Homework 3

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1 The following output was obtained from a computer program that performed a two-factor ANOVA on a factorial experiment.

Source	DF	SS	MS	F	Р
A	1	-	0.0002	-	_
В	-	180.378	-	-	-
Interaction	3	8.479	-	-	0.932
Error	8	158.797	-		
Total	15	347.653			

a) Fill in the blanks in the ANOVA table.

```
# calculating missing p-values # P(F > 0.00001), df1 from the A factor, df2 from the Error pf(q = 0.00001, df1 = 1, df2 = 8, lower.tail = F)
```

[1] 0.9975543

```
# P(F > 3.02917), df1 from the B factor, df2 from the Error pf(q = 3.02917, df1 = 3, df2 = 8, lower.tail = F)
```

[1] 0.09334106

Source	DF	SS	MS	\mathbf{F}	Р
A	1	0.0002	0.0002	0.00001	0.9975543
В	3	180.378	60.126	3.02917	0.09334106
Interaction	3	8.479	2.826	0.14237	0.932
Error	8	158.797	19.849		
Total	15	347.653			

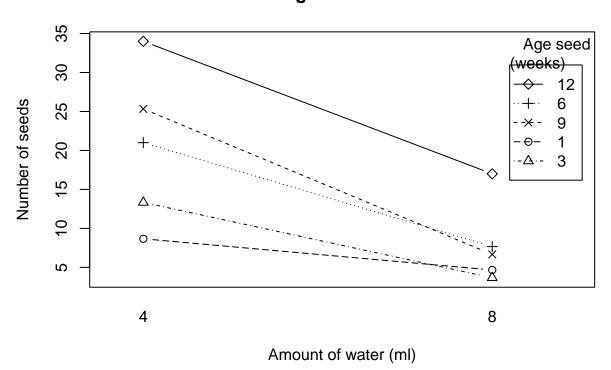
- b) How many levels were used for factor B? 4 levels because DF from B treatment is b-1=3, so b=4.
- c) How many replicates of the experiment were performed? Degrees of freedom from Error is ab(r-1)=8, then $2\times 4\times (r-1)=8$, then 8r=16, then r=2 replicates.

2 Brewer's malt is produced from germinating barley, so brewers like to know under what conditions they should germinate their barley. The following is part of an experiment on barley germination. Barley seeds were divided into 30 lots of 100 seeds, and each lot of 100 seeds was germinated under one of ten conditions chosen at random. The conditions are the ten combinations of weeks after harvest (1, 3, 6, 9, or 12 weeks) and the amount of water used in germination (4 ml or 8 ml). The response is the number of seeds germinating. We are interested in whether the timing and/or amount of water affect germination. Analyze these data to determine how the germination rate depends on the treatments.

	Age of Seeds (weeks)				
$ml H_2O$	1	3	6	9	12
4	11 9 6	7 16 17	9 19 35	13 35 28	20 37 45
8	8 3 3	$egin{array}{c} 1 \\ 7 \\ 3 \end{array}$	15 9 9	1 10 9	11 15 25

```
df \leftarrow expand.grid(h20 = c(4, 8), age_seeds = c(1, 3, 6, 9, 12))
df <- rbind(df, df, df) # 3 reps</pre>
df <- df[order(df$h20), ]</pre>
rownames(df) <- 1:nrow(df) # fix row numbers</pre>
df$h20 <- as.factor(df$h20)
df$age_seeds <- as.factor(df$age_seeds)</pre>
# assign response
df$seeds <- c(
  11, 7, 9, 13, 20,
  9, 16, 19, 35, 37,
  6, 17, 35, 28, 45,
  8, 1, 5, 1, 11,
  3, 7, 9, 10, 15,
  3, 3, 9, 9, 25
)
tibble::glimpse(df)
```

Interaction Plot of Age seeds and Amount of water



In all different harvesting weeks (1, 3, 6, 9, 12) we observe a decreasing of count of seeds when we increase the water amount of water (in ml) from 4 to 8, however, the count of seeds decreases a lot (from ~35 to ~20) when we change the amount of water from 4 to 8 ml and harvest after 12 weeks (losango symbol), whereas a smaller decrease is seen when we change the amount of water from 4 to 8 ml but harvest after only 1 week (circle symbol).

When looking only to the Amount of water, using 4 mls rather than 8 always produced a larger number of seeds, despite the harvesting weeks.

