a reliable communication channel with each agent, or participate in the process of distributed spectrum auction. The CCS only needs to check the consistency and clears the transaction when a connection is available after the auction.

4.3 Mechanism Analysis

In this subsection, we show that FAITH meets our design requirements for a distributed mechanism, especially in terms of network complexity and faithfulness.

4.3.1 Network Complexity

Feigenbaum *et al.* [12] proposed the concept of network complexity with respect to five metrics to measure the complexity of a distributed algorithm over an interconnected network $G=(\mathbb{V},\mathbb{E})$, where $\mathbb{V}=\mathbb{A}$ is the set of agents and \mathbb{E} contains all the communication links among the agents in G. Here we demonstrate the network complexity of FAITH, in terms of the following five metrics.

- Total number of messages sent over G: Every agent broadcasts two messages, *i.e.*, one for bid exchange, and the other for integrated channel selection and payment calculation, resulting in $4|\mathbb{E}|$ messages.
- Maximum number of messages sent over any link in *G*: There are 4 messages on each link due to mutual message exchanges in the two phases.
- Maximum size of a message: In the worst case, the agent with the lowest bid may inherit all the payment determination request messages from her preemptive neighbors (i.e., the agent that ranks lowest in a ring topology will extract all other agents' payment determination request messages when there are more than one channels being auctioned), which will result in a merged MSG with $2|\mathbb{V}|$ sub-messages (i.e., 1 for MSGC, $|\mathbb{V}|$ for MSGP, and $|\mathbb{V}|-1$ for MSGR). Since each sub-message has a maximum length of c-byte, the

- maximum size of a message is $O(2c|\mathbb{V}|)$, where c is a constant.
- Local computation overhead: The most computation consuming part throughout the mechanism is the payment determining channel reselection, which takes $O(\delta|\mathbb{V}|)$ time in the worst case, where δ is the maximum degree of the network.
- Local storage overhead: Every agent is required at most $O(\delta|\mathbb{V}|)$ space to store propagated messages and local outcome in the worst case.

4.3.2 Faithfulness

To prove the faithfulness of FAITH, we begin by presenting the definition of *strong-CC* and *strong-AC*, followed by an important lemma.

Definition 7 (Strong-CC/Strong-AC [13]). A distributed mechanism $\mathcal{M} = (\Sigma, s^M, g)$ satisfies strong-CC/strong-AC if no agent can gain higher utility by deviating from the prescribed message-passing strategy/computation strategy, whatever the other two strategies are, when other agents follow the prescribed strategies.

Lemma 1 (Faithful Implementation [13]). A distributed mechanism $\mathcal{M} = (\Sigma, \mathbf{s}^M, g)$ is a faithful implementation of outcome $g(\mathbf{s}^M)$ if the corresponding centralized mechanism is strategyproof and \mathcal{M} satisfies strong-CC and strong-AC.

It suggests that given a centralized mechanism which is strategyproof (also known as dominant strategy incentive compatible), we can prove that a distributed mechanism is faithful by combining the properties of strong communication compatibility (*strong-CC*) and strong algorithm compatibility (*strong-AC*). We assume that, for each agent, a complete implementation of the auction is much preferable than dropping out without any affirmed outcome.

In FAITH, the intended strategy for each agent is to report bidding information truthfully, pass messages correctly, and calculate channel selection, reselection and payment correctly. A rational agent a_i may deviate from the intended

strategy to increase her utility by performing the following actions:

- Misreport: to report false bidding information, i.e., b_i ≠ v_i (reporting false number of demanded channels will obviously hurt a_i herself).
- Miscommunication: to drop or distort messages received from her neighbor a_j (e.g., MSGB $_j$ or MSG $_j$), or withhold her own messages.
- Miscalculation: to divide neighbors into wrong sets, or incorrectly determine channel selection \mathbb{C}_i^* , channel reselection \mathbb{C}_{i-k}^* or payment p_i .

Theorem 2. FAITH is a faithful distributed implementation of the critical price-based spectrum allocation mechanism.

Proof. To prove the faithfulness of FAITH, we show that FAITH satisfies centralized strategyproofness, strong-CC and strong-AC respectively.

The corresponding centralized auction mechanism is strategyproof. The critical price-based centralized spectrum auction is proved to be strategyproof in [9].

FAITH satisfies strong-CC. Based on the redundancy principle and "catch and punish" scheme, any miscommunication behavior will be detected and punished. On one hand, each agent has no incentive to drop or distort her neighbors' messages, since doing so will cause message mismatch and will be caught and punished by the CCS in consistency check. On the other hand, agent a_i will not withhold her own messages, because doing so will block the auction and thus prevent herself from participating in the auction. Hence, each agent a_i has no incentive to deviate from her intended message-passing strategy.

FAITH satisfies strong-AC. In the bid exchange phase, each agent a_i 's neighbors are divided into two sets with different priorities. Any unilateral miscalculation will breach the determination order and cause communication chaos. In the channel selection and payment calculation phases, agent a_i selects channel sets based on her preemptive neighbors' choices \mathbb{C}_j ($\mathbb{C}_{j|-k}$), and calculates payments based on her feedback neighbors' choices $\mathbb{C}_{j|-i}$. All the necessary information is packed in MSG $_j$ and sent to the CCS. Since any miscalculation will be caught and punished, a_i has no incentive to deviate from the intended computation strategy.

Therefore, FAITH is a faithful distributed implementation of the critical price-based spectrum allocation mechanism. \Box

5 ADAPTION TO DYNAMIC ENVIRONMENT

In previous sections, agents are considered to be static in the auction. A more practical scenario is that agents may come and go at any time. An intuitive adaptation is a "reboot" scheme, *i.e.*, to rerun the entire auction process, whenever a new arrival or a departure occurs. However, this scheme is inflexible and costly in terms of computation and communication overheads. In this section, we extend FAITH to support agents' dynamics by only updating the smallest part of affected allocation profile.

