

Understanding Precisely How Scan, Fold, and Reduce Work



Vitthal Srinivasan

CO-FOUNDER, LOONYCORN

www.loonycorn.com

Overview

Recognise the importance of higher order methods

Apply higher order methods that operate on one element at a time

Understand higher order methods that operate on multiple elements

Higher Order Methods



Higher Order Methods

Apply function objects to
contents of collection



For-loops

Iterate over collection, freely
access contents

Higher Order Methods



Map, Foreach, Filter

Act on one element at a time



Scan, Fold, Reduce

Act on multiple elements at a
time

For-each Style Higher Order Methods

Demo

Higher order methods

- foreach
- map
- filter
- partition
- sortBy

Scan-style Higher Order Methods

Scan, Fold and Reduce

Scan Right

Fold Right

Reduce Right

Scan Left

Fold Left

Reduce Left

Scan, Fold and Reduce

Scan Right

Fold Right

Reduce Right

Scan Left

Fold Left

Reduce Left

Demo

Scan Right

```
val someNumbers = List(10, 20, 30, 40, 50, 60)
someNumbers.scanRight(0)(_ - _)

List[Int] = List(-30, 40, -20, 50, -10, 60, 0) // Result
```

ScanRight

A right-associative higher-order method that takes in an initial value and applies it pairwise, returning a list

```
val someNumbers = List(10,20,30,40,50,60)
```

```
someNumbers.scanRight(0)(_ - _)
```

```
List[Int] = List(-30, 40, -20, 50, -10, 60, 0) // Result
```

ScanRight

List

10

20

30

40

50

60

0

Initial Value

Function

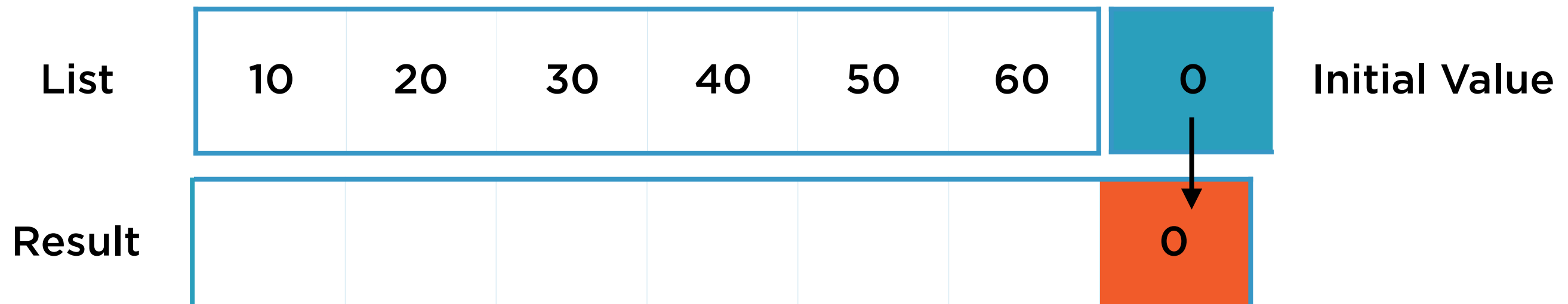
_ - _

```
val someNumbers = List(10, 20, 30, 40, 50, 60)
```

```
someNumbers.scanRight(0)(_ - _)
```

```
List[Int] = List(-30, 40, -20, 50, -10, 60, 0) // Result
```

ScanRight



```
val someNumbers = List(10, 20, 30, 40, 50, 60)
```

```
someNumbers.scanRight(0)(_ - _)
```

```
List[Int] = List(-30, 40, -20, 50, -10, 60, 0) // Result
```

ScanRight

List

10

20

30

40

50

60

0

Initial Value

Result

--	--	--	--	--	--	--

```
val someNumbers = List(10, 20, 30, 40, 50, 60)
```

```
someNumbers.scanRight(0)(_ - _)
```

```
List[Int] = List(-30, 40, -20, 50, -10, 60, 0) // Result
```

ScanRight

List

10	20	30	40	50	60	0
----	----	----	----	----	----	---

Initial Value

Result

						0
--	--	--	--	--	--	---

```
val someNumbers = List(10,20,30,40,50,60)
```

```
someNumbers.scanRight(0)(_ - _)
```

```
List[Int] = List(-30, 40, -20, 50, -10, 60, 0) // Result
```

