



Universidade Federal do Rio Grande do Norte
Departamento de Engenharia de Computação e Automação

Programação Concorrente e Distribuída

Segunda Lista de Exercícios

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Sumário

1	Descrição	6
2	Questões	7
2.1	Questão 3.1	7
2.2	Questão 3.2	7
2.3	Questão 3.4	8
2.4	Questão 3.5	8
2.5	Questão 3.6	9
2.6	Questão 3.7	10
2.7	Questão 3.8	10
2.8	Questão 3.9	11
2.9	Questão 3.10	20
2.10	Questão 3.11	20
2.11	Questão 3.12 *	26
2.12	Questão 3.13	27
2.13	Questão 3.14	37
2.14	Questão 3.16	39
2.15	Questão 3.17	39
2.16	Questão 3.19	41
2.17	Questão 3.20	43
2.18	Questão 3.21	45

Lista de Figuras

1	Scatter em comunicação baseada em árvore	10
2	Gather em comunicação baseada em árvore	10
3	Allgather em comunicação butterfly	39
4	Comportamento dos tempos de execução	45

Lista de Tabelas

1 Distribuição dos elementos do vetor 9

1 Descrição

Lista da 2a unidade Descrição: Apresentar as respostas a todas as questões de exercício do livro texto, com exceção às questões: 3.3, 3.15 e 3.18.

Instruções para resolução (LEIAM!):

- Procure responder corretamente todas as questões da lista;
- Suas respostas serão validadas de forma oral por amostragem - geralmente de 2 à 3 defesas orais;
- Se não conseguir responder alguma questão, procure esclarecer as dúvidas em tempo em sala de aula com o professor, pelo SIGAA, com um colega, ou por e-mail. Se necessário, é possível marcar um horário para tirar dúvidas na sala do professor;
- Não serão aceitas respostas "mágicas", ou seja, quando a resposta está na lista entregue mas você não sabe explicar como chegou a ela. Sua nota nesse caso será 0 (zero). Mesmo que não saiba explicar apenas parte da sua resposta;
- Procure entregar a resolução da lista de forma organizada. Isso pode favorecer a sua nota;
- Os códigos dos programas requisitados (ou as partes relevantes) deverão aparecer no corpo da resolução da questão;
- A resolução da lista deverá ser entregue em formato PDF em apenas 1 (um) arquivo;
- O envio da resolução pode ser feito inúmeras vezes. Utilize-se disso para manter sempre uma versão atualizada das suas respostas e evite problemas com o envio próximo ao prazo de submissão devido a instabilidades no SIGAA;
- A lista com o número das questões respondidas deve aparecer na primeira folha da lista. Não será aceita alteração nessa lista.
- Procure preparar sua defesa oral para cada questão. Explicações diretas e sem arroubos favorecerão a sua nota;
- A defesa deverá ser agendada com antecedência. Para isso, indique por email (samuel@dca.ufrn.br) no mínimo 3 horários dentro dos intervalos disponíveis em pelo menos 3 turnos diferentes. Caso não tenha disponibilidade em 3 turnos diferentes, deverá apresentar uma justificativa.
- Os horários disponíveis serão disponibilizados em uma notícia na turma virtual e serão atualizados a medida que os agendamentos forem sendo fixados.
- A defesa oral leva apenas de 10 a 15 minutos em horários fixados com antecedência. Não será tolerado que o aluno chegue atrasado para a sua prova.

Período: Inicia em 20/09/2017 às 00h00 e finaliza em 11/10/2017 às 23h59

2 Questões

2.1 Questão 3.1

What happens in the greetings program if, instead of `strlen(greeting) + 1`, we use `strlen(greeting)` for the length of the message being sent by processes `1, 2, ..., comm_sz - 1`? What happens if we use `MAX_STRING` instead of `strlen(greeting) + 1`? Can you explain these results?

Neste caso, o `+ 1` indica que o caractere de terminação da string também deve ser incluído no envio da mensagem. Se substituirmos por apenas `strlen(greeting)` a mensagem pode ser impressa corretamente ou não, dependendo do conteúdo presente no buffer de recebimento. Caso o buffer de recebimento esteja preenchido com zeros (`"\0"`), o comando `printf()` vai conseguir imprimir a mensagem corretamente mesmo que não exista um terminador nulo na mensagem enviada.

Em testes feitos localmente, as mensagens sempre foram exibidas corretamente, pois os buffers estavam sempre sendo iniciados com zero em suas posições de memória.

2.2 Questão 3.2

Modify the trapezoidal rule so that it will correctly estimate the integral even if `comm_sz` doesn't evenly divide `n`. (You can still assume that $n \geq \text{comm_sz}$.)

Se `comm_sz` não divide perfeitamente `n`, devemos alocar os trapézios restantes nos processos de maneira mais deliberada. o pseudocódigo poderia ser:

```

1  get a, b, n;
2  h = (b - a) / n;
3  local_n = n / comm_sz; //Devemos garantir que a divisao sera inteira
4
5  n_mod_comm = n % comm_sz;
6  local_a = a + (my_rank * local_n * +
7              my_rank * ((int)(my_rank < n_mod_comm)) +
8              n_mod_comm * ((int)(my_rank >= n_mod_comm && n_mod_comm
9                               > 0))) * h;
10
11 local_b = local_a + (local_n + (int)(my_rank < n_mod_comm)) * h;
12 local_integral = Trap(local_a, local_b, local_n, h);

```

O trecho da linha 7 se refere ao acréscimo incremental que deve acontecer ao `h` para cada rank. Isto é, no caso de `n_mod_comm = 3`, o primeiro `local_a` deve receber um acréscimo de 0, o segundo, de 1, o terceiro, de 3 e assim sucessivamente. Isso acontece pois é uma compensação ao `local_b` que está sendo acrescido de 1 até o momento em que todos os trapézios extras (no caso de `n` não exatamente divisível por `comm_sz`) forem alocados em algum processo. E isso vai acontecer somente quando `my_rank \geq n_mod_comm`

2.3 Questão 3.4

Modify the program that just prints a line of output from each process (`mpi_output.c`) so that the output is printed in process rank order: process 0s output first, then process 1s, and so on.

```

1  #include <stdio.h>
2  #include <mpi.h>
3  #include <string.h> /* For strlen */
4
5  const int MAX_STRING = 100;
6  int main(void) {
7      char phrase[MAX_STRING];
8      int my_rank, comm_sz;
9
10     MPI_Init(NULL, NULL);
11     MPI_Comm_size(MPI_COMM_WORLD, &comm_sz);
12     MPI_Comm_rank(MPI_COMM_WORLD, &my_rank);
13
14     if (my_rank != 0) {
15         sprintf(phrase, "Proc %d of %d > Does anyone have a toothpick
16             ?", my_rank, comm_sz);
17         MPI_Send(phrase, strlen(phrase)+1, MPI_CHAR, 0, 0,
18             MPI_COMM_WORLD);
19     } else {
20         printf("Proc %d of %d > Does anyone have a toothpick?\n",
21             my_rank, comm_sz);
22         for (int q = 1; q < comm_sz; q++) {
23             MPI_Recv(phrase, MAX_STRING, MPI_CHAR, q, 0,
24                 MPI_COMM_WORLD, MPI_STATUS_IGNORE);
25             printf("%s\n", phrase);
26         }
27     }
28
29     MPI_Finalize();
30     return 0;
31 } /* main */

```

O princípio da resolução desta questão é perceber que para lidar com o não-determinismo do output de um programa MPI, nós devemos mandar todas as mensagens de saída para um único processo, neste caso o processo 0. Dessa forma, apenas um processo é responsável por gerenciar as mensagens de saída e, assim, podemos controlar a ordem de saída das mensagens.

2.4 Questão 3.5

In a binary tree, there is a unique shortest path from each node to the root. The length of this path is often called the depth of the node. A binary tree in which every nonleaf has two children is called a full binary

tree, and a full binary tree in which every leaf has the same depth is sometimes called a complete binary tree. See Figure 3.14. Use the principle of mathematical induction to prove that if T is a complete binary tree with n leaves, then the depth of the leaves is $\log_2(n)$.

Para fazer a indução vamos considerar $\log_2(n) = d$, onde d é a profundidade.

Então,

$$\log_2(n) = d \implies 2^d = n \quad (1)$$

Considerando o caso base em que $d = 0$,

$$\begin{aligned} 2^d &= n \\ 2^0 &= n \\ 2^0 &= 1 \end{aligned} \quad (2)$$

Tomamos que $d = k$ e assumimos que $2^k = n$ é verdadeiro. Então, aplicamos o passo de indução, onde $d = k + 1$, e para a próxima profundidade, $n_i = n_{i-1} \cdot 2$. Logo,

$$\begin{aligned} 2^{k+1} &= n \cdot 2 \\ &= 2^k 2^1 \\ &= 2^{k+1} \end{aligned} \quad (3)$$

Portanto, $2^d = n$ e, logo $\log_2(n) = d$, onde n é o número de folhas e d é a profundidade.

2.5 Questão 3.6

Suppose `comm_sz` = 4 and suppose that x is a vector with $n = 14$ components.

a. How would the components of x be distributed among the processes in a program that used a block distribution?

b. How would the components of x be distributed among the processes in a program that used a cyclic distribution?

c. How would the components of x be distributed among the processes in a program that used a block-cyclic distribution with blocksize $b = 2$?

