

IN2009
Language Processors

Week 3

Parsing I (syntax analysis)

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Before we start...

- Discussion of last week's optional regular expression exercises:
 - UK phone numbers
 - UK postcodes
 - Email addresses

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Session Plan

Session 3: Parsing (syntax analysis)

- syntax definition
 - context free grammars (BNF)
- parsing
- ambiguous grammars
- removal of left recursion
- top down recursive descent parsing
- extended BNF (EBNF)
- parsing using JavaCC

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Syntax definition

- We need to recognise structures like expressions with parentheses, or nested statements:
 - (109+23) (1+(250+3))
 - `if (...) then if (...) stmts... else ... else ...`
- How do we do this?

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Syntax definition

- It is tempting to attempt to use regular expressions
 - digits = [0-9]+
 - sum = expr "+" expr
 - expr = "(" sum ")" | digits

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Syntax definition

- But remember that regular expression abbreviations like digits are only abbreviations and are *substituted* directly (they are macros), so we would get
 - expr = "(" sum ")" | digits
 - expr = "(" (*expr* "+" *expr*) ")" | digits (*substitute sum*)
 - expr = "(" ("(" (*expr* "+" *expr*) ")" | *digits*) "+" *expr* ")" | digits (*substitute expr, then what?*)
 - ...

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Syntax definition

- An automaton cannot be created from such definitions.
- What we need is a notation where the recursion does not mean abbreviation and substitution, but instead means **definition...**

Syntax definition

- Then, $(1+(250+3))$ can be recognised by our recursive definitions

```

expr => "(" sum ")" | digits
=> "(" expr "+" expr ")" (using the sum definition)
=> "(" digits "+" expr ")" (using the expr definition)
=> "(" 1 "+" expr ")"
=> "(" 1 "+" "(" sum ")" ")"
=> "(" 1 "+" "(" expr "+" expr ")" ")"
=> "(" 1 "+" "(" digits "+" expr ")" ")"
=> "(" 1 "+" "(" digits "+" digits ")" ")"
=> "(" 1 "+" "(" 250 "+" digits ")" ")"
=> "(" 1 "+" "(" 250 "+" 3 ")" ")"

```

Syntax definition

- Alternation within definitions is then not needed, since
 - $r = ab(c|d)e$ is the same as:
 - $n = (c|d)$ and $r = abne$
 - or even $n = c$ with $n = d$ with $r = abne$, so alternation not needed at all!
 - we will however retain alternation at the top level of definition.

Syntax definition

- repetition via Kleene closure $*$ is not needed, since
 - $e = (abc)^*$ is the same as $e = (abc)e$ with $e = \epsilon$
- this recursive notation is called *context-free grammars* or BNF (see Session 1)
 - recognised by pushdown automata (PDA); recognition is implemented in many ways
 - involves (implicitly or explicitly) building the concrete syntax (parse) tree, matching against the tokens produced by the lexical analyser
 - building the tree can be top-down or bottom-up
 - once again, a tool can produce a parser for us

Context-free grammars

- A *language* is a set of *strings*
- Each string is a finite sequence of *symbols* taken from a finite *alphabet*
- For parsing: symbols = lexical tokens, alphabet = set of token types returned by the lexical analyser
- A grammar describes a language
- A grammar has a set of *productions* of the form $symbol \rightarrow symbol\ symbol\ \dots\ symbol$
- Zero or more symbols on RHS
- Each symbol either a *terminal* from the alphabet or a *non-terminal* (appears on LHS of some productions)
- No token ever on LHS of production
- One non-terminal distinguished as *start symbol* of the grammar

Syntax for straight-line programs

```

1  S → S ; S
2  S → id := E
3  S → print ( L )
4  E → id
5  E → num
6  E → E + E
7  E → ( S , E )
8  L → E
9  L → L , E

```

- a *context-free grammar*
- terminal symbols (tokens):
id print num , () := ; +
- non-terminal symbols:
S E L
- start symbol S

Derivations

$a := 7 ;$
 $b := c + (d := 5+6, d)$

\underline{S}
 $\underline{S} ; id := E$
 $id := \underline{E} ; id := E$
 $id := num ; id := \underline{E}$
 $id := num ; id := E + \underline{E}$
 $id := num ; id := \underline{E} + (S, E)$
 $id := num ; id := id + (\underline{S}, E)$
 $id := num ; id := (id := \underline{E}, E)$
 $id := num ; id := (id := E + E, \underline{E})$
 $id := num ; id := (id := \underline{E} + E, id)$
 $id := num ; id := (id := num + \underline{E}, id)$
 $id := num ; id := (id := num + num, id)$