We observe that the design rationale of FAITH can also be applied to dynamic scenarios. Intuitively, for a newly arrived agent, her neighborhood information is enough for

Algorithm 4: Extended FAITH for Newly Arrived Agent a_i

```
1 Send MSGB+_i \leftarrow < BID, i, b_i, d_i > to \mathbb{N}_i;
 2 \mathbb{PN}_i \leftarrow \varnothing, \mathbb{FN}_i \leftarrow \varnothing, \mathbb{N}_i' \leftarrow \varnothing, \mathbb{AC}_i \leftarrow \mathbb{C}, \mathbb{FC}_i \leftarrow \varnothing, p_i \leftarrow 0;
 a_i foreach a_i ∈ N_i do
             Receive MSG_j from agent a_j;
             Extract MSGB_j = \langle BID, j, b_j, d_j \rangle from MSG_j;
             if a_i \succ a_i then \mathbb{PN}_i \leftarrow \mathbb{PN}_i \cup \{a_i\}, \mathbb{AC}_i \leftarrow \mathbb{AC}_i \setminus \mathbb{C}_i^*;
             foreach MSGP_k = \langle PAY, k \rangle in MSG_j do
                \mathbb{N}'_i \leftarrow \mathbb{N}'_i \cup \{a_k\};
             else \mathbb{FN}_i \leftarrow \mathbb{FN}_i \cup \{a_j\}, \mathbb{FC}_i \leftarrow \mathbb{FC}_i \cup \mathbb{C}_j^*;
10 Sort agents in \mathbb{F}\mathbb{N}_i in decreasing order of bids as \overline{\mathbb{F}\mathbb{N}_i};
11 if |\mathbb{AC}_i| < d_i then \mathbb{C}_i^* \leftarrow \emptyset;
12 else
             if |\mathbb{AC}_i \setminus \mathbb{FC}_i| \geq d_i then
             \mathbb{C}_i^* \leftarrow \operatorname{Random}(\mathbb{AC}_i \setminus \mathbb{FC}_i, d_i);
            else \mathbb{C}_i^* \leftarrow \text{LIP}(\overline{\mathbb{FN}}_i, \mathbb{AC}_i, d_i), \text{MSGP+}_i \leftarrow < \text{PAY}, i >;
15 MSGC+_i \leftarrow < CHL, i, \mathbb{C}_i^* >;
16 foreach a_k \in \mathbb{N}_i' do
17
             \mathbb{AC}_{i|-k} \leftarrow \mathbb{C}, \mathbb{FC}_{i|-k} \leftarrow \emptyset;
             foreach a_j \in \mathbb{PN}_i do
18
                     if MSGR_{j,k} exists then \mathbb{AC}_{i|-k} \leftarrow \mathbb{AC}_{i|-k} \setminus \mathbb{C}_{j|-k};
19
                    else \mathbb{AC}_{i|-k} \leftarrow \mathbb{AC}_{i|-k} \setminus \mathbb{C}_{j}^{*};
20
             foreach a_j \in \mathbb{F}\mathbb{N}_i do
21
                    if MSGR_{j,k} exists then \mathbb{FC}_{i|-k} \leftarrow \mathbb{FC}_{i|-k} \cup \mathbb{C}_{j|-k};
22
                    else \mathbb{FC}_{i|-k} \leftarrow \mathbb{FC}_{i|-k} \cup \mathbb{C}_{j}^{*};
23
             if |\mathbb{AC}_{i|-k}| < d_i then \mathbb{C}_{i|-k} \leftarrow \emptyset;
24
             else if |\mathbb{AC}_{i|-k} \setminus \mathbb{FC}_{i|-k}| \ge d_i then
25
26
                \mathbb{C}_{i|-k} \leftarrow \operatorname{Random}(\mathbb{AC}_{i|-k} \setminus \mathbb{FC}_{i|-k}, d_i);
             else \mathbb{C}_{i|-k} \leftarrow \text{LIP}(\overline{\mathbb{FN}}_i, \mathbb{AC}_{i|-k}, d_i);
27
             MSGR+_{i,k} \leftarrow < RPY, i, k, \mathbb{C}_{i|-k} >;
28
             MSGR+_i \leftarrow MSGR+_i \mid\mid MSGR+_{i,k};
29
             MSGP+_i \leftarrow MSGP+_i \mid\mid MSGP_k;
31 Send MSG+_i \leftarrow \text{MSGC}+_i \mid\mid \text{MSGP}+_i \mid\mid \text{MSGR}+_i \text{ to } \mathbb{N}_i;
32 if preemption occurs then
             foreach a_i \in \overline{\mathbb{FN}}_i do
33
                     Receive \langle RPY, j, i, \mathbb{C}_{j|-i} \rangle from agent a_j \in \overline{\mathbb{FN}}_i;
34
                     \mathbb{AC}_i \leftarrow \mathbb{AC}_i \setminus \mathbb{C}_{j|-i};
35
                    if |\mathbb{AC}_i| < d_i then p_i \leftarrow b_i \times d_i; Break;
37 Return \mathbb{C}_i^* and p_i;
```

her to determine her channel selection and the corresponding payment. Besides, the arrival or departure of an agent normally affects only a part of the existing agents.

Algorithm 4 shows our proposed procedures for a newly arrived agent a_i . When agent a_i arrives the market, she first broadcasts her bid statement message (MSGB+), in the format of

$$MSGB+_i = \langle BID, i, b_i, d_i \rangle$$

to her neighbors in \mathbb{N}_i to inform her arrival (Line 1), and collects their MSG messages, based on which she then selects her required channels and calculate the corresponding payment.