You should try to make your distributions general so that they could be used regardless of what `comm_sz` and n are. You should also try to make your distributions “fair” so that if q and r are any two processes, the difference between the number of components assigned to q and the number of components assigned to r is as small as possible.

Processos	Bloco	Cíclico	Bloco-Cíclico (tamanho do bloco = 2)
0	0, 1, 2, 3	0, 4, 8, 12	0 1, 8 9
1	4, 5, 6, 7	1, 5, 9, 13	2 3, 10 11
2	8, 9, 10,	2, 6, 10,	4 5, 12 13
3	11, 12, 13,	3, 7, 11,	6 7

Tabela 1: Distribuição dos elementos do vetor

2.6 Questão 3.7

What do the various MPI collective functions do if the communicator contains a single process?

O processo MPI não terá qualquer outro processo para enviar os dados, logo o processamento deve ser feito nesse único processo. É um princípio que permite que os processo MPI sejam executados corretamente independente de número de nós/processos disponíveis.

A forma que isso é implementado é enviar os dados para si mesmo, algo que várias funções coletivas do MPI executam. Em alguns casos, para reduzir o movimento desnecessário de dados na memória, o MPI fornece uma flag chamada `MPI_IN_PLACE`, que permite que o buffer de recebimento seja o mesmo do de envio, melhorando o desempenho. Essa flag não funciona em todas as funções coletivas.

<https://www.mcs.anl.gov/research/projects/mpi/mpi-standard/mpi-report-2.0/node145.htm>

2.7 Questão 3.8

Suppose `comm_sz = 8` and `n = 16`.

- Draw a diagram that shows how MPI Scatter can be implemented using tree-structured communication with `comm_sz` processes when process 0 needs to distribute an array containing `n` elements.
- Draw a diagram that shows how MPI Gather can be implemented using tree-structured communication when an `n`-element array that has been distributed among `comm_sz` processes needs to be gathered onto process 0.

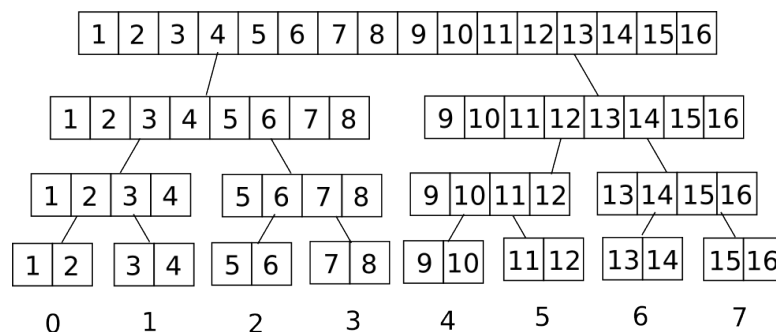


Figura 1: Scatter em comunicação baseada em árvore

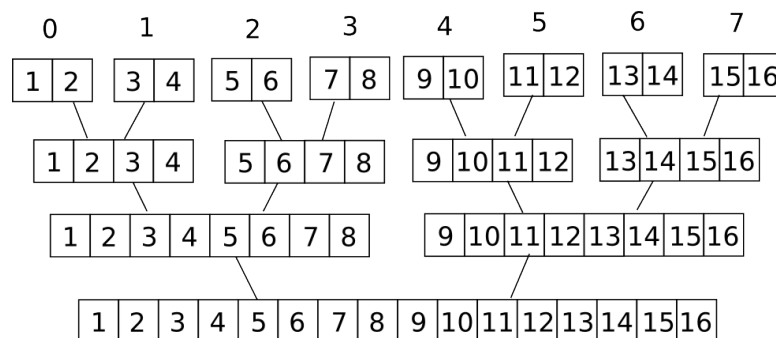


Figura 2: Gather em comunicação baseada em árvore

2.8 Questão 3.9

Write an MPI program that implements multiplication of a vector by a scalar and dot product. The user should enter two vectors and a scalar, all of which are read in by process 0 and distributed among the processes. The results are calculated and collected onto process 0, which prints them. You can assume that n , the order of the vectors, is evenly divisible by `comm_sz`.

```

1  /*Esse codigo foi modificado de mpi_vector_add.c */
2
3  /* File:      mpi_vector_add.c
4   *
5   * Purpose:   Implement parallel vector addition using a block
6   *            distribution of the vectors. This version also
7   *            illustrates the use of MPI_Scatter and MPI_Gather.
8   *
9   * Compile:   mpicc -g -Wall -o mpi_vector_add mpi_vector_add.c
10  * Run:       mpiexec -n <comm_sz> ./ vector_add
11  *
12  * Input:     The order of the vectors , n, and the vectors x and y
13  * Output:    The sum vector z = x+y
14  *
15  * Notes:
16  * 1. The order of the vectors , n, should be evenly divisible
17  *    by comm_sz
18  * 2. DEBUG compile flag.
19  * 3. This program does fairly extensive error checking. When
20  *    an error is detected, a message is printed and the processes
21  *    quit. Errors detected are incorrect values of the vector
22  *    order (negative or not evenly divisible by comm_sz), and
23  *    malloc failures.
24  *
25  * IPP:  Section 3.4.6 (pp. 109 and ff.)
26  */
27
28 #include <stdio.h>
29 #include <stdlib.h>
30 #include <mpi.h>
31
32 void Check_for_error(int local_ok , char fname[] , char message[] ,
33                     MPI_Comm comm);
34 void Read_n(int* n_p , int* local_n_p , int my_rank , int comm_sz ,
35            MPI_Comm comm);
36 void Allocate_vectors(double** local_x_pp , double** local_y_pp ,
37                      double** local_z_pp , int local_n , MPI_Comm comm);

```

```

38 void Read_vector(double local_a[], int local_n, int n, char vec_name
    [] ,
39         int my_rank, MPI_Comm comm);
40 void Read_scalar(double* scalar_p, int my_rank, int comm_sz, MPI_Comm
    comm);
41 void Print_vector(double local_b[], int local_n, int n, char title[],
42         int my_rank, MPI_Comm comm);
43 void Parallel_vector_dotproduct(double local_x[], double local_y[],
44         double local_z[], double* result, int local_n, int n, MPI_Comm
    comm);
45 void Parallel_scalar_multiplication(double scalar, double local_x[],
46         double local_z[], int local_n);
47
48
49 /*-----
    */
50 int main(void) {
51     int n, local_n;
52     int comm_sz, my_rank;
53     double *local_x, *local_y, *local_z;
54     double scalar, result;
55     MPI_Comm comm;
56
57     MPI_Init(NULL, NULL);
58     comm = MPI_COMM_WORLD;
59     MPI_Comm_size(comm, &comm_sz);
60     MPI_Comm_rank(comm, &my_rank);
61
62     Read_n(&n, &local_n, my_rank, comm_sz, comm);
63
64     Allocate_vectors(&local_x, &local_y, &local_z, local_n, comm);
65
66     Read_vector(local_x, local_n, n, "x", my_rank, comm);
67     Print_vector(local_x, local_n, n, "x is", my_rank, comm);
68     Read_vector(local_y, local_n, n, "y", my_rank, comm);
69     Print_vector(local_y, local_n, n, "y is", my_rank, comm);
70
71     Read_scalar(&scalar, my_rank, comm_sz, comm);
72
73     Parallel_scalar_multiplication(scalar, local_x, local_x, local_n);
74     Print_vector(local_x, local_n, n, "now x is", my_rank, comm);
75     Parallel_vector_dotproduct(local_x, local_y, local_z, &result,
        local_n,
76                                 n, comm);
77

```

```

78     if (my_rank == 0) {
79         printf("The result of (scalar*x[]).y[] is %lf \n", result);
80     }
81
82     free(local_x);
83     free(local_y);
84     free(local_z);
85
86     MPI_Finalize();
87
88     return 0;
89 } /* main */
90
91 /*-----
92  * Function:  Check_for_error
93  * Purpose:   Check whether any process has found an error.  If so,
94  *            print message and terminate all processes.  Otherwise,
95  *            continue execution.
96  * In args:   local_ok: 0 if calling process has found an error, 1
97  *            otherwise
98  *            fname:     name of function calling Check_for_error
99  *            message:   message to print if there's an error
100  *            comm:      communicator containing processes calling
101  *            Check_for_error: should be MPI_COMM_WORLD.
102  *
103  * Note:
104  *   The communicator containing the processes calling
105  *   Check_for_error
106  *   should be MPI_COMM_WORLD.
107  */
108 void Check_for_error(
109     int      local_ok    /* in */,
110     char      fname[]    /* in */,
111     char      message[]  /* in */,
112     MPI_Comm  comm       /* in */) {
113     int ok;
114
115     /* Pega o minimo do vetor
116        Se o minimo for zero, aconteceu algum erro,
117        caso contrario, todos os processos retornaram 1 e estao ok
118    */
119     MPI_Allreduce(&local_ok, &ok, 1, MPI_INT, MPI_MIN, comm);
120     if (ok == 0) {
121         int my_rank;
122         MPI_Comm_rank(comm, &my_rank);