ScanRight

List	10	20	30	40	50	60	0	Initial Value
Result							0	


```
val someNumbers = List(10,20,30,40,50,60)
```

```
someNumbers.scanRight(0)(_ - _)
```

```
List[Int] = List(-30, 40, -20, 50, -10, 60, 0) // Result
```

ScanRight

List	10	20	30	40	50	60	0	Initial Value
Result						60	0	

```
val someNumbers = List(10,20,30,40,50,60)
```

```
someNumbers.scanRight(0)(_ - _)
```

```
List[Int] = List(-30, 40, -20, 50, -10, 60, 0) // Result
```

ScanRight

List

10	20	30	40	50	60	0
----	----	----	----	----	----	---

Initial Value

Result

					60	0
--	--	--	--	--	----	---

```
val someNumbers = List(10,20,30,40,50,60)
```

```
someNumbers.scanRight(0)(_ - _)
```

```
List[Int] = List(-30, 40, -20, 50, -10, 60, 0) // Result
```

ScanRight

List	10	20	30	40	50	60	0	Initial Value
Result						60	0	

```
val someNumbers = List(10, 20, 30, 40, 50, 60)
```

```
someNumbers.scanRight(0)(_ - _)
```

```
List[Int] = List(-30, 40, -20, 50, -10, 60, 0) // Result
```

ScanRight

List	10	20	30	40	50	60	0	Initial Value
Result					-10	60	0	

```
val someNumbers = List(10, 20, 30, 40, 50, 60)
```

```
someNumbers.scanRight(0)(_ - _)
```

```
List[Int] = List(-30, 40, -20, 50, -10, 60, 0) // Result
```

ScanRight

List

10	20	30	40	50	60	0
----	----	----	----	----	----	---

Initial Value

Result

				-10	60	0
--	--	--	--	-----	----	---

```
val someNumbers = List(10, 20, 30, 40, 50, 60)
```

```
someNumbers.scanRight(0)(_ - _)
```

```
List[Int] = List(-30, 40, -20, 50, -10, 60, 0) // Result
```

ScanRight

List

10	20	30	40	50	60	0
----	----	----	----	----	----	---

Initial Value

Result

				-10	60	0
--	--	--	--	-----	----	---

```
val someNumbers = List(10,20,30,40,50,60)
```

```
someNumbers.scanRight(0)(_ - _)
```

```
List[Int] = List(-30, 40, -20, 50, -10, 60, 0) // Result
```

ScanRight

List	10	20	30	40	50	60	0	Initial Value
Result				50	-10	60	0	

```
val someNumbers = List(10, 20, 30, 40, 50, 60)
```

```
someNumbers.scanRight(0)(_ - _)
```

```
List[Int] = List(-30, 40, -20, 50, -10, 60, 0) // Result
```

ScanRight

List

10	20	30	40	50	60	0
----	----	----	----	----	----	---

Initial Value

Result

			50	-10	60	0
--	--	--	----	-----	----	---


```
val someNumbers = List(10, 20, 30, 40, 50, 60)
```

```
someNumbers.scanRight(0)(_ - _)
```

```
List[Int] = List(-30, 40, -20, 50, -10, 60, 0) // Result
```

ScanRight

List

10	20	30	40	50	60	0
----	----	----	----	----	----	---

Initial Value

Result

			50	-10	60	0
--	--	--	----	-----	----	---

```
val someNumbers = List(10, 20, 30, 40, 50, 60)
```

```
someNumbers.scanRight(0)(_ - _)
```

```
List[Int] = List(-30, 40, -20, 50, -10, 60, 0) // Result
```

ScanRight

List	10	20	30	40	50	60	0	Initial Value
Result			-20	50	-10	60	0	

```
val someNumbers = List(10, 20, 30, 40, 50, 60)
```

```
someNumbers.scanRight(0)(_ - _)
```

```
List[Int] = List(-30, 40, -20, 50, -10, 60, 0) // Result
```