Same as FAITH, agent a_i divides her neighbors \mathbb{N}_i into preemptive neighbor $\mathbb{P}\mathbb{N}_i$ and feedback neighbor $\mathbb{F}\mathbb{N}_i$ according to their bids. Then, agent a_i updates the set of her available channels \mathbb{AC}_i by deactivating the channels selected by her preemptive neighbors, and stores the set of channels selected by her feedback neighbors into \mathbb{FC}_i for possible preemption. There are three cases needed to be considered:

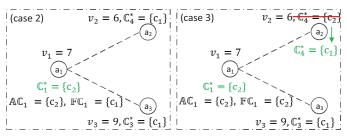


Fig. 4: An Example of Case (2) and Case (3)

- (1) If $|\mathbb{AC}_i| < d_i$, agent a_i gets nothings (Line 11); Otherwise, she can always meet her demand.
- (2) If $|\mathbb{AC}_i \setminus \mathbb{FC}_i| \geq d_i$, agent a_i can randomly select a subset of d_i channels out of $\mathbb{AC}_i \setminus \mathbb{FC}_i$, without disturbing her neighbors (Line 13);
- (3) If $|\mathbb{AC}_i| \geq d_i$ and $|\mathbb{AC}_i \setminus \mathbb{FC}_i| < d_i$, agent a_i needs to preempt channels from her feedback neighbors. We propose a Least Impactive Preemption (LIP) scheme, shown in Algorithm 5, *i.e.*, agent a_i preempts channels from one of her feedback neighbors, who critically leads to the channel unavailability of a_i .

In case (1) and case (2), agent a_i 's payment should be zero, since she has no critical neighbor. However, in case (3), agent a_i 's critical neighbor is not straightforward to see. For example, in Fig. 4, there are 2 channels $\mathbb{C} = \{c_1, c_2\}$ for sale and 3 agents $\mathbb{A} = \{a_1, a_2, a_3\}$, where each agent demands one channel. We assume that agent a_1 arrives after the other two agents having been allocated channels. Since the priority is $a_3 \succ a_1 \succ a_2$, agent a_1 can only preempt the channel from agent a_2 . We note that agent a_2 may have selected c_1 (case 2), or c_2 (case 3). In the former case, agent a_1 figures out that $\mathbb{AC}_1 \setminus \mathbb{FC}_1 = \{c_2\}$, and directly selects c_2 as her allocation with zero payment; In the latter case, $\mathbb{AC}_1 = \{c_2\}$, but $\mathbb{AC}_1 \setminus \mathbb{FC}_1 = \emptyset$, which means that agent a_2 's selection forces agent a_1 to preempt a channel. However, agent a_2 is not agent a_1 's critical neighbor, since agent a_2 can reselect channel c_1 when channel c_2 is preempted by agent a_1 . Therefore, if a preemption occurs, agent a_i needs to check the reply messages from her feedback neighbors to determine her payment (Lines 32 to 36). Besides determining her own payment, agent a_i also needs to compose the reply message $MSGR+_{i,k}$ for every agent a_k , whose MSGP_k message is received by a_i , to help a_k to calculate her payment, since a_i 's arrival may change a_k 's critical neighbor (Lines 17 to 31).

Under dynamic network environment, any existing agent a_j should keep listening to the control channel for incoming messages. We provide the procedures for an existing agent a_j upon the arrival of a new agent a_i in Algorithm 6. If agent a_j is one of the agent a_i 's neighbors, agent a_j will receive agent a_i 's bid statement message MSGB+i, based on which she can mark agent a_i as her preemptive neighbor or feedback neighbor. Then, agent a_j sends agent a_i her information MSG $_j$ to help agent a_i to select channels, and wait for agent a_i 's MSG+ $_i$ message (Lines 2 to 6). Upon receiving agent a_i 's response, if agent a_j is agent a_i 's preemptive neighbor, then agent a_j only needs to recalculate her payment p_j . Otherwise, agent a_j needs to check if her pre-occupied channels have been preempted, to update her channel selection \mathbb{C}_j^* and reselection $\{\mathbb{C}_j|_{-n}\}$, to recalculate

```
Algorithm 5: Least Impactive Preemption (LIP)
```

```
1 Input: \overline{\mathbb{FN}}_i, \mathbb{AC}_i, d_i; Output: \mathbb{C}_i^*;
2 foreach a_j \in \overline{\mathbb{FN}}_i do
3 | if |\mathbb{AC}_i \setminus \mathbb{C}_j^*| < d_i then
4 | \mathbb{C}_i^* \leftarrow \operatorname{Random}(\mathbb{AC}_i, d_i); Break;
5 | \mathbb{AC}_i \leftarrow \mathbb{AC}_i \setminus \mathbb{C}_j^*;
6 return \mathbb{C}_i^*;
```

the corresponding messages (MSGC $_j$, MSGP $_j$, and MSGR $_j$), and to send the updated MSG $_j'$ to her neighbors (Lines 7 to 12). If agent a_j is not agent a_i 's neighbor, she will not directly respond to the newly arrived agent, but only react to the updated messages {MSG $_k'$ } received from her neighbors (Lines 13 to 18).

Once an agent a_i finishes her job, she leaves the market. Before the departure, she broadcasts the leaving message (MSGL-), in the format of

$$MSGL_{i} = \langle LVE, i, \mathbb{C}_{i}^{*} \rangle,$$

to inform her neighbors to recycle her channels and recalculate their payments. We observe that if agent a_i did not win the auction, her departure will not influence the remaining agents' channel selections. In this case, agents only need to update their payments. If agent a_i won the auction, then every other agent a_j has already known her allocation $\mathbb{C}^*_{j|-i}$ upon a_i 's departure, since agent a_i 's payment is calculated based on the allocation profile when a_i is absent. In this case, every existing agent a_j will directly change her channel selection to $\mathbb{C}^*_{j|-i}$. Newly allocated agents and a_i 's preemptive neighbors will calculate their payments by broadcasting their updated MSG messages.

Extended FAITH follows the same design rationale as FAITH, and thus is still faithful with polynomial computation and communication overhead. Comparing with FAITH, extended FAITH is likely to result in more communication overhead due to the dynamic arrival/departure of agents.

Theorem 3. Extended FAITH is a faithful distributed mechanism in a dynamic environment.

Proof. (Sketch) Similar to the proof of FAITH, we show that extended FAITH satisfies centralized strategyproofness, strong-CC and strong-AC.

First, the channel allocation of extended FAITH follows the critical price-based method on either a new arrival or a new departure, thus is still centralized strategyproof.