```

```

122     if (my_rank == 0) {
123         fprintf(stderr, "Proc %d > In %s, %s\n", my_rank, fname,
124             message);
125         fflush(stderr);
126     }
127     MPI_Finalize();
128     exit(-1);
129 }
130 } /* Check_for_error */
131
132
133 /*-----
134  * Function:  Read_n
135  * Purpose:   Get the order of the vectors from stdin on proc 0 and
136  *            broadcast to other processes.
137  * In args:   my_rank:    process rank in communicator
138  *            comm_sz:    number of processes in communicator
139  *            comm:       communicator containing all the processes
140  *                        calling Read_n
141  * Out args:  n_p:        global value of n
142  *            local_n_p:  local value of n = n/comm_sz
143  *
144  * Errors:    n should be positive and evenly divisible by comm_sz
145  */
146 void Read_n(
147     int*      n_p          /* out */,
148     int*      local_n_p    /* out */,
149     int       my_rank      /* in  */,
150     int       comm_sz      /* in  */,
151     MPI_Comm  comm         /* in  */) {
152     int local_ok = 1;
153     char *fname = "Read_n";
154
155     if (my_rank == 0) {
156         printf("What's the order of the vectors?\n");
157         scanf("%d", n_p);
158     }
159     MPI_Bcast(n_p, 1, MPI_INT, 0, comm);
160     if (*n_p <= 0 || *n_p % comm_sz != 0) local_ok = 0;
161     Check_for_error(local_ok, fname,
162         "n should be > 0 and evenly divisible by comm_sz", comm);
163     *local_n_p = *n_p/comm_sz;
164 } /* Read_n */
165
166

```

```

167  /*
168  * Function:   Allocate_vectors
169  * Purpose:    Allocate storage for x, y, and z
170  * In args:    local_n:   the size of the local vectors
171  *             comm:      the communicator containing the calling
172  *                       processes
173  * Out args:    local_x_pp, local_y_pp, local_z_pp: pointers to memory
174  *             blocks to be allocated for local vectors
175  *
176  * Errors:      One or more of the calls to malloc fails
177  */
178 void Allocate_vectors(
179     double** local_x_pp /* out */,
180     double** local_y_pp /* out */,
181     double** local_z_pp /* out */,
182     int local_n /* in */,
183     MPI_Comm comm /* in */) {
184     int local_ok = 1;
185     char* fname = "Allocate_vectors";
186
187     *local_x_pp = malloc(local_n*sizeof(double));
188     *local_y_pp = malloc(local_n*sizeof(double));
189     *local_z_pp = malloc(local_n*sizeof(double));
190
191     if (*local_x_pp == NULL || *local_y_pp == NULL ||
192         *local_z_pp == NULL) local_ok = 0;
193     Check_for_error(local_ok, fname, "Can't allocate local vector(s)",
194                     comm);
195 } /* Allocate_vectors */
196
197  /*
198  * Function:   Read_vector
199  * Purpose:    Read a vector from stdin on process 0 and distribute
200  *             among the processes using a block distribution.
201  * In args:    local_n:   size of local vectors
202  *             n:         size of global vector
203  *             vec_name:  name of vector being read (e.g., "x")
204  *             my_rank:   calling process' rank in comm
205  *             comm:      communicator containing calling processes
206  * Out arg:    local_a:   local vector read
207  *
208  * Errors:      if the malloc on process 0 for temporary storage
209  *             fails the program terminates
210  */

```

```

211  * Note:
212  *      This function assumes a block distribution and the order
213  *      of the vector evenly divisible by comm_sz.
214  */
215 void Read_vector(
216     double    local_a[]    /* out */,
217     int        local_n      /* in  */,
218     int        n            /* in  */,
219     char       vec_name[]   /* in  */,
220     int        my_rank      /* in  */,
221     MPI_Comm   comm         /* in  */) {
222
223     double* a = NULL;
224     int i;
225     int local_ok = 1;
226     char* fname = "Read_vector";
227
228     if (my_rank == 0) {
229         a = malloc(n*sizeof(double));
230         if (a == NULL) local_ok = 0;
231         Check_for_error(local_ok, fname, "Can't allocate temporary
232             vector",
233             comm);
234         printf("Enter the vector %s\n", vec_name);
235         for (i = 0; i < n; i++)
236             scanf("%lf", &a[i]); // reads a double (long float)
237         MPI_Scatter(a, local_n, MPI_DOUBLE, local_a, local_n,
238             MPI_DOUBLE, 0,
239             comm);
240         free(a);
241     } else {
242         Check_for_error(local_ok, fname, "Can't allocate temporary
243             vector",
244             comm);
245         MPI_Scatter(a, local_n, MPI_DOUBLE, local_a, local_n,
246             MPI_DOUBLE, 0,
247             comm);
248     }
249 } /* Read_vector */
250
251 /*-----
252  * Function:  Read_scalar
253  * Purpose:   Get the the scalar number from stdin on proc 0 and
254  *            broadcast to other processes.
255  * In args:   my_rank:    process rank in communicator

```



```

252 *          comm_sz:    number of processes in communicator
253 *          comm:       communicator containing all the processes
254 *                      calling Read_n
255 * Out args:  scalar_p:    global value of n
256 *
257 */
258 void Read_scalar(
259     double*    scalar_p      /* out */,
260     int        my_rank       /* in  */,
261     int        comm_sz       /* in  */,
262     MPI_Comm   comm          /* in  */) {
263
264     if (my_rank == 0) {
265         printf("What's the scalar value?\n");
266         scanf("%lf", scalar_p); // reads double
267     }
268     MPI_Bcast(scalar_p, 1, MPI_DOUBLE, 0, comm);
269
270 } /* Read_scalar */
271
272 /*-----
273 * Function:  Print_vector
274 * Purpose:   Print a vector that has a block distribution to stdout
275 * In args:   local_b:  local storage for vector to be printed
276 *            local_n:  order of local vectors
277 *            n:        order of global vector (local_n*comm_sz)
278 *            title:    title to precede print out
279 *            comm:     communicator containing processes calling
280 *                      Print_vector
281 *
282 * Error:     if process 0 can't allocate temporary storage for
283 *            the full vector, the program terminates.
284 *
285 * Note:
286 *     Assumes order of vector is evenly divisible by the number of
287 *     processes
288 */
289 void Print_vector(
290     double     local_b[]    /* in  */,
291     int        local_n      /* in  */,
292     int        n            /* in  */,
293     char       title[]      /* in  */,
294     int        my_rank      /* in  */,
295     MPI_Comm   comm         /* in  */) {
296

```

```

297     double* b = NULL;
298     int i;
299     int local_ok = 1;
300     char* fname = "Print_vector";
301
302     if (my_rank == 0) {
303         b = malloc(n*sizeof(double));
304         if (b == NULL) local_ok = 0;
305         Check_for_error(local_ok, fname, "Can't allocate temporary
306             vector",
307             comm);
308         MPI_Gather(local_b, local_n, MPI_DOUBLE, b, local_n, MPI_DOUBLE
309             ,
310             0, comm);
311         printf("%s\n", title);
312         for (i = 0; i < n; i++)
313             printf("%f ", b[i]);
314         printf("\n");
315         free(b);
316     } else {
317         Check_for_error(local_ok, fname, "Can't allocate temporary
318             vector",
319             comm);
320         MPI_Gather(local_b, local_n, MPI_DOUBLE, b, local_n, MPI_DOUBLE
321             , 0,
322             comm);
323     }
324 } /* Print_vector */
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```

```

323 /*-----
324 * Function:  Parallel_vector_dotproduct
325 * Purpose:   Add a vector that's been distributed among the
326               processes
327 * In args:   local_x:  local storage of one of the vectors being
328               added
329               local_y:  local storage for the second vector being
330               added
331               local_n:  the number of components in local_x, local_y,
332               and local_z
333 * Out arg:   local_z:  local storage for the sum of the two vectors
334 */
335 void Parallel_vector_dotproduct(
336     double local_x[], /* in */ ,
337     double local_y[], /* in */ ,

```