ScanRight

List

10

20

30

40

50

60

0

Initial Value

Result

-20

50

-10

60

0

```
val someNumbers = List(10, 20, 30, 40, 50, 60)
```

```
someNumbers.scanRight(0)(_ - _)
```

```
List[Int] = List(-30, 40, -20, 50, -10, 60, 0) // Result
```

ScanRight

List	10	20	30	40	50	60	0	Initial Value
Result			-20	50	-10	60	0	

```
val someNumbers = List(10, 20, 30, 40, 50, 60)
```

```
someNumbers.scanRight(0)(_ - _)
```

```
List[Int] = List(-30, 40, -20, 50, -10, 60, 0) // Result
```

ScanRight

List	10	20	30	40	50	60	0	Initial Value
Result		40	-20	50	-10	60	0	

```
val someNumbers = List(10, 20, 30, 40, 50, 60)
```

```
someNumbers.scanRight(0)(_ - _)
```

```
List[Int] = List(-30, 40, -20, 50, -10, 60, 0) // Result
```

ScanRight

List

10	20	30	40	50	60	0
----	----	----	----	----	----	---

Initial Value

Result

	40	-20	50	-10	60	0
--	----	-----	----	-----	----	---

```
val someNumbers = List(10, 20, 30, 40, 50, 60)
```

```
someNumbers.scanRight(0)(_ - _)
```

```
List[Int] = List(-30, 40, -20, 50, -10, 60, 0) // Result
```

ScanRight

List	10	20	30	40	50	60	0	Initial Value
Result		40	-20	50	-10	60	0	

```
val someNumbers = List(10, 20, 30, 40, 50, 60)
```

```
someNumbers.scanRight(0)(_ - _)
```

```
List[Int] = List(-30, 40, -20, 50, -10, 60, 0) // Result
```

ScanRight

List	10	20	30	40	50	60	0	Initial Value
Result	-30	40	-20	50	-10	60	0	


```
val someNumbers = List(10, 20, 30, 40, 50, 60)
```

```
someNumbers.scanRight(0)(_ - _)
```

```
List[Int] = List(-30, 40, -20, 50, -10, 60, 0) // Result
```

ScanRight

List

10

20

30

40

50

60

0

Initial Value

Result

-30

40

-20

50

-10

60

0

Scan, Fold and Reduce

Scan Right

Fold Right

Reduce Right

Scan Left

Fold Left

Reduce Left

Demo

Scan Left

```
val someNumbers = List(10, 20, 30, 40, 50, 60)
someNumbers.scanLeft(0)(_ - _)
List[Int] = List(0, -10, -30, -60, -100, -150, -210) // Result
```

ScanLeft

A left-associative higher-order method that takes in an initial value and applies it pairwise, returning a list

```
val someNumbers = List(10, 20, 30, 40, 50, 60)
```

```
someNumbers.scanLeft(0)(_ - _)
```

```
List[Int] = List(0, -10, -30, -60, -100, -150, -210) // Result
```

ScanLeft

Initial Value

0

10

20

30

40

50

60

List

Function

_ - _

```
val someNumbers = List(10, 20, 30, 40, 50, 60)
```

```
someNumbers.scanLeft(0)(_ - _)
```

```
List[Int] = List(0, -10, -30, -60, -100, -150, -210) // Result
```

ScanLeft

Initial Value

0

10

20

30

40

50

60

List

Result

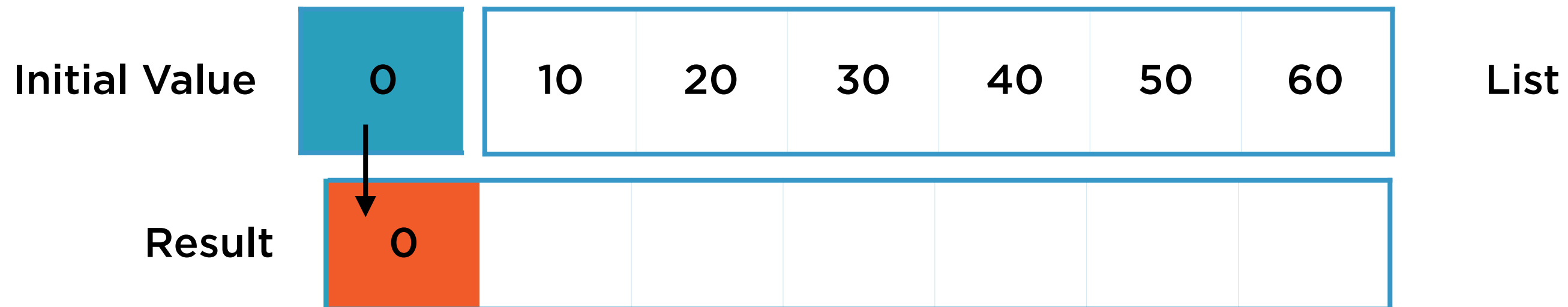
--	--	--	--	--	--	--

```
val someNumbers = List(10, 20, 30, 40, 50, 60)
```

```
someNumbers.scanLeft(0)(_ - _)
```

```
List[Int] = List(0, -10, -30, -60, -100, -150, -210) // Result
```