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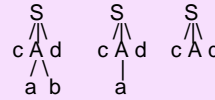
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Parsing

$S \rightarrow c A d$
 $A \rightarrow ab \mid a$

input: c a d



Bottom-up or top-down

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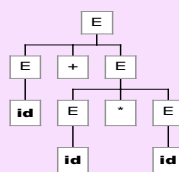
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Concrete syntax derivations and parse trees

$E \rightarrow E * E \mid E / E \mid E + E \mid E - E \mid (E) \mid id \mid num$

Leftmost derivation of $id + id * id$:

Concrete syntax tree
(parse tree):



E
 $\Rightarrow E * E$
 $\Rightarrow E + E * E$
 $\Rightarrow id + E * E$
 $\Rightarrow id + id * E$
 $\Rightarrow id + id * id$

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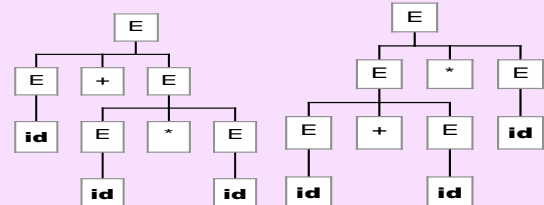
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Ambiguous grammars

$E \rightarrow E * E \mid E / E \mid E + E \mid E - E \mid (E) \mid id \mid num$

Two parse trees for $id + id * id$



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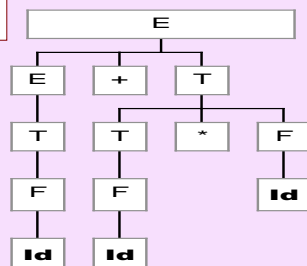
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Disambiguating the grammar

$E \rightarrow E + T$
 $E \rightarrow E - T$
 $E \rightarrow T$
 $T \rightarrow T * F$
 $T \rightarrow T / F$
 $T \rightarrow F$
 $F \rightarrow id$
 $F \rightarrow num$
 $F \rightarrow (E)$

Only one tree now possible
from this BNF for input string
 $id + id * id$



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Recursive descent parsing

• AKA "Top down"

- Each grammar production turns into one clause of a recursive function
- Only works on grammars where the first terminal symbol of each grammatical construct provides enough information to choose the production

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Recursive descent parsing

$S \rightarrow \text{if } E \text{ then } S \text{ else } S$
 $S \rightarrow \text{begin } S \text{ L}$
 $S \rightarrow \text{print } E$
 $L \rightarrow \text{end}$
 $L \rightarrow ; S L$
 $E \rightarrow \text{num} = \text{num}$

```

void S() {
    switch (tok) {
        case IF:
            eat(IF); E(); eat(THEN);
            S(); eat(ELSE); S(); break;
        case BEGIN: eat(BEGIN); S(); L();
            break;
        case PRINT: eat(PRINT); E();
            break;
    }
    void E() { eat(NUM); eat(EQ);
        eat(NUM); }
    void eat(int t) { if tok==t
        advance()
        else error();
    }
}
    
```

Appel 2002, (p46, Gram 3.11)

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But... (p46, Gram 3.10)

- if we try to implement a recursive descent parser for the disambiguated expression grammar...

$E \rightarrow E + T$	$T \rightarrow T * F$	$F \rightarrow \text{id}$
$E \rightarrow E - T$	$T \rightarrow T / F$	$F \rightarrow \text{num}$
$E \rightarrow T$	$T \rightarrow F$	$F \rightarrow (E)$

```

void E() {
    switch (tok) {
        case ???: E(); eat(PLUS); T(); break;
        case ???: E(); eat(MINUS); T(); break;
        case ???: T(); break;
    }
}
    
```

- TWO problems:

- no initial terminal symbol to tell us which production to choose
- left-recursion means E() is called immediately...

