

Universidade Federal do Rio Grande do Norte Departamento de Engenharia de Computação e Automação

Programação Concorrente e Distribuida

Segunda Lista de Exercícios

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1 Descrição

Lista da 2a unidade Descrição: Apresentar as respostas a todas as questões de exercício do livro texto, com exceção às questões: 3.3, 3.15 e 3.18.

Instruções para resolução (LEIAM!):

- Procure responder corretamente todas as questões da lista;
- Suas respostas serão validadas de forma oral por amostragem geralmente de 2 à 3 defesas orais;
- Se não conseguir responder alguma questão, procure esclarecer as dúvidas em tempo em sala de aula com o professor, pelo SIGAA, com um colega, ou por e-mail. Se necessário, é possível marcar um horário para tirar dúvidas na sala do professor;
- Não serão aceitas respostas "mágicas", ou seja, quando a resposta está na lista entregue mas você não sabe explicar como chegou a ela. Sua nota nesse caso será 0 (zero). Mesmo que não saiba explicar apenas parte da sua resposta;
- Procure entregar a resolução da lista de forma organizada. Isso pode favorecer a sua nota;
- Os códigos dos programas requisitados (ou as partes relevantes) deverão aparecer no corpo da resolução da questão;
- A resolução da lista deverá ser entregue em formato PDF em apenas 1 (um) arquivo;
- O envio da resolução pode ser feito inúmeras vezes. Utilize-se disso para manter sempre uma versão atualizada das suas respostas e evite problemas com o envio próximo ao prazo de submissão devido a instabilidades no SIGAA;
- A lista com o número das questões respondidas deve aparecer na primeira folha da lista. Não será aceita alteração nessa lista.
- Procure preparar sua defesa oral para cada questão. Explicações diretas e sem arrodeios favorecerão a sua nota;
- A defesa deverá ser agendada com antecedência. Para isso, indique por email (samuel@dca.ufrn.br) no mínimo 3 horários dentro dos intervalos disponíveis em pelo menos 3 turnos diferentes. Caso não tenha disponibilidade em 3 turnos diferentes, deverá apresentar uma justificativa.
- Os horários disponíveis serão disponibilizados em uma notícia na turma virtual e serão atualizados a medida que os agendamentos forem sendo fixados.
- A defesa oral leva apenas de 10 a 15 minutos em horários fixados com antecedência. Não será tolerado que o aluno chegue atrasado para a sua prova.

Período: Inicia em 20/09/2017 às 00h00 e finaliza em 11/10/2017 às 23h59

2 Questões

2.1 Questão 3.1

What happens in the greetings program if, instead of strlen (greeting) + 1, we use strlen (greeting) for the length of the message being sent by processes 1, 2, ..., comm_sz- 1? What happens if we use MAX_STRING instead of strlen (greeting) + 1? Can you explain these results?

Neste caso, o + 1 indica que o caractere de terminação da string também deve ser incluido no envio da mensagem. Se substituirmos por apenas strlen (greeting) a mensagem pode ser impressa corretamente ou não, dependendo do conteúdo presente no buffer de recebimento. Caso o buffer de recebimento esteja preenchido com zeros ("\0"), o comando printf () vai conseguir imprimir a mensagem corretamente mesmo que não exista um terminador nulo na mensagem enviada.

Em testes feitos localmente, as mensagens sempre foram exibidas corretamente, pois os buffers estavam sempre sendo iniciados com zero em suas posições de memória.

2.2 Questão 3.2

Modify the trapezoidal rule so that it will correctly estimate the integral even if $comm_sz$ doesn't evenly divide n. (You can still assume that $n \ge comm_sz$.)

Se comm_sz não divide perfeitamente n, devemos alocar os trapézios restantes nos processos de maneira mais deliberada. o pseudocódigo poderia ser:

O trecho da linha 7 se refere ao acrescimo incremental que deve acontecer ao h para cada rank. Isto é, no caso de n_mod_comm = 3, o primeiro local_a deve receber um acrescimo de 0, o segundo, de 1, o terceiro, de 3 e assim sucessivamente. Isso acontece pois é uma compensação ao local_b que está sendo acrescido de 1 até o momento em que todos os trapézios extras (no caso de n não exatamente divisivel por comm_sz) forem alocados em algum processo. E isso vai acontecer somente quando my_rank \geq n_mod_comm

2.3 Questão 3.4

Modify the program that just prints a line of output from each process (mpi_output.c) so that the output is printed in process rank order: process 0s output first, then process 1s, and so on.

```
#include <stdio.h>
  #include <mpi.h>
  #include <string.h> /* For strlen */
  const int MAX_STRING = 100;
  int main(void) {
       char phrase[MAX_STRING];
       int my_rank, comm_sz;
       MPI_Init (NULL, NULL);
10
      MPI Comm size (MPI COMM WORLD, &comm sz);
      MPI_Comm_rank (MPI_COMM_WORLD, &my_rank);
12
13
       if (my_rank != 0) {
14
           sprintf (phrase, "Proc %d of %d > Does anyone have a toothpick
15
              ?", my_rank, comm_sz);
           MPI_Send(phrase, strlen(phrase)+1, MPI_CHAR, 0, 0,
16
              MPI COMM WORLD);
       } else {
17
           printf("Proc %d of %d > Does anyone have a toothpick?\n",
18
              my_rank , comm_sz);
           for (int q = 1; q < comm_sz; q++) {
19
               MPI_Recv(phrase, MAX_STRING, MPI_CHAR, q, 0,
20
                  MPI_COMM_WORLD, MPI_STATUS_IGNORE);
               printf("%s\n", phrase);
21
           }
22
       }
23
       MPI_Finalize();
25
       return 0;
26
     /* main */
  }
```

O princípio da resulução desta questão é perceber que para lidar com o não-determinismo do output de um programa MPI, nós devemos mandar todas as mensagens de saída para um único processo, neste caso o processo 0. Dessa forma, apenas um processo é responsável por gerenciar as mensagens de saída e, assim, podemos controlar a ordem de saída das mensagens.

2.4 Questão 3.5

In a binary tree, there is a unique shortest path from each node to the root. The length of this path is often called the depth of the node. A binary tree in which every nonleaf has two children is called a full binary

tree, and a full binary tree in which every leaf has the same depth is sometimes called a complete binary tree. See Figure 3.14. Use the principle of mathematical induction to prove that if T is a complete binary tree with n leaves, then the depth of the leaves is log 2 (n).

Para fazer a indução vamos considerar $\log_2(n)=d$, onde d é a profundidade. Então,

$$\log_2(n) = d \implies 2^d = n \tag{1}$$

Considerando o caso base em que d = 0,

$$2^{d} = n$$

$$2^{0} = n$$

$$2^{0} = 1$$

$$(2)$$

Tomamos que d=k e assumimos que $2^k=n$ é verdadeiro. Então, aplicamos o passo de indução, onde d=k+1, e para a próxima profundidade, $n_i=n_{i-1}\cdot 2$. Logo,

$$2^{k+1} = n \cdot 2$$

$$= 2^{k}2^{1}$$

$$= 2^{k+1}$$
(3)

Portanto, $2^d = n$ e, logo $log_2(n) = d$, onde n é o número de folhas e d é a profundidade.

2.5 Questão 3.6

Suppose comm sz = 4 and suppose that x is a vector with n = 14 components.