```

335     double local_z [] /* out */,
336     double* result /* out */,
337     int local_n /* in */,
338     int n /* in */,
339     MPI_Comm comm /* in */) {
340     int local_i;
341
342     for (local_i = 0; local_i < local_n; local_i++){
343         local_z[local_i] = local_x[local_i] * local_y[local_i];
344     }
345
346     double local_total_z = 0.0;
347     for (local_i = 0; local_i < local_n; local_i++){
348         local_total_z += local_z[local_i];
349     }
350
351     MPI_Reduce(&local_total_z, result, 1, MPI_DOUBLE, MPI_SUM, 0, comm)
352         ;
353 } /* Parallel_vector_dotproduct */
354
355 /*-----
356 * Function: Parallel_scalar_multiplication
357 * Purpose: Add a vector that's been distributed among the
358             processes
359 * In args: scalar: storage for the scalar value
360            local_x: local storage for the second vector being
361            added
362            local_n: the number of components in local_x, local_y,
363            and local_z
364 * Out arg: local_z: local storage for the scalar multiplication of
365             the vector
366 */
367 void Parallel_scalar_multiplication(
368     double scalar /* in */,
369     double local_x [] /* in */,
370     double local_z [] /* out */,
371     int local_n /* in */) {
372     int local_i;
373
374     for (local_i = 0; local_i < local_n; local_i++){
375         local_z[local_i] = local_x[local_i] * scalar;
376     } /* Parallel_scalar_multiplication */

```

2.9 Questão 3.10

In the `Read_vector` function shown in Program 3.9, we use `local_n` as the actual argument for two of the formal arguments to `MPI_Scatter`: `send_count` and `recv_count`. Why is it OK to alias these arguments?

É possível alinhar os dois argumentos porque `send_count` deve ser o número de elementos, de acordo com `send_type`, que serão enviados para cada processo. E, de forma semelhante, o `recv_count` deve ser o número de elementos recebidos do processo raiz, de acordo com `recv_type`. Portanto, neste caso, ambos os argumentos devem receber o valor de `local_n`.

2.10 Questão 3.11

Finding **prefix sums** is a generalization of global sum. Rather than simply finding the sum of n values,

$$x_0 + x_1 + \dots + x_{n-1},$$

the prefix sums are the n partial sums

$$x_0, x_0 + x_1, x_0 + x_1 + x_2, \dots, x_0 + x_1 + \dots + x_{n-1}.$$

- Devise a serial algorithm for computing the n prefix sums of an array with n elements.
- Parallelize your serial algorithm for a system with n processes, each of which is storing one of the x_i s.
- Suppose $n = 2^k$ for some positive integer k . Can you devise a serial algorithm and a parallelization of the serial algorithm so that the parallel algorithm requires only k communication phases?
- MPI provides a collective communication function, `MPI_Scan`, that can be used to compute prefix sums:

```

1  int MPI_Scan(
2      void*          sendbuf_p    /* in  */,
3      void*          recvbuf_p    /* out */,
4      int            count        /* in  */,
5      MPI_Datatype    datatype     /* in  */,
6      MPI_Op          op          /* in  */,
7      MPI_Comm        comm        /* in  */);

```

It operates on arrays with `count` elements; both `sendbuf_p` and `recvbuf_p` should refer to blocks of `count` elements of type `datatype`. The `op` argument is the same as `op` for `MPI_Reduce`. Write an MPI program that generates a random array of `count` elements on each MPI process, finds the prefix sums, and prints the results.

a.

```

1  #include <stdio.h>
2  #include <time.h>
3  #include <stdlib.h>
4
5  int main() {
6      int n = 15;

```

```

7      srand( time(NULL) );
8
9      int vec[n];
10     int prefix_sum[n];
11
12     for(int i = 0; i < n; i++){
13         vec[i] = rand() % 10; // number between 0 and 9
14         printf("%d ", vec[i]);
15     }
16     printf("\n");
17
18     for(int i = 0; i < n; i++){
19         prefix_sum[i] = 0;
20         for(int j = 0; j <= i; j++){
21             prefix_sum[i] += vec[j];
22         }
23         printf("%d ", prefix_sum[i]);
24     }
25 }

```

b.

```

1  #include <stdio.h>
2  #include <time.h>
3  #include <stdlib.h>
4  #include <mpi.h>
5
6  int main() {
7      int comm_sz; /* Number of processes */
8      int my_rank; /* My process rank */
9      MPI_Init(NULL, NULL);
10     MPI_Comm comm = MPI_COMM_WORLD;
11     MPI_Comm_size(comm, &comm_sz);
12     MPI_Comm_rank(comm, &my_rank);
13
14     int vec_i;
15     int prefix_sum = 0;
16     int n = comm_sz;
17     int vec[n];
18
19     if (my_rank == 0){
20         srand( time(NULL) );
21         for(int i = 0; i < n; i++){
22             vec[i] = rand() % 10; // number between 0 and 9
23             printf("%d ", vec[i]);
24         }

```

```

25     printf("\n");
26
27     MPI_Scatter(vec, 1, MPI_INT, &vec_i, 1, MPI_INT, 0, comm);
28 }
29 else {
30     MPI_Scatter(vec, 1, MPI_INT, &vec_i, 1, MPI_INT, 0, comm);
31 }
32
33 // envia para todos os processo maiores do que ele mesmo
34 for(int i = my_rank; i < comm_sz; i++){
35     MPI_Send(&vec_i, 1, MPI_INT, i, 0, comm);
36 }
37
38 // recebe de todos os processos menores que ele mesmo
39 prefix_sum += vec_i;
40 for(int i = 0; i < my_rank; i++){
41     int aux_vec_i = 0;
42     MPI_Recv(&aux_vec_i, 1, MPI_INT, i, 0, comm,
43             MPI_STATUS_IGNORE);
44     prefix_sum += aux_vec_i;
45 }
46
47 // Imprime o resultado na tela
48 if (my_rank != 0) {
49     MPI_Send(&prefix_sum, 1, MPI_INT, 0, 1, comm);
50 } else {
51     printf("%d ", vec_i);
52     for (int q = 1; q < comm_sz; q++) {
53         int aux;
54         MPI_Recv(&aux, 1, MPI_INT, q, 1, comm, MPI_STATUS_IGNORE)
55         ;
56         printf("%d ", aux);
57     }
58     printf("\n");
59 }
60
61 MPI_Finalize();
62 return 0;
63 }

```

c. Serial

```

1 #include <stdio.h>
2 #include <time.h>

```

```

3  #include <stdlib.h>
4  #include <math.h>
5
6  int main() {
7      int n = 8;
8      srand(time(NULL));
9
10     int vec[n];
11
12     for(int i = 0; i < n; i++){
13         vec[i] = 1; //rand() % 10; // number between 0 and 9
14         printf("%d ", vec[i]);
15     }
16     printf("\n");
17
18     for(int k = 0; k < log2(n); k++){
19         printf("k is %d\n", k);
20         for(int i = pow(2, k) - 1; i < pow(2, log2(n)); i = i + pow(2, k
21             + 1)){
22             printf("i is %d\n", i);
23             for(int j = 1; j <= pow(2, k); j++){
24                 printf("vec[%d] = vec[%d] + vec[%d]\n", i+j, i, i+j);
25                 vec[i+j] = vec[i] + vec[i+j];
26             }
27             for(int i = 0; i < n; i++){
28                 printf("%d ", vec[i]);
29             }
30             printf("\n");
31         }
32
33         for(int i = 0; i < n; i++){
34             printf("%d ", vec[i]);
35         }
36         printf("\n");
37     }

```

Paralelo

```

1  #include <stdio.h>
2  #include <time.h>
3  #include <stdlib.h>
4  #include <mpi.h>
5  #include <math.h>
6
7  void print_vec(int vec[], int n);

```

```

8  int main() {
9      int comm_sz; /* Number of processes */
10     int my_rank; /* My process rank */
11     MPI_Init(NULL, NULL);
12     MPI_Comm comm = MPI_COMM_WORLD;
13     MPI_Comm_size(comm, &comm_sz);
14     MPI_Comm_rank(comm, &my_rank);
15
16     int vec_i;
17     int n = comm_sz;
18     int vec[n];
19
20     if (my_rank == 0) {
21         srand(time(NULL));
22         for(int i = 0; i < n; i++) {
23             vec[i] = 1; //rand() % 10; // number between 0 and 9
24         }
25         print_vec(vec, n);
26         MPI_Scatter(vec, 1, MPI_INT, &vec_i, 1, MPI_INT, 0, comm);
27     }
28     else {
29         MPI_Scatter(vec, 1, MPI_INT, &vec_i, 1, MPI_INT, 0, comm);
30     }
31
32     for(int k = 0; k < log2(n); k++) {
33         for(int i = pow(2, k) - 1; i < pow(2, log2(n)); i = i + pow(2, k
34             + 1)) {
35             for(int j = 1; j <= pow(2, k); j++) {
36                 if (my_rank == i) {
37                     MPI_Send(&vec_i, 1, MPI_INT, i+j, 0, comm);
38                     printf("This is %d, Sending to %d\n", my_rank, i+
39                         j);
40                 } else if (my_rank == i + j) {
41                     int aux_vec_i = 0;
42                     printf("This is %d, Receiving from %d\n", my_rank,
43                         i);
44                     MPI_Recv(&aux_vec_i, 1, MPI_INT, i, 0, comm,
45                         MPI_STATUS_IGNORE);
46                     vec_i += aux_vec_i;
47                 }
48             }
49         }
50     }
51
52     int vec_sum[n];

```



```

49     if (my_rank == 0) {
50         MPI_Gather(&vec_i, 1, MPI_INT, vec_sum, 1, MPI_INT, 0, comm);
51         print_vec(vec_sum, n);
52     } else {
53         MPI_Gather(&vec_i, 1, MPI_INT, vec_sum, 1, MPI_INT, 0, comm);
54     }
55
56     MPI_Finalize();
57     return 0;
58 }
59
60 void print_vec(int vec[], int n){
61     for(int i = 0; i < n; i++){
62         printf("%d ", vec[i]);
63     }
64     printf("\n");
65 }

```

d.

