

# Theory and Practice of Vaccination

Tini Garske

Lecturer in Infectious Disease Analysis  
Director of the Vaccine Impact Modelling Consortium

# Lecture plan

- Review the basic theory of vaccination.
- The effect of vaccination on endemic disease in a population.
- The effect of vaccination on the disease dynamics.
- Rubella vaccination: perverse outcomes.
- Vaccination in practice: an example of a successful and an unsuccessful vaccination implementation.
- Pertussis vaccination.
- Vaccination in practice: Vaccine Impact Modelling Consortium

# Review of the theory of vaccination

Vaccination is the generation of immunity to a pathogen in an individual through administering an appropriate antigen.

To prevent the spread of disease within a population, it's necessary to vaccinate enough individuals to achieve **herd immunity**.

With herd immunity, each infectious individual infects only 1 other, on average.

$R_0$  is mean number of infections generated by an infectious individual in a susceptible population.

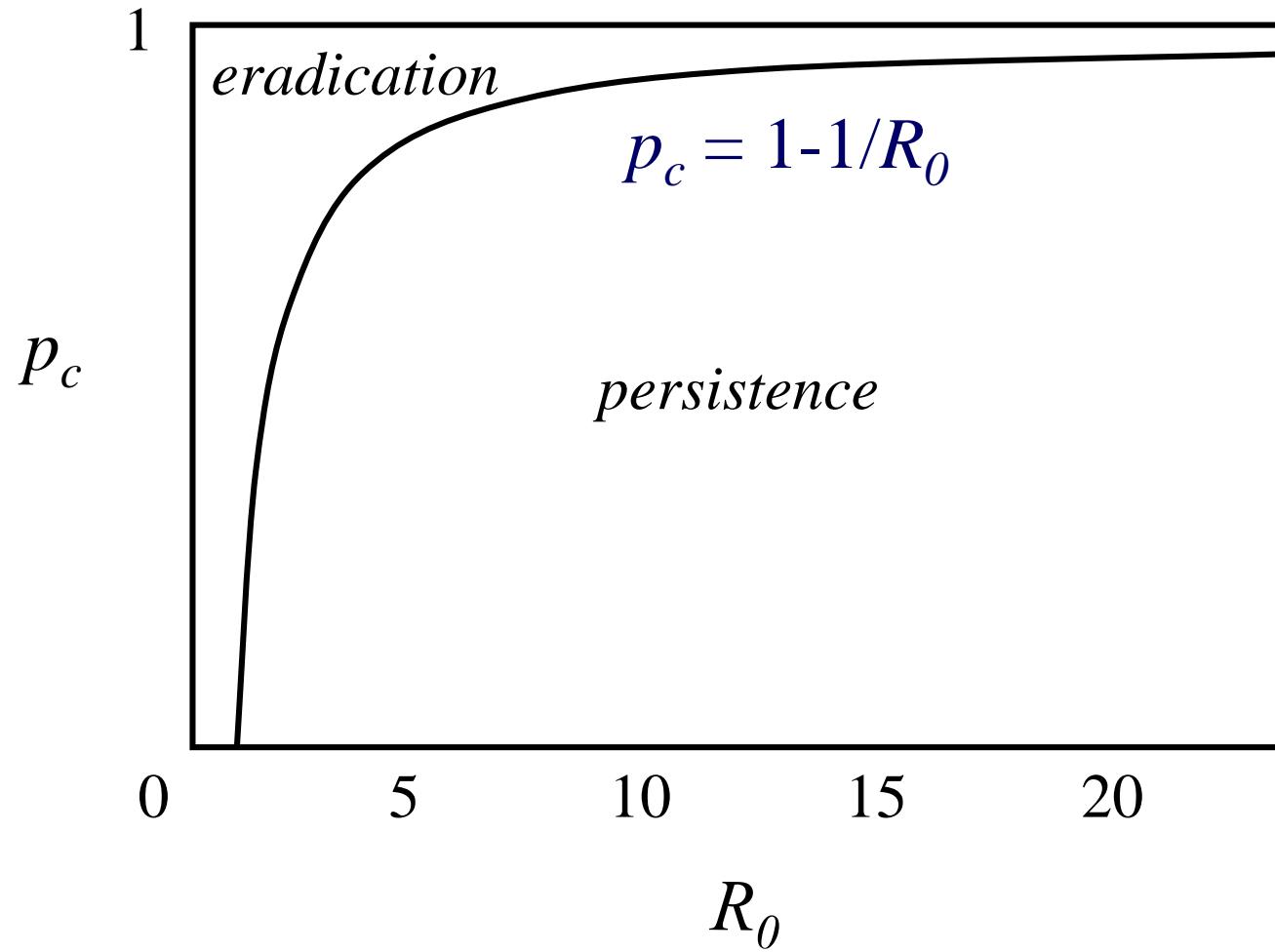
For vaccination coverage  $p$  of the whole population, effective reproductive number:

$$R = (1 - p)R_0$$

The minimum vaccination coverage for eradication is

$$R = 1 \Rightarrow p_c = 1 - 1/R_0$$

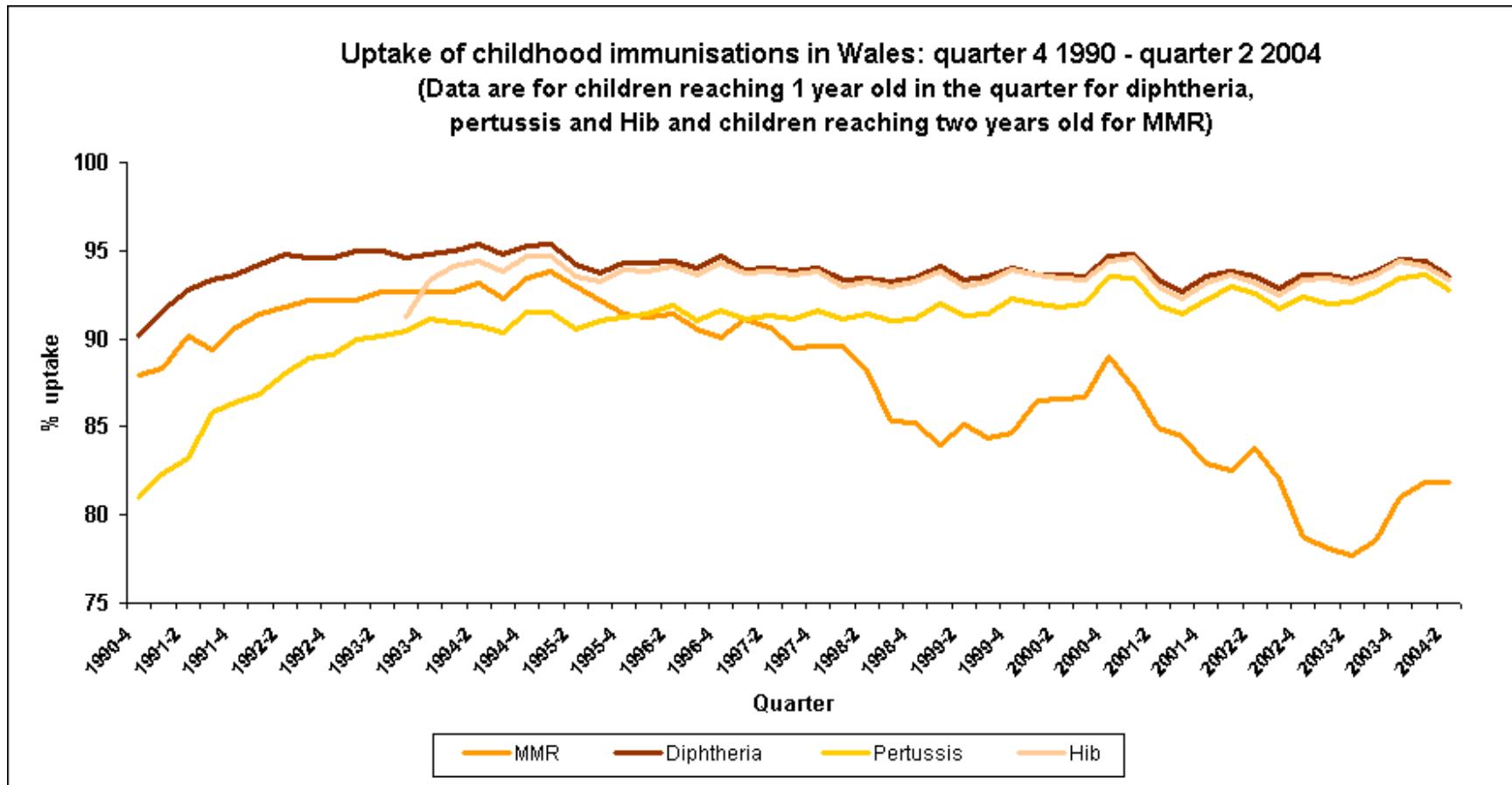
# Review of the theory of vaccination



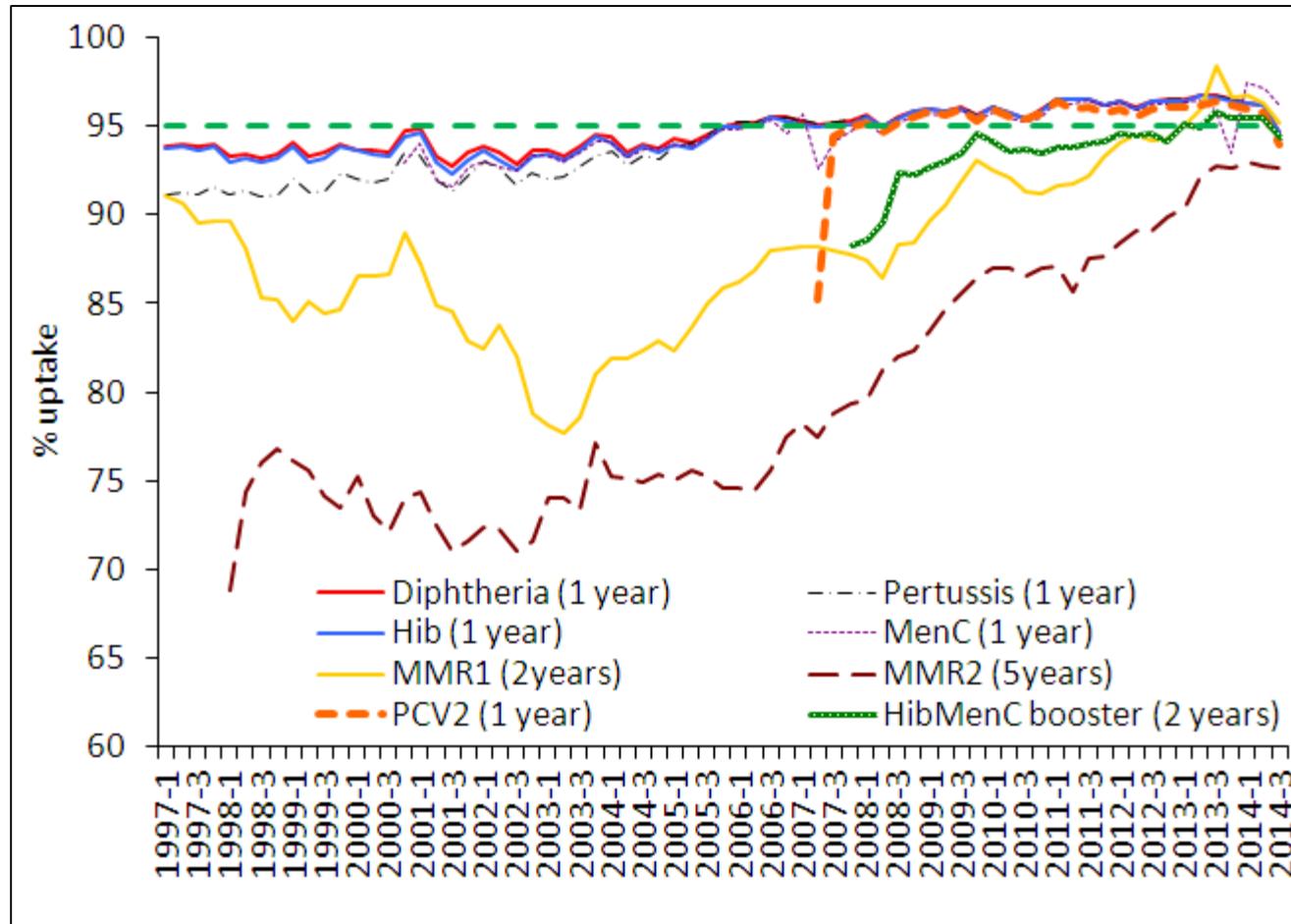
# Pre-vaccination $R_0$ estimates for England and Wales