- a. How would the components of x be distributed among the processes in a program that used a block distribution?
- b. How would the components of x be distributed among the processes in a program that used a cyclic distribution?
- c. How would the components of x be distributed among the processes in a program that used a block-cyclic distribution with blocksize b = 2?

You should try to make your distributions general so that they could be used regardless of what comm sz and n are. You should also try to make your distributions "fair" so that if q and r are any two processes, the difference between the number of components assigned to q and the number of components assigned to r is as small as possible.

Processos	Bloco	Cíclico	Bloco-Cíclico
			(tamanho do bloco = 2)
0	0, 1, 2, 3	0, 4, 8, 12	0 1, 8 9
1	4, 5, 6, 7	1, 5, 9, 13	2 3, 10 11
2	8, 9, 10,	2, 6, 10,	4 5, 12 13
3	11, 12, 13,	3, 7, 11,	6 7

Tabela 1: Distribuição dos elementos do vetor

2.6 Questão 3.7

What do the various MPI collective functions do if the communicator contains a single process?

O processo MPI não terá qualquer outro processo para enviar os dados, logo o processamento deve ser feito nesse único processo. É um principio que permite que os processo MPI sejam executados corretamente independente de número de nós/processos disponíveis.

A forma que isso é implementado é enviar os dados para si mesmo, algo que várias funções coletivas do MPI executam. Em alguns casos, para reduzir o movimento desnecessário de dados na memória, o MPI fornece uma flag chamada MPI_IN_PLACE, que permite que o buffer de recebimento seja o mesmo do de envio, melhorando o desempenho. Essa flag não funciona em todas as funções coletivas.

https://www.mcs.anl.gov/research/projects/mpi/mpi-standard/mpi-report-2.0/node145.htm

2.7 Questão 3.8

Suppose comm_sz = 8 and n = 16.

- a. Draw a diagram that shows how MPI Scatter can be implemented using tree-structured communication with comm_sz processes when process 0 needs to distribute an array containing n elements.
- b. Draw a diagram that shows how MPI Gather can be implemented using tree-structured communication when an n-element array that has been distributed among comm_sz processes needs to be gathered onto process 0.

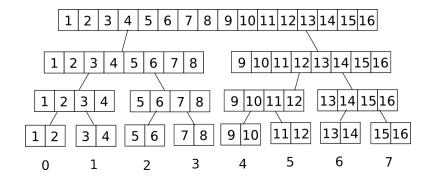


Figura 1: Scatter em comunição baseada em árvore

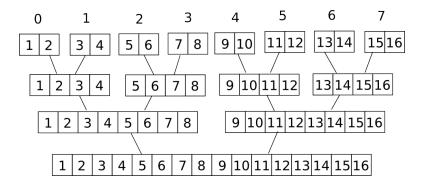


Figura 2: Gather em comunição baseada em árvore

2.8 Questão 3.9

Write an MPI program that implements multiplication of a vector by a scalar and dot product. The user should enter two vectors and a scalar, all of which are read in by process 0 and distributed among the processes. The results are calculated and collected onto process 0, which prints them. You can assume that n, the order of the vectors, is evenly divisible by comm_sz.

```
/*Esse codigo foi modificado de mpi_vector_add.c */
  /* File:
                mpi_vector_add.c
                Implement parallel vector addition using a block
     Purpose:
                distribution of the vectors. This version also
                illustrates the use of MPI_Scatter and MPI_Gather.
     Compile:
                mpicc -g -Wall -o mpi_vector_add mpi_vector_add.c
     Run:
                mpiexec -n <comm_sz> ./vector_add
10
11
     Input:
                The order of the vectors, n, and the vectors x and y
12
     Output:
                The sum vector z = x+y
13
14
     Notes:
15
          The order of the vectors, n, should be evenly divisible
     1.
16
          by comm_sz
17
         DEBUG compile flag.
     2.
          This program does fairly extensive error checking.
19
          an error is detected, a message is printed and the processes
20
                 Errors detected are incorrect values of the vector
21
          order (negative or not evenly divisible by comm_sz), and
22
          malloc failures.
23
24
   * IPP:
            Section 3.4.6 (pp. 109 and ff.)
25
   */
26
27
  #include <stdio.h>
28
  #include < stdlib.h>
  #include <mpi.h>
30
31
  void Check_for_error(int local_ok, char fname[], char message[],
32
        MPI_Comm comm);
33
  void Read_n(int* n_p, int* local_n_p, int my_rank, int comm_sz,
34
        MPI Comm comm);
35
  void Allocate_vectors(double** local_x_pp , double** local_y_pp ,
         double ** local_z_pp , int local_n , MPI_Comm comm);
37
```

```
void Read_vector(double local_a[], int local_n, int n, char vec_name
         int my_rank , MPI_Comm comm);
39
  void Read_scalar(double* scalar_p, int my_rank, int comm_sz, MPI_Comm
      comm);
  void Print_vector(double local_b[], int local_n, int n, char title[],
41
         int my_rank , MPI_Comm comm);
42
  void Parallel_vector_dotproduct(double local_x[], double local_y[],
43
         double local_z[], double* result, int local_n, int n, MPI_Comm
            comm);
  void Parallel_scalar_mutiplication(double scalar, double local_x[],
       double local_z[], int local_n);
46
47
48
      */
  int main(void) {
50
     int n, local_n;
51
      int comm_sz, my_rank;
52
     double *local_x , *local_y , *local_z;
53
     double scalar, result;
54
     MPI_Comm comm;
55
     MPI_Init (NULL, NULL);
57
     comm = MPI COMM WORLD;
58
     MPI_Comm_size(comm, &comm_sz);
59
     MPI_Comm_rank(comm, &my_rank);
61
     Read_n(&n, &local_n, my_rank, comm_sz, comm);
62
63
      Allocate_vectors(&local_x, &local_y, &local_z, local_n, comm);
65
     Read_vector(local_x, local_n, n, "x", my_rank, comm);
66
     Print_vector(local_x, local_n, n, "x is", my_rank, comm);
67
     Read\_vector(local\_y\ ,\ local\_n\ ,\ n\ ,\ "y"\ ,\ my\_rank\ ,\ comm)\ ;
68
     Print_vector(local_y, local_n, n, "y is", my_rank, comm);
70
     Read_scalar(&scalar, my_rank, comm_sz, comm);
71
72
      Parallel_scalar_mutiplication(scalar, local_x, local_x, local_n);
73
      Print_vector(local_x, local_n, n, "now x is", my_rank, comm);
74
      Parallel_vector_dotproduct(local_x, local_y, local_z, &result,
75
         local_n,
                                     n, comm);
76
```

