

Trabalho 3 - Cálculo II

$$y^2 = 2x \rightarrow y = \sqrt{2x}$$

$$x^2 = 2y \rightarrow y = \frac{x^2}{2}$$

limites da integral: $\left(\frac{x^2}{2}\right)^2 = 2x$

$$\frac{x^4}{4} = 2x \rightarrow x^4 - 8x = 0$$

$$x(x^3 - 8) = 0$$

$\sqrt{2x} \geq \frac{x^2}{2}$ no intervalo de 0 a 2.

$x=0, x=2$

$$A = \int_a^b f(x) dx - \int_a^b g(x) dx$$

$$A = \int_0^2 \sqrt{2x} dx - \int_0^2 \frac{x^2}{2} dx = \int_0^2 (2x)^{\frac{1}{2}} dx - \int_0^2 \frac{x^2}{2} dx$$

$$\sqrt{2} \int_0^2 x^{\frac{1}{2}} dx - \frac{1}{2} \int_0^2 x^2 dx = \left[\sqrt{2} \frac{x^{\frac{3}{2}}}{\frac{3}{2}} \right]_0^2 - \left[\frac{x^3}{6} \right]_0^2$$

$$= \frac{2\sqrt{2}}{3} x^{\frac{3}{2}} \Big|_0^2 - \frac{x^3}{6} \Big|_0^2 = \left(\frac{2\sqrt{2} \cdot 2^{\frac{3}{2}}}{3} - \frac{2\sqrt{2} \cdot 0^{\frac{3}{2}}}{3} \right) - \left(\frac{2^3}{6} - \frac{0^3}{6} \right)$$

$$= \left(\frac{2\sqrt{2}}{3} \sqrt{2^3} - 0 \right) - \left(\frac{8}{6} - 0 \right) = \frac{2\sqrt{2^4}}{3} - \frac{8}{6}$$

$$= \frac{2 \cdot 4}{3} - \frac{8}{6} = \frac{8}{3} - \frac{8}{6} = \frac{48-24}{18} = \frac{24}{18} = \frac{4}{3} \text{ u.a.}$$