Second, extended FAITH satisfies strong-CC. For a newly arrived agent, she has to follow the prescribed message-passing strategy, since withholding her own messages will prevent herself from being allocated, and any other deviation in communication will be detected and punished by the CCS. The newly departured agent also cannot benefit from manipulating her prescribed message-passing strategy. For any other agent, the "catch and punish" scheme ensures that she has no incentive to deviate from her intended message-passing strategy under the intended strategy profile.

Finally, extended FAITH satisfies strong-CC. For a newly arrived agent, miscalculation may cause chaos in channel allocation and get punished. The newly departured agent no

Algorithm 6: Extended FAITH for Existing Agent a_j upon a Newly Arrived Agent a_i

```
1 switch Received message do
          case MSGB+_i
               if a_i \succ a_j then \mathbb{PN}_j \leftarrow \mathbb{PN}_j \cup \{a_i\};
 3
                else \mathbb{FN}_j \leftarrow \mathbb{FN}_j \cup \{a_i\};
 4
                MSG_j \leftarrow MSGB_j ||MSGC_j||MSGP_j||MSGR_j;
 5
 6
               Send MSG_j to a_i; Break;
          case MSG+_i
                if a_i \in \mathbb{PN}_i then
                     Update \mathbb{C}_{j}^{*}, \{\mathbb{C}_{j|-n}\}, MSGC<sub>j</sub>, MSGP<sub>j</sub>, MSGR<sub>j</sub>, MSG<sub>j</sub> based on MSG+<sub>i</sub>;
                     Send updated MSG'_i to \mathbb{N}_j;
10
                else Update p_j based on MSG+_i;
11
12
               Break;
          case MSG'_k
13
               if a_k \in \mathbb{PN}_i then
14
                      Update \mathbb{C}_{j}^{*}, \{\mathbb{C}_{j|-n}\}, MSGC<sub>j</sub>, MSGP<sub>j</sub>,
15
                      MSGR_j, MSG_j based on \{MSG'_k\};
                     Send updated MSG'_j to \mathbb{N}_j;
16
                else Update p_i based on {MSG'_k};
17
                Break;
19 Return \mathbb{C}_{i}^{*} and p_{j};
```

longer participates in the auction and thus has no computation strategy. We note that any deviation from the prescribed strategy will be detected and punished by the CCS, thus no agent has the incentive to deviate from the intended computation strategy under the intended strategy profile.

Therefore, extended FAITH is a faithful distributed mechanism in a dynamic environment.

6 Discussion

In this section, we present further discussions of this work.

6.1 Optimality and Convergence

Optimality: Distributed VCG mechanism achieves optimal social welfare, while FAITH achieves sub-optimal social welfare based on a greedy channel allocation algorithm. However, it is infeasible to provide an approximation ratio for FAITH. The key reason is that the social welfare of FAITH are determined by multiple factors (whose instances could be arbitrary), including the agents' bids, agents' channel requests, and the conflicting relationships between agents. In this case, analyzing the approximation ratios for spectrum allocation algorithms, even in centralized scenarios, is extremely difficult and cannot be addressed by this work. In fact, due to the infeasibility, the optimality analysis of is often missing in current researches of spectrum allocation, such as [9], [11]. Thus, we do believe that it would be the best to treat it as a potential future work.

Convergence: The convergence of distributed VCG is clear, since it terminates after a bottom-up and then a top-down traversal. The convergence of FAITH and extended FAITH is also guaranteed. Note that the auctions determine the channel allocation results sequentially, *i.e.*, the agent with the highest bid will be allocated first, and then the one with the second highest bid, and so on. The channel

TABLE 2: Properties of Our Mechanisms

	Faithful	Opt	Conv	DSE	IR	CS	NPT	VP
DVCG				×				
FAITH		×		×				
E-FAITH	$\sqrt{}$	×	$\sqrt{}$	×	$\sqrt{}$		$\sqrt{}$	

assignment of each agent will be determined eventually. As for the payment determination, each agent first collects channel assignment information from her neighbors, and determines which one of her feedback neighbors is her critical neighbor. These calculations require finite searches, and will be done in finite time.

6.2 Other Mechanism Design Properties

We also analyze our mechanisms with several widely used properties of algorithmic mechanism design. The properties of our proposed mechanisms are summarized in Table 2.

Dominant Strategy Equilibrium (DSE): As discussed in Section 2.2, distributed VCG mechanism cannot guarantee dominant strategy equilibrium. Weaker mechanisms — FAITH and extended FAITH cannot achieve it as well.

Individual Rationality (IR): Each participating agent will have a non-negative utility, *i.e.*, $\forall i, u_i \geq 0$. It has been proved that VCG mechanism satisfies individual rationality [33]. Since our distributed VCG mechanism follows the payment rule of original VCG mechanism, it also satisfies individual rationality. As for FAITH and extended FAITH, since the critical neighbor of each winner, if it exists, is one of her feedback neighbors, the payment of each winner is always no higher than her bid.

Consumer Sovereignty (CS): The mechanism cannot arbitrarily exclude any agent, and the mechanism has to allow an agent to win if she is willing to pay a sufficiently high payment (while others' bids are fixed). The consumer sovereignty of VCG mechanism has already been proved [33]. As for FAITH and extended FAITH, agents cannot be arbitrarily rejected by the mechanisms. Due to the greedy allocation rule, if an agent has the highest bid, she will win the auction. Thus, FAITH and extended FAITH also satisfy consumer sovereignty.

No Positive Transfer (NPT): The payments are nonnegative, *i.e.*, $\forall i, p_i \geq 0$. This property obviously holds for each of our proposed mechanism.

Voluntary Participation (VP): An agent who does not participate the auction will not be charged, and an agent who wins the auction will not be charged more than her bid. In our proposed mechanisms, only winning agents will need to pay. Also, each winning agent's payment must be no more than her bid, thus voluntary participation holds.