ScanLeft



```
val someNumbers = List(10, 20, 30, 40, 50, 60)
```

```
someNumbers.scanLeft(0)(_ - _)
```

```
List[Int] = List(0, -10, -30, -60, -100, -150, -210) // Result
```

ScanLeft

Initial Value

0

10

20

30

40

50

60

List

Result

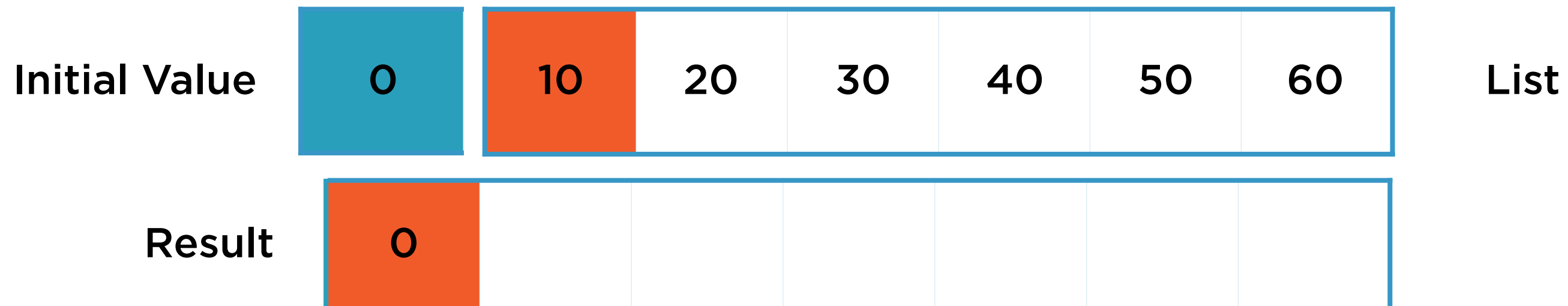
0


```
val someNumbers = List(10, 20, 30, 40, 50, 60)
```

```
someNumbers.scanLeft(0)(_ - _)
```

```
List[Int] = List(0, -10, -30, -60, -100, -150, -210) // Result
```

ScanLeft

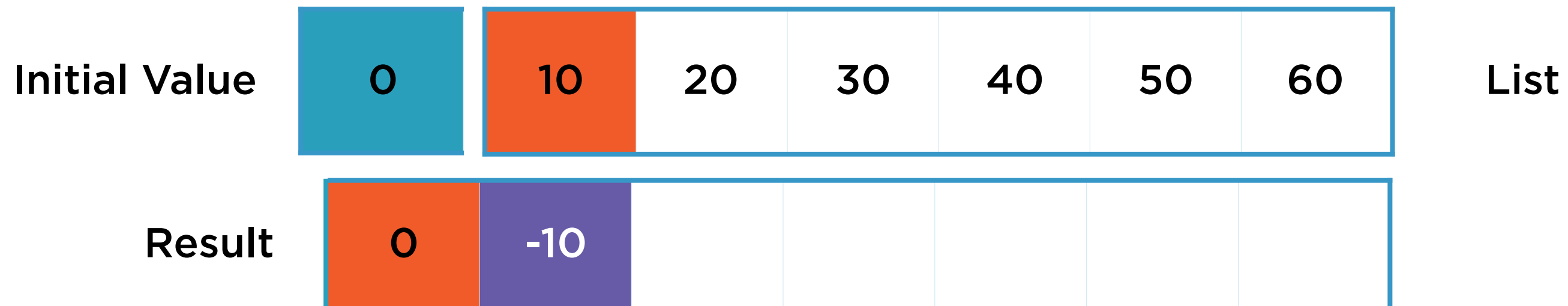


```
val someNumbers = List(10, 20, 30, 40, 50, 60)
```

```
someNumbers.scanLeft(0)(_ - _)
```

```
List[Int] = List(0, -10, -30, -60, -100, -150, -210) // Result
```