77

```
if (my_rank == 0) {
78
          printf("The result of (scalar*x[]).y[] is %lf \n", result);
      }
80
81
      free (local_x);
82
      free (local y);
83
      free (local_z);
84
85
      MPI_Finalize();
87
      return 0;
      /* main */
89
90
91
    * Function:
                  Check_for_error
92
      Purpose:
                  Check whether any process has found an error.
93
                   print message and terminate all processes. Otherwise,
94
                  continue execution.
                               0 if calling process has found an error, 1
      In args:
                  local ok:
96
                      otherwise
                               name of function calling Check_for_error
                  fname:
98
                  message:
                               message to print if there's an error
                               communicator containing processes calling
                  comm:
100
                               Check_for_error: should be MPI_COMM_WORLD.
101
102
    * Note:
103
         The communicator containing the processes calling
104
       Check for error
          should be MPI_COMM_WORLD.
105
    */
106
   void Check_for_error(
107
                     local ok
                                 /* in */,
          int
108
                     fname []
                                 /* in */,
          char
109
          char
                     message[]
                                 /* in */,
110
         MPI_Comm
                                 /* in */) {
                    comm
111
      int ok;
112
113
      /* Pega o minimo do vetor
114
            Se o minimo for zero, aconteceu algum erro,
115
            caso contrario, todos os processos retornaram 1 e estao ok
116
117
      MPI_Allreduce(&local_ok, &ok, 1, MPI_INT, MPI_MIN, comm);
118
      if (ok == 0) {
119
          int my_rank;
120
         MPI_Comm_rank(comm, &my_rank);
121
```

```
if (my_rank == 0) {
122
             fprintf(stderr, "Proc %d > In %s, %s\n", my_rank, fname,
123
                    message);
124
             fflush (stderr);
125
126
          MPI_Finalize();
127
          exit(-1);
128
129
      /* Check_for_error */
130
131
132
133
    * Function:
                   Read_n
134
                   Get the order of the vectors from stdin on proc 0 and
      Purpose:
135
                   broadcast to other processes.
136
      In args:
                   my_rank:
                                 process rank in communicator
137
                   comm_sz:
                                 number of processes in communicator
138
                   comm:
                                 communicator containing all the processes
139
                                 calling Read_n
140
    * Out args:
                                 global value of n
                   n_p:
                                 local value of n = n/comm_sz
                   local_n_p:
142
143
                   n should be positive and evenly divisible by comm_sz
    * Errors:
144
145
    */
   void Read n(
146
          int*
                                  /* out */,
                     n_p
147
                     local_n_p
                                  /* out */,
          int*
148
          int
                     my_rank
                                  /* in
                                          */,
149
                                  /* in
          int
                     comm_sz
                                          */,
150
          MPI Comm
                     comm
                                  /* in
                                          */) {
151
      int local_ok = 1;
152
      char *fname = "Read_n";
153
154
      if (my_rank == 0) {
155
          printf("What's the order of the vectors?\n");
156
          scanf("%d", n_p);
157
      }
158
      MPI_Bcast(n_p, 1, MPI_INT, 0, comm);
159
      if (*n_p \le 0 \mid | *n_p \% comm_sz != 0) local_ok = 0;
160
      Check_for_error(local_ok, fname,
161
             "n should be > 0 and evenly divisible by comm_sz", comm);
162
      *local_n_p = *n_p/comm_sz;
163
      /* Read_n */
164
165
166
```

```
167
                   Allocate_vectors
    * Function:
168
     Purpose:
                   Allocate storage for x, y, and z
169
                              the size of the local vectors
      In args:
                   local n:
170
                              the communicator containing the calling
                  comm:
171
       processes
                  local_x_pp , local_y_pp , local_z_pp:
                                                            pointers to memory
    * Out args:
172
                      blocks to be allocated for local vectors
173
174
    * Errors:
                  One or more of the calls to malloc fails
175
176
   void Allocate_vectors(
177
          double **
                      local_x_pp
                                  /* out */,
178
          double **
                      local_y_pp
                                   /* out */,
179
          double **
                      local_z_pp
                                   /* out */,
180
                      local n
                                   /* in
          int
                                           */,
181
         MPI_Comm
                                           */) {
                      comm
                                   /* in
182
      int local_ok = 1;
183
      char* fname = "Allocate_vectors";
184
185
      *local_x_pp = malloc(local_n*sizeof(double));
186
      *local_y_pp = malloc(local_n*sizeof(double));
187
      *local_z_pp = malloc(local_n*sizeof(double));
188
189
      if (*local_x_pp == NULL || *local_y_pp == NULL ||
190
           *local_z_pp == NULL) local_ok = 0;
191
      Check_for_error(local_ok, fname, "Can't allocate local vector(s)",
192
             comm);
193
      /* Allocate_vectors */
194
195
196
197
    * Function:
                    Read_vector
198
                    Read a vector from stdin on process 0 and distribute
      Purpose:
199
                    among the processes using a block distribution.
200
                               size of local vectors
      In args:
                    local_n:
201
                               size of global vector
                    n:
202
                    vec_name: name of vector being read (e.g., "x")
203
                               calling process' rank in comm
                    my rank:
204
                               communicator containing calling processes
                   comm:
205
      Out arg:
                    local_a:
                               local vector read
206
207
                    if the malloc on process 0 for temporary storage
    * Errors:
208
                    fails the program terminates
209
210
```

```
* Note:
211
          This function assumes a block distribution and the order
         of the vector evenly divisible by comm_sz.
213
    */
214
   void Read_vector(
215
          double
                     local a[]
                                   /* out */,
216
                     local n
                                   /* in
          int
                                           */,
217
          int
                                      in
                                           */,
218
          char
                     vec_name[]
                                   /* in
                                           */,
219
          int
                     my_rank
                                   /* in
                                           */,
220
          MPI Comm
                     comm
                                   /* in
                                           */) {
221
222
      double* a = NULL;
223
      int i:
224
      int local_ok = 1;
225
      char* fname = "Read_vector";
226
227
      if (my_rank == 0) {
228
          a = malloc(n*sizeof(double));
229
          if (a == NULL) local_ok = 0;
230
          Check_for_error(local_ok, fname, "Can't allocate temporary
231
             vector",
                comm);
232
          printf("Enter the vector %s\n", vec_name);
233
          for (i = 0; i < n; i++)
234
             scanf("%lf", &a[i]); // reads a double (long float)
235
          MPI_Scatter(a, local_n, MPI_DOUBLE, local_a, local_n,
236
             MPI DOUBLE, 0,
             comm);
237
          free(a);
238
      } else {
239
          Check_for_error(local_ok, fname, "Can't allocate temporary
240
             vector",
                comm);
241
          MPI_Scatter(a, local_n, MPI_DOUBLE, local_a, local_n,
242
             MPI_DOUBLE, 0,
             comm);
243
244
      /* Read vector */
   }
245
247
    * Function:
                   Read scalar
248
                   Get the the scalar number from stdin on proc 0 and
    * Purpose:
249
                   broadcast to other processes.
250
                                 process rank in communicator
    * In args:
                   my_rank:
251
```

```
number of processes in communicator
                   comm_sz:
252
                                 communicator containing all the processes
                   comm:
253
                                 calling Read_n
254
                                       global value of n
    * Out args:
                   scalar_p:
255
256
    */
257
   void Read_scalar(
258
          double*
                      scalar_p
                                        /* out */,
259
          int
                     my_rank
                                  /* in
                                          */,
260
          int
                     comm_sz
                                  /* in
                                          */,
261
          MPI Comm
                                  /* in
                     comm
                                          */) {
262
263
       if (my_rank == 0) {
264
          printf("What's the scalar value?\n");
265
          scanf("%lf", scalar_p); // reads double
266
267
      MPI_Bcast(scalar_p, 1, MPI_DOUBLE, 0, comm);
268
      /* Read_scalar */
270
271
272
    * Function:
                   Print_vector
273
      Purpose:
                   Print a vector that has a block distribution to stdout
274
      In args:
                   local_b:
                              local storage for vector to be printed
275
                   local n:
                               order of local vectors
276
                               order of global vector (local_n*comm_sz)
277
                   title:
                               title to precede print out
278
                   comm:
                               communicator containing processes calling
279
                               Print_vector
280
281
                   if process 0 can't allocate temporary storage for
      Error:
282
                   the full vector, the program terminates.
283
284
    * Note:
285
          Assumes order of vector is evenly divisible by the number of
286
          processes
287
    */
288
   void Print_vector(
289
          double
                     local b[]
                                  /* in */,
290
                      local_n
                                  /* in */,
          int
291
          int
                                  /* in */,
292
                      title []
                                  /* in */,
          char
293
          int
                     my_rank
                                  /* in */,
294
                                  /* in */) {
          MPI Comm
                     comm
295
296
```

```
double* b = NULL;
297
      int i;
298
      int local_ok = 1;
299
      char* fname = "Print_vector";
300
301
      if (my_rank == 0) {
302
          b = malloc(n*sizeof(double));
303
          if (b == NULL) local_ok = 0;
304
          Check_for_error(local_ok, fname, "Can't allocate temporary
305
             vector",
                comm);
306
          MPI_Gather(local_b, local_n, MPI_DOUBLE, b, local_n, MPI_DOUBLE
307
                 0, comm);
308
          printf("%s\n", title);
309
          for (i = 0; i < n; i++)
310
             printf("%f ", b[i]);
311
          printf("\n");
312
          free(b);
313
      } else {
          Check_for_error(local_ok, fname, "Can't allocate temporary
315
             vector",
                comm);
316
          MPI_Gather(local_b, local_n, MPI_DOUBLE, b, local_n, MPI_DOUBLE
317
             , 0,
             comm);
318
319
      /* Print_vector */
320
321
322
323
    * Function:
                   Parallel_vector_dotproduct
324
                   Add a vector that's been distributed among the
    * Purpose:
325
        processes
    * In args:
                   local_x:
                              local storage of one of the vectors being
326
       added
                   local_y:
                              local storage for the second vector being
327
       added
                   local n:
                              the number of components in local_x, local_y,
328
                              and local_z
329
    * Out arg:
                   local_z:
                              local storage for the sum of the two vectors
330
331
   void Parallel_vector_dotproduct(
332
                   local x[]
          double
                              /* in
                                       */,
333
          double
                   local_y[]
                               /* in
                                       */,
334
```

```
double
                   local_z[]
                              /* out */,
335
          double* result
                               /* out */,
336
                   local n
                               /* in */,
          int
337
                               /* in
                                       */.
          int
                   n
338
                               /* in */) {
         MPI_Comm comm
339
      int local i;
340
341
     for (local_i = 0; local_i < local_n; local_i++){
342
          local_z[local_i] = local_x[local_i] * local_y[local_i];
343
     }
344
345
     double local_total_z = 0.0;
346
     for (local_i = 0; local_i < local_n; local_i++){
347
          local_total_z += local_z[local_i];
348
     }
349
350
     MPI_Reduce(&local_total_z, result, 1, MPI_DOUBLE, MPI_SUM, 0, comm)
351
352
      /* Parallel_vector_dotproduct */
353
354
355
    * Function:
                   Parallel_scalar_mutiplication
356
                   Add a vector that's been distributed among the
    * Purpose:
357
        processes
                              storage for the scalar value
    * In args:
                   scalar:
358
                   local_x:
                              local storage for the second vector being
359
       added
                              the number of components in local_x, local_y,
                   local_n:
360
                              and local z
361
                   local_z:
                              local storage for the scalar mutiplication of
    * Out arg:
362
                              the vector
363
    */
364
   void Parallel_scalar_mutiplication(
365
          double
                   scalar
                               /* in
                                       */,
366
          double
                   local_x[]
                               /* in
                                       */,
367
                   local_z[]
          double
                               /* out */.
368
                   local_n
          int
                               /* in
                                       */) {
      int local i;
370
371
      for (local_i = 0; local_i < local_n; local_i++)
372
          local_z[local_i] = local_x[local_i] * scalar;
      /* Parallel_scalar_mutiplication */
374
```