6.3 Alternative Interference Models

This work, following the convention of spectrum auction literature, adopts the conflict graph to model the physical interference conditions among agents. The benefit of using a conflict graph model is the great simplification of the spectrum allocation design, *s.t.*, one can focus on the development of highly efficient allocation mechanisms with nice game-theoretical properties and polynomial complexity. Other alternative physical inference models, such as

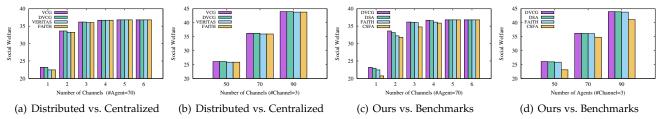


Fig. 5: Social Welfare Comparison, (a)-(b) compare distributed mechanisms with centralized mechanisms, (c)-(d) compare DVCG and FAITH with two benchmarks

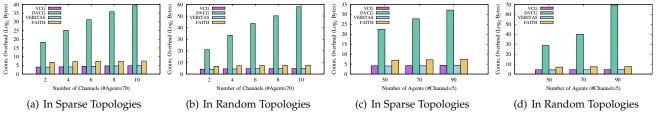


Fig. 6: Transmission Overhead Comparison, (a)-(b) vary the number of channels, (c)-(d) vary the number of agents

SINR-based and power-based models [2], are also promising but require specific catering of the current problem settings, including redefining the optimization and constraint terms and reconsidering the agents' manipulation strategies, thus may not be directly solved by our proposed distributed VCG and FAITH. Despite that, the design intuitions of our proposed distributed mechanisms could provide implications for subsequent designs of faithful distributed spectrum allocation methods for these models.

6.4 Synchronization

Synchronization is an important issue in distributed algorithms. Based on the way the agents update their local information, distributed algorithms can be generally classified as *synchronous* or *asynchronous* [34]. In asynchronous algorithms, each agent has its own view of the problem and updates their local variables independently from the actual decisions of other agents. In contrast, synchronous algorithms update the agents' decisions in a particular order, which is usually enforced by the representation structure adopted. It tends to delay the decisions of some agents guaranteeing their local view of the problem is always consistent with that of the other agents.

The proposed distributed VCG mechanism synchronous, since its execution follows a pre-defined order (bottom-up and then top-down) and the update of an agent's decision is postponed until all the dependent agents have been updated. As for FAITH, the channel assignment part is synchronous, as it determines the channel assignments of agents in the decreasing order of bids. In the payment determination part, each winning agent first sends payment determination request message to her feedback neighbors, and waits until all her feedback neighbors have sent her channel assignment messages. After that, each agent can calculate her own payment. Since each agent only needs to update her own payment, there's no shared agreement in this part, s.t., no synchronization technique is needed. One particular part we need to deal with is that in the extended FAITH, the handling of a new arrival or departure is postponed if the auction is in progress (due to the efficiency of our algorithm, this delay is short).

7 EVALUATION RESULTS

In this section, we employ NS-2 to evaluate the performance of distributed VCG and FAITH on allocation efficiency and transmission overhead. First, we explore the social welfare and communication overhead of distributed VCG and FAITH in a small spectrum market. Second, we further examine the performance of FAITH by comparing it to a non-faithful distributed allocation algorithm [35]. Finally, we investigate the efficiency of extended FAITH in a dynamic environment by comparing it to the "reboot" scheme.

We consider both real network data and simulated data. The real network data, collected by [10], records 78 access points (AP) in a $7km^2$ area of the Google WiFi network in Mountain View, California. The simulated data consists of three different kinds of topologies, i.e., sparse topologies, random topologies and clustered topologies. In sparse topologies and random topologies, agents are randomly distributed in a square area of $2500m \times 2500m$. We restrict that each connected component in sparse topologies has no more than 10 agents. For clustered topologies, same as [9], we initially distributed 100 agents in a square area of $1200m \times 1200m$, and then increase agents up to 300 by adding 100 agents in the center iteratively. We apply a widely used distance-based interference model [9], [10], [18] to generate the simulated conflict graphs. In our setting, any two agents within 250m will conflict with each other and thus cannot utilize the same channel simultaneously. Without loss of generality, we uniformly distribute the bids of agents in (0, 1], and the channel demands in $\{1, 2, 3, 4, 5\}$. The results are averaged over 1000 runs.

7.1 Distributed VCG versus FAITH

We evaluate the social welfare (*i.e.*, the sum of winning agents' valuations) and transmission overhead (*i.e.*, the size of the largest message) of distributed VCG and FAITH. We first compare the proposed distributed mechanisms with centralized mechanisms. For distributed VCG, we compare it to the centralized VCG mechanism, and for FAITH, it is compared to a strategyproof centralized spectrum auction mechanism [9], namely VERITAS. Then, we compare distributed VCG

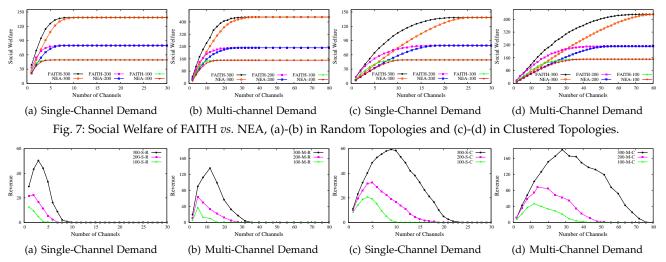


Fig. 8: Revenue of FAITH, (a)-(b) in Random Topologies and (c)-(d) in Clustered Topologies.

and FAITH with two additional benchmarks. One of the benchmarks is distributed stochastic search algorithm (DSA) [36], which is a incomplete and synchronous algorithm for distributed constraint optimization problem (DCOP). It can achieve near-optimal solution with polynomial time and space complexity, and has often been used as a benchmark algorithm for DCOP [26]. The other benchmark is a centralized strategyproof and fair auction mechanism for secondary spectrum markets [37]. For simplicity, we refer to this algorithm as "CSFA" in the evaluation. Due to the exponential complexity of distributed VCG, we evaluate it only in a small scale spectrum market with sparse network topologies. The number of agents ranging from 50 to 90 and the number of channels from 1 to 10. We also assume that each agent only requires a single channel.