Infection	$R_0$	$p_c$
Measles	16-18	94-96%
Mumps	11-14	91-93%
Rubella	6-7	83-87%
Pertussis	16-18	94-96%

# Vaccine coverage in Wales, 1990-2004



# Vaccine coverage in Wales, 1997-2014

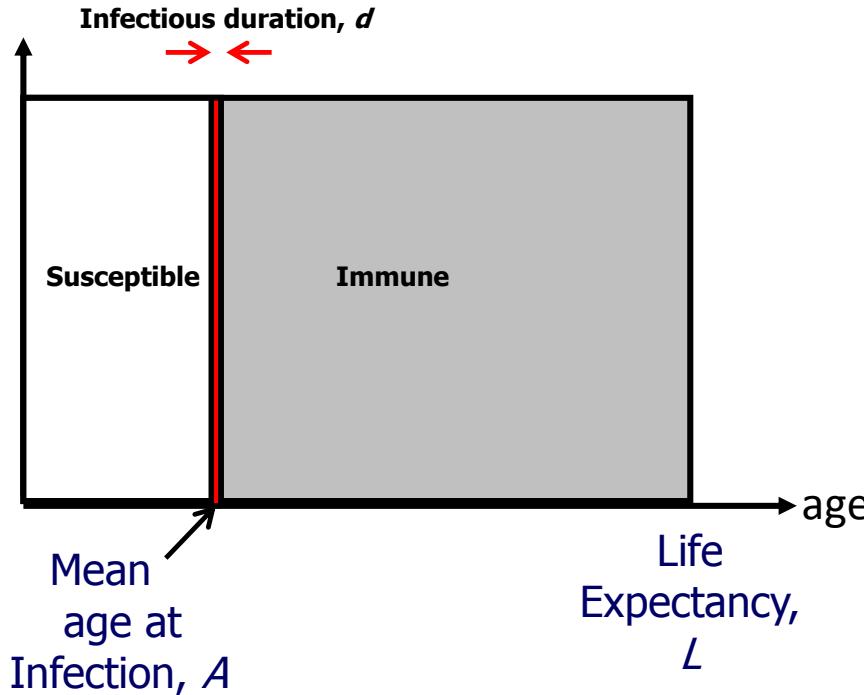


# Endemic disease in an unvaccinated population

Consider a population in a stable endemic state with a disease that confers lifelong immunity.

$$R_0 = \frac{L}{A}$$

$$\text{Disease prevalence} = \frac{d}{L}$$



$A$  is closely related to **force of infection**, the probability per unit time of an individual becoming infected:

Force of infection,  $\lambda = 1/A$

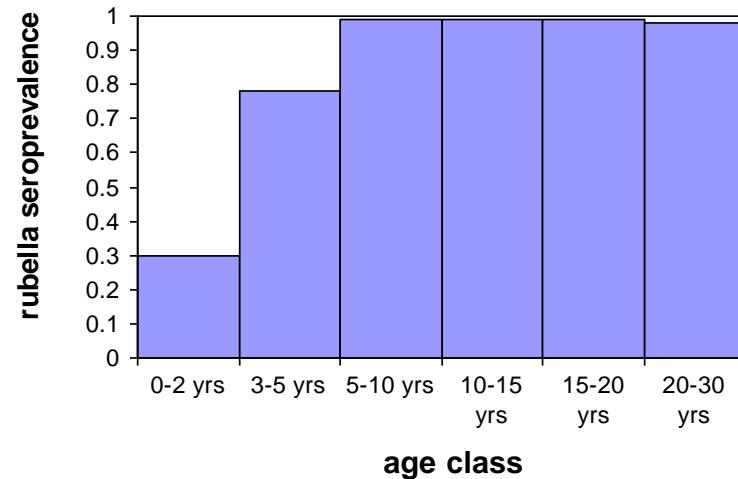
# $R_0$ and the mean age at infection $A$

## Rubella sero-prevalence by age

United Kingdom 1970-1972 data



The Gambia 1966-1976 data



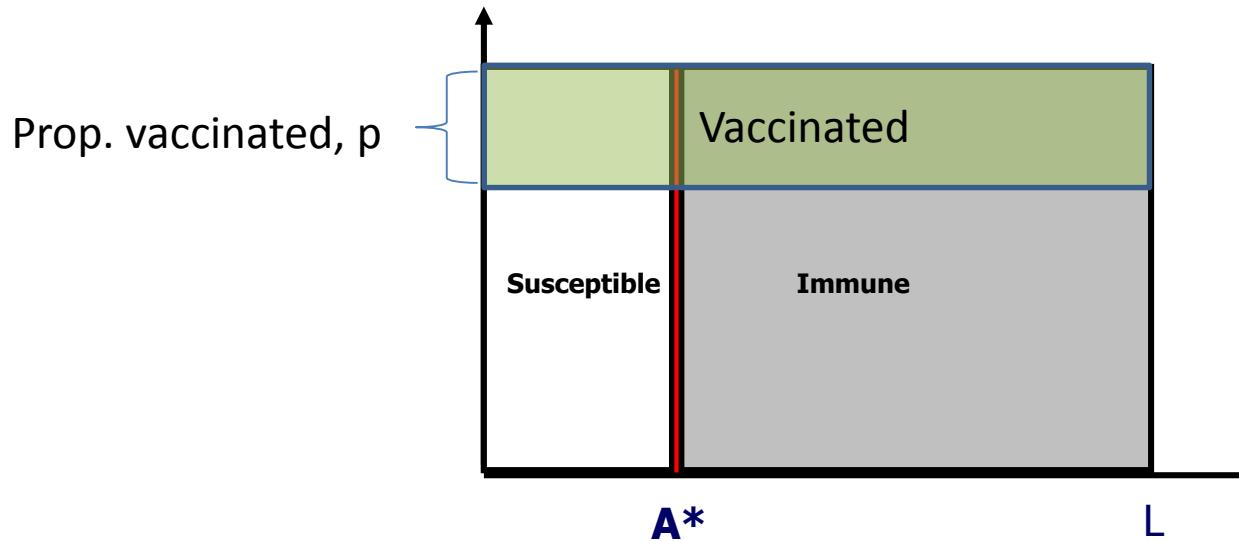
$$A_{\text{UK}} = 9-10 \text{ yrs}$$

$$A_{\text{Gambia}} = 2-3 \text{ yrs}$$

Force of infection =  $1/A$

# Endemic disease in a vaccinated population

Consider same population with a proportion  $p$  vaccinated, insufficient for eradication. It now has average age of infection,  $A^*$ .



Proportion of pop<sup>n</sup> susceptible is now

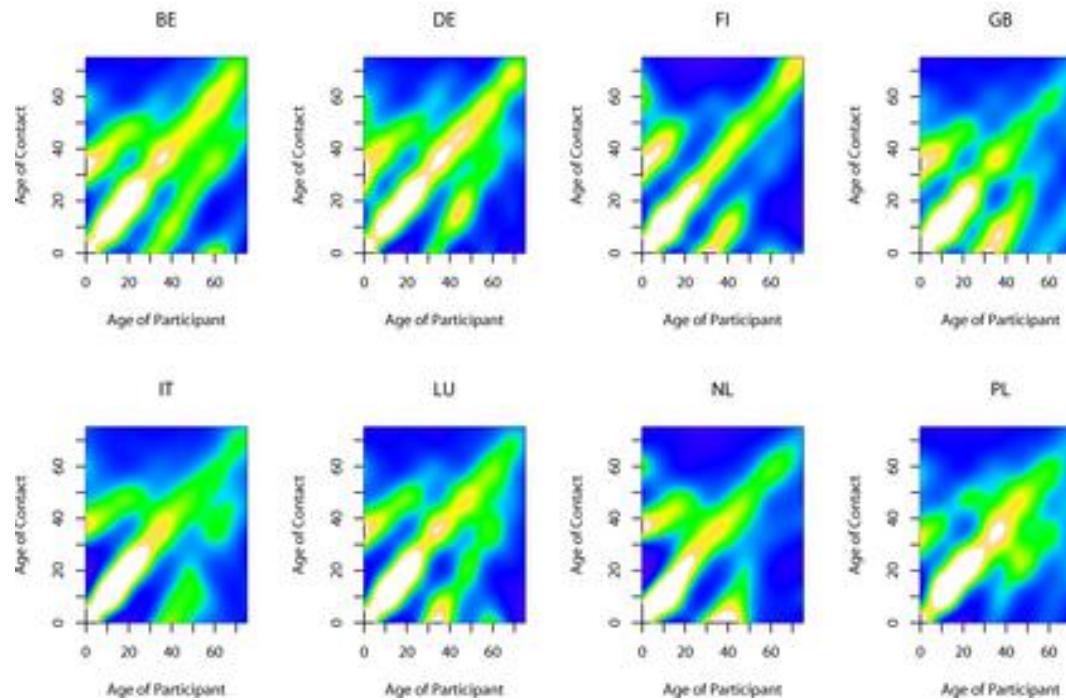
$$\frac{A^*(1-p)}{L} \rightarrow R_0 \frac{A^*(1-p)}{L} = 1$$

Comparing to the unvaccinated case:

$$A^* = \frac{A}{(1-p)}, \text{ prevalence} = \frac{(1-p)d}{L}$$

# Realistic infectious contacts

Real patterns of contact between individuals are strongly correlated with age. Figure shows intensity of contact as a function of ages of participants:

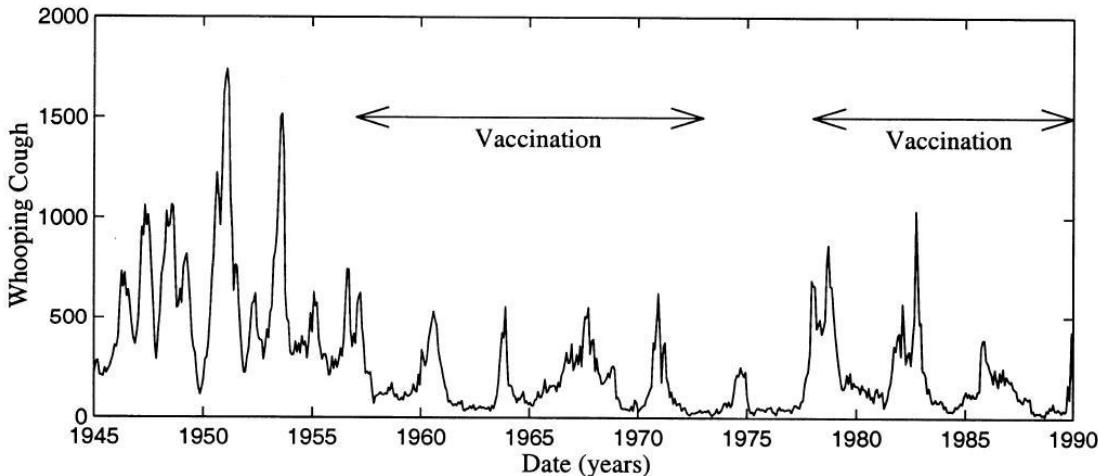


- Contact strongest between people of similar age.
- Contact most intense between school children.
- Note contacts between children and parents and also grandparents.