2.9 Questão 3.10

In the Read_vector function shown in Program 3.9, we use local_n as the actual argument for two of the formal arguments to MPI_Scatter: send_count and recv_count. Why is it OK to alias these arguments?

É possível alinhar os dois argumentos porque send_count deve ser o número de elementos, de acordo com send_type, que serão enviados para cada processo. E, de forma semelhante, o recv_count deve ser o número de elementos recebidos do procesos raíz, de acordo com recv_type. Portanto, neste caso, ambos os argumentos devem receber o valor de local_n.

2.10 Questão 3.11

Finding **prefix sums** is a generalization of global sum. Rather than simply finding the sum of n values,

$$x_0 + x_1 + \dots + x_{n-1}$$
,

the prefix sums are the n partial sums

$$x_0, x_0 + x_1, x_0 + x_1 + x_2, ..., x_0 + x_1 + ... + x_{n-1}$$
.

- a. Devise a serial algorithm for computing the n prefix sums of an array with n elements.
- b. Parallelize your serial algorithm for a system with n processes, each of which is storing one of the x_i s.
- c. Suppose $n = 2^k$ for some positive integer k. Can you devise a serial algorithm and a parallelization of the serial algorithm so that the parallel algorithm requires only k communication phases?
- d. MPI provides a collective communication function, MPI_Scan, that can be used to compute prefix sums:

```
int MPI Scan(
      void*
                       sendbuf_p
      void*
                       recvbuf_p
                                    /* out */,
      int
                       count
                                    /* in */.
                                    /* in
      MPI_Datatype
                       datatype
      MPI_Op
                                    /* in
                       op
      MPI_Comm
                                    /* in
                                          */):
                       comm
```

It operates on arrays with count elements; both sendbuf_p and recvbuf_p should refer to blocks of count elements of type datatype. The op argument is the same as op for MPI_Reduce. Write an MPI program that generates a random array of count elements on each MPI process, finds the prefix sums, and prints the results.