Fig. 5 shows the comparisons of social welfare between our proposed mechanisms and the benchmarks. From Fig. 5(a)-(b), we can see that distributed VCG achieves the same social welfare as VCG. This is because the distributed VCG implements the same outcome function and payment function as the original VCG mechanism. FAITH and VERITAS also have the same social welfare, since they both follow the greedy-based channel allocation rule and the critical price-based payment determination rule. Fig. 5(c)-(d) shows the social welfare comparison between our proposed distributed mechanisms and additional two benchmarks: DSA and CSFA. We can observe that DSA achieves lower social welfare than distributed VCG but higher social welfare than FAITH. That is due to the reason that although DSA does not guarantee an optimal solution, it is based on a carefully designed searching method that allows the agents iteratively update their variables to achieve a near-optimal solution. Besides, CSFA achieve the lowest social welfare, because it sacrifices a portion of social welfare to ensure the fairness of the spectrum allocation. In addition, we observe that social welfare grows as the number of channels increases and reaches saturation when the number of channels is 5. When the number of channels is fixed, a larger number of agents leads to higher social welfare. Under the same parameters, distributed VCG achieves higher social welfare than FAITH before saturation, which is because that distributed VCG is designed to choose the optimal allocation, while FAITH

prefers the greedy policy.

Fig. 6 compares the transmission overhead of distributed VCG, FAITH, and the centralized mechanisms in sparse topologies and random topologies respectively. We note that the y-axis is in logarithmic form, i.e., log_2S , where S is the size of the largest message in units of bytes. It can be seen that centralized mechanisms have the lowest transmission overhead since they only need basic communications (i.e., bid reporting, outcome and payment announcement) between the agents and the centralized auctioneer. As for distributed mechanisms, we observe that the transmission overhead of distributed VCG grows dramatically as the number of channels/agents increases, due to the fact that distributed VCG requires each agent to enumerate every possible channel assignment of her constraint view, which results in exponential space complexity. In contrast, the transmission overhead of FAITH grows slightly with the increase in the number of agents/channels, supporting our claim that FAITH has bounded transmission overhead. Despite the slight loss of social welfare, the polynomial communication complexity makes FAITH more feasible and practical, especially in large spectrum markets.

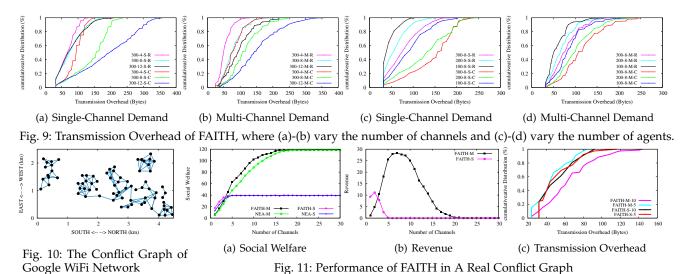
7.2 More Evaluations on FAITH

In Section 7.2.1 and Section 7.2.2, we evaluate the allocation efficiency and transmission overhead of FAITH in both random topologies and clustered topologies. The number of agents ranges from 100 to 300 and the number of channels ranges from 1 to 80. We also evaluate the performance of FAITH in a real network topology in Section 7.2.3.

7.2.1 FAITH versus Non-Faithful Distributed Allocations

We measure the allocation efficiency of FAITH in terms of social welfare and revenue (*i.e.*, the sum of payments), and compare it with a non-faithful distributed Nash equilibrium based channel allocation algorithm [35] (denoted by NEA in our evaluation).

Fig. 7 shows the comparison results on social welfare between FAITH and NEA in random topologies and clustered topologies. We observe that social welfare of both algorithms grows as the number of channels gets larger



and finally reaches saturation, where every agent's demand is satisfied. Besides, FAITH outperforms NEA with much higher social welfare when saturation has not been reached, due to the fact that FAITH allocates channels to higher bidders with higher priorities, while NEA allows the agents to compete for the channels in an arbitrary way.

Compared with cases in clustered topologies, FAITH saturates at fewer channels in random topologies (*e.g.*, under single-channel demand, 9 channels for 300 agents in random topologies, while 23 channels for 300 agents in clustered topologies). This is because agents in clustered topologies are densely located, resulting in more intensive conflicts. Besides, the multi-channel demand cases also show a lag of increase compared with single-channel demand scenarios (*e.g.*, in clustered topologies, FAITH saturates at 22 channels for 300 agents with single-channel demand, while 80 channels for 300 agents with multi-channel demand).

Fig. 8 presents the revenue of FAITH in both random topologies and clustered topologies. We do not show the results of NEA because it does not have a pricing scheme. Different from the growth trend of social welfare, revenue cannot always stay at a high level with the increment of the number of channels. This non-monotonic growth trend is caused by our critical price-based payment scheme. At first, few agents get satisfied when the number of channels is small. In this case, increasing the number of channels improves the percentage of winning agents, thus increases revenue. However, a large number of available channels alleviates the auction competition, s.t., some agents no longer have critical neighbors and thus are charged zero payments. Finally, the revenue decreases to zero when every agent is satisfied. Due to different intensity levels of competition, the four subfigures of Fig. 8 show different growth and saturation speed.

7.2.2 Transmission Overhead of FAITH

We also measure FAITH's per agent transmission overhead, which is defined as the total size of messages each agent generates. Fig. 9 shows the cumulative distribution of transmission overhead in bytes, where "n-m-S/M-R/C" denotes that n agents bid for m channels

TABLE 3: Statistics on the Number of Agents' Neighbors in Google WiFi Network

#Neighbors	2	3	4	5	6	7	8
Counts	4	12	13	21	15	11	2

with single-channel(S)/multi-channel(M) demand in random(R)/clustered(C) topologies.