Let's check whether these factors and the interaction are significant.

```
fit <- aov(seeds ~ h20 * age_seeds, data = df)
summary(fit)</pre>
```

```
##
                 Df Sum Sq Mean Sq F value
                                             Pr(>F)
                                   19.723 0.000251 ***
## h20
                  1 1178.1
                           1178.1
                             330.3
                  4 1321.1
                                     5.529 0.003645 **
## age_seeds
                                     0.874 0.496726
## h20:age_seeds
                  4
                     208.9
                              52.2
## Residuals
                 20 1194.7
                              59.7
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
```

Using a significance level of $\alpha = 0.05$, we see that both the amount of water and harvesting weeks affect germination (i.e. are significant), however, the interaction between both treatments is not significant to the germination because p-value = $0.4906 > \alpha$.

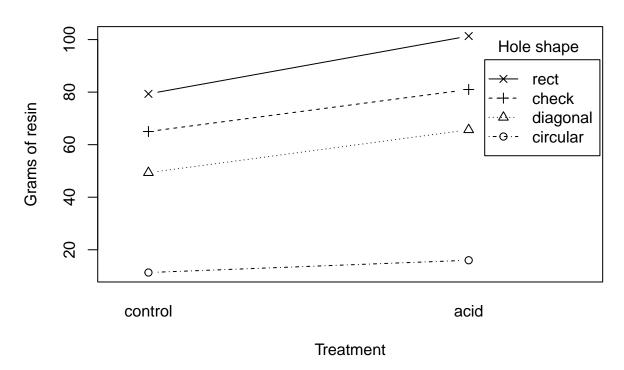
3 Pine oleoresin is obtained by tapping the trunks of pine trees. Tapping is done by cutting a hole in the bark and collecting the resin that oozes out. This experiment compares four shapes for the holes and the efficacy of acid treating the holes. Twenty-four pine trees are randomly selected from a plantation, and the 24 are assigned randomly to the eight combinations of whole shape (circular, diagonal slash, check, rectangular) and acid treatment (yes or no). The response is the total grams of resin collected from the hole (data from Low and Bin Mohd. Ali 1985). Analyze these data to determine how the treatments affect resin yield. Include the Tukey HSD test in your analysis.

	Circular	Diagonal	Check	Rect.
Control	9	43	60	77
	13	48	65	70
	12	57	70	91
Acid	15	66	75	97
	13	58	78	108
	20	73	90	99

```
# similar to the previous question
df <- expand.grid(acid = c('control', 'acid'), shape = c('circular', 'diagonal', 'check', 'rect'))
df <- rbind(df, df, df)
df$acid <- factor(df$acid, c('control', 'acid')) # control level first
df$shape <- as.factor(df$shape)
df <- df[order(df$acid), ]
rownames(df) <- 1:nrow(df)
df$resin <- c(
    9, 43, 60, 77,
    13, 48, 65, 70,
    12, 57, 70, 91,
    15, 66, 75, 97,
    13, 58, 78, 108,
    20, 73, 90, 99
)
tibble::glimpse(df)</pre>
```

```
## Rows: 24
## Columns: 3
## $ acid <fct> control, control, control, control, control, control, control, control, control, cet, circular, diagonal, check, rect, circular, diagonal, check, rect=
## $ resin <dbl> 9, 43, 60, 77, 13, 48, 65, 70, 12, 57, 70, 91, 15, 66, 75, 97, 1
```

Interaction Plot of Control/Acid and Hole shape



When looking only to the first treatment (control or acid), we can see that despite the hole shape the grams of resin are always bigger when using the control rather the acid treatment.

In addition, the rate of grams of resin seems bigger when changing from control to acid treatment when using the rectangular shape hole rather the circular one, for example.

The lines are quite parallel, which means that we would not expect an significant interaction.

We can fit an two-way ANOVA first and check the results:

```
fit <- aov(resin ~ acid * shape, data = df)
summary(fit)</pre>
```

```
##
               Df Sum Sq Mean Sq F value
                                            Pr(>F)
## acid
                    1305
                            1305 28.955 6.12e-05 ***
                3
                   19407
                             6469 143.493 8.93e-12 ***
## shape
                              79
## acid:shape
                3
                     237
                                    1.756
                                             0.196
               16
## Residuals
                              45
                     721
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
```

From this result, using a significance level of $\alpha = 0.05$, we can see that both control/acid treatment and hole

shape treatments affect the quantity of grams of resin, i.e, they are significant. However, the interaction is not significant because the p-value > 0.05.