a.

```
#include <stdio.h>
#include <time.h>
#include <stdlib.h>

int main() {
    int n = 15;
```

```
srand(time(NULL));
7
       int vec[n];
9
       int prefix_sum[n];
10
11
       for (int i = 0; i < n; i++){
12
           vec[i] = rand() \% 10; // number between 0 and 9
13
           printf("%d ", vec[i]);
14
       printf("\n");
16
       for(int i = 0; i < n; i++){
18
           prefix_sum[i] = 0;
19
           for (int j = 0; j \le i; j++) {
20
                prefix_sum[i] += vec[j];
21
           }
22
           printf("%d", prefix_sum[i]);
23
       }
24
  }
25
    b.
  #include <stdio.h>
  #include <time.h>
  #include < stdlib.h>
  #include <mpi.h>
  int main(){
       int comm_sz; /* Number of processes */
       int my_rank; /* My process rank */
       MPI_Init(NULL, NULL);
       MPI_Comm comm = MPI_COMM_WORLD;
10
       MPI_Comm_size(comm, &comm_sz);
11
       MPI_Comm_rank(comm, &my_rank);
12
13
       int vec_i;
       int prefix_sum = 0;
15
       int n = comm_sz;
16
       int vec[n];
17
18
       if (my_rank == 0)
19
           srand(time(NULL));
20
           for (int i = 0; i < n; i++)
21
                vec[i] = rand() \% 10; // number between 0 and 9
22
                printf("%d ", vec[i]);
23
           }
24
```

```
printf("\n");
25
           MPI_Scatter(vec, 1, MPI_INT, &vec_i, 1, MPI_INT, 0, comm);
27
       }
28
       else {
29
           MPI_Scatter(vec, 1, MPI_INT, &vec_i, 1, MPI_INT, 0, comm);
30
       }
31
32
       // envia para todos os processo maiores do que ele mesmo
33
       for(int i = my_rank; i < comm_sz; i++){
34
           MPI_Send(&vec_i, 1, MPI_INT, i, 0, comm);
       }
36
37
       // recebe de todos os processos menores que ele mesmo
38
       prefix_sum += vec_i;
39
       for (int i = 0; i < my_rank; i++){
40
           int aux_vec_i = 0;
41
           MPI_Recv(&aux_vec_i, 1, MPI_INT, i, 0, comm,
42
              MPI_STATUS_IGNORE);
           prefix_sum += aux_vec_i;
       }
44
45
46
       // Imprime o resultado na tela
47
       if (my_rank != 0) {
48
           MPI_Send(&prefix_sum, 1, MPI_INT, 0, 1, comm);
49
       } else {
50
           printf("%d ", vec_i);
51
           for (int q = 1; q < comm_sz; q++) {
52
                int aux;
53
                MPI_Recv(&aux, 1, MPI_INT, q, 1, comm, MPI_STATUS_IGNORE)
54
                printf("%d ", aux);
55
           }
56
           printf("\n");
57
       }
58
59
       MPI Finalize();
61
       return 0;
  }
63
    c. Serial
1 #include < stdio.h>
2 #include <time.h>
```

```
3 #include <stdlib.h>
  #include <math.h>
  int main(){
       int n = 8;
       srand(time(NULL));
       int vec[n];
10
       for(int i = 0; i < n; i++){
12
           vec[i] = 1; //rand() \% 10; // number between 0 and 9
           printf("%d ", vec[i]);
14
15
       printf("\n");
16
17
       for (int k = 0; k < log 2(n); k++){
18
           printf("k is %d n,k);
19
           for (int i = pow(2,k) - 1; i < pow(2,log2(n)); i = i + pow(2,k)
20
                printf("i is %d\n",i);
21
                for (int j = 1; j \le pow(2,k); j++){
22
                    printf("vec[\%d] = vec[\%d] + vec[\%d] \setminus n", i+j, i, i+j);
23
                    vec[i+j] = vec[i] + vec[i+j];
24
                }
25
           }
26
           for (int i = 0; i < n; i++){
27
                printf("%d ", vec[i]);
28
29
           printf("\n");
       }
31
32
       for (int i = 0; i < n; i++) {
33
            printf("%d ", vec[i]);
35
       printf("\n");
36
  }
37
  Paralelo
#include <stdio.h>
2 #include <time.h>
3 #include <stdlib.h>
4 #include <mpi.h>
5 #include <math.h>
void print_vec(int vec[], int n);
```

```
int main(){
       int comm_sz; /* Number of processes */
       int my_rank; /* My process rank */
10
       MPI_Init(NULL, NULL);
11
       MPI_Comm comm = MPI_COMM_WORLD;
12
       MPI Comm size (comm, &comm sz);
13
       MPI_Comm_rank(comm, &my_rank);
14
15
       int vec_i;
16
       int n = comm_sz;
17
       int vec[n];
18
19
       if (my_rank == 0)
20
           srand(time(NULL));
21
           for (int i = 0; i < n; i++){
22
                vec[i] = 1; //rand() \% 10; // number between 0 and 9
23
           }
24
           print_vec(vec,n);
25
           MPI_Scatter(vec, 1, MPI_INT, &vec_i, 1, MPI_INT, 0, comm);
26
       }
27
       else {
28
           MPI_Scatter(vec, 1, MPI_INT, &vec_i, 1, MPI_INT, 0, comm);
29
       }
30
31
       for (int k = 0; k < log 2(n); k++){
32
           for (int i = pow(2,k) - 1; i < pow(2,log2(n)); i = i + pow(2,k)
33
               +1)){
                for (int j = 1; j \le pow(2,k); j++){
34
                    if (my_rank == i){
                         MPI\_Send(\&vec_i, 1, MPI\_INT, i+j, 0, comm);
36
                         printf("This is %d, Sending to %d\n", my_rank, i+
37
                            i);
                    else\ if\ (my\_rank == i + j)
38
                         int aux_vec_i = 0;
39
                         printf("This is %d, Receiving from %d\n", my_rank,
40
                            i);
                         MPI_Recv(&aux_vec_i, 1, MPI_INT, i, 0, comm,
41
                            MPI_STATUS_IGNORE);
                         vec_i += aux_vec_i;
42
                    }
43
                }
44
           }
       }
46
47
       int vec_sum[n];
48
```

```
if (my_rank == 0) {
49
          MPI_Gather(&vec_i, 1, MPI_INT, vec_sum, 1, MPI_INT, 0, comm);
          print_vec(vec_sum,n);
51
       } else {
52
           MPI_Gather(&vec_i, 1, MPI_INT, vec_sum, 1, MPI_INT, 0, comm);
       }
54
55
       MPI_Finalize();
56
       return 0;
  }
58
  void print_vec(int vec[], int n){
60
       for(int i = 0; i < n; i++){
61
           printf("%d ", vec[i]);
62
63
       printf("\n");
64
  }
65
    d.
1 #include < stdio.h>
  #include <stdlib.h>
  #include <time.h>
  #include <mpi.h>
  void print_vec(int vec[], int n);
  int main(void) {
       int comm_sz; /* Number of processes */
       int my_rank; /* My process rank */
10
       MPI_Init(NULL, NULL);
11
      MPI_Comm comm = MPI_COMM_WORLD;
12
       MPI_Comm_size(comm, &comm_sz);
13
       MPI_Comm_rank(comm, &my_rank);
15
       int count = comm_sz;
       int vec[count];
17
       int sum[count];
18
19
20
       srand (my_rank+1);
       for (int i = 0; i < count; i++){
21
           vec[i] = rand() \% 10; // number between 0 and 9
22
           sum[i] = 0;
23
       }
24
25
       MPI_Scan(vec, sum, count, MPI_INT, MPI_SUM, comm);
26
```

```
27
       if (my_rank != 0) {
28
            MPI\_Send(vec, count, MPI\_INT, 0, 0, comm);
29
            MPI_Send(sum, count, MPI_INT, 0, 0, comm);
30
       } else {
31
            printf("rank %d - [", my_rank);
32
            print_vec(vec, count);
33
            printf("] => [");
34
            print_vec(sum, count);
35
            printf("]\n");
36
            for (int q = 1; q < comm_sz; q++) {
37
                 MPI_Recv(vec, count, MPI_INT, q, 0, comm,
38
                    MPI_STATUS_IGNORE);
                 MPI_Recv(sum, count, MPI_INT, q, 0, comm,
39
                    MPI_STATUS_IGNORE);
                 printf("rank %d - [", q);
40
                 print_vec(vec, count);
41
                 printf("] => [");
                 print_vec(sum, count);
43
                 printf("]\n");
            }
45
       }
46
47
       MPI_Finalize();
48
       return 0:
49
50
51
   void print_vec(int vec[], int n){
52
       for(int i = 0; i < n; i++){
53
            printf("%d ", vec[i]);
54
       }
55
  }
56
    Output: [vec] => [sum]
  rank 0 - [3 6 7 5 3] => [3 6 7 5 3]
  rank 1 - [0 9 8 5 1] => [3 15 15 10 4]
  rank 2 - [6 5 8 0 5] => [9 20 23 10 9]
  rank 3 - [1 3 4 6 3 ] => [10 23 27 16 12 ]
  rank 4 - [5 5 0 2 6] => [15 28 27 18 18]
```

