STAT 53533: R Assignments 03 Upload your answers, as a single file, in Blackboard by 11:59 PM on Wednesday, December 11, 2024

- A. Separate your answer in two parts (within the same file) as follows:
- 1. Part 1 must contain complete answers for all questions **without** any R code. It must have all numbers/values/diagrams as asked in the questions and should be accompanied by necessary explanations.
- 2. Part 2 contains only the R code and nothing else. **Any output/numbers/explanations written inside the R Code will NOT be graded**.
- 3. You must type all your answers and explanations for submission, as a professional report. Scanned copy of any handwritten answers/explanations will not be graded.

Consider the factor application dataset. The dataset consists of measurements on a large number of variables collected from a relatively small number of observations. Each row represents data from one observation. Each column represents data for one specific variable across all observations. Now, answer the following questions. [1+2+3+3+1=10 points]

- (i) For this dataset, report *n* and *p*.
- (ii) Use Parallel Analysis to choose the number of factors k using 95% quantile as summary criterion. Use 2000 simulated datasets. Report the comparison table and justify what the number of factors should be.
- (iii) With the number of factors as decided in Part (ii), estimate the factor loading matrix using PCA method and then improve it using varimax criterion.
 - (a) Report the overall improvement as the ratio of values of varimax criterion before and after applying the criterion.
 - (b) Report the improvement for each factor by showing the ratio of factor-specific variances before and after applying the criterion.
 - (c) Which factor showed maximum improvement due to varimax? Which factor showed minimum improvement due to varimax?
- (iv) Now, using the improved loading matrix from Part (iii), complete the following table:

How many variables have at most 30% variability explained by factors	The variable which is worst explained by the factors	Communality of 236 th variable
Proportion of overall variability explained by 2 nd factor	Correlation between 23 rd and 317 th variables	Specific variance of 840 th variable

(v) Report the factor scores for 16th observation.