fit_tukey <- TukeyHSD(fit, ordered = F)</pre>

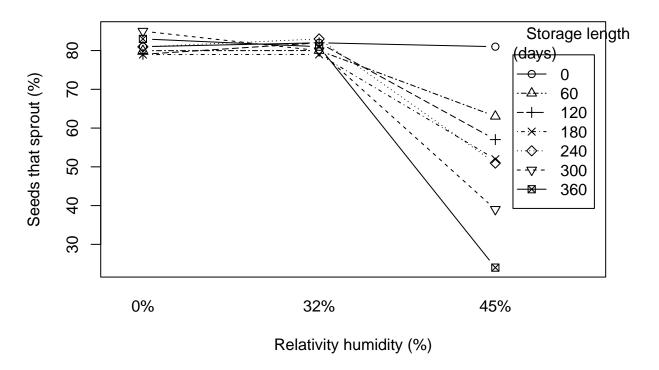
```
fit_tukey
##
     Tukey multiple comparisons of means
##
       95% family-wise confidence level
##
##
  Fit: aov(formula = resin ~ acid * shape, data = df)
##
## $acid
##
                 diff
                           lwr
                                     upr
                                            p adj
  acid-control 14.75 8.939027 20.56097 6.12e-05
##
##
  $shape
##
                         diff
                                     lwr
                                              upr
                                                      p adj
## diagonal-circular 43.83333 32.742396 54.92427 0.0000000
## check-circular
                     59.33333 48.242396 70.42427 0.0000000
## rect-circular
                     76.66667 65.575729 87.75760 0.0000000
## check-diagonal
                     15.50000
                               4.409063 26.59094 0.0051399
## rect-diagonal
                     32.83333 21.742396 43.92427 0.0000014
## rect-check
                               6.242396 28.42427 0.0019665
                     17.33333
##
## $'acid:shape'
##
                                            diff
                                                         lwr
                                                                   upr
                                                                           p adj
## acid:circular-control:circular
                                       4.6666667 -14.313864
                                                              23.64720 0.9866494
## control:diagonal-control:circular 38.0000000
                                                  19.019469
                                                              56.98053 0.0000733
## acid:diagonal-control:circular
                                      54.3333333
                                                  35.352803
                                                              73.31386 0.0000007
## control:check-control:circular
                                      53.6666667
                                                  34.686136
                                                              72.64720 0.0000008
## acid:check-control:circular
                                      69.6666667
                                                  50.686136
                                                              88.64720 0.0000000
## control:rect-control:circular
                                      68.0000000
                                                  49.019469
                                                              86.98053 0.0000000
## acid:rect-control:circular
                                      90.0000000
                                                  71.019469 108.98053 0.0000000
## control:diagonal-acid:circular
                                      33.333333
                                                  14.352803
                                                              52.31386 0.0003337
## acid:diagonal-acid:circular
                                      49.6666667
                                                  30.686136
                                                              68.64720 0.0000024
## control:check-acid:circular
                                      49.0000000
                                                  30.019469
                                                              67.98053 0.0000029
                                                  46.019469
## acid:check-acid:circular
                                                              83.98053 0.0000001
                                      65.0000000
## control:rect-acid:circular
                                      63.3333333
                                                  44.352803
                                                              82.31386 0.0000001
## acid:rect-acid:circular
                                      85.3333333
                                                  66.352803 104.31386 0.0000000
## acid:diagonal-control:diagonal
                                                  -2.647197
                                                              35.31386 0.1199600
                                      16.3333333
## control:check-control:diagonal
                                      15.6666667
                                                  -3.313864
                                                              34.64720 0.1477801
## acid:check-control:diagonal
                                      31.6666667
                                                  12.686136
                                                              50.64720 0.0005852
## control:rect-control:diagonal
                                      30.0000000
                                                  11.019469
                                                              48.98053 0.0010360
## acid:rect-control:diagonal
                                      52.0000000
                                                  33.019469
                                                              70.98053 0.0000013
## control:check-acid:diagonal
                                      -0.6666667
                                                 -19.647197
                                                              18.31386 1.0000000
## acid:check-acid:diagonal
                                      15.3333333
                                                  -3.647197
                                                              34.31386 0.1636475
## control:rect-acid:diagonal
                                      13.6666667
                                                  -5.313864
                                                              32.64720 0.2651715
## acid:rect-acid:diagonal
                                      35.6666667
                                                  16.686136
                                                              54.64720 0.0001547
## acid:check-control:check
                                                  -2.980531
                                      16.0000000
                                                              34.98053 0.1332427
## control:rect-control:check
                                      14.3333333
                                                  -4.647197
                                                              33.31386 0.2199118
                                                  17.352803
## acid:rect-control:check
                                      36.3333333
                                                              55.31386 0.0001247
## control:rect-acid:check
                                      -1.6666667 -20.647197
                                                              17.31386 0.9999817
## acid:rect-acid:check
                                      20.3333333
                                                   1.352803
                                                              39.31386 0.0313384
## acid:rect-control:rect
                                      22.0000000
                                                   3.019469
                                                             40.98053 0.0174419
```

From ANOVA, we saw that both treatments are significant (i.e. at least one treatment level differs from another). Now, with the Tukey HSD test, we can see that all the differences are significant as well (e.g., acid - control regarding the first treatment, and diagonal - circular and check - circular regarding the second treatment). In addition, ANOVA shows us the interaction was not significant, so we don't need to check it using a post hoc test such as Tukey HSD).