2.11 Questão 3.12 *

An alternative to a butterfly-structured allreduce is a ring-pass structure. In a ring-pass, if there are p processes, each process q sends data to process q + 1, except that process p - 1 sends data to process 0. This is repeated until each process has the desired result. Thus, we can implement allreduce with the

following code:

- a. Write an MPI program that implements this algorithm for all reduce. How does its performance compare to the butterfly-structured all reduce?
 - b. Modify the MPI program you wrote in the first part so that it implements prefix sums.

2.12 Questão 3.13

27

MPI_Scatter and MPI_Gather have the limitation that each process must send or receive the same number of data items. When this is not the case, we must use the MPI functions MPI_Gatherv and MPI_Scatterv. Look at the man pages for these functions, and modify your vector sum, dot product program so that it can correctly handle the case when n isn't evenly divisible by comm_sz.

```
/*Esse codigo foi modificado de mpi_vector_add.c */
  /* File:
                mpi_vector_add.c
                Implement parallel vector addition using a block
     Purpose:
                distribution of the vectors. This version also
                illustrates the use of MPI_Scatter and MPI_Gather.
                mpicc -g -Wall -o mpi_vector_add mpi_vector_add.c
   * Compile:
   * Run:
                mpiexec -n <comm_sz> ./vector_add
10
11
   * Input:
                The order of the vectors, n, and the vectors x and y
12
   * Output:
                The sum vector z = x+y
13
14
   * Notes:
         The order of the vectors, n, should be evenly divisible
16
         by comm_sz
17
         DEBUG compile flag.
     2.
18
         This program does fairly extensive error checking.
19
          an error is detected, a message is printed and the processes
20
                 Errors detected are incorrect values of the vector
21
          order (negative or not evenly divisible by comm_sz), and
22
          malloc failures.
23
24
            Section 3.4.6 (pp. 109 and ff.)
   * IPP:
25
   */
26
```

```
#include <stdio.h>
  #include < stdlib.h>
  #include <mpi.h>
31
  void Check_for_error(int local_ok, char fname[], char message[],
32
        MPI Comm comm);
33
  void Read_n(int * n_p, int * local_n_p, int * rest, int my_rank, int
     comm_sz,
        MPI_Comm comm);
  void Allocate_vectors(double** local_x_pp , double** local_y_pp ,
36
         double** local_z_pp , int local_n , MPI_Comm comm);
  void Read_vector(int rest, double local_a[], int local_n, int n, char
38
      vec_name[],
         int my_rank , MPI_Comm comm);
39
  void Read_scalar(double* scalar_p, int my_rank, int comm_sz, MPI_Comm
      comm);
  void Print_vector(double local_b[], int local_n, int n, char title[],
41
         int my_rank , MPI_Comm comm);
42
  void Parallel_vector_dotproduct(double local_x[], double local_y[],
43
         double local_z[], double* result, int local_n, int n, MPI_Comm
            comm);
  void Parallel_scalar_mutiplication(double scalar, double local_x[],
45
       double local_z[], int local_n);
46
47
48
49
      */
  int main(void) {
50
     int n, local_n, rest;
51
      int comm_sz, my_rank;
52
     double *local_x , *local_y , *local_z;
53
     double scalar, result;
54
     MPI_Comm comm;
55
56
     MPI_Init(NULL, NULL);
57
     comm = MPI_COMM_WORLD;
58
     MPI_Comm_size(comm, &comm_sz);
59
     MPI_Comm_rank(comm, &my_rank);
60
61
     Read_n(&n, &local_n, &rest, my_rank, comm_sz, comm);
62
63
      Allocate_vectors(&local_x, &local_y, &local_z, local_n, comm);
65
     Read_vector(rest, local_x, local_n, n, "x", my_rank, comm);
66
      Print_vector(local_x, local_n, n, "x is", my_rank, comm);
67
```

```
printf("Done ok" );
68
      Read_vector(rest, local_y, local_n, n, "y", my_rank, comm);
      Print_vector(local_y, local_n, n, "y is", my_rank, comm);
70
71
      Read_scalar(&scalar, my_rank, comm_sz, comm);
72
73
      Parallel_scalar_mutiplication(scalar, local_x, local_x, local_n);
74
      \label{local_x} Print\_vector(local\_x \;,\; local\_n \;,\; n \,,\; "now \; x \; is" \,,\; my\_rank \,,\; comm) \,;
75
      Parallel_vector_dotproduct(local_x, local_y, local_z, &result,
          local_n,
                                       n, comm);
77
78
      if (my_rank == 0) {
79
          printf("The result of (scalar*x[]).y[] is %lf \n", result);
80
      }
81
82
      free (local_x);
83
      free (local_y);
      free (local_z);
85
      MPI_Finalize();
87
      return 0;
89
      /* main */
90
91
92
    * Function:
                   Check_for_error
93
      Purpose:
                   Check whether any process has found an error.
94
                   print message and terminate all processes. Otherwise,
                   continue execution.
96
                               0 if calling process has found an error, 1
                   local_ok:
      In args:
                      otherwise
98
                   fname:
                               name of function calling Check_for_error
                               message to print if there's an error
                   message:
100
                               communicator containing processes calling
                   comm:
101
                               Check_for_error: should be MPI_COMM_WORLD.
102
103
    * Note:
104
         The communicator containing the processes calling
105
        Check_for_error
          should be MPI_COMM_WORLD.
106
107
   void Check_for_error(
108
                     local ok
                                 /* in */,
109
                     fname []
                                /* in */,
          char
110
```

```
char
                     message[]
                                 /* in */,
111
         MPI Comm
                     comm
                                  /* in */) {
112
      int ok;
113
114
      /* Pega o minimo do vetor
115
            Se o minimo for zero, aconteceu algum erro,
116
            caso contrario, todos os processos retornaram 1 e estao ok
117
118
      MPI_Allreduce(&local_ok, &ok, 1, MPI_INT, MPI_MIN, comm);
119
      if (ok == 0) {
120
          int my_rank;
121
          MPI_Comm_rank(comm, &my_rank);
122
          if (my_rank == 0) {
123
             fprintf(stderr, "Proc %d > In %s, %s\n", my_rank, fname,
124
                    message);
125
             fflush (stderr);
126
127
          MPI_Finalize();
128
          exit(-1);
129
130
      /* Check_for_error */
131
132
133
134
    * Function:
                   Read n
135
                   Get the order of the vectors from stdin on proc 0 and
      Purpose:
136
                   broadcast to other processes.
137
      In args:
                   my_rank:
                                 process rank in communicator
138
                   comm_sz:
                                 number of processes in communicator
139
                                 communicator containing all the processes
                   comm:
140
                                 calling Read_n
141
                                 global value of n
    * Out args:
                   n_p:
142
                   local_n_p:
                                 local value of n = n/comm_sz
143
144
                   n should be positive and evenly divisible by comm_sz
    * Errors:
145
    */
146
   void Read_n(
147
          int*
                                  /* out */,
148
                     n_p
          int*
                     local n p
                                  /* out */.
149
          int*
                     rest
                                  /* out */,
150
          int
                     my_rank
                                  /* in
                                          */,
151
                     comm sz
                                  /* in
          int
                                          */,
152
         MPI_Comm
                     comm
                                  /* in
                                          */) {
153
      int local_ok = 1;
154
      char *fname = "Read_n";
155
```

```
156
      if (my_rank == 0) {
157
          printf("What's the order of the vectors?\n");
158
          scanf("%d", n_p);
159
160
      MPI Bcast(n p, 1, MPI INT, 0, comm);
161
      if (*n_p \le 0) local_ok = 0;
162
      Check_for_error(local_ok, fname,
163
             "n should be > 0.", comm);
      *local_n_p = *n_p/comm_sz + 1;
165
      *rest = *n_p \% comm_sz;
166
      /* Read_n */
167
168
169
170
    * Function:
                  Allocate_vectors
171
    * Purpose:
                  Allocate storage for x, y, and z
172
                  local_n:
                              the size of the local vectors
    * In args:
173
                              the communicator containing the calling
                  comm:
174
       processes
    * Out args:
                  local_x_pp , local_y_pp , local_z_pp: pointers to memory
175
                      blocks to be allocated for local vectors
176
177
                  One or more of the calls to malloc fails
    * Errors:
178
179
   void Allocate_vectors(
180
          double **
                      local_x_pp
                                  /* out */,
181
          double **
                      local_y_pp
                                   /* out */,
182
                      local_z_pp
          double **
                                   /* out */,
183
                      local n
          int
                                   /* in
                                            */.
184
         MPI_Comm
                      comm
                                           */) {
                                   /* in
185
      int local_ok = 1;
186
      char* fname = "Allocate_vectors";
187
188
      *local_x_pp = malloc(local_n*sizeof(double));
189
      *local_y_pp = malloc(local_n*sizeof(double));
190
      *local_z_pp = malloc(local_n*sizeof(double));
191
192
      if (*local_x_pp == NULL || *local_y_pp == NULL ||
193
           *local_z_pp == NULL) local_ok = 0;
      Check_for_error(local_ok, fname, "Can't allocate local vector(s)",
195
             comm);
196
      /* Allocate_vectors */
197
198
199
```

```
200
    * Function:
                    Read vector
201
      Purpose:
                    Read a vector from stdin on process 0 and distribute
202
                    among the processes using a block distribution.
203
                                size of local vectors
      In args:
                    local n:
204
                    n:
                                size of global vector
205
                    vec_name: name of vector being read (e.g., "x")
206
                                calling process' rank in comm
                    my_rank:
207
                    comm:
                                communicator containing calling processes
      Out arg:
                    local a:
                                local vector read
209
210
                    if the malloc on process 0 for temporary storage
      Errors:
211
                    fails the program terminates
212
213
    * Note:
214
          This function assumes a block distribution and the order
215
         of the vector evenly divisible by comm_sz.