```

1  #include <stdio.h>
2  #include <stdlib.h>
3  #include <time.h>
4  #include <mpi.h>
5
6  void print_vec(int vec[], int n);
7
8  int main(void) {
9      int comm_sz; /* Number of processes */
10     int my_rank; /* My process rank */
11     MPI_Init(NULL, NULL);
12     MPI_Comm comm = MPI_COMM_WORLD;
13     MPI_Comm_size(comm, &comm_sz);
14     MPI_Comm_rank(comm, &my_rank);
15
16     int count = comm_sz;
17     int vec[count];
18     int sum[count];
19
20     srand(my_rank+1);
21     for(int i = 0; i < count; i++){
22         vec[i] = rand() % 10; // number between 0 and 9
23         sum[i] = 0;
24     }
25
26     MPI_Scan(vec, sum, count, MPI_INT, MPI_SUM, comm);

```

```

27
28     if (my_rank != 0) {
29         MPI_Send(vec, count, MPI_INT, 0, 0, comm);
30         MPI_Send(sum, count, MPI_INT, 0, 0, comm);
31     } else {
32         printf("rank %d - [", my_rank );
33         print_vec(vec, count);
34         printf("] => [");
35         print_vec(sum, count);
36         printf("]\n");
37         for (int q = 1; q < comm_sz; q++) {
38             MPI_Recv(vec, count, MPI_INT, q, 0, comm,
39                     MPI_STATUS_IGNORE);
40             MPI_Recv(sum, count, MPI_INT, q, 0, comm,
41                     MPI_STATUS_IGNORE);
42             printf("rank %d - [", q);
43             print_vec(vec, count);
44             printf("] => [");
45             print_vec(sum, count);
46             printf("]\n");
47         }
48     }
49     MPI_Finalize();
50     return 0;
51 }
52 void print_vec(int vec[], int n){
53     for(int i = 0; i < n; i++){
54         printf("%d ", vec[i]);
55     }
56 }

```

Output: [vec] => [sum]

```

rank 0 - [3 6 7 5 3] => [3 6 7 5 3]
rank 1 - [0 9 8 5 1] => [3 15 15 10 4]
rank 2 - [6 5 8 0 5] => [9 20 23 10 9]
rank 3 - [1 3 4 6 3] => [10 23 27 16 12]
rank 4 - [5 5 0 2 6] => [15 28 27 18 18]

```

2.11 Questão 3.12 *

An alternative to a butterfly-structured allreduce is a ring-pass structure. In a ring-pass, if there are p processes, each process q sends data to process $q + 1$, except that process $p - 1$ sends data to process 0. This is repeated until each process has the desired result. Thus, we can implement allreduce with the

following code:

```

1 sum = temp_val = my_val;
2   for (i = 1; i < p; i++) {
3       MPI_Sendrecv_replace(&temp_val, 1, MPI_INT, dest,
4       sendtag, source, recvtag, comm, &status);
5       sum += temp_val;
6   }

```

- Write an MPI program that implements this algorithm for allreduce. How does its performance compare to the butterfly-structured allreduce?
- Modify the MPI program you wrote in the first part so that it implements prefix sums.

2.12 Questão 3.13

`MPI_Scatter` and `MPI_Gather` have the limitation that each process must send or receive the same number of data items. When this is not the case, we must use the MPI functions `MPI_Gatherv` and `MPI_Scatterv`. Look at the man pages for these functions, and modify your vector sum, dot product program so that it can correctly handle the case when `n` isn't evenly divisible by `comm_sz`.

```

1 /*Esse codigo foi modificado de mpi_vector_add.c */
2
3 /* File:      mpi_vector_add.c
4  *
5  * Purpose:   Implement parallel vector addition using a block
6  *            distribution of the vectors. This version also
7  *            illustrates the use of MPI_Scatter and MPI_Gather.
8  *
9  * Compile:   mpicc -g -Wall -o mpi_vector_add mpi_vector_add.c
10 * Run:       mpiexec -n <comm_sz> ./vector_add
11 *
12 * Input:     The order of the vectors, n, and the vectors x and y
13 * Output:    The sum vector z = x+y
14 *
15 * Notes:
16 * 1. The order of the vectors, n, should be evenly divisible
17 *    by comm_sz
18 * 2. DEBUG compile flag.
19 * 3. This program does fairly extensive error checking. When
20 *    an error is detected, a message is printed and the processes
21 *    quit. Errors detected are incorrect values of the vector
22 *    order (negative or not evenly divisible by comm_sz), and
23 *    malloc failures.
24 *
25 * IPP:      Section 3.4.6 (pp. 109 and ff.)
26 */
27

```

```

28 #include <stdio.h>
29 #include <stdlib.h>
30 #include <mpi.h>
31
32 void Check_for_error(int local_ok, char fname[], char message[],
33                     MPI_Comm comm);
34 void Read_n(int* n_p, int* local_n_p, int* rest, int my_rank, int
35            comm_sz,
36            MPI_Comm comm);
37 void Allocate_vectors(double** local_x_pp, double** local_y_pp,
38                      double** local_z_pp, int local_n, MPI_Comm comm);
39 void Read_vector(int rest, double local_a[], int local_n, int n, char
40                vec_name[],
41                int my_rank, MPI_Comm comm);
42 void Read_scalar(double* scalar_p, int my_rank, int comm_sz, MPI_Comm
43                comm);
44 void Print_vector(double local_b[], int local_n, int n, char title[],
45                 int my_rank, MPI_Comm comm);
46 void Parallel_vector_dotproduct(double local_x[], double local_y[],
47                                double local_z[], double* result, int local_n, int n, MPI_Comm
48                                comm);
49 void Parallel_scalar_multiplication(double scalar, double local_x[],
50                                   double local_z[], int local_n);
51
52 /*-----*/
53 */
54 int main(void) {
55     int n, local_n, rest;
56     int comm_sz, my_rank;
57     double *local_x, *local_y, *local_z;
58     double scalar, result;
59     MPI_Comm comm;
60
61     MPI_Init(NULL, NULL);
62     comm = MPI_COMM_WORLD;
63     MPI_Comm_size(comm, &comm_sz);
64     MPI_Comm_rank(comm, &my_rank);
65
66     Read_n(&n, &local_n, &rest, my_rank, comm_sz, comm);
67
68     Allocate_vectors(&local_x, &local_y, &local_z, local_n, comm);
69
70     Read_vector(rest, local_x, local_n, n, "x", my_rank, comm);
71     Print_vector(local_x, local_n, n, "x is", my_rank, comm);

```

```

68     printf("Done ok" );
69     Read_vector(rest , local_y , local_n , n, "y", my_rank , comm);
70     Print_vector(local_y , local_n , n, "y is", my_rank , comm);
71
72     Read_scalar(&scalar , my_rank , comm_sz , comm);
73
74     Parallel_scalar_mutiplication(scalar , local_x , local_x , local_n);
75     Print_vector(local_x , local_n , n, "now x is", my_rank , comm);
76     Parallel_vector_dotproduct(local_x , local_y , local_z , &result ,
77                                local_n ,
78                                n, comm);
79
80     if (my_rank == 0) {
81         printf("The result of (scalar*x[]).y[] is %lf \n", result);
82     }
83
84     free(local_x);
85     free(local_y);
86     free(local_z);
87
88     MPI_Finalize();
89
90     return 0;
91 } /* main */
92
93 /*-----
94 * Function:  Check_for_error
95 * Purpose:   Check whether any process has found an error.  If so,
96 *            print message and terminate all processes.  Otherwise,
97 *            continue execution.
98 * In args:   local_ok:  0 if calling process has found an error, 1
99 *            otherwise
100 *            fname:     name of function calling Check_for_error
101 *            message:   message to print if there's an error
102 *            comm:      communicator containing processes calling
103 *            Check_for_error:  should be MPI_COMM_WORLD.
104 * Note:
105 *   The communicator containing the processes calling
106 *   Check_for_error
107 *   should be MPI_COMM_WORLD.
108 */
109 void Check_for_error(
110     int      local_ok    /* in */,
111     char     fname[]     /* in */,

```

```

111     char        message[] /* in */,
112     MPI_Comm    comm      /* in */) {
113     int ok;
114
115     /* Pega o minimo do vetor
116        Se o minimo for zero, aconteceu algum erro,
117        caso contrario, todos os processos retornaram 1 e estao ok
118     */
119     MPI_Allreduce(&local_ok, &ok, 1, MPI_INT, MPI_MIN, comm);
120     if (ok == 0) {
121         int my_rank;
122         MPI_Comm_rank(comm, &my_rank);
123         if (my_rank == 0) {
124             fprintf(stderr, "Proc %d > In %s, %s\n", my_rank, fname,
125                         message);
126             fflush(stderr);
127         }
128         MPI_Finalize();
129         exit(-1);
130     }
131 } /* Check_for_error */
132
133
134 /*-----
135  * Function:  Read_n
136  * Purpose:   Get the order of the vectors from stdin on proc 0 and
137  *            broadcast to other processes.
138  * In args:   my_rank:    process rank in communicator
139  *            comm_sz:    number of processes in communicator
140  *            comm:       communicator containing all the processes
141  *            calling Read_n
142  * Out args:  n_p:        global value of n
143  *            local_n_p:  local value of n = n/comm_sz
144  *
145  * Errors:    n should be positive and evenly divisible by comm_sz
146  */
147 void Read_n(
148     int*        n_p          /* out */,
149     int*        local_n_p    /* out */,
150     int*        rest         /* out */,
151     int         my_rank      /* in */,
152     int         comm_sz     /* in */,
153     MPI_Comm    comm        /* in */) {
154     int local_ok = 1;
155     char *fname = "Read_n";

```