According to Fig. 9(a)-(b), we observe that more channels lead to heavier transmission overhead (*e.g.*, over 85% of agents transmit no more than 100 bytes in "300-4-S-R" while the percentage is only 70% in "300-12-S-R"). This is because more channels result in more winners and thus more messages are generated to perform channel reselection and payment determination. Another observation is that the cumulative distribution of clustered topologies grows more slowly than that of random topologies. For example, while there is only a tiny portion of agents generating transmission overhead over 200 bytes in 300-12-S-R, the percentage is about 50% in "300-12-S-C". The reason is that some agents in the cluster have the most intense conflicts and thus have to transmit more messages.

Fig. 9(c)-(d) present the transmission overhead with various numbers of agents. We can see that the transmission overhead grows with the increasing number of agents (e.g., over 70% of agents transmit no more than 50 bytes in "100-8-S-R" while the percentage is down to 30% in "300-8-S-R"), due to the fact that more agents lead to more intensive conflicts. Besides, single-channel demand causes larger transmission overhead than multi-channel demand. That is because that under the single-channel request of each agent, conflicting agents will have more opportunities to select channels than they do under multi-channel request, which will further result in more winners and thus more message exchanges.

7.2.3 FAITH in A Real Network Topology

Besides simulated network topologies, we also evaluate the performance of FAITH based on a Google WiFi dataset, which was collected by Zhou *et al.*in April 2010 [10]. The dataset covers a $7km^2$ residential area of the Google WiFi network in Mountain View, California. They recorded the

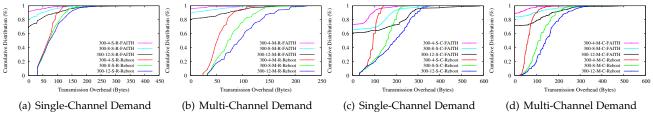


Fig. 12: Transmission Overhead of Extended FAITH vs. Reboot Scheme on Agent Arrival, (a)-(b) in Random Topologies and (c)-(d) in Clustered Topologies

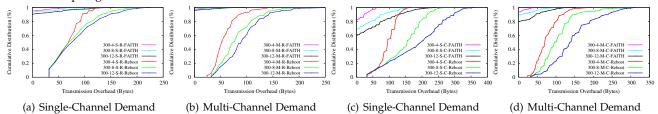


Fig. 13: Transmission Overhead of Extended FAITH vs. Reboot Scheme on Agent Departure, (a)-(b) in Random Topologies and (c)-(d) in Clustered Topologies

detailed signal strength values of 78 APs, and built a measured conflict graph, which is shown in Fig. 10. The black dots represent the APs, and the blue edges represent the conflicting relationship between the APs. We present the statistics of the number of each node's neighbors in Table 3. We can see that the number of each node's neighbors ranges from 2 to 8, while the average and the mode are 4.92 and 5, respectively. In our simulation, we treat each AP as an agent, and apply FAITH to the conflict graph. The number of channels is set to 5. The agents' bids are uniformly distributed in $\{0,1\}$, and their channel demands in $\{1,2,3,4,5\}$.

Fig. 11 shows the social welfare, revenue, and transmission overhead of FAITH in the real network topology. We observe that these metrics follow the similar patterns as in simulated network topologies. Specifically, Fig. 11(a) shows that under either single-channel demand (denoted by "FAITH-S") or multi-channel demand (denoted by "FAITH-M"), FAITH achieves higher social welfare than NEA before saturation is reached. We observe that in average, saturation can be reached when the number of channels is over 5 for single-channel demand, and 20 for multi-channel demand. In Fig. 11(b), the revenue of FAITH first increases and then decreases as the number of channels grows, and finally saturates at zero. This growth trend is similar to that in simulated network topologies (shown in Fig. 8), due to the critical price-based pricing scheme of FAITH. The transmission overhead of FAITH is shown in Fig. 11(c), where "FAITH-M-10" denotes the transmission overhead of FAITH under multi-channel demand with 10 channels. We see that under either single-channel demand or multichannel demand, the transmission overhead of each agent is low (e.g., no agent needs to transmit over 160 bytes).

7.3 Adaptation to Dynamic Environment

We also implement extended FAITH to evaluate its performance in dynamic environment. We compare the transmission overhead of extended FAITH to the "reboot" scheme (Section 5) on both agent arrival and agent departure. The evaluation results are presented in Fig. 12 and Fig. 13.

Fig. 12 shows the comparisons of extended FAITH and the "reboot" scheme on agent arrival, where Fig. 12(a)-(b) are in random topologies and Fig. 12(c)-(d) in clustered topologies. We observe that extended FAITH significantly reduces the transmission overhead required by the "reboot" scheme. For example, in "300-4-S-R-Reboot", about 70% of agents transmit over 50 bytes, while the percentage is only about 5% in "300-4-S-R-FAITH". That is because extended FAITH takes advantage of the existing information, instead of regenerating this information and rerunning the whole allocation. Besides, the transmission overhead under singlechannel demand is heavier than under multi-channel demand, due to the fact that under single-channel demand, a new arrival usually lead to a larger variation in the allocation profile. We also observe that clustered topologies generate heavier transmission overhead than random topologies (e.g., about 80% of agents do not transmit messages in "300-12-M-R-FAITH", while only 70% in "300-12-M-C-FAITH"). This is because the clustered topologies have more conflicts than random topologies, s.t., a newly arrived agent will disturb more agents in clustered topologies than in random topologies.

Fig. 13 presents the comparisons of the transmission overhead of extended FAITH and the "reboot" scheme on agent departure, where Fig. 13(a)-(b) are in random topologies and Fig. 13(c)-(d) in clustered topologies. It can be observed that extended FAITH greatly reduced the transmission overhead of the "reboot" scheme. Comparing Fig. 13 to Fig. 12, we can see that extended FAITH requires less transmission overhead on agent departure than agent arrival. This is because that the allocation profile under the absence of an agent is known when calculating the agent's payment, *s.t.*, remaining agents only need to update necessary payments.