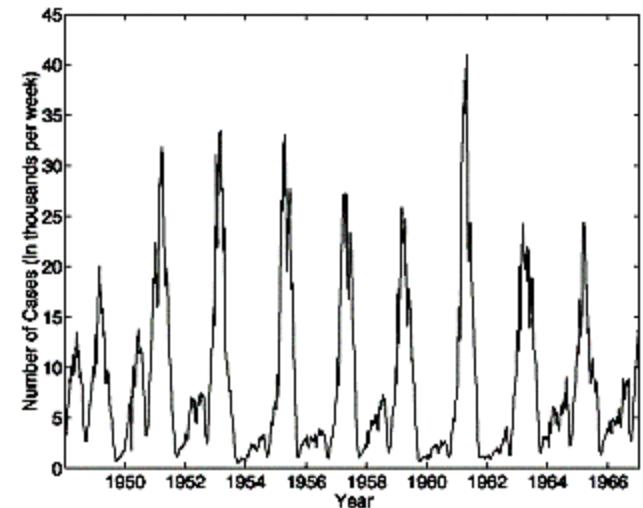
# Periodicity in incidence

- Infectious diseases are often characterised by periodicity in incidence rates.
- The degree of annual variability can be extremely high.
- Period can be annual, biannual, three or four yearly or highly variable.

London pertussis notifications



Measles, UK

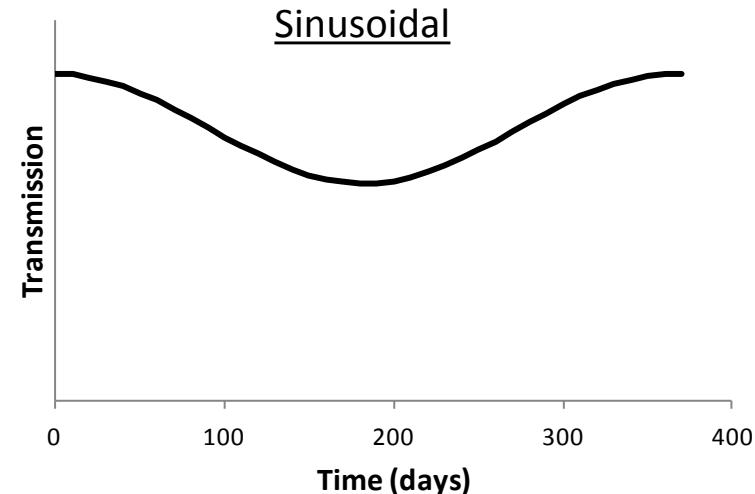
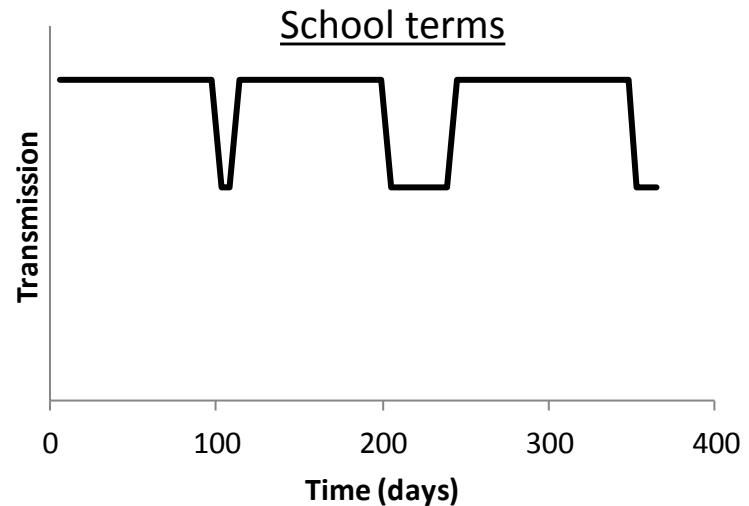


# Seasonality in transmission

Seasonal variation in incidence is mainly generated by annual cycles in transmissibility between individuals.

The possible mechanisms of variation are:

- Social distance: people spend more time indoors in winter, increasing the frequency and strength of contacts.
- School terms: Children in school experience more transmission in school than during holidays.
- Absolute humidity: drier air during winter facilitates aerosol transmission of disease (influenza).
- Vitamin D levels: Lower winter light levels leads lower Vitamin D levels which increase susceptibility



# Effect of vaccination on disease dynamics

The periodicity of disease incidence depends on:

- Mean age of infection.
- Birth rates in the population
- Seasonality of contact rates

with a period approximately given by

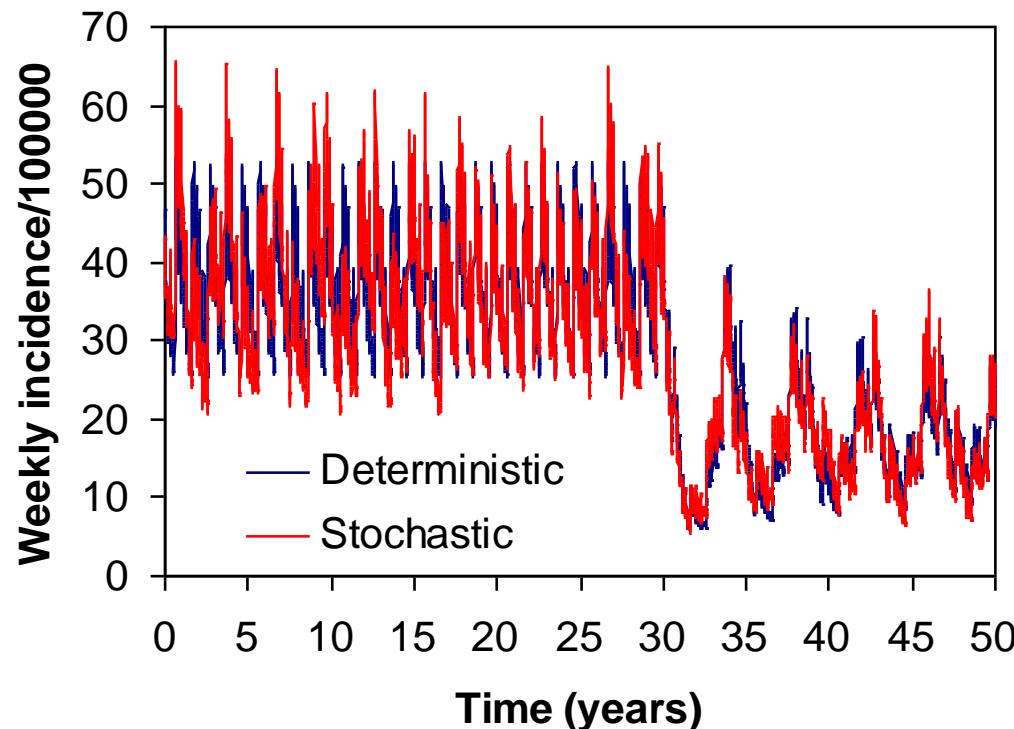
$$T \approx 2\pi\sqrt{Ad} = 2\pi\sqrt{\frac{d}{\lambda}}$$

The altered mean age of infection under vaccination gives a new longer period:

$$T \approx 2\pi\sqrt{\frac{Ad}{(1-p)}}$$

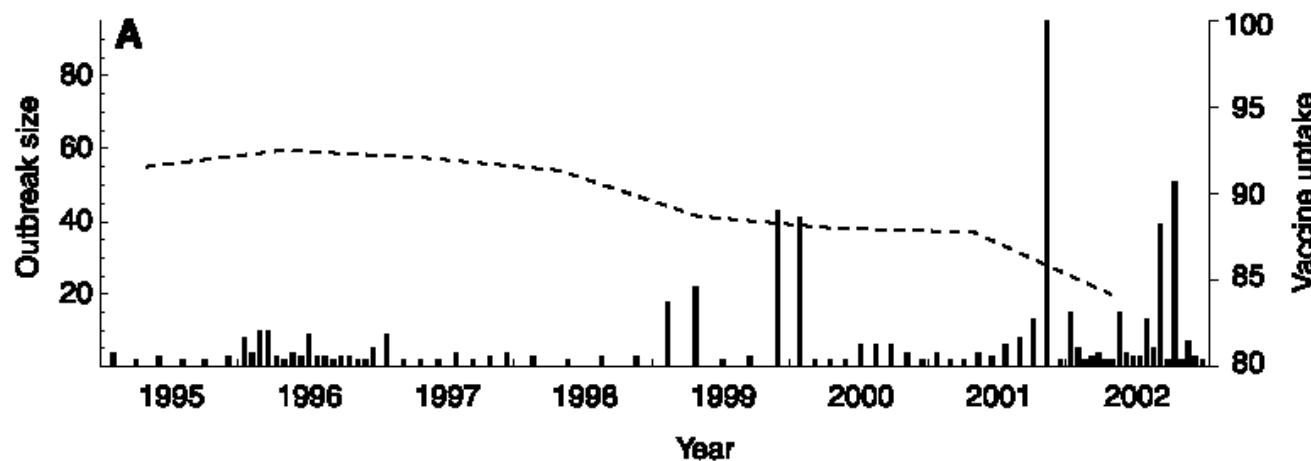
# Simulating the impact of vaccination

- Simple SEIR model, modeling 70% vaccination (at birth) with 85% efficacy.
- Assume vaccination reduces infectiousness.
- Switch from predominantly annual to 4-5 year cycles.
- Stochastic model somewhat more realistic.



# The impact of reduced MMR uptake

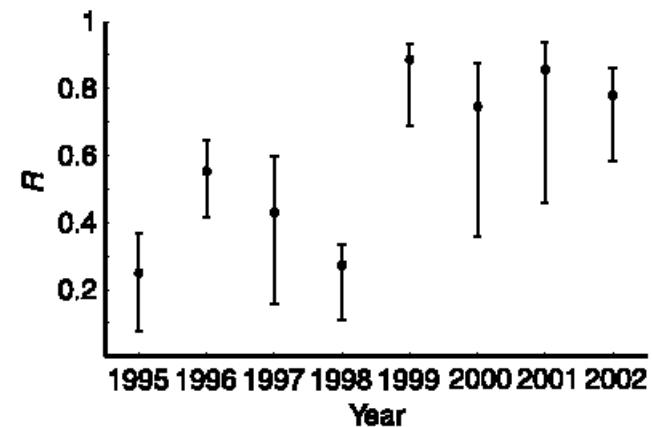
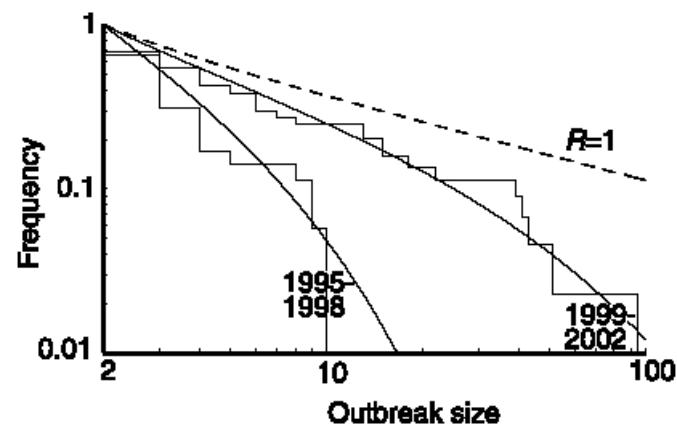
- The current concern about MMR uptake levels makes predicting the likelihood of a large measles outbreak a priority.
- Can data on the current small outbreaks seen in the last few years tell us anything?



[Jansen, V.A.A. et al, Science (2002), 301:804]

# Inferring $R$ from outbreak size distributions

- For sub-critical transmission, possible to estimate  $R$  from the distribution of outbreak sizes ( $m=2/(1-R)$ , where  $m$  is mean outbreak size).
- This analysis shows a significantly increased level of transmission in the period 1999-2002 compared with 1995-98.
- $R$  is now dangerously close to 1 – meaning a major measles outbreak is due any time.
- This is an intrinsically stochastic analysis – since outbreak size is a random variable.