```

156
157     if (my_rank == 0) {
158         printf("What's the order of the vectors?\n");
159         scanf("%d", n_p);
160     }
161     MPI_Bcast(n_p, 1, MPI_INT, 0, comm);
162     if (*n_p <= 0 ) local_ok = 0;
163     Check_for_error(local_ok , fname ,
164         "n should be > 0. ", comm);
165     *local_n_p = *n_p/comm_sz + 1;
166     *rest = *n_p % comm_sz;
167 } /* Read_n */
168
169
170 /*-----
171  * Function:   Allocate_vectors
172  * Purpose:    Allocate storage for x, y, and z
173  * In args:    local_n:   the size of the local vectors
174  *              comm:      the communicator containing the calling
175                        processes
176  * Out args:   local_x_pp, local_y_pp, local_z_pp: pointers to memory
177                        blocks to be allocated for local vectors
178  *
179  * Errors:     One or more of the calls to malloc fails
180  */
181 void Allocate_vectors(
182     double** local_x_pp /* out */,
183     double** local_y_pp /* out */,
184     double** local_z_pp /* out */,
185     int local_n /* in */,
186     MPI_Comm comm /* in */) {
187     int local_ok = 1;
188     char* fname = "Allocate_vectors";
189
190     *local_x_pp = malloc(local_n*sizeof(double));
191     *local_y_pp = malloc(local_n*sizeof(double));
192     *local_z_pp = malloc(local_n*sizeof(double));
193
194     if (*local_x_pp == NULL || *local_y_pp == NULL ||
195         *local_z_pp == NULL) local_ok = 0;
196     Check_for_error(local_ok , fname , "Can't allocate local vector(s)",
197         comm);
198 } /* Allocate_vectors */
199

```

```

200  /*
201  *  Function:    Read_vector
202  *  Purpose:    Read a vector from stdin on process 0 and distribute
203  *              among the processes using a block distribution.
204  *  In args:    local_n:  size of local vectors
205  *              n:        size of global vector
206  *              vec_name: name of vector being read (e.g., "x")
207  *              my_rank:  calling process' rank in comm
208  *              comm:     communicator containing calling processes
209  *  Out arg:    local_a:  local vector read
210  *
211  *  Errors:     if the malloc on process 0 for temporary storage
212  *              fails the program terminates
213  *
214  *  Note:
215  *      This function assumes a block distribution and the order
216  *      of the vector evenly divisible by comm_sz.
217  */
218  void Read_vector(
219      int      rest      /* in */,
220      double   local_a[] /* out */,
221      int      local_n   /* in */,
222      int      n         /* in */,
223      char     vec_name[] /* in */,
224      int      my_rank   /* in */,
225      MPI_Comm comm      /* in */) {
226
227      double* a = NULL;
228      int i;
229      int local_ok = 1;
230      char* fname = "Read_vector";
231
232      int comm_sz;
233      MPI_Comm_size(MPI_COMM_WORLD, &comm_sz);
234      int* sendcounts = malloc(sizeof(int)*comm_sz);
235      int* displs = malloc(sizeof(int)*comm_sz);
236
237      // Calculating send counts and displacement
238      int sum = 0;
239      int rem = rest;
240      for (int i = 0; i < comm_sz; i++) {
241          sendcounts[i] = n/comm_sz;
242          if (rem > 0) {
243              sendcounts[i]++;
244              rem--;

```



```

245     }
246
247     displs[i] = sum;
248     sum += sendcounts[i];
249 }
250
251 // print calculated send counts and displacements for each
252 // process
253 if (0 == my_rank) {
254     for (int i = 0; i < comm_sz; i++) {
255         printf("sendcounts[%d] = %d\tdispls[%d] = %d\n", i,
256             sendcounts[i], i, displs[i]);
257     }
258 }
259
260 a = malloc(n*sizeof(double));
261 if (a == NULL) local_ok = 0;
262 Check_for_error(local_ok, fname, "Can't allocate temporary vector",
263     comm);
264
265 if (my_rank == 0) {
266     printf("Enter the vector %s\n", vec_name);
267     for (i = 0; i < n; i++)
268         scanf("%lf", &a[i]); // reads a double (long float)
269 }
270
271 // divide the data among processes as described by sendcounts and
272 // displs
273 MPI_Scatterv(&data, sendcounts, displs, MPI_CHAR, &rec_buf,
274     100, MPI_CHAR, 0, MPI_COMM_WORLD);
275 MPI_Scatterv(a, sendcounts, displs, MPI_DOUBLE, local_a, local_n,
276     MPI_DOUBLE, 0, comm);
277
278 // print what each process received
279 printf("%d: ", my_rank);
280 for (int i = 0; i < sendcounts[my_rank]; i++) {
281     printf("%lf\t", local_a[i]);
282 }
283 printf("\n");
284
285 free(a);
286 free(sendcounts);
287 free(displs);
288 } /* Read_vector */

```

```

284
285  /*-----
286  * Function:   Read_scalar
287  * Purpose:    Get the the scalar number from stdin on proc 0 and
288  *             broadcast to other processes.
289  * In args:    my_rank:    process rank in communicator
290  *             comm_sz:    number of processes in communicator
291  *             comm:       communicator containing all the processes
292  *                         calling Read_n
293  * Out args:   scalar_p:    global value of n
294  *
295  */
296 void Read_scalar(
297     double*    scalar_p      /* out */,
298     int        my_rank       /* in  */,
299     int        comm_sz       /* in  */,
300     MPI_Comm   comm          /* in  */) {
301
302     if (my_rank == 0) {
303         printf("What's the scalar value?\n");
304         scanf("%lf", scalar_p); // reads double
305     }
306     MPI_Bcast(scalar_p, 1, MPI_DOUBLE, 0, comm);
307
308 } /* Read_scalar */
309
310 /*-----
311 * Function:   Print_vector
312 * Purpose:    Print a vector that has a block distribution to stdout
313 * In args:    local_b:    local storage for vector to be printed
314 *             local_n:    order of local vectors
315 *             n:          order of global vector (local_n*comm_sz)
316 *             title:      title to precede print out
317 *             comm:       communicator containing processes calling
318 *                         Print_vector
319 *
320 * Error:      if process 0 can't allocate temporary storage for
321 *             the full vector, the program terminates.
322 *
323 * Note:
324 *     Assumes order of vector is evenly divisible by the number of
325 *     processes
326 */
327 void Print_vector(
328     double     local_b[]     /* in  */,

```

```

329     int          local_n      /* in */,
330     int          n            /* in */,
331     char         title []     /* in */,
332     int          my_rank      /* in */,
333     MPI_Comm     comm         /* in */) {
334
335     double* b = NULL;
336     int i;
337     int local_ok = 1;
338     char* fname = "Print_vector";
339
340     int comm_sz;
341     MPI_Comm_size(MPI_COMM_WORLD, &comm_sz);
342     int* recvcnts = malloc(sizeof(int)*comm_sz);
343     int* displs = malloc(sizeof(int)*comm_sz);
344
345     // Calculating send counts and displacement
346     int sum = 0;
347     int rem = n%comm_sz;
348     for (int i = 0; i < comm_sz; i++) {
349         recvcnts[i] = n/comm_sz;
350         if (rem > 0) {
351             recvcnts[i]++;
352             rem--;
353         }
354
355         displs[i] = sum;
356         sum += recvcnts[i];
357     }
358
359     if (0 == my_rank) {
360         for (int i = 0; i < comm_sz; i++) {
361             printf("recvcnts[%d] = %d\tdispls[%d] = %d\n", i,
362                 recvcnts[i], i, displs[i]);
363         }
364
365
366     b = malloc(n*sizeof(double));
367     if (b == NULL) local_ok = 0;
368     Check_for_error(local_ok, fname, "Can't allocate temporary vector",
369         comm);
370
371     if (my_rank == 0) {

```

```

372     MPI_Gatherv(local_b , recvcnts[my_rank] , MPI_DOUBLE, b ,
373               recvcnts , displs ,
374               MPI_DOUBLE, 0, comm);
375     printf("%s\n" , title);
376     for (i = 0; i < n; i++)
377         printf("%f " , b[i]);
378     printf("\n");
379 } else {
380     MPI_Gatherv(local_b , recvcnts[my_rank] , MPI_DOUBLE, b ,
381               recvcnts , displs ,
382               MPI_DOUBLE, 0, comm);
383 }
384 free(b);
385 } /* Print_vector */
386
387
388 /*-----
389  * Function:  Parallel_vector_dotproduct
390  * Purpose:   Add a vector that's been distributed among the
391               processes
392  * In args:   local_x:  local storage of one of the vectors being
393               added
394               local_y:  local storage for the second vector being
395               added
396               local_n:  the number of components in local_x , local_y ,
397               and local_z
398  * Out arg:   local_z:  local storage for the sum of the two vectors
399  */
400 void Parallel_vector_dotproduct(
401     double local_x[] /* in */ ,
402     double local_y[] /* in */ ,
403     double local_z[] /* out */ ,
404     double* result /* out */ ,
405     int local_n /* in */ ,
406     int n /* in */ ,
407     MPI_Comm comm /* in */) {
408     int local_i;
409
410     for (local_i = 0; local_i < local_n; local_i++){
411         local_z[local_i] = local_x[local_i] * local_y[local_i];
412     }
413
414     double local_total_z = 0.0;

```