8 RELATED WORK

Spectrum Allocation Protocols: There are many research works addressing the problem of spectrum allocation in various network settings, such as cellular networks [38], wireless LANs [39], wireless mesh networks [40], [41], mobile ad-hoc networks [42], 5G networks [43], [44], hetero-

geneous networks [45], and vehicular networks [46]. Most of them assume that agents in the networks strictly follow the prescribed protocols, thus cannot be applied to scenarios where agents are rational and only interested in maximizing their own utilities.

Auction-based Spectrum Allocation: Auction-based spectrum allocation mechanisms, which model the problem as a game over rational agents, have been extensively studied to improve spectrum utilization and allocation fairness. Following the pioneer work of Zhou *et al.* [9], various researchers have addressed the problem from from different perspectives listed as follows:

- **Double Auction:** TRUST [11] considers the incentive problem of both sellers and buyers, and elegantly extends spectrum market to double auction. SMALL [8] further improves TRUST to achieve a higher channel utilization ratio. TAHES [6] addresses heterogeneous spectrum in a double auction. Dong *et al.* [47] proposed a double auction based spectrum allocation algorithm that can achieve truthfulness, individual rationality, and budget-balance.
- **Combinatorial Auction:** Dong *et al.* [5] studied combinatorial auction in cognitive radio networks. Zheng *et al.* [48] further modeled the heterogeneous spectrum market as a combinatorial auction.
- Online Auction: Deek *et al.* [4] designed a truthful online spectrum auction mechanism. Li *et al.* [49] proposed an online spectrum allocation mechanism for secondary wireless communication, which can dynamically evaluate the true value of the spectrum channels and achieve sub-optimal social welfare. Hyder *et al.* [50] extended the online spectrum auction design to dynamic spectrum markets with varying transmission deadlines and random availability of spectrum units.
- **Revenue Maximization:** Al-Ayyoub and Gupta [3] proposed a truthful spectrum auction to maximize the total revenue with polynomial-time complexity.
- **Privacy Preserving Auction:** SPRING [7] is a strategy-proof and privacy preserving spectrum auction mechanism. DEAR [51] is a differentially private spectrum auction with approximate revenue maximization.
- Collusion-Resistent Mechanism: Gao and Wang [52] proposed a min-max coalition-proof Nash equilibrium channel allocation mechanism for multi-channel allocation in multi-hop wireless networks. THEMIS *et al.* [53] is a truthful and collusion-resistent online spectrum auction mechanism that provides price fairness under unknown and dynamic spectrum supply.
- Other: Gopinathan *et al.* [37] considered the balance between social welfare and fairness in spectrum markets. Li *et al.* [54] proposed an extensible and flexible truthful auction framework for heterogeneous spectrum market. ALETHEIA [55] is a large-scale strategy-proof spectrum auction mechanism that can prevent false-name bidding. Nadendla *et al.* [56] considered the problem of optimal spectrum auction design under the scenarios where the spectrum availability is not always certain. Yang *et al.* [57] applied the group buying strategy into secondary spectrum market, and proposed two group buying auctions that can dramatically improve

the utility of spectrum users.

A good survey of spectrum auctions can be found in [58]. However, all of the existing spectrum auction mechanisms are centralized, and may suffer from the critical drawbacks discussed in Section 1. In contrast, we consider the design of distributed spectrum auction mechanisms. A preliminary version of this work appears in INFOCOM 2015 [59], while this work has substantial revisions over the previous one, including the design of extended FAITH, additional technical details, and more comprehensive evaluations.

Early Researches on DAMD: To overcome the limitations of centralized mechanisms, Feigenbaum et al. [12] initiated the study of distributed algorithmic mechanism design (DAMD), and pointed out two key aspects that DAMD differed from traditional centralized algorithmic mechanism design (AMD): agents' additional ways of manipulations and the measure of network complexity. To prevent the agents' manipulations in distributed implementation of VCG mechanism, they proposed the idea of replication, i.e., breaking the agents into two groups and letting each group compute its own version of the outcomes and payments. Then, a central enforcer will conduct consensus check and penalize all agents if the outcomes and payments do not agree. Feigenbaum and her colleges also articulated the concept of network complexity, and proposed efficient distributed mechanisms for multicast transmissions [60] and interdomain routing [61] without addressing agents' additional manipulations. Later, Parkes and Shneidman [23] proposed several general principles, such as partition principle, informationrevelation principle, and redundancy principle, to guide the distribution of mechanisms, which shaped our faithfulness implementation of distributed VCG and FAITH. Shneidman and Parks also [13] studied the agents' strategy space in distributed scenarios, and introduced the notions of communication compatibility and algorithm compatibility. In [62] and [13], Shneidman and Parkes extended the interdomain routing mechanism proposed by [61] to address the agents' manipulations in communications and computations based on the idea of redundancy and "catch and punish" scheme. Different from the existing studies on distributed VCG mechanism, where the implementation of the outcome function was based on standard protocols, we focused on the design of a distributed spectrum allocation mechanism, and in particular, customized a distributed social welfare optimization algorithm that takes both the agents' multichannel requests and the spatial reusability of the spectrum into consideration.

Recent Applications of DAMD: Yang *et al.* [63] considered the problem of stochastic data collection in mobile phone sensing systems, and proposed a distributed mechanism. However, they only considered the agents' manipulations in information-revelation actions and assumed that the agents are obedient in message-passing and computations. Mhanna *et al.* [64] considered the problem of sharing the cost of electricity among a large number of strategic agents, and proposed faithful distributed mechanisms to determine the price of each consumer. Similar to [60], they focused on the network complexity part without addressing the agents' additional ways of manipulations.

9 CONCLUSION

In this paper, we have modeled the problem of wireless spectrum allocation as a distributed auction, and have proposed two faithful distributed auction mechanisms, namely distributed VCG and FAITH. In addition, we have extended FAITH to adapt to dynamic scenarios where agents can come and go at any time. We have analyzed their economic properties and complexities, and implemented them in various settings. Our evaluation results well demonstrate the properties of distributed VCG and FAITH in terms of social welfare and transmission overhead. As for our future work, we are interested in designing similar distributed mechanisms that can prevent collusion among multiple agents.

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