ScanLeft



```
val someNumbers = List(10, 20, 30, 40, 50, 60)
```

```
someNumbers.scanLeft(0)(_ - _)
```

```
List[Int] = List(0, -10, -30, -60, -100, -150, -210) // Result
```

ScanLeft

Initial Value

0

10

20

30

40

50

60

List

Result

0

-10

```
val someNumbers = List(10, 20, 30, 40, 50, 60)
```

```
someNumbers.scanLeft(0)(_ - _)
```

```
List[Int] = List(0, -10, -30, -60, -100, -150, -210) // Result
```

ScanLeft

Initial Value

0	10	20	30	40	50	60
---	----	----	----	----	----	----

List

Result

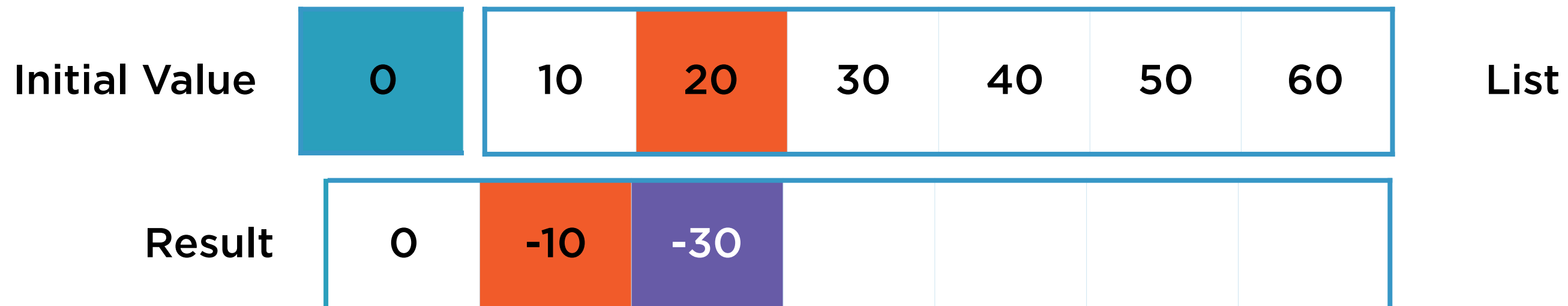
0	-10					
---	-----	--	--	--	--	--

```
val someNumbers = List(10, 20, 30, 40, 50, 60)
```

```
someNumbers.scanLeft(0)(_ - _)
```

```
List[Int] = List(0, -10, -30, -60, -100, -150, -210) // Result
```

ScanLeft



```
val someNumbers = List(10, 20, 30, 40, 50, 60)
```

```
someNumbers.scanLeft(0)(_ - _)
```

```
List[Int] = List(0, -10, -30, -60, -100, -150, -210) // Result
```

ScanLeft

Initial Value

0

10

20

30

40

50

60

List

Result

0

-10

-30

```
val someNumbers = List(10, 20, 30, 40, 50, 60)
```

```
someNumbers.scanLeft(0)(_ - _)
```

```
List[Int] = List(0, -10, -30, -60, -100, -150, -210) // Result
```

ScanLeft

Initial Value

0

10

20

30

40

50

60

List

Result

0

-10

-30

```
val someNumbers = List(10, 20, 30, 40, 50, 60)
```

```
someNumbers.scanLeft(0)(_ - _)
```

```
List[Int] = List(0, -10, -30, -60, -100, -150, -210) // Result
```

ScanLeft




```
val someNumbers = List(10, 20, 30, 40, 50, 60)
```

```
someNumbers.scanLeft(0)(_ - _)
```

```
List[Int] = List(0, -10, -30, -60, -100, -150, -210) // Result
```