```

412     for (local_i = 0; local_i < local_n; local_i++){
413         local_total_z += local_z[local_i];
414     }
415
416     int my_rank;
417     MPI_Comm_rank(comm, &my_rank);
418     printf("rank: %d > %lf\n", my_rank, local_total_z );
419
420     MPI_Reduce(&local_total_z, result, 1, MPI_DOUBLE, MPI_SUM, 0, comm)
421         ;
422 } /* Parallel_vector_dotproduct */
423
424 /*-----
425  * Function: Parallel_scalar_multiplication
426  * Purpose: Add a vector that's been distributed among the
427             processes
428  * In args: scalar: storage for the scalar value
429             local_x: local storage for the second vector being
430             added
431             local_n: the number of components in local_x, local_y,
432             and local_z
433  * Out arg: local_z: local storage for the scalar multiplication of
434             the vector
435  */
436 void Parallel_scalar_multiplication(
437     double scalar /* in */,
438     double local_x[] /* in */,
439     double local_z[] /* out */,
440     int local_n /* in */) {
441     int local_i;
442
443     for (local_i = 0; local_i < local_n; local_i++)
444         local_z[local_i] = local_x[local_i] * scalar;
445 } /* Parallel_scalar_multiplication */

```

2.13 Questão 3.14

a. Write a serial C program that defines a two-dimensional array in the main function. Just use numeric constants for the dimensions: `int two d[3][4];`

Initialize the array in the main function. After the array is initialized, call a function that attempts to print the array. The prototype for the function should look something like this.

```
void Print_two_d(int two d[][], int rows, int cols);
```

After writing the function try to compile the program. Can you explain why it won't compile?

b. After consulting a C reference (e.g., Kernighan and Ritchie [29]), modify the program so that it will

compile and run, but so that it still uses a two-dimensional C array.

O código abaixo não compila pois o compilador precisa saber as dimensões para fazer a aritmética de ponteiros corretamente. Isto é, se o compilador não tiver as dimensões do array quando ele é passado para uma função (e passado como ponteiro), a expressão `array[x][y]` não pode ser calculada, pois não há como saber onde uma linha ou coluna começa ou termina.

```

1 #include <stdio.h>
2 #include <stdlib.h>
3
4 void Print_two_d(int two_d[][], int rows, int cols);
5
6 int main() {
7     int two_d[3][4] = {{1,1,1,1},
8                        {2,2,2,2},
9                        {3,3,3,3}};
10
11     Print_two_d(two_d,3,4);
12     return 0;
13 }
14
15 void Print_two_d(int two_d[][], int rows, int cols){
16     int i, j;
17     for(i = 0; i < rows; i++){
18         for(j = 0; j < cols; j++){
19             printf("%d\n", two_d[i][j]);
20         }
21     }
22 }

1 #include <stdio.h>
2 #include <stdlib.h>
3
4 void Print_two_d(int two_d[][4], int rows, int cols);
5
6 int main() {
7     int two_d[3][4] = {{1,1,1,1},
8                        {2,2,2,2},
9                        {3,3,3,3}};
10
11     Print_two_d(two_d,3,4);
12     return 0;
13 }
14
15 void Print_two_d(int two_d[][4], int rows, int cols){
16     int i, j;

```

```

17     for(i = 0; i < rows; i++){
18         for(j = 0; j < cols; j++){
19             printf("%d\n", two_d[i][j]);
20         }
21     }
22 }

```

2.14 Questão 3.16

Suppose `comm_sz = 8` and the vector `x = (0, 1, 2, ..., 15)` has been distributed among the processes using a block distribution. Draw a diagram illustrating the steps in a butterfly implementation of allgather of `x`.

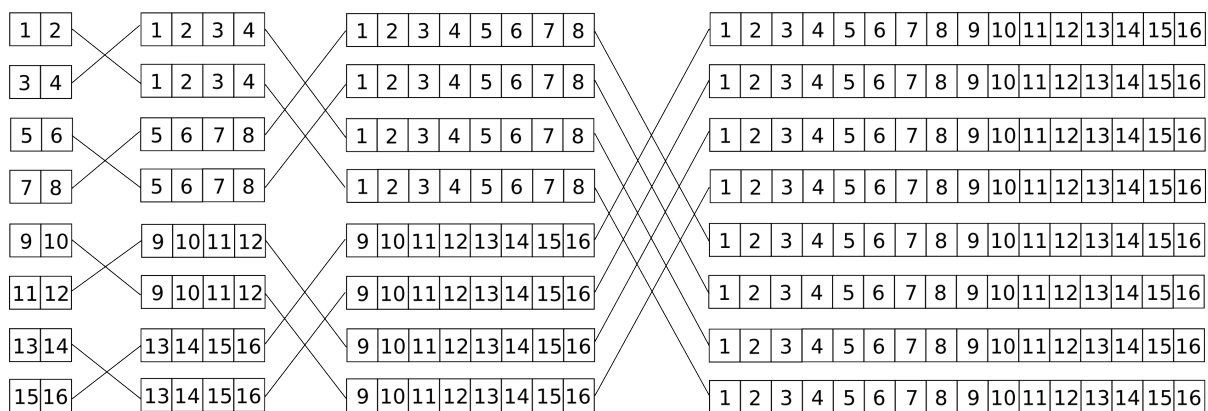


Figura 3: Allgather em comunicação butterfly

2.15 Questão 3.17

`MPI_Type_contiguous` can be used to build a derived datatype from a collection of contiguous elements in an array. Its syntax is

```

1  int MPI_Type_contiguous(
2      int count          /* in */,
3      MPI_Datatype old_mpi_t /* in */,
4      MPI_Datatype* new_mpi_t_p /* out */);

```

Modify the `Read_vector` and `Print_vector` functions so that they use an MPI datatype created by a call to `MPI_Type_contiguous` and a count argument of 1 in the calls to `MPI_Scatter` and `MPI_Gather`.

```

1  void Read_vector(
2      double local_a[] /* out */,
3      int local_n /* in */,
4      int n /* in */,
5      char vec_name[] /* in */,
6      int my_rank /* in */,

```

```

7      MPI_Comm comm      /* in */) {
8
9      double* a = NULL;
10     int i;
11     int local_ok = 1;
12     char* fname = "Read_vector";
13
14     MPI_Datatype CONTIGUOUS;
15     MPI_Type_contiguous(local_n, MPI_DOUBLE, &CONTIGUOUS);
16     MPI_Type_commit(&CONTIGUOUS);
17
18     if (my_rank == 0) {
19         a = malloc(n*sizeof(double));
20         if (a == NULL) local_ok = 0;
21         Check_for_error(local_ok, fname, "Can't allocate temporary
22             vector",
23             comm);
24         printf("Enter the vector %s\n", vec_name);
25         for (i = 0; i < n; i++)
26             scanf("%lf", &a[i]); // reads a double (long float)
27         MPI_Scatter(a, 1, CONTIGUOUS, local_a, 1, CONTIGUOUS, 0, comm);
28         free(a);
29     } else {
30         Check_for_error(local_ok, fname, "Can't allocate temporary
31             vector",
32             comm);
33         MPI_Scatter(a, 1, CONTIGUOUS, local_a, 1, CONTIGUOUS, 0, comm);
34     }
35 } /* Read_vector */
36
37 void Print_vector(
38     double local_b[], /* in */,
39     int local_n /* in */,
40     int n /* in */,
41     char title[] /* in */,
42     int my_rank /* in */,
43     MPI_Comm comm /* in */) {
44
45     double* b = NULL;
46     int i;
47     int local_ok = 1;
48     char* fname = "Print_vector";
49
50     MPI_Datatype CONTIGUOUS;
51     MPI_Type_contiguous(local_n, MPI_DOUBLE, &CONTIGUOUS);

```



```

16 MPI_Type_commit(&CONTIGUOUS);
17
18 if (my_rank == 0) {
19     b = malloc(n*sizeof(double));
20     if (b == NULL) local_ok = 0;
21     Check_for_error(local_ok, fname, "Can't allocate temporary
        vector",
22                     comm);
23     MPI_Gather(local_b, 1, CONTIGUOUS, b, 1, CONTIGUOUS, 0, comm);
24     printf("%s\n", title);
25     for (i = 0; i < n; i++)
26         printf("%f ", b[i]);
27     printf("\n");
28     free(b);
29 } else {
30     Check_for_error(local_ok, fname, "Can't allocate temporary
        vector",
31                     comm);
32     MPI_Gather(local_b, 1, CONTIGUOUS, b, 1, CONTIGUOUS, 0, comm);
33 }
34 } /* Print_vector */

```

2.16 Questão 3.19

`MPI_Type_indexed` can be used to build a derived datatype from arbitrary array elements. Its syntax is

```

1 int MPI_Type_indexed(
2     int count /* in */,
3     int array_of_blocklengths[] /* in */,
4     int array_of_displacements[] /* in */,
5     MPI_Datatype old_mpi_t /* in */,
6     MPI_Datatype* new_mpi_t_p /* out */);

```

Unlike `MPI_Type_create_struct`, the displacements are measured in units of `old_mpi_t` - not bytes. Use `MPI_Type_indexed` to create a derived datatype that corresponds to the upper triangular part of a square matrix. For example, in the 4 x 4 matrix

$$\begin{pmatrix} 0 & 1 & 2 & 3 \\ 4 & 5 & 6 & 7 \\ 8 & 9 & 10 & 11 \\ 12 & 13 & 14 & 15 \end{pmatrix}$$

the upper triangular part is the elements 0, 1, 2, 3, 5, 6, 7, 10, 11, 15. Process 0 should read in an $n \times n$ matrix as a one-dimensional array, create the derived datatype, and send the upper triangular part with a single call to `MPI_Send`. Process 1 should receive the upper triangular part with a single call to `MPI_Recv` and then print the data it received.