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Eliminating left recursion

$X \rightarrow X \gamma$
 $X \rightarrow \alpha$

can always be rewritten

$X \rightarrow \alpha X'$
 $X' \rightarrow \gamma X'$
 $X' \rightarrow$

$S \rightarrow E \$$ $E \rightarrow T E'$ $E' \rightarrow + T E'$ $E' \rightarrow - T E'$ $E' \rightarrow$	$T \rightarrow F T'$ $T' \rightarrow * F T'$ $T' \rightarrow / F T'$ $T' \rightarrow$	$F \rightarrow \text{id}$ $F \rightarrow \text{num}$ $F \rightarrow (E)$
--	--	--

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Sketch of resulting recursive descent parser

$S \rightarrow E \$$ $E \rightarrow T E'$ $E' \rightarrow + T E'$ $E' \rightarrow - T E'$ $E' \rightarrow$	$T \rightarrow F T'$ $T' \rightarrow * F T'$ $T' \rightarrow / F T'$ $T' \rightarrow$	$F \rightarrow \text{id}$ $F \rightarrow \text{num}$ $F \rightarrow (E)$
--	--	--

```

void E() { T(); E'(); }

void E'() {
    switch (tok) {
        case PLUS: eat(PLUS); T(); E'(); break;
        case MINUS: eat(MINUS); T(); E'(); break;
        default: /* empty - that's ok */ break;
    }
}
    
```

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Extended BNF (EBNF)

- A few additional operators to shorten definitions:
 - $e_1 \mid e_2 \mid e_3 \mid \dots$: choice of e_1, e_2, e_3 , etc
 - (\dots) bracketting allowed
 - $[\dots]$: the expression in $[\dots]$ may be omitted
 - (may also be written as $(\dots)?$).
 - $(e)^+$: One or more occurrences of e
 - $(e)^*$: Zero or more occurrences of e

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Extended BNF (EBNF)

- Note that these may be nested within each other, so we can have
 - $((e_1 \mid e_2)^* [e_3]) \mid e_4$
- examples:
 - IfStatement $\rightarrow \text{if } (\text{Expression}) \text{ StatementBlock } [\text{else StatementBlock}]$
 - StatementBlock $\rightarrow \{ (\text{Statement})^+ \}$

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Expression grammar in EBNF

$E \rightarrow E + T$	$T \rightarrow T * F$	$F \rightarrow \text{id}$	<i>Original</i>
$E \rightarrow E - T$	$T \rightarrow T / F$	$F \rightarrow \text{num}$	
$E \rightarrow T$	$T \rightarrow F$	$F \rightarrow (E)$	

$E \rightarrow T E'$	$T \rightarrow F T'$	$F \rightarrow \text{id}$	<i>Left-recursion eliminated</i>
$E' \rightarrow + T E'$	$T' \rightarrow * F T'$	$F \rightarrow \text{num}$	
$E' \rightarrow - T E'$	$T' \rightarrow / F T'$	$F \rightarrow (E)$	
$E' \rightarrow$	$T' \rightarrow$		

$E \rightarrow T (+ T - T)^*$	$T \rightarrow F (* T / T)^*$	$F \rightarrow \text{id}$	<i>EBNF</i>
		$F \rightarrow \text{num}$	
		$F \rightarrow (E)$	

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JavaCC:parser & lexical analysis

- Fortunately, we don't have to hand-code parsers...
- Given an (E)BNF grammar, software tools like JavaCC will produce a parser for us.
- Reminder – lexical analysis:
 - tokens defined by regular expressions are recognised by finite state automata (FSA) (see previous session)

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JavaCC:parser & lexical analysis

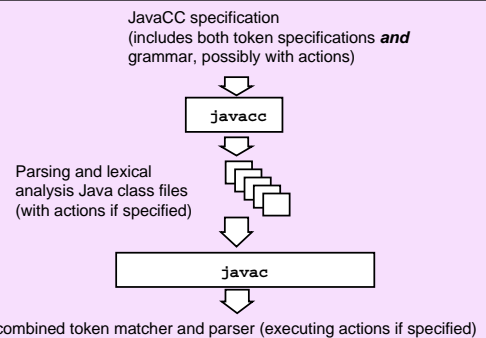
- Fortunately, we don't have to draw out a FSA and implement it to recognise tokens, because, given regular expressions, tools can produce a token matcher program for us
- In our case, given token definitions, our tool JavaCC will produce a lexical analysis method which simulates a FSA and matches tokens and sends them to the parser...

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JavaCC



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JavaCC

- JavaCC is a *parser generator*. Given as input a set of token definitions, a programming language syntax grammar, and a set of actions written in Java, it produces a Java program which will perform lexical analysis to find tokens and then parse the tokens according to the grammar and execute the actions as appropriate.

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JavaCC

- it works on LL(1) grammars (no need to understand this definition), which are similar to those that recursive descent works for.
- it requires a non-ambiguous grammar with left-recursion removed, so we use the techniques from earlier this session.