# Introduction to rubella and CRS

## Rubella infection

- Virus, directly transmitted
- Mild fever
- Rash (punctate and maculopapular)
- Transmission to foetus possible ( $p>0.25$ ) when acquired during 1<sup>st</sup> trimester of pregnancy

## Congenital rubella infection

- causes Congenital Rubella Syndrome in about 80% of cases
- CRS: deafness, blindness, heart defects

# Epidemiology of CRS in the United Kingdom

<i>years</i>	71-75	76-80	81-85	86-90	91-95	96-00
CRI only	40	34	61	25	2	1
CRS	201	172	140	88	19	16
Total CRI/CRS births	241	206	201	113	21	17
Terminations for rubella (EW only)	3709	2002	759	268	43	17

## Vaccination policies in the UK

1970- 1988: selective immunisation: all schoolgirls, susceptible adult women

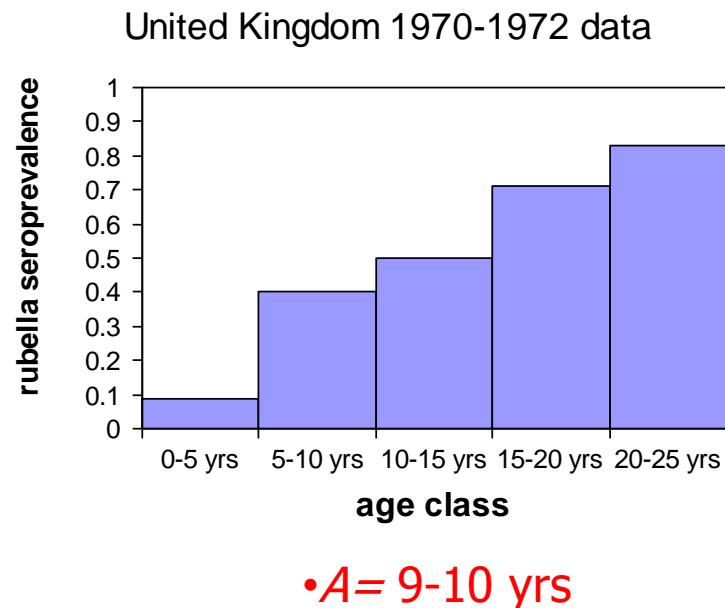
1988- now: MMR in second year of life

1996: schoolgirl immunisation program ceased

# Vaccination: a possible perverse outcome

The existence of an important risk group (women of child-bearing age) outside the usual age-range of infection can lead to unexpected effects.

- Pre-vaccination, most women are already immune to rubella by child-bearing age.
- Introducing vaccination will increase  $A$ , and hence the number of susceptibles in the risk group,  $S_\alpha$ .
- However, vaccination also decreases the force of infection,  $\lambda_\alpha$ , experienced by the risk group.

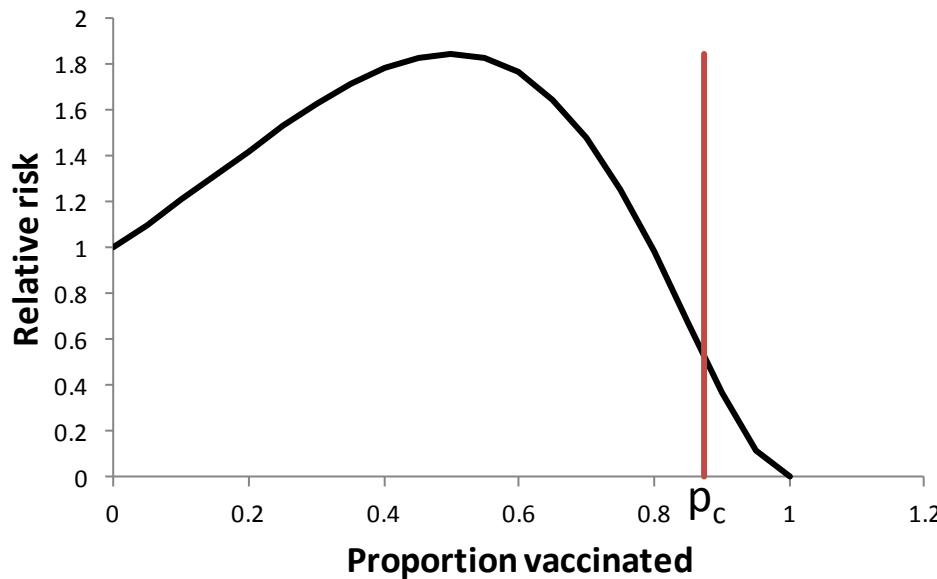


Case rate in the risk group is given by  $S_\alpha \lambda_\alpha$ , so:

If  $\lambda_\alpha \downarrow$  and  $S_\alpha \uparrow$  then  $\lambda_\alpha S_\alpha \downarrow$  or  $\uparrow$  ?

# Prediction of a simple model

A very simple model, based on vaccination at birth and uniform mixing shows an equilibrium increase in relative risk for a risk group at age 30. Risk increases with age and  $R_0$ .



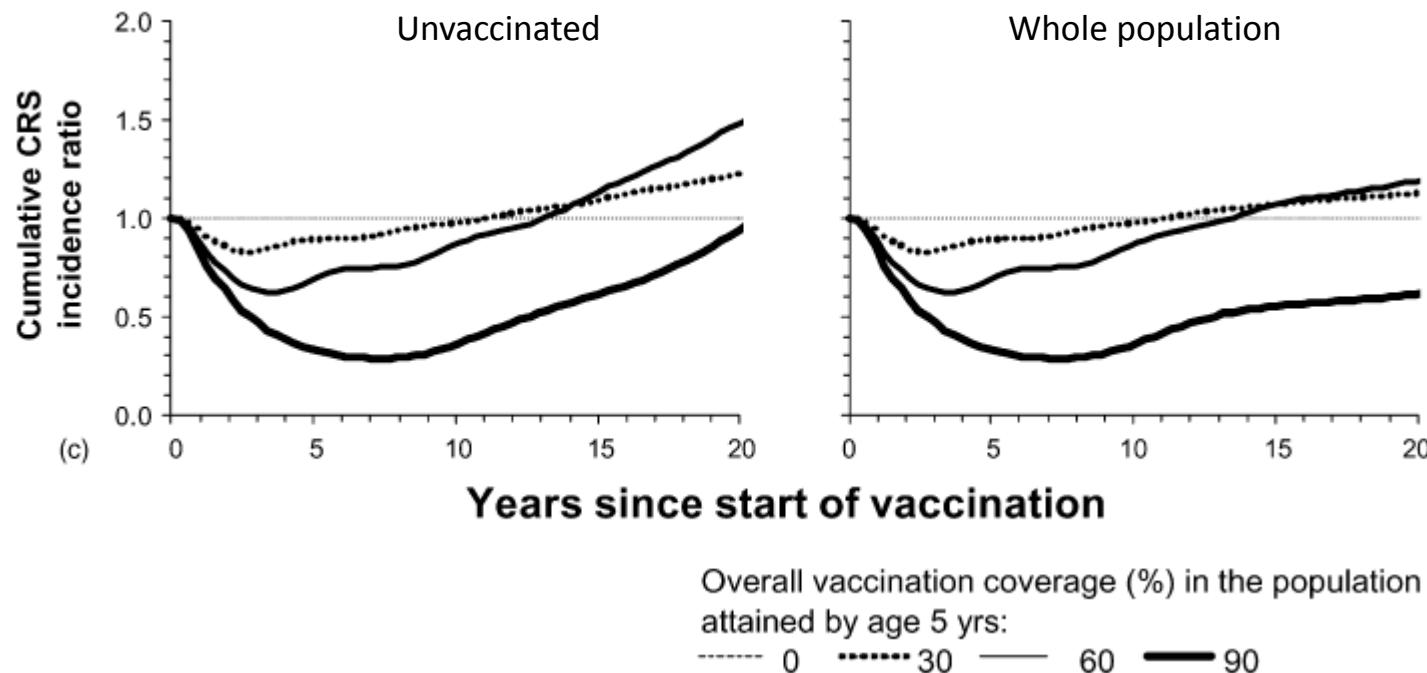
Is this effect seen in reality and, if so, how should vaccination programs be implemented to avoid it?

# CRS: partially vaccinated populations – short term

- MMR is recommended vaccine, but relatively expensive.
- In many countries, availability is through private healthcare and hence covers only a fraction of the population.

Vaccinated group pushes FOI down. What happens to unprotected in short and long term?

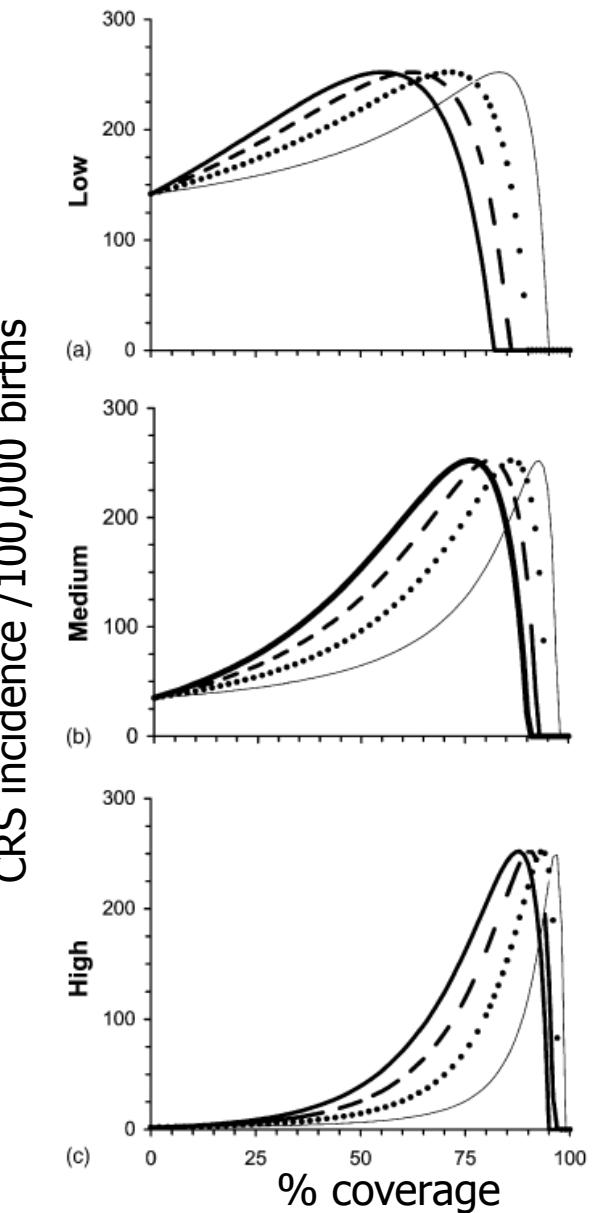
Short term:



# CRS: partially vaccinated populations – long term

Long term effects:

- Vaccination always increases CRS incidence in unvaccinated group.
- Incidence increases with coverage, up to a point.
- For medium-high pre-vaccination FOI, there is increase in the population as a whole.



