

/ / almost perfect tree = nearly complete tree

1.) a-) $\log n, \log n^{100} \rightarrow \Theta(\log n)$

b-) $n, 2^n \rightarrow \Omega(n), O(2^n)$

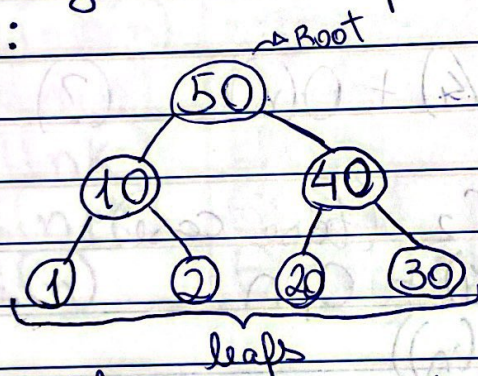
c-) $n^4 - n^3, 2022n^3 + \log n \rightarrow \Omega(n), O(n^3)$

2.)

14	8	12	2	5	1	10
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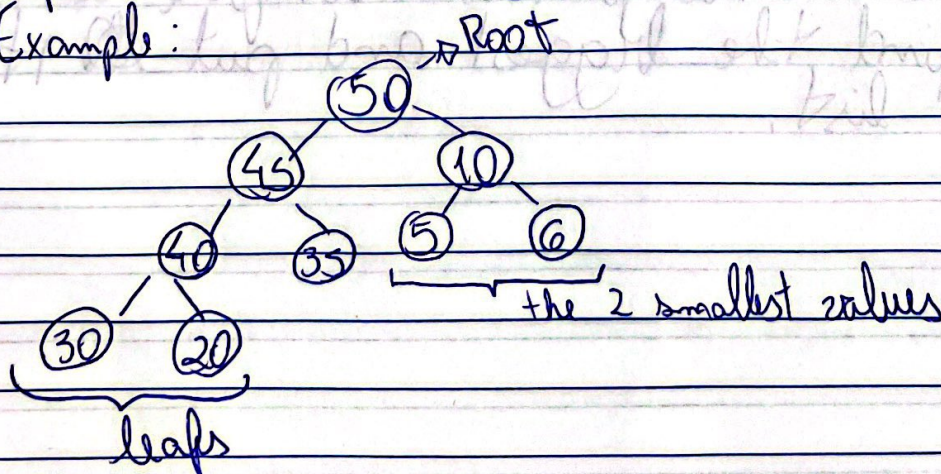
3.) a-) False; in an almost perfect tree, all the smallest values are not always at the leaves.

For Example:



In this case we have 20 and 30 being leaves, but they are still bigger than 10 that's not a leaf, so this proves that not always the smallest elements will be in the leaves. Actually, in an almost perfect tree, it's possible that the k th smallest element is not even in the leaves.

For Example:



order of values

b-) The only ~~value order~~ we get with heaps is between "parents" and "kids". This means that for a Minimum heap the "parent" is always smaller than his kids ~~and the kids of his kids~~ (also for the kids of his kids) and the root will be the smallest value.

4.) a.)

b-) def check_numbers(A, m):

 counter = 0

 for e in A:

 if $e = m$ or $e = 4m$:

 counter += 1

~~return counter~~

 if counter ≥ 2 :

 return True

Bonus Question:

d-) This is a MergeSort algorithm. It works by dividing the array in two minimal list (each one with one element) in a recursive way, then after that it return ~~and~~ a ~~sorted~~ array from two minimal array, until it's all full, by using Selection Sort.