216
217
   void Read_vector(
218
          int
                     rest
                                   /* in
                                            */,
219
          double
                     local_a[]
                                       out */.
220
          int
                     local_n
                                   /*
                                      in
                                            */,
221
          int
                                       in
                                            */,
222
                     vec_name[]
223
          char
                                   /*
                                       i n
                                            */,
                     my_rank
                                   /*
                                      in
          int
                                           */,
224
          MPI_Comm
                     comm
                                   /* in
                                           */) {
225
226
      double* a = NULL;
227
      int i;
228
      int local_ok = 1;
229
      char* fname = "Read_vector";
230
231
      int comm_sz;
232
      MPI_Comm_size(MPI_COMM_WORLD, &comm_sz);
233
      int* sendcounts = malloc(sizeof(int)*comm_sz);
234
      int* displs = malloc(sizeof(int)*comm_sz);
235
236
      // Calculating send counts and displacement
237
      int sum = 0:
238
      int rem = rest;
239
        for (int i = 0; i < comm_sz; i++) {
240
            sendcounts[i] = n/comm_sz;
241
            if (rem > 0) {
242
                 sendcounts[i]++;
243
                 rem --;
244
```

```
}
245
246
            displs[i] = sum;
247
            sum += sendcounts[i];
248
       }
249
250
       // print calculated send counts and displacements for each
251
           process
       if (0 == my_rank) {
252
           for (int i = 0; i < comm_sz; i++) {
253
               printf("sendcounts[%d] = %d\tdispls[%d] = %d\n", i,
254
                   sendcounts[i], i, displs[i]);
           }
255
       }
256
257
       a = malloc(n*sizeof(double));
258
       if (a == NULL) local_ok = 0;
259
       Check_for_error(local_ok, fname, "Can't allocate temporary vector
260
              comm);
261
262
       if (my_rank == 0) {
263
          printf("Enter the vector %s\n", vec_name);
264
          for (i = 0; i < n; i++)
265
             scanf("%lf", &a[i]); // reads a double (long float)
266
       }
267
268
       // divide the data among processes as described by sendcounts and
269
            displs
       // MPI_Scatterv(&data, sendcounts, displs, MPI_CHAR, &rec_buf,
270
           100, MPI_CHAR, 0, MPI_COMM_WORLD);
       MPI_Scatterv(a, sendcounts, displs, MPI_DOUBLE, local_a, local_n,
271
            MPI_DOUBLE, 0, comm);
272
       // print what each process received
273
         printf("%d: ", my_rank);
274
         for (int i = 0; i < sendcounts[my_rank]; i++) {
275
             printf("%lf\t", local_a[i]);
276
277
         printf("\n");
278
279
         free(a);
280
         free (sendcounts);
281
         free (displs);
282
      /* Read_vector */
283
```

```
284
285
    * Function:
                   Read_scalar
286
                   Get the the scalar number from stdin on proc 0 and
      Purpose:
287
                   broadcast to other processes.
288
                                 process rank in communicator
                   my rank:
      In args:
289
                   comm sz:
                                 number of processes in communicator
290
                                 communicator containing all the processes
                   comm:
291
                                 calling Read_n
                   scalar_p:
    * Out args:
                                      global value of n
293
294
    */
295
   void Read_scalar(
296
          double*
                                       /* out */,
                     scalar_p
297
          int
                     my_rank
                                  /* in
                                          */,
298
                     comm sz
                                  /* in
                                          */,
          int
299
          MPI_Comm
                                  /* in
                                          */) {
                     comm
300
301
      if (my_rank == 0) {
302
          printf("What's the scalar value?\n");
303
          scanf("%lf", scalar_p); // reads double
304
305
      MPI_Bcast(scalar_p, 1, MPI_DOUBLE, 0, comm);
306
307
      /* Read scalar */
308
309
310
    * Function:
                   Print vector
311
      Purpose:
                   Print a vector that has a block distribution to stdout
312
      In args:
                   local b:
                              local storage for vector to be printed
313
                              order of local vectors
                   local_n:
314
                              order of global vector (local_n*comm_sz)
                   n:
315
                              title to precede print out
                   title:
316
                              communicator containing processes calling
                   comm:
317
                              Print_vector
318
319
                   if process 0 can't allocate temporary storage for
      Error:
320
                   the full vector, the program terminates.
321
322
    * Note:
323
          Assumes order of vector is evenly divisible by the number of
324
          processes
325
    */
326
   void Print vector (
327
          double
                     local_b[]
                                /* in */,
328
```

```
int
                      local n
                                   /* in */,
329
          int
                                   /* in */,
330
                      title []
                                   /* in */,
          char
331
                                   /* in */,
                      my_rank
          int
332
          MPI_Comm
                                   /* in */) {
                      comm
333
334
        double* b = NULL;
335
        int i;
336
        int local_ok = 1;
337
        char* fname = "Print_vector";
338
339
        int comm_sz;
340
        MPI_Comm_size(MPI_COMM_WORLD, &comm_sz);
341
        int* recvcounts = malloc(sizeof(int)*comm_sz);
342
        int* displs = malloc(sizeof(int)*comm_sz);
343
344
        // Calculating send counts and displacement
345
        int sum = 0;
346
        int rem = n%comm_sz;
347
        for (int i = 0; i < comm_sz; i++) {
348
             recvcounts[i] = n/comm_sz;
349
             if (rem > 0) {
350
                 recvcounts[i]++;
351
                 rem --;
352
            }
353
354
             displs[i] = sum;
355
            sum += recvcounts[i];
356
        }
357
358
        if (0 == my_rank) {
359
           for (int i = 0; i < comm_sz; i++) {
360
                printf("recvcounts[%d] = %d \land tdispls[%d] = %d \land n", i,
361
                    recvcounts[i], i, displs[i]);
362
        }
364
365
        b = malloc(n*sizeof(double));
366
        if (b == NULL) local_ok = 0;
367
        Check_for_error(local_ok, fname, "Can't allocate temporary vector
368
              comm);
369
370
       if (my_rank == 0) {
371
```

```
MPI_Gatherv(local_b, recvcounts[my_rank], MPI_DOUBLE, b,
372
             recvcounts, displs,
               MPI_DOUBLE, 0, comm);
373
          printf("%s\n", title);
374
          for (i = 0; i < n; i++)
375
             printf("%f ", b[i]);
376
          printf("\n");
377
378
      } else {
379
          MPI_Gatherv(local_b, recvcounts[my_rank], MPI_DOUBLE, b,
380
             recvcounts, displs,
                   MPI_DOUBLE, 0, comm);
381
      }
382
383
      free(b);
384
      /* Print_vector */
385
386
387
388
                   Parallel_vector_dotproduct
    * Function:
389
                   Add a vector that's been distributed among the
    * Purpose:
390
        processes
                              local storage of one of the vectors being
    * In args:
                   local_x:
391
       added
                   local y:
                              local storage for the second vector being
392
       added
                   local_n:
                              the number of components in local_x, local_y,
393
                              and local z
394
                              local storage for the sum of the two vectors
    * Out arg:
                   local_z:
395
    */
396
   void Parallel_vector_dotproduct(
          double
                   local_x[]
                              /* in
                                        */,
398
          double
                   local_y[]
                               /* in
                                        */,
399
                   local_z[]
          double
                               /* out */,
400
          double* result
                               /* out */,
401
          int
                   local_n
                               /* in
                                       */,
402
          int
                               /* in */.
                   n
403
         MPI_Comm comm
                               /* in */) {
404
      int local i;
405
406
     for (local_i = 0; local_i < local_n; local_i++){
407
          local_z[local_i] = local_x[local_i] * local_y[local_i];
408
     }
409
410
     double local_total_z = 0.0;
411
```

```
for (local_i = 0; local_i < local_n; local_i++){
412
          local_total_z += local_z[local_i];
     }
414
415
     int my_rank;
416
     MPI Comm rank(comm, &my rank);
417
     printf("rank: %d > %lf\n", my_rank, local_total_z);
418
419
     MPI_Reduce(&local_total_z, result, 1, MPI_DOUBLE, MPI_SUM, 0, comm)
420
421
      /* Parallel_vector_dotproduct */
422
423
424
    * Function:
                   Parallel_scalar_mutiplication
425
    * Purpose:
                  Add a vector that's been distributed among the
426
        processes
                              storage for the scalar value
      In args:
                   scalar:
427
                              local storage for the second vector being
                   local x:
428
       added
                   local n:
                              the number of components in local_x, local_y,
429
                              and local_z
430
                              local storage for the scalar mutiplication of
    * Out arg:
                   local_z:
431
                              the vector
432
433
   void Parallel_scalar_mutiplication(
434
          double
                  scalar
                               /* in
                                       */,
435
          double
                  local x[]
                              /* in
                                       */,
436
                  local_z[]
          double
                               /* out */,
437
                   local n
                               /* in
                                       */) {
          int
438
      int local_i;
439
440
      for (local_i = 0; local_i < local_n; local_i++)
441
          local_z[local_i] = local_x[local_i] * scalar;
442
      /* Parallel_scalar_mutiplication */
443
```