ScanLeft

Initial Value

0

10

20

30

40

50

60

List

Result

0

-10

-30

-60

```
val someNumbers = List(10, 20, 30, 40, 50, 60)
```

```
someNumbers.scanLeft(0)(_ - _)
```

```
List[Int] = List(0, -10, -30, -60, -100, -150, -210) // Result
```

ScanLeft

Initial Value

0

10

20

30

40

50

60

List

Result

0

-10

-30

-60

```
val someNumbers = List(10, 20, 30, 40, 50, 60)
```

```
someNumbers.scanLeft(0)(_ - _)
```

```
List[Int] = List(0, -10, -30, -60, -100, -150, -210) // Result
```

ScanLeft

Initial Value

0

10

20

30

40

50

60

List

Result

0

-10

-30

-60

-100

```
val someNumbers = List(10, 20, 30, 40, 50, 60)
```

```
someNumbers.scanLeft(0)(_ - _)
```

```
List[Int] = List(0, -10, -30, -60, -100, -150, -210) // Result
```

ScanLeft

Initial Value

0

10

20

30

40

50

60

List

Result

0

-10

-30

-60

-100

```
val someNumbers = List(10, 20, 30, 40, 50, 60)
```

```
someNumbers.scanLeft(0)(_ - _)
```

```
List[Int] = List(0, -10, -30, -60, -100, -150, -210) // Result
```

ScanLeft

Initial Value

0

10

20

30

40

50

60

List

Result

0

-10

-30

-60

-100

```
val someNumbers = List(10, 20, 30, 40, 50, 60)
```

```
someNumbers.scanLeft(0)(_ - _)
```

```
List[Int] = List(0, -10, -30, -60, -100, -150, -210) // Result
```

ScanLeft

Initial Value

0

10

20

30

40

50

60

List

Result

0

-10

-30

-60

-100

-150

```
val someNumbers = List(10, 20, 30, 40, 50, 60)
```

```
someNumbers.scanLeft(0)(_ - _)
```

```
List[Int] = List(0, -10, -30, -60, -100, -150, -210) // Result
```

ScanLeft

Initial Value

0

10

20

30

40

50

60

List

Result

0

-10

-30

-60

-100

-150

```
val someNumbers = List(10, 20, 30, 40, 50, 60)
```

```
someNumbers.scanLeft(0)(_ - _)
```

```
List[Int] = List(0, -10, -30, -60, -100, -150, -210) // Result
```

ScanLeft

Initial Value

0

10

20

30

40

50

60

List

Result

0

-10

-30

-60

-100

-150


```
val someNumbers = List(10, 20, 30, 40, 50, 60)
```

```
someNumbers.scanLeft(0)(_ - _)
```

```
List[Int] = List(0, -10, -30, -60, -100, -150, -210) // Result
```

ScanLeft

Initial Value

0

10

20

30

40

50

60

List

Result

0

-10

-30

-60

-100

-150

-210

```
val someNumbers = List(10, 20, 30, 40, 50, 60)
```

```
someNumbers.scanLeft(0)(_ - _)
```

```
List[Int] = List(0, -10, -30, -60, -100, -150, -210) // Result
```

ScanLeft

Initial Value

0

10

20

30

40

50

60

List

Result

0

-10

-30

-60

-100

-150

-210

Scan, Fold and Reduce

Scan Right

Fold Right

Reduce Right

Scan Left

Fold Left

Reduce Left

Scan and Fold



Scan Left, Scan Right

Return the entire result list from the scan operation



Fold Left, Fold Right

Return only the 'last' element of the result list

Demo

Fold Left and Fold Right

```
val someNumbers = List(10, 20, 30, 40, 50, 60)
```

```
someNumbers.scanLeft(0)(_ - _)
```

```
List[Int] = List(0, -10, -30, -60, -100, -150, -210) // Result
```

ScanLeft

Initial Value

0

10

20

30

40

50

60

List

Result

0

-10

-30

-60

-100

-150

-210

```
val someNumbers = List(10, 20, 30, 40, 50, 60)
```

```
someNumbers.scanLeft(0)(_ - _)
```

```
List[Int] = List(0, -10, -30, -60, -100, -150, -210) // Result
```