```

1  #include <stdio.h>
2  #include <stdlib.h>
3  #include <mpi.h>
4
5  int main(int argc , char *argv[])
6  {
7      int rank , size , i;
8      MPI_Datatype type;
9      int n = 4;
10
11     int blocklen[n], displacement[n];
12     for (int i = n, j = 0;
13         i > 0 && j < n; i--, j++)
14         { blocklen[j] = i;}
15
16     for (int i = 0, j = 0;
17         i < n, j < n; i+=5, j++)
18         { displacement[j] = i;}
19
20     int buffer[n*n];
21     MPI_Init(&argc , &argv);
22     MPI_Comm_rank(MPI_COMM_WORLD, &rank);
23     MPI_Comm_size(MPI_COMM_WORLD, &size);
24
25     if (size < 2)
26     {
27         printf("Please run with 2 processes.\n");
28         MPI_Finalize();
29         return 1;
30     }
31
32     MPI_Type_indexed(n, blocklen , displacement , MPI_INT, &type);
33     MPI_Type_commit(&type);
34
35     if (rank == 0)
36     {
37         printf("Enter the matrix: ");
38         fflush(stdout);
39         for (int i = 0; i < n*n; i++){
40             scanf("%d", &buffer[i]);
41         }
42
43         MPI_Send(buffer , 1, type , 1, 123, MPI_COMM_WORLD);
44     }
45

```

```

46     if (rank == 1)
47     {
48         for (i=0; i<n*n; i++)
49             buffer[i] = -1;
50         MPI_Recv(buffer, 1, type, 0, 123, MPI_COMM_WORLD,
51                 MPI_STATUS_IGNORE);
52         for (i=0; i<n*n; i++)
53             printf("buffer[%d] = %d\n", i, buffer[i]);
54         fflush(stdout);
55     }
56     MPI_Finalize();
57     return 0;
58 }

```

2.17 Quest o 3.20

The functions `MPI_Pack` and `MPI_Unpack` provide an alternative to derived datatypes for grouping data. `MPI_Pack` copies the data to be sent, one block at a time, into a user-provided buffer. The buffer can then be sent and received. After the data is received, `MPI_Unpack` can be used to unpack it from the receive buffer. The syntax of `MPI_Pack` is

```

1     int MPI_Pack(
2         void*          in_buf          /* in      */,
3         int            in_buf_count    /* in      */,
4         MPI_Datatype   datatype        /* in      */,
5         void*          pack_buf        /* out     */,
6         int            pack_buf_sz     /* in      */,
7         int*           position_p      /* in/out  */,
8         MPI_Comm       comm           /* in      */);

```

We could therefore pack the input data to the trapezoidal rule program with the following code:

```

1     char pack_buf[100];
2     int position = 0;
3
4     MPI_Pack(&a, 1, MPI_DOUBLE, pack_buf, 100, &position, comm);
5     MPI_Pack(&b, 1, MPI_DOUBLE, pack_buf, 100, &position, comm);
6     MPI_Pack(&n, 1, MPI_INT, pack_buf, 100, &position, comm);

```

The key is the position argument. When `MPI_Pack` is called, position should refer to the first available slot in pack buf. When `MPI_Pack` returns, it refers to the first available slot after the data that was just packed, so after process 0 executes this code, all the processes can call `MPI_Bcast`:

```

1     MPI_Bcast(pack_buf, 100, MPI_PACKED, 0, comm);

```

Note that the MPI datatype for a packed buffer is `MPI_PACKED`. Now the other processes can unpack the data using: `MPI_Unpack`:

```

1  int MPI_Unpack(
2      void*      pack_buf      /* in      */,
3      int        pack_buf_sz   /* in      */,
4      int*       position_p    /* in/out */,
5      void*      out_buf       /* out     */,
6      int        out_buf_count /* in      */,
7      MPI_Datatype datatype    /* in      */,
8      MPI_Comm   comm          /* in      */);

```

This can be used by “reversing” the steps in `MPI_Pack`, that is, the data is unpacked one block at a time starting with position = 0. Write another Get input function for the trapezoidal rule program. This one should use `MPI_Pack` on process 0 and `MPI_Unpack` on the other processes.

```

1  void Get_input(int my_rank, int comm_sz, double* a_p, double* b_p,
2      int* n_p) {
3      //int dest;
4
5      MPI_Comm comm = MPI_COMM_WORLD;
6      char pack_buf[100];
7      int position = 0;
8
9      if (my_rank == 0) {
10         printf("Enter a, b, and n\n");
11         scanf("%lf %lf %d", a_p, b_p, n_p);
12
13         printf("rank %d: %d\n", my_rank, *n_p);
14         printf("rank %d: %lf\n", my_rank, *b_p);
15         printf("rank %d: %lf\n", my_rank, *a_p);
16
17         MPI_Pack(a_p, 1, MPI_DOUBLE, pack_buf, 100, &position, comm);
18         MPI_Pack(b_p, 1, MPI_DOUBLE, pack_buf, 100, &position, comm);
19         MPI_Pack(n_p, 1, MPI_INT, pack_buf, 100, &position, comm);
20
21         MPI_Bcast(pack_buf, 100, MPI_PACKED, 0, comm);
22     }
23     else { /* my_rank != 0 */
24         MPI_Bcast(pack_buf, 100, MPI_PACKED, 0, comm);
25
26         MPI_Unpack(pack_buf, 100, &position, a_p, 1, MPI_DOUBLE, comm);
27         MPI_Unpack(pack_buf, 100, &position, b_p, 1, MPI_DOUBLE, comm);
28         MPI_Unpack(pack_buf, 100, &position, n_p, 1, MPI_INT, comm);
29     }
30 } /* Get_input */

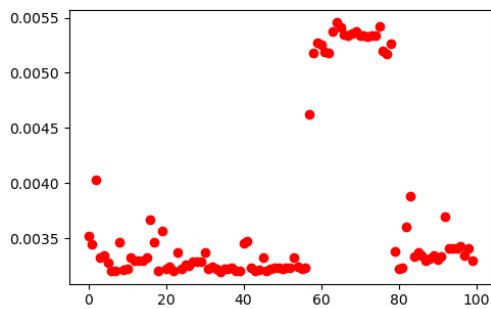
```

2.18 Questão 3.21

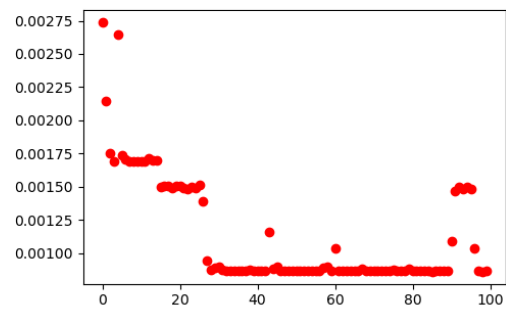
How does your system compare to ours? What run-times does your system get for matrix-vector multiplication? What kind of variability do you see in the times for a given value of `comm_sz` and n ? Do the results tend to cluster around the minimum, the mean, or the median?

	Ordem da Matriz				
<code>comm_sz</code>	1024	2048	4096	8192	16384
1	3.7561	12.8853	52.0139	210.4686	846.9655
2	2.0700	10.2071	41.1858	107.3081	438.0811
4	1.7275	6.8219	25.0998	64.2229	245.5204
8	1.7007	4.1896	14.3932	56.5015	219.8544
16	2.1960	6.0016	20.8711	76.8699	236.1451

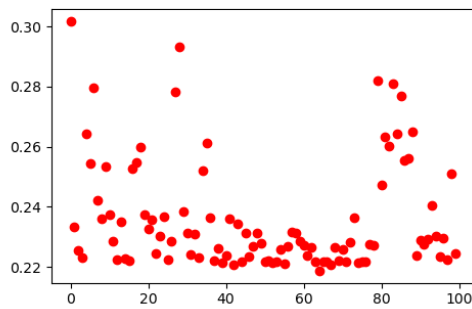
A medida que o `comm_sz` aumenta, é possível ver que o tempo de execução diminui. Contudo, a execução nem sempre tem um comportamento constante. Isso pode ser observado na Figura 4.



(a) `comm_sz` = 1, Ordem = 1024, (s)



(b) `comm_sz` = 4, Ordem = 1024, (s)



(c) `comm_sz` = 16, Ordem = 16384, (s)

Figura 4: Comportamento dos tempos de execução