## TABELA 12,2

Carga	Função da carga w = w(x)	Cisalhamento $V = -\int w(x) dx$	Momento $M = \int V dx$
$ \begin{array}{c c}  & \mathbf{M}_0 \\  & -x \\  & -a \\  & -a \end{array} $	$w = M_0 < x - a >^{-2}$	$V = -M_0 < x - a >^{-1}$	$M = -M_0 < x - a > 0$
	$w = P < x - a >^{-1}$	V = -P < x - a > 0	M = -P < x - a > 1
$(3) \qquad w_0$ $-x \rightarrow a \rightarrow a$	$w = w_0 < x - a > 0$	$V = -w_0 < x - a > 1$	$M = -\frac{w_0}{2} < x - a > 2$
(4) Inclinação = $m$ $ -x $ $ -a $	w = m < x - a > 1	$V = \frac{-m}{2} \langle x - a \rangle^2$	$M = \frac{-m}{6} < x - a > 3$

Inclinações e deslocamen	tos de vigas simple	esmente apoiadas	
Viga	Inclinação	Deflexão	Curva da linha elástica
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	$\theta_{\text{max}} = \frac{-PL^2}{16EI}$	$v_{\text{máx}} = \frac{-PL^3}{48EI}$	$v = \frac{-Px}{48EI}(3L^2 - 4x^2)$ $0 \le x \le L/2$
$\theta_1$ $\theta_2$ $A$	$\theta_1 = \frac{-Pab(L+b)}{6EIL}$ $\theta_2 = \frac{Pab(L+a)}{6EIL}$	$v\Big _{x=a} = \frac{-Pba}{6EIL}(L^2 - b^2 - a^2)$	$v = \frac{-Pbx}{6EIL}(L^2 - b^2 - x^2)$ $0 \le x \le a$
$M_0$ $\theta_1$ $\theta_2$	$\theta_1 = \frac{-M_0 L}{3EI}$ $\theta_2 = \frac{M_0 L}{6EI}$	$v_{\text{máx}} = \frac{-M_0 L^2}{\sqrt{243}EI}$	$v = \frac{-M_0 x}{6EIL} (x^2 - 3Lx + 2L^2)$
U L W W X	$\theta_{\text{máx}} = \frac{-wL^3}{24EI}$	$v_{\text{max}} = \frac{-5wL^4}{384EI}$	$v = \frac{-wx}{24EI}(x^3 - 2Lx^2 + L^3)$
$ \begin{array}{c c} v \\ \downarrow & \downarrow & \downarrow & \downarrow \\ \hline L & \theta_1 & \downarrow & L \\ \hline 2 & & & \\ \hline \end{array} $	$\theta_1 = \frac{-3wL^3}{128EI}$ $\theta_2 = \frac{7wL^3}{384EI}$	$v \bigg _{x=L/2} = \frac{-5wL^4}{768EI}$ $v_{\text{máx}} = -0,006563 \frac{wL^4}{EI}$ $\text{em } x = 0,4598L$	$v = \frac{-wx}{384EI} (16x^3 - 24Lx^2 + 9L^3)$ $0 \le x \le L/2$ $v = \frac{-wL}{384EI} (8x^3 - 24Lx^2 + 17L^2x - L^3)$ $L/2 \le x < L$
$\theta_1$ $\theta_2$ $x$	$\theta_1 = \frac{-7w_0 L^3}{360EI}$ $\theta_2 = \frac{w_0 L^3}{45EI}$	$v_{\text{máx}} = -0,00652 \frac{w_0 L^4}{EI}$ em $x = 0,5193L$	$v = \frac{-w_0 x}{360EIL} (3x^4 - 10L^2 x^2 + 7L^4)$

Inclinações e deflexões de vigas em balanço			
Viga	Inclinação	Deflexão	Curva da linha elástica
P v <sub>máx</sub> x  d máx	$\theta_{\text{máx}} = \frac{-PL^2}{2EI}$	$v_{\text{máx}} = \frac{-PL^3}{3EI}$	$v = \frac{-Px^2}{6EI}(3L - x)$
$\begin{array}{c c} v & P & v_{\text{máx}} \\ \hline & L & L \\ \hline & L & \theta_{\text{máx}} \end{array}$	$\theta_{\text{máx}} = \frac{-PL^2}{8EI}$	$v_{\text{máx}} = \frac{-5PL^3}{48EI}$	$v = \frac{-Px^2}{6EI} \left(\frac{3}{2}L - x\right) \qquad 0 \le x \le L/2$ $v = \frac{-PL^2}{24EI} \left(3x - \frac{1}{2}L\right)  L/2 \le x \le L$
v v <sub>máx</sub> x d d d d d d d d d d d d d d d d d d	$\theta_{\text{máx}} = \frac{-wL^3}{6EI}$	$v_{\text{máx}} = \frac{-wL^4}{8EI}$	$v = \frac{-wx^2}{24EI}(x^2 - 4Lx + 6L^2)$
$v$ $\theta_{max}$ $M_0$ $v_{max}$	$\theta_{\text{máx}} = \frac{M_0 L}{EI}$	$v_{\text{máx}} = \frac{M_0 L^2}{2EI}$	$v = \frac{M_0 x^2}{2EI}$
v $v$ $v$ $v$ $v$ $v$ $v$ $v$ $v$ $v$	$\theta_{\text{máx}} = \frac{-wL^3}{48EI}$	$v_{\text{max}} = \frac{-7wL^4}{384EI}$	$v = \frac{-wx^{2}}{24EI} \left(x^{2} - 2Lx + \frac{3}{2}L^{2}\right)$ $0 \le x \le L/2$ $v = \frac{-wL^{3}}{192EI} (4x - L/2)$ $L/2 \le x \le L$
v $v$ $v$ $v$ $v$ $v$ $v$ $v$ $v$ $v$	$\theta_{\text{máx}} = \frac{-w_0 L^3}{24EI}$	$v_{\text{máx}} = \frac{-w_0 L^4}{30EI}$	$v = \frac{-w_0 x^2}{120EIL} (10L^3 - 10L^2 x + 5Lx^2 - x^3)$