ScanLeft

Initial Value

0

10

20

30

40

50

60

List

Result

0

-10

-30

-60

-100

-150

-210

```
val someNumbers = List(10, 20, 30, 40, 50, 60)
someNumbers.foldLeft(0)(_ - _)
```

Int = -210 // Result

FoldLeft

Initial Value

0

10

20

30

40

50

60

List

Result

0

-10

-30

-60

-100

-150

-210


```
val someNumbers = List(10, 20, 30, 40, 50, 60)
```

```
someNumbers.scanRight(0)(_ - _)
```

```
List[Int] = List(-30, 40, -20, 50, -10, 60, 0) // Result
```

ScanRight

List

10

20

30

40

50

60

0

Initial Value

Result

-30

40

-20

50

-10

60

0

```
val someNumbers = List(10, 20, 30, 40, 50, 60)
```

```
someNumbers.scanRight(0)(_ - _)
```

```
List[Int] = List(-30, 40, -20, 50, -10, 60, 0) // Result
```

ScanRight

List	10	20	30	40	50	60	0	Initial Value
Result	-30	40	-20	50	-10	60	0	

```
val someNumbers = List(10, 20, 30, 40, 50, 60)
someNumbers.foldRight(0)(_ - _)

Int = -30    // Result
```

FoldRight

List	10	20	30	40	50	60	0	Initial Value
Result	-30	40	-20	50	-10	60	0	

Scan, Fold and Reduce

Scan Right

Fold Right

Reduce Right

Scan Left

Fold Left

Reduce Left

Scan and Reduce



Scan Left, Scan Right

Take in an initial value; use this initial value as second operand in first step



Reduce Left, Reduce Right

No initial value - first two list elements as operands in first step

Demo

Reduce Right

```
val someNumbers = List(10, 20, 30, 40, 50, 60)
someNumbers.reduceRight(_ - _)

Int = -30      // Result
```

ReduceRight

A right-associative higher-order method that does not take an initial value, instead using the first two list elements as operands

```
val someNumbers = List(10, 20, 30, 40, 50, 60)
someNumbers.reduceRight(_ - _)
Int = -30      // Result
```

ReduceRight

List

10	20	30	40	50	60
----	----	----	----	----	----

Function

_ - _


```
val someNumbers = List(10, 20, 30, 40, 50, 60)
someNumbers.reduceRight(_ - _)

Int = -30      // Result
```

ReduceRight

List	10	20	30	40	50	60
Result						

```
val someNumbers = List(10, 20, 30, 40, 50, 60)
someNumbers.reduceRight(_ - _)
Int = -30      // Result
```

ReduceRight

List	10	20	30	40	50	60
Result					-10	

```
val someNumbers = List(10, 20, 30, 40, 50, 60)
someNumbers.reduceRight(_ - _)

Int = -30      // Result
```

ReduceRight

List	10	20	30	40	50	60
Result					-10	

```
val someNumbers = List(10, 20, 30, 40, 50, 60)
someNumbers.reduceRight(_ - _)

Int = -30      // Result
```

ReduceRight

List	10	20	30	40	50	60
Result					-10	

```
val someNumbers = List(10, 20, 30, 40, 50, 60)
someNumbers.reduceRight(_ - _)
Int = -30      // Result
```

ReduceRight

List	10	20	30	40	50	60
Result				50	-10	

```
val someNumbers = List(10, 20, 30, 40, 50, 60)
someNumbers.reduceRight(_ - _)
Int = -30      // Result
```

ReduceRight

List	10	20	30	40	50	60
Result				50	-10	

```
val someNumbers = List(10, 20, 30, 40, 50, 60)
someNumbers.reduceRight(_ - _)
Int = -30      // Result
```

ReduceRight

List	10	20	30	40	50	60
Result				50	-10	

```
val someNumbers = List(10, 20, 30, 40, 50, 60)
someNumbers.reduceRight(_ - _)
Int = -30      // Result
```

ReduceRight

List	10	20	30	40	50	60
Result			-20	50	-10	


```
val someNumbers = List(10, 20, 30, 40, 50, 60)
someNumbers.reduceRight(_ - _)

Int = -30      // Result
```