4 Big sagebrush is often planted in range restoration projects. An experiment is performed to determine the effects of storage length and relative humidity on the viability of seeds. Sixty-three batches of 300 seeds each are randomly divided into 21 groups of three. These 21 groups each receive a different treatment, namely the combinations of storage length (0, 60, 120, 180, 240, 300, or 360 days) and storage relative humidity (0, 32, or 45%). After the storage time, the seeds are planted, and the response is the percentage of seeds that sprout. Use the data set HW3_Q4.xlsx and analyze these data for the effects of the factors on viability.

```
df \leftarrow expand.grid(rel_hum = c('0\%', '32\%', '45\%'), storage_length = c(0, 60, 120, 180, 240, 300, 360))
df <- rbind(df, df, df) # 3 reps
df$rel_hum <- as.factor(df$rel_hum)</pre>
df$storage_length <- as.factor(df$storage_length)</pre>
df <- df[order(df$rel_hum), ]</pre>
rownames(df) <- 1:nrow(df)</pre>
df$seeds sprout <- c(
  82.1, 78.6,
                79.8,
                        82.3,
                                81.7,
                                        85, 82.7,
  79,
       80.8,
                79.1,
                        75.5,
                                80.1,
                                        87.9,
                                                 84.6,
  81.9, 80.5,
                                        82.1,
                78.2,
                        79.1,
                                81.1,
                                                 81.7,
  83.1, 78.1,
                80.4,
                        77.8,
                                83.8,
                                        82, 81,
  80.5, 83.6,
                81.8,
                        80.4,
                                83.7,
                                        77.6,
                                                 78.9,
  82.4, 78.3,
                83.8,
                        78.8,
                                81.5,
                                        80.3,
                                                 83.1,
  83.1, 66.5,
                52.9,
                        52.9,
                                52.2,
                                        38.6,
                                                 25.2,
  78.9, 61.4,
                                        37.9,
                58.9,
                        54.3,
                                51.9,
                                                 25.8,
       61.2,
                59.3,
                        48.7, 48.8, 40.6,
  81,
tibble::glimpse(df)
## Rows: 63
## Columns: 3
                    ## $ rel_hum
## $ storage_length <fct> 0, 60, 120, 180, 240, 300, 360, 0, 60, 120, 180, 240, 3~
## $ seeds_sprout
                    <dbl> 82.1, 78.6, 79.8, 82.3, 81.7, 85.0, 82.7, 79.0, 80.8, 7~
with(df, {interaction.plot(rel_hum, storage_length, seeds_sprout, type = 'b',
                           pch = c(1, 2, 3, 4, 5, 6, 7), leg.bty = 'o',
                           main = 'Interaction Plot of Relativity humidity and Storage length',
                           xlab = 'Relativity humidity (%)', ylab = 'Seeds that sprout (%)',
                           trace.label = 'Storage length\n(days)')})
```

Interaction Plot of Relativity humidity and Storage length



From the interaction plot we can see that when changing the relativity humidity from 32% to 45% the percentage of seeds that sprout varies depending of the days of storage length, which seems to show there is an interaction.

When changing the relativity humidity from 0% to 32% the percentage of seeds that sprout seems not to change that much when using different storage lengths. With very different slope lines across the last two levels of relativity humidity, we could suspect that there are interactions.

```
fit <- aov(seeds_sprout ~ rel_hum * storage_length, data = df)
summary(fit)</pre>
```

```
##
                           Df Sum Sq Mean Sq F value Pr(>F)
## rel hum
                               11476
                                         5738 1178.93 <2e-16 ***
## storage_length
                            6
                                1789
                                          298
                                                61.25 <2e-16 ***
## rel_hum:storage_length 12
                                 4154
                                          346
                                                71.12 <2e-16 ***
## Residuals
                           42
                                 204
                                            5
##
                      '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Signif. codes:
```

Using a significance level of $\alpha = 0.05$, we conclude that both treatments are significant. The interaction interaction is also significant, as we suspected from the interaction plot.