# Vaccination in Greece

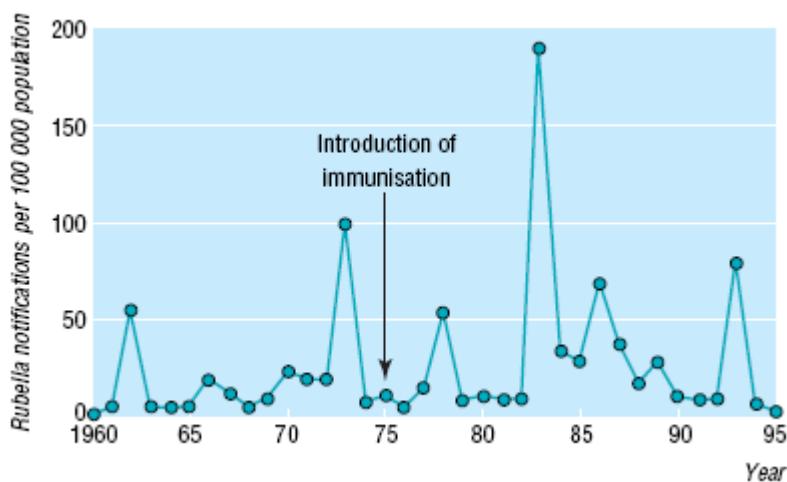
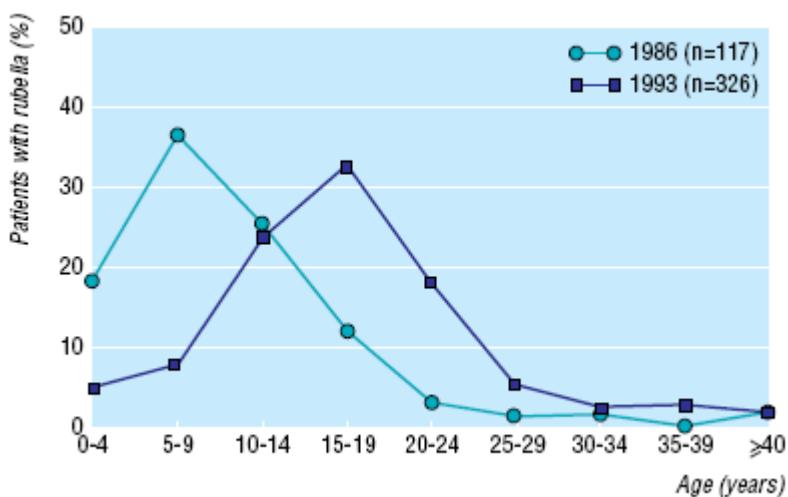
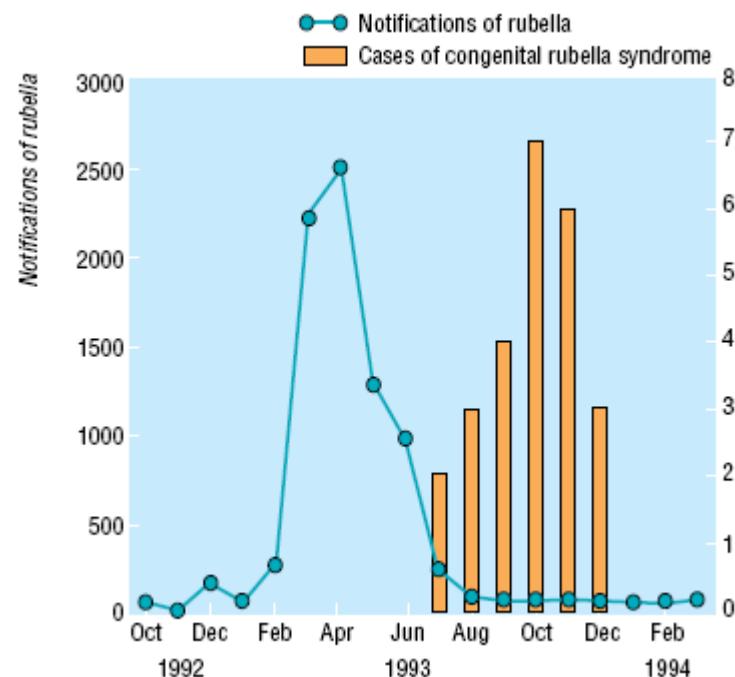
- Rubella vaccination in Greece started in '77; not compulsory and mainly in private sector.
- Aimed primarily at young children (indirect strategy).
- Compulsory MMR for 1 year-olds from 1989.
- Poor assessment of vaccine uptake and notification of rubella cases. However, coverage probably <<50% for children up to 1989.

Susceptibility in risk group

Year	% pregnant women susceptible
1971-5	12%
1980	11%
1981	17%
1984-9	24%
1990-1	36%

# Rubella and CRS in Greece

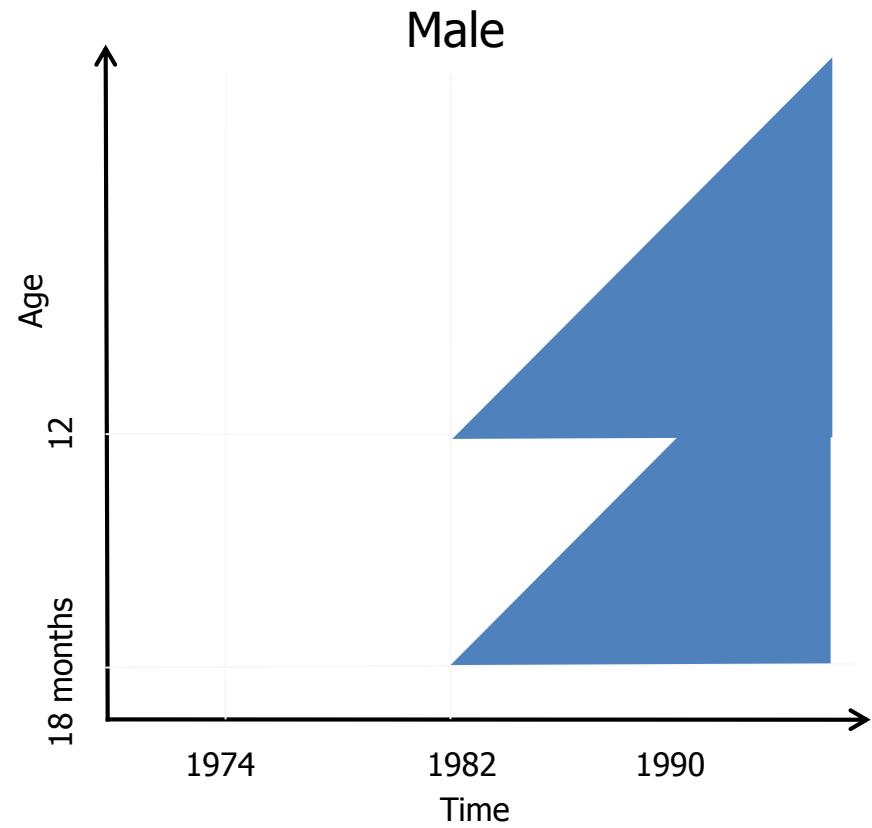
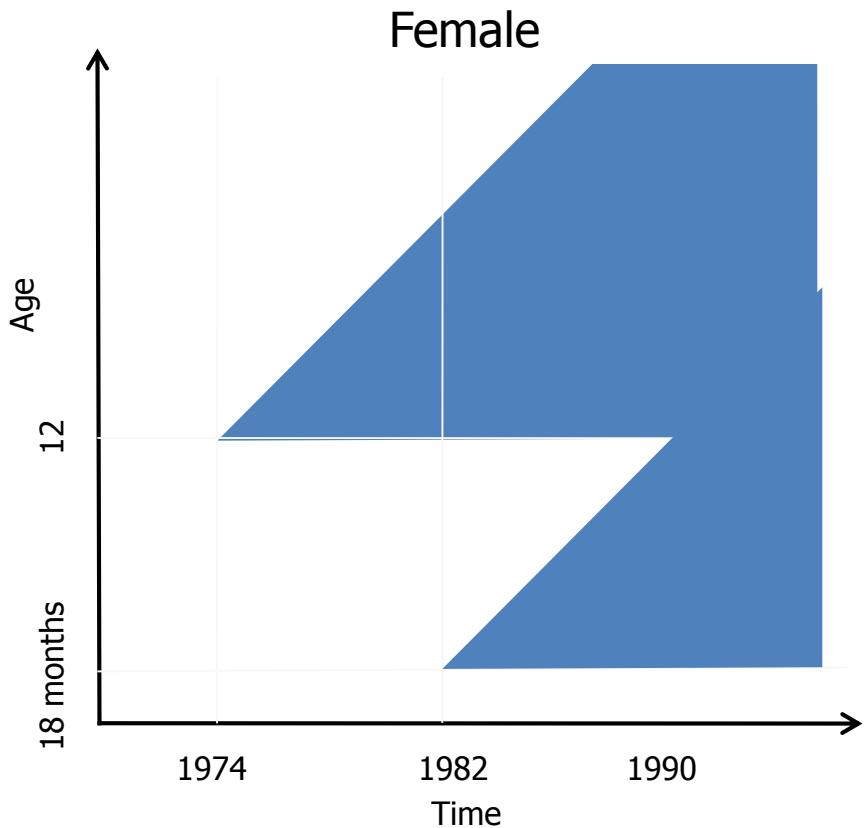
- In 1993, a major rubella epidemic occurred in Greece, resulting in 25 confirmed CRS cases.
- Note shift in age distribution of rubella cases.
- CRS incidence matches outbreak, shifted by 7 months.



# Implementation of vaccination in Sweden

'Standard' vaccination strategy (as used in UK, USA):

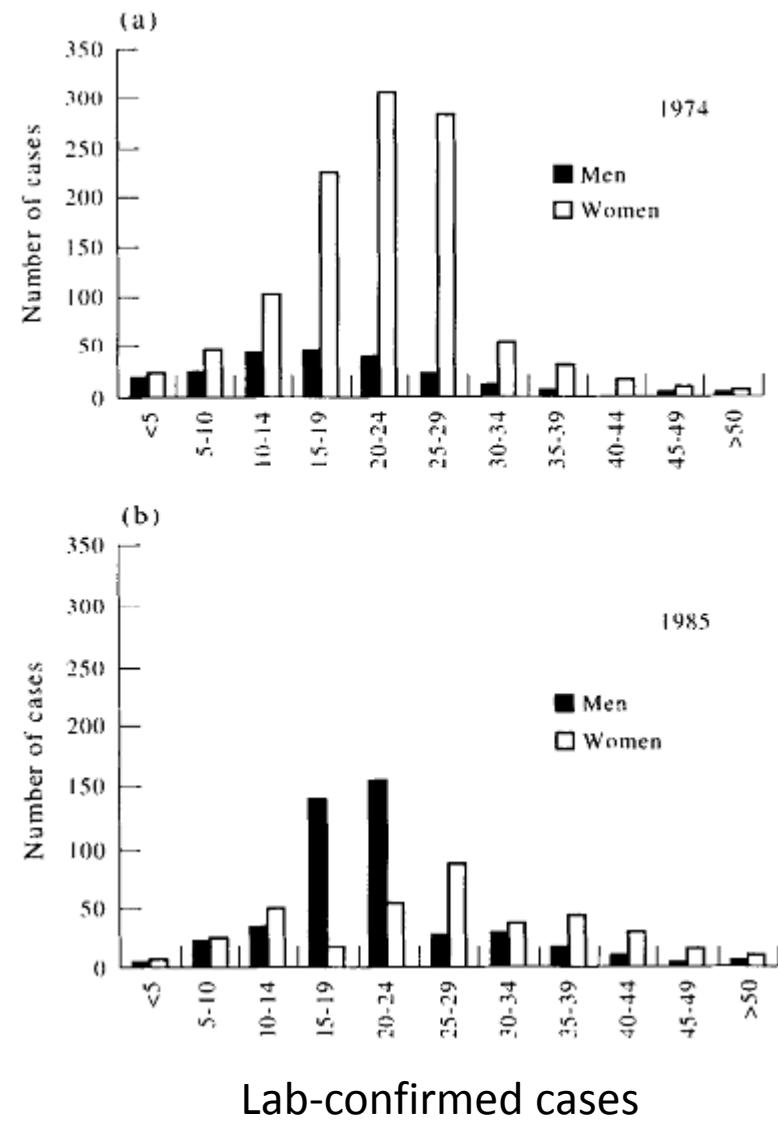
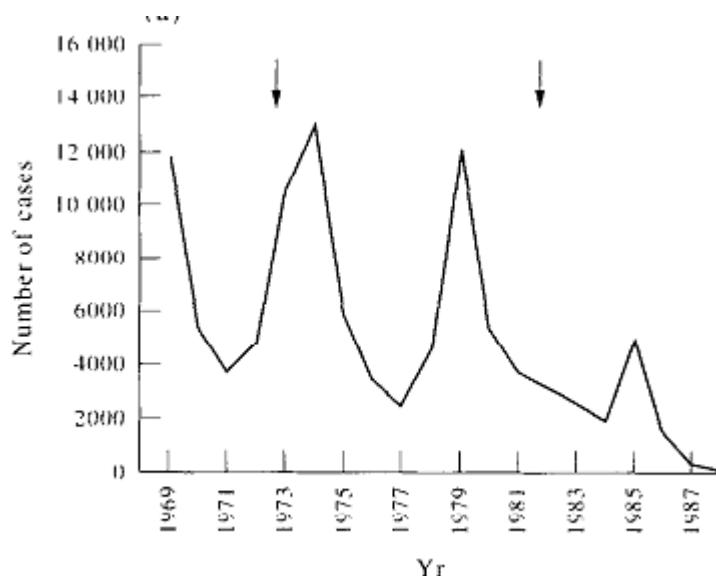
- 1974: direct phase. Vaccination of girls at 12 years. Also women, post-partum, if susceptible.
- 1982: indirect phase. vaccination of all 12-year-olds and children at 18 months.
- Coverage of target groups approximately 90% and increasing.