ReduceRight

List	10	20	30	40	50	60
Result			-20	50	-10	

```
val someNumbers = List(10, 20, 30, 40, 50, 60)
someNumbers.reduceRight(_ - _)

Int = -30      // Result
```

ReduceRight

List	10	20	30	40	50	60
Result			-20	50	-10	

```
val someNumbers = List(10, 20, 30, 40, 50, 60)
someNumbers.reduceRight(_ - _)
Int = -30      // Result
```

ReduceRight

List	10	20	30	40	50	60
Result		40	-20	50	-10	

```
val someNumbers = List(10, 20, 30, 40, 50, 60)
someNumbers.reduceRight(_ - _)

Int = -30      // Result
```

ReduceRight

List	10	20	30	40	50	60
Result		40	-20	50	-10	

```
val someNumbers = List(10, 20, 30, 40, 50, 60)
someNumbers.reduceRight(_ - _)

Int = -30      // Result
```

ReduceRight

List	10	20	30	40	50	60
Result		40	-20	50	-10	

```
val someNumbers = List(10, 20, 30, 40, 50, 60)
someNumbers.reduceRight(_ - _)

Int = -30      // Result
```

ReduceRight

List	10	20	30	40	50	60
Result	-30	40	-20	50	-10	

```
val someNumbers = List(10, 20, 30, 40, 50, 60)
someNumbers.reduceRight(_ - _)
Int = -30      // Result
```

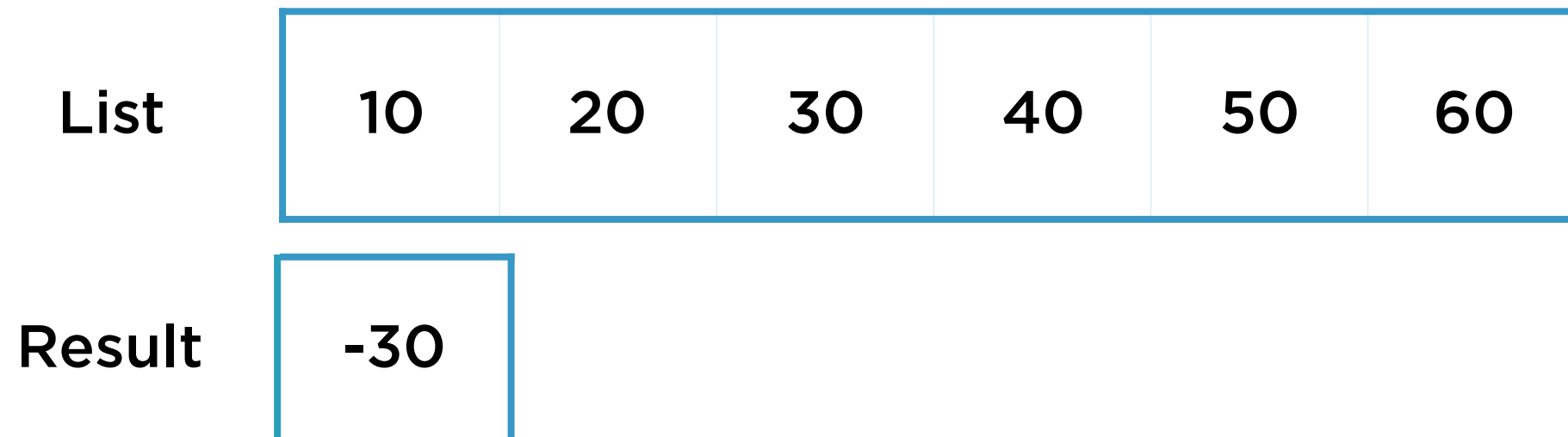
ReduceRight

List	10	20	30	40	50	60
Result	-30	40	-20	50	-10	

```
val someNumbers = List(10, 20, 30, 40, 50, 60)
someNumbers.reduceRight(_ - _)

Int = -30      // Result
```

ReduceRight



Scan, Fold and Reduce

Scan Right

Fold Right

Reduce Right

Scan Left

Fold Left

Reduce Left

Summary

Higher order methods of collections are a key functional construct

Map, for-each, filter apply function objects to one element of the collection at a time

Variants of scan, fold and reduce operate on multiple container elements at a time