For the record:

Left-to-right parse, *leftmost* derivation, 1 symbol lookahead

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JavaCC BNF example

$E \rightarrow TE'$	$T \rightarrow FT'$	$F \rightarrow \text{num}$
		$F \rightarrow (E)$
$E' \rightarrow +TE'$	$T' \rightarrow *FT'$	
$E' \rightarrow -TE'$	$T' \rightarrow / FT'$	
$E' \rightarrow$	$T' \rightarrow$	

```

void E() :
{
    T() Eprime()
}

void Eprime() :
{
    { "==" T() Eprime() }
    { "!=" T() Eprime() }
    {} /* empty */
}

void T() :
{
    F() Tprime()
}

void Tprime() :
{
    { "" F() Tprime() }
    { "" F() Tprime() }
    {} /* empty */
}

void F() :
{
    <NUM>
    | "(" E() ")"
}

TOKEN :
{
    < NUM: ([ "0"-"9" ]) >
}

```

JavaCC EBNF example

$E \rightarrow T (+ T - T)^*$	<code>void E() :</code>	<code>void F() :</code>
	<code>{</code>	<code>{</code>
$T \rightarrow F (* T / T)^*$	<code>{</code>	<code>{</code>
	<code>T() ("+" T() "-" T()) *</code>	<code><NUM></code>
	<code>}</code>	<code> "(" E() "</code>
$F \rightarrow \text{num}$		<code>}</code>
$F \rightarrow (E)$	<code>void T() :</code>	
	<code>{</code>	
	<code>{</code>	
	<code>F() ("*" F() "/" F()) *</code>	
	<code>}</code>	

```
TOKEN :
{
  < NUM: ([ "0" - "9" ])+ >
}
```

JavaCC input file format (.jj)

```
PARSER_BEGIN(Parser-name)

class Parser-name { }

PARSER_END(Parser-name)

/* Lexical items (ie token definitions) – see previous examples */

Token-definitions

/* Grammar rules – in a stylised form of EBNF (see next slide). */

Syntax-definitions
```

Parser-name must be the same in all three places

JavaCC Syntax-definitions

A BNF production: non-terminal-name \rightarrow right-hand-side is written:

```

java_return_type non-terminal-name ( java_parameter_list ) : (1)
java_block                                             (2)
{ expansion_choices }                                (3)

```

- gives the name of the non-terminal being defined

The rest of (1) looks like a Java method declaration. Using this feature we can cause values to be passed up and down the parse tree while the parse takes place (up via return values and down via parameters).

(2) (java_block) introduces some Java code which is usually used to declare variables for use in the production

(3) is the EBNF definition and actions...see next slide

JavaCC EBNF expansion choices

expansion | expansion | ... where the `|` separates alternatives.

expansion expansion ...	matches first expansion then second and so on
(expansion_choices)*	matches zero or more expansion_choices
(expansion_choices)+	matches one or more expansion_choices
(expansion_choices)?	matches expansion_choices or empty string
[expansion_choices]	ditto (ie same as ?)
regex	matches the token matched by the regex
java_id = regex	ditto, assigning token to java_id
non-terminal-name (...)	matches the non-terminal
java_id = non-terminal-name (...)	ditto, assigning returned value to java_id

The `java id` will usually be declared in the `java` block.

Any of these expansions may be followed by some Java code written in {...} and this code (often called an action) will be **executed** when the generated parser matches the expansion.

JavaCC example: Exp.jj file

```

PARSER_BEGIN(Exp)

public class Exp {
}

PARSER_END(Exp)

SKIP :
{
    " " | "\t" | "\r"
}

TOKEN :
{
    < NUM: ["0"- "9"]> | < EOL: "\n" >
}

void S() :
{
    E() <EOL>
    | <EOL>
    | <EOF>
}

```

JavaCC example: Main.java file

```
public class Main {
    public static void main(String args[]) throws ParseException {
        Exp parser = new Exp(System.in);
        try {
            System.out.println("Type in an expression on a single line.");
            parser.S();
            System.out.println("Expression parser - parse successful");
        } catch (ParseException e) {
            System.out.println("Expression parser - error in parse");
        }
    }
}
```

What you should do now...

- Read, digest and understand chapter 3
 - don't worry about parsing tables & table generation
- Understand the JavaCC document and how to write token regular expressions and EBNF definitions in JavaCC
- Now take a first look at the MiniJava language.
 - we'll be using this through the rest of the module

Next Lecture

- This session continued and...
- ***Parsing II (abstract analysis)***
- Monday 11th February, 2008
 - 11:00 - 12:50
 - C.348