# Effect of vaccination in Sweden

## Effect of vaccination strategy:

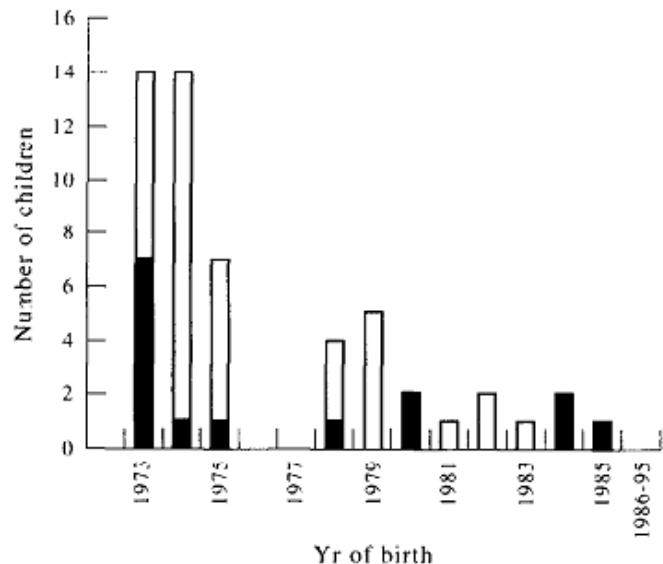
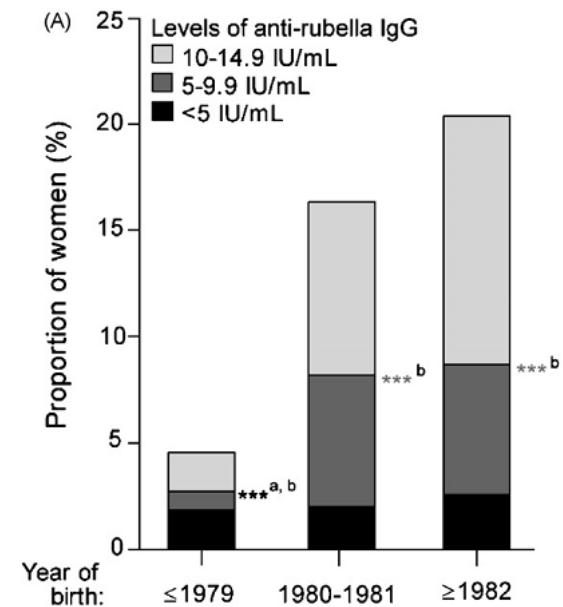
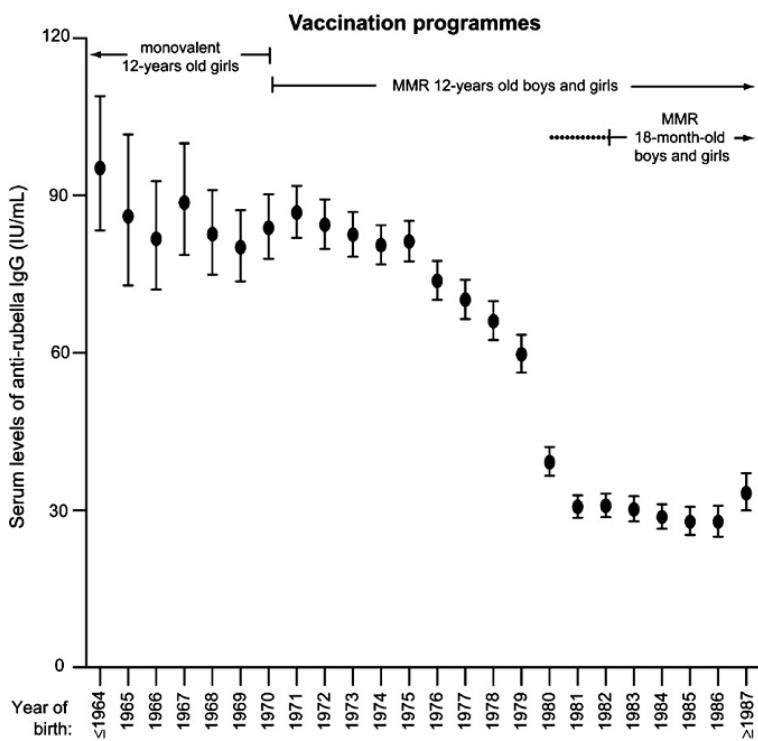
- Rubella effectively eradicated since mid-90s.
- CRS: since 1973 53 severe cases, since 1985, none.
- Pregnant women: 12% susc. -> 3% by '87.
- Changing coverage reflected in gender distribution of cases.
- Note gender-specific reporting bias.



# Serology in post-vaccination Sweden

Antenatal sera from primapara women:

- 95% of pregnant women protected.
- Serum IgG levels strongly depend on year of birth.
- Weaker protection for those born after ~1980.
- ‘Natural’ immunity stronger? Frequent challenge?
- Possible sub-clinical infections...



# Pertussis

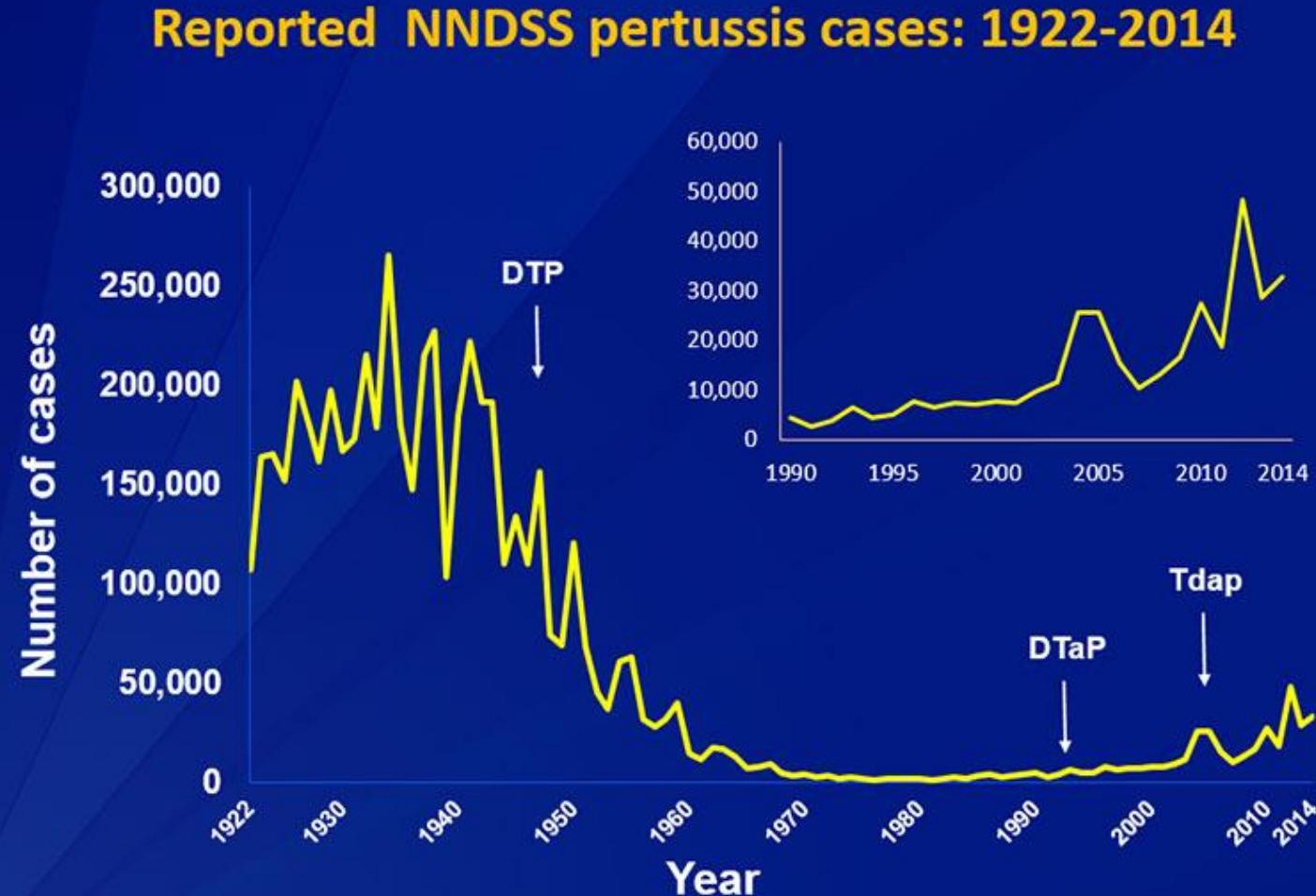
**Aetiological agent:** *Bordetella pertussis*, a gram-negative coccobacillus.

**Transmission:** Highly transmissible ( $R_0 \approx 16$ ), via direct contact with discharges from respiratory mucous membranes of infected persons.

**Clinical Features:** Highly communicable, vaccine-preventable disease that lasts for many weeks – can result in very severe coughing, whooping, and post-tussive vomiting.

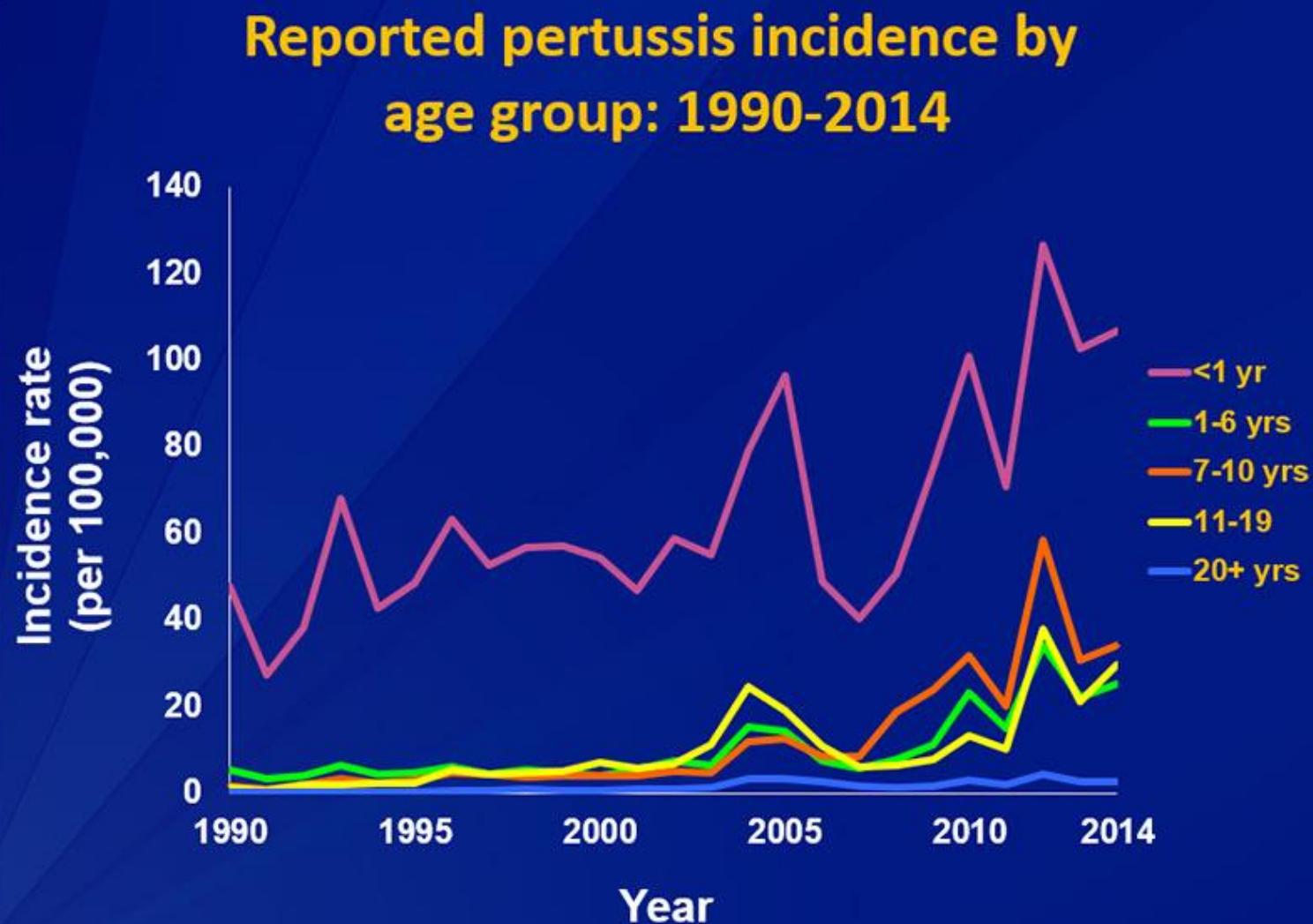
**Major complications:** most common in infants and young children and include hypoxia, apnea, pneumonia, seizures, encephalopathy, and malnutrition. High mortality in developing world.

# Pertussis incidence trend: US



SOURCE: CDC, National Notifiable Diseases Surveillance System and Supplemental Pertussis Surveillance System and 1922-1949, passive reports to the Public Health Service

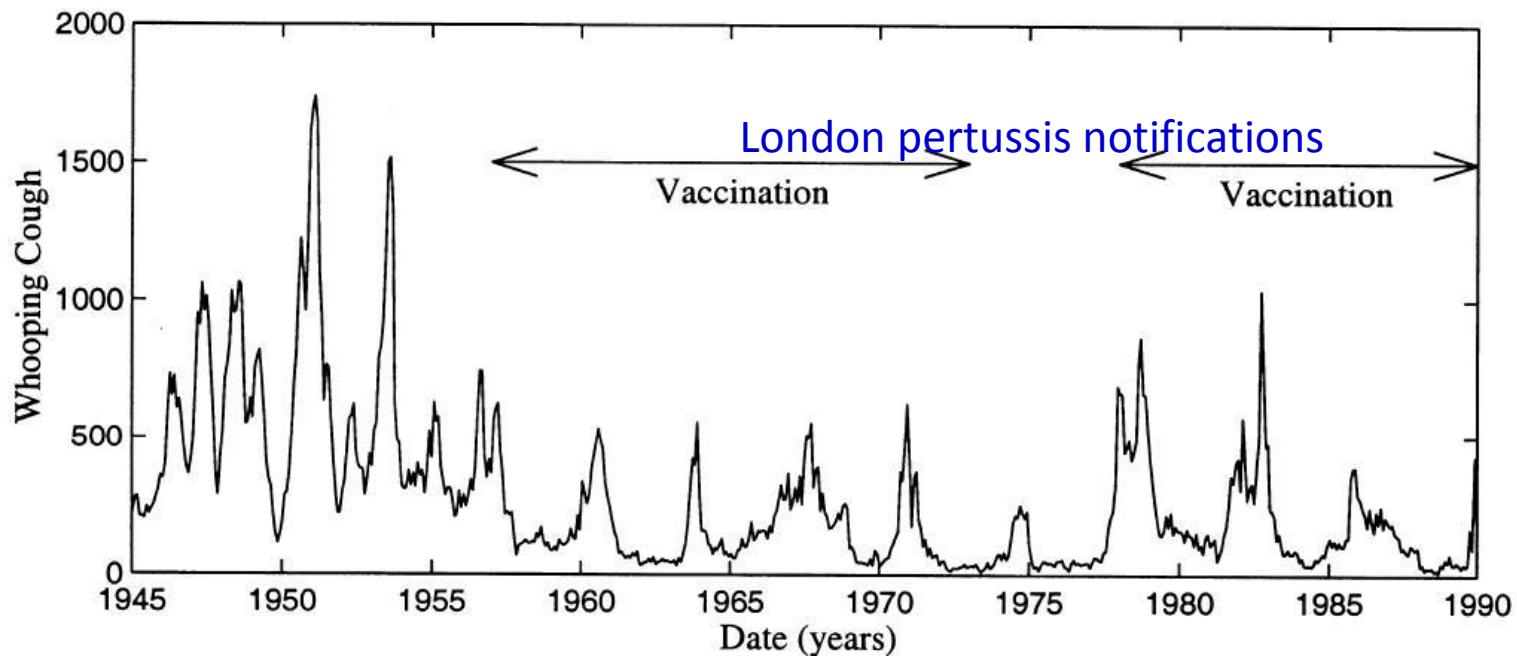
# Pertussis incidence trend: by age



SOURCE: CDC, National Notifiable Diseases Surveillance System and Supplemental Pertussis Surveillance System

# Dynamics

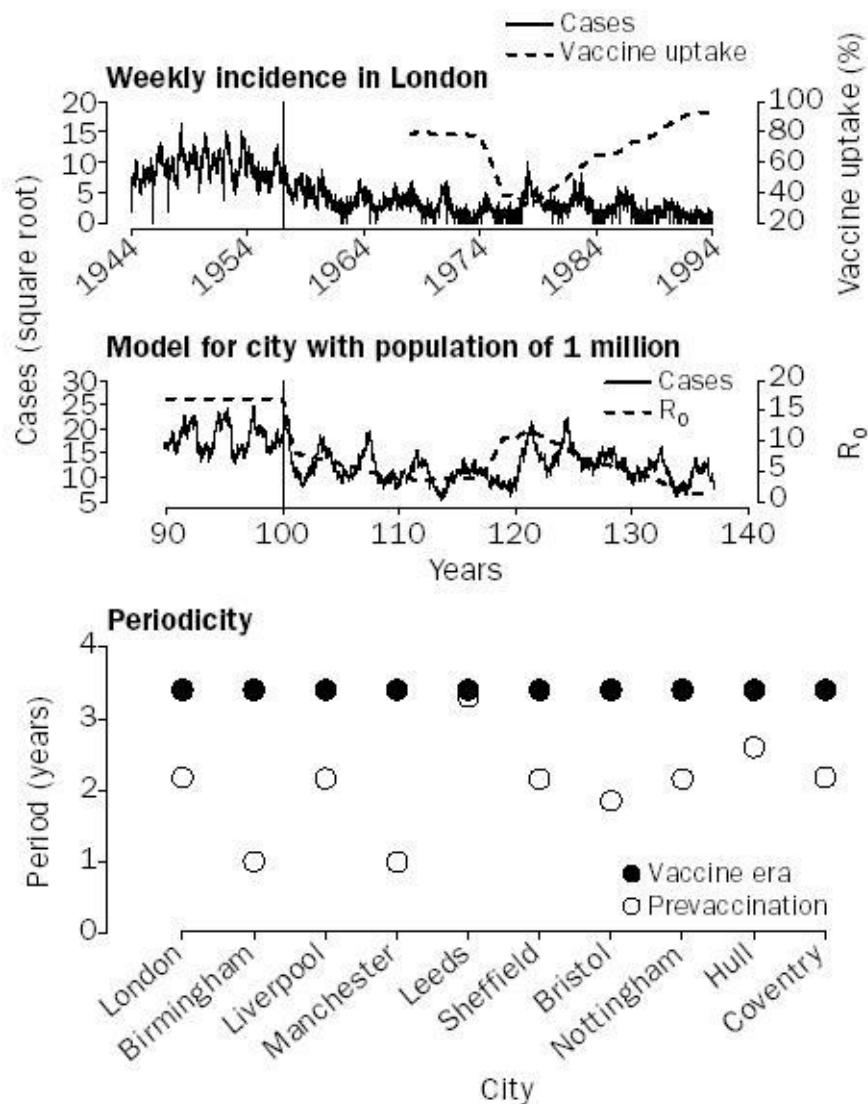
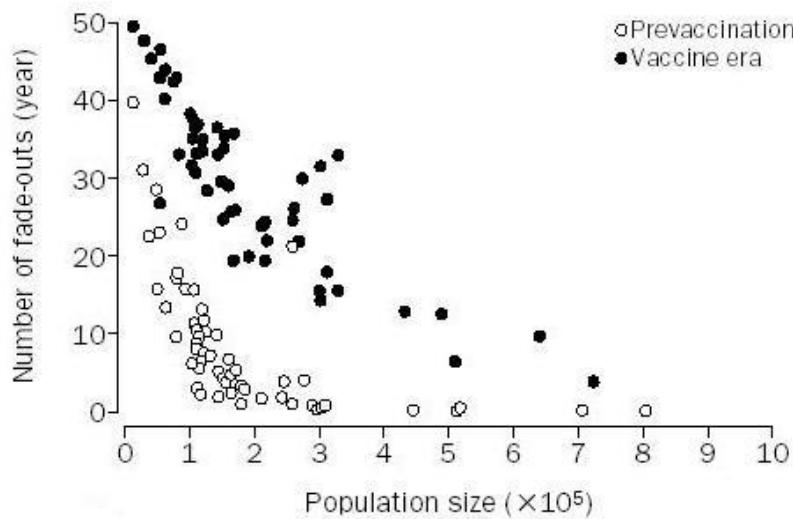
- Pre-vaccination dynamics show irregular annual epidemic cycles.
- Post-vaccination epidemics show ~4 year oscillations.



$$T \simeq 2\pi\sqrt{Ad} = 2\pi\sqrt{\frac{d}{\lambda}}$$

# Does vaccination reduce transmission?

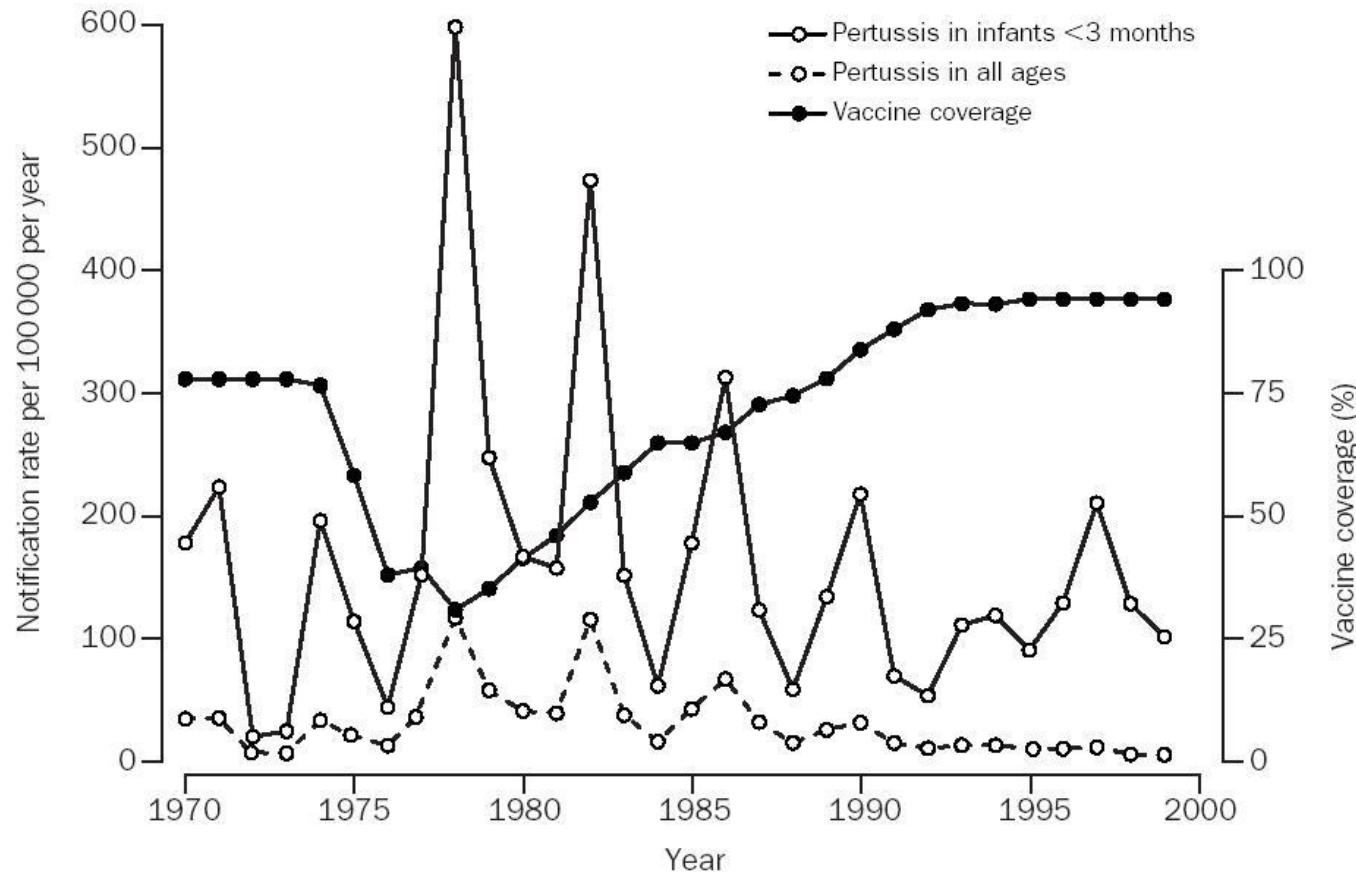
- Since whole cell vaccine is live, perhaps it contributes to asymptomatic infection?
- Can look for signatures of decline in temporal dynamics.



from Rohani et al, Lancet (2000) 355:285-6

# Does vaccination reduce transmission?

- Possibly simpler method is to look at age-related patterns of infection.
- In particular, look at reported case in infants <3 months (prior to vacc.)



from Gay & Miller, Lancet (2000) 355:1553

# Global vaccination programmes

- EPI – enhanced programme for immunization
  - Routine immunization in early childhood for a number of well established vaccines to prevent or reduce endemic disease burden
  - Which vaccines included, and at which ages differs between countries
- Vaccination campaigns
  - To increase population-level vaccination coverage quickly
  - To address gaps from low coverage of routine programmes



- New initiative (since Jan 2017, [www.vaccineimpact.org](http://www.vaccineimpact.org))
- Aim:
  - to quantify the impact of vaccination in low- and middle income countries globally
  - Impact = deaths and cases averted over the lifetime of vaccinated birth cohorts
  - Focussing on established vaccines (currently 10 antigens)
- Funded by Gavi, the Vaccine Alliance, and the Gates foundation
  - Impact estimates used to inform their investments, and to track progress against targets.



- Consortium approach:
  - Various modelling groups provide disease-specific estimates
  - These are then combined by the secretariat at Imperial College
  - Impact evaluated by estimating burden:
    - Assuming “best estimate” of vaccination coverage
    - Counterfactual scenario of no vaccination
    - Impact = difference in burden with and without vaccine

# Conclusions

- Vaccination protects individuals directly, but also indirectly through the effect of herd immunity.
- Vaccination reduces the force of infection in the population and this has indirect effects on the mean age of infection and the age distribution of sero-positive individuals.
- Vaccination strategies can have unexpected consequences, developing over many years to produce a negative outcome.
- In situations, in which the risk group and population driving the infection differ, great care is needed in designing vaccine interventions.

# References

- Kakoulidou, M., Forsgren, M., Lewensohn-Fuchs, I., & Johansen, K. (2009). Serum levels of rubella-specific antibodies in Swedish women following three decades of vaccination programmes. *Vaccine*, 28(4), 1002-1007.
- Bottinger, M., & Forsgren, M. (1997). Twenty years' experience of rubella vaccination in Sweden: 10 years of selective vaccination (of 12-year-old girls and of women postpartum) and 13 years of a general two-dose vaccination. *Vaccine*, 15(14), 1538-1544.
- Panagiotopoulos, T. et al., 1999. Increase in congenital rubella occurrence after immunisation in Greece: retrospective survey and systematic review. *BMJ (Clinical research ed.)*, 319(7223), pp.1462-7.
- Vynnycky, E., Gay, N. J., & Cutts, F. (2003). The predicted impact of private sector MMR vaccination on the burden of Congenital Rubella Syndrome. *Vaccine*, 21(21-22), 2708-2719.
- Rohani, P., Earn, D. J., & Grenfell, B. T. (2000). Impact of immunisation on pertussis transmission in England and Wales. *Lancet*, 355(9200), 285-6.
- A good mathematical but also practical approach can be found in the early chapters of Infectious Diseases of Humans: Dynamics and Control. by Anderson and May.

Unused slides

# The effect of vaccination on the age-susceptibility profile: a simple model calculation

In endemic equilibrium, prevalence only changes with age (not with time). Hence, for the susceptible population:

$$\frac{dX}{da} = -\lambda X - \mu X$$

Pre-vaccination:

vacc.

$$X(0) = 1$$

Post-vaccination:

$$X(0) = (1 - p)$$

FOI

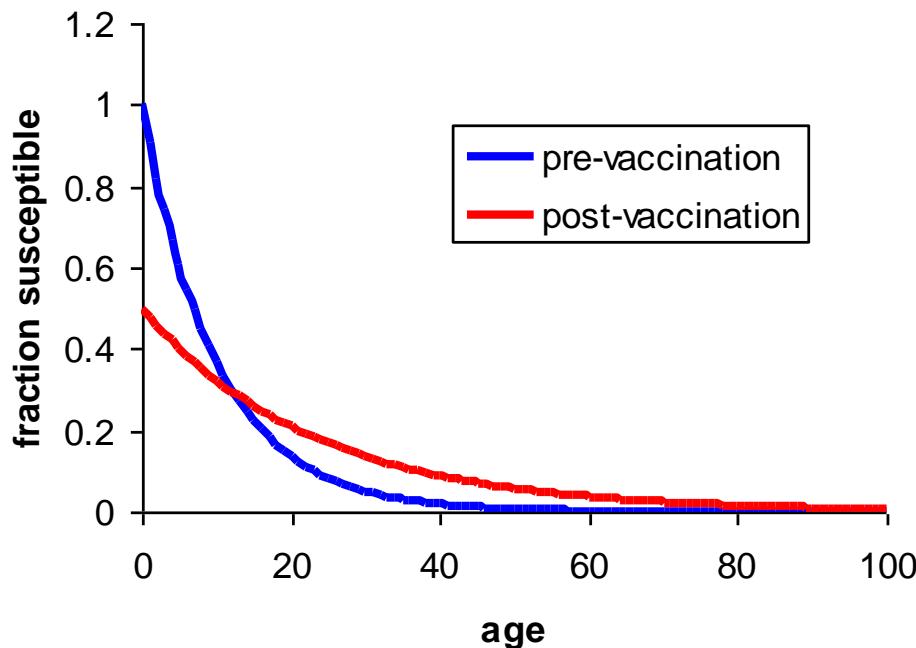
$$\lambda = \frac{1}{A} = R_0 \frac{1}{L} = R_0 \mu \quad \lambda^* = \frac{1}{A^*} = R_0 \frac{(1-p)}{L} = R_0(1-p)\mu$$

# Vaccination and age-susceptibility profiles

Pre-vaccination: Susc. fraction =  $\exp(-(\mu R_0 + \mu)a)$

Post-vaccination: Susc. fraction =  $(1-p)\exp(-(\mu(1-p)R_0 + \mu)a)$

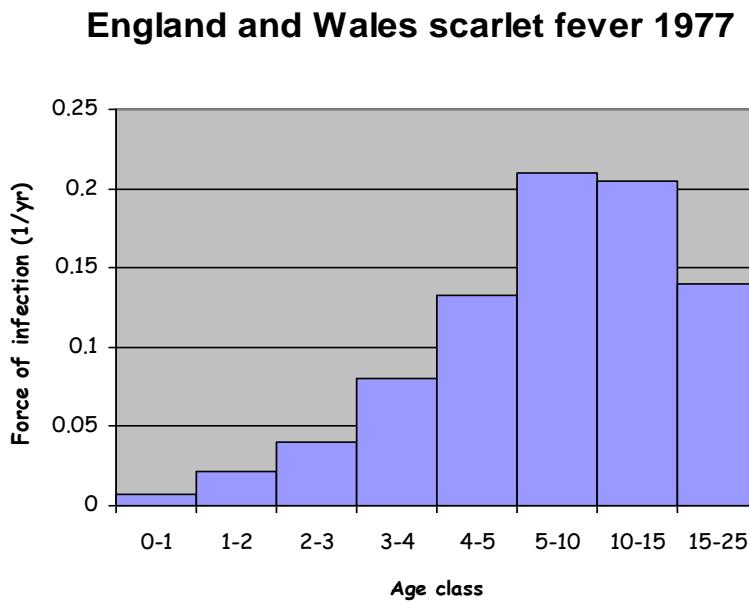
Example with  $p=50\%$



Ratio of risk =  
 $(1-p)^2 \exp(\mu R_0 pa)$

# Empirical evidence for age heterogeneity

For childhood diseases, studies measuring the force of infection have shown that it is age-dependent



**England and Wales 1956 pertussis data**



The effects of immunization programmes and other observed patterns cannot be reproduced with models without introducing age heterogeneity

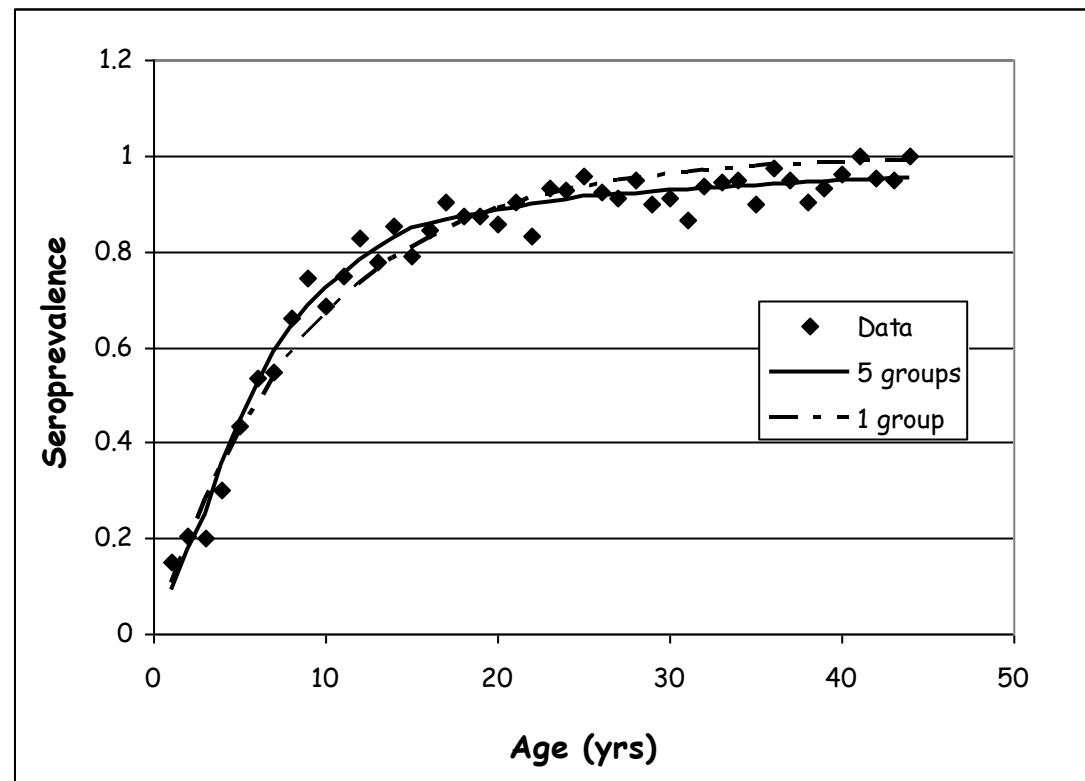
## Example: Seroprevalence data by age for Rubella, 1987 (Farrington, 2001)

$$\bar{\lambda}(A_0, A_1) = \frac{1}{A_1 - A_0} \ln \left[ \frac{1 - p(A_0)}{1 - p(A_1)} \right]$$

### Results of fitting

Homogeneous mixing:  
 $\lambda=0.11/\text{yr}$

Heterogeneous mixing:  
0-3 yrs:  $\lambda=0.098$   
3-8 yrs:  $\lambda=0.15$   
8-15 yrs:  $\lambda=0.12$   
15-25 yrs:  $\lambda=0.056$   
25+ yrs:  $\lambda=0.033$



Steeper curve at younger ages and flatter at older ages reflects the stronger contact among children at school compared to adults.

# Periodicity in incidence

- Incidence rates are usually highly variable over time.
- A range of periods are observed (annual, biennial, 3, 4, 5...)
- Behaviour often varies over longer time periods.
- Sometimes, behaviour appears random