2.13 Questão 3.14

a. Write a serial C program that defines a two-dimensional array in the main function. Just use numeric constants for the dimensions: int two d[3][4];

Initialize the array in the main function. After the array is initialized, call a function that attempts to print the array. The prototype for the function should look something like this.

```
void Print two d(int two d[][], int rows, int cols);
```

After writing the function try to compile the program. Can you explain why it won't compile?

b. After consulting a C reference (e.g., Kernighan and Ritchie [29]), modify the program so that it will

compile and run, but so that it still uses a two-dimensional C array.

O código abaixo não compila pois o compilador precisa saber as dimensões para fazer a aritmética de ponteiros corretamente. Isto é, se o compilador não tiver as dimensões do array quando ele é passado para uma função (e passado como ponteiro), a expressão array[x][y] não pode ser calculada, pois não há como sabe onde uma linha ou coluna começa ou termina.

```
#include <stdio.h>
  #include <stdlib.h>
  void Print_two_d(int two_d[][], int rows, int cols);
  int main(){
       int two_d[3][4] = \{\{1,1,1,1,1\},
                            \{2,2,2,2\}
                            {3,3,3,3};
      Print_two_d (two_d, 3, 4);
11
      return 0;
12
  }
13
14
  void Print_two_d(int two_d[][], int rows, int cols){
15
       int i, j;
16
       for(i = 0; i < rows; i++){
17
           for(j = 0; j < cols; j++){}
18
                printf("%d\n", two_d[i][j]);
           }
20
  }
22
  #include <stdio.h>
  #include < stdlib.h>
  void Print_two_d(int two_d[][4], int rows, int cols);
  int main(){
       int two_d[3][4] = \{\{1,1,1,1,1\},
                            \{2,2,2,2\},
                            {3,3,3,3};
10
      Print_two_d (two_d, 3, 4);
11
      return 0;
12
  }
13
14
  void Print_two_d(int two_d[][4], int rows, int cols){
       int i, j;
16
```

```
for(i = 0; i < rows; i++){
    for(j = 0; j < cols; j++){
        printf("%d\n", two_d[i][j]);
}
</pre>
```

2.14 Questão 3.16

Suppose comm_s z = 8 and the vector x = (0, 1, 2, ..., 15) has been distributed among the processes using a block distribution. Draw a diagram illustrating the steps in a butterfly implementation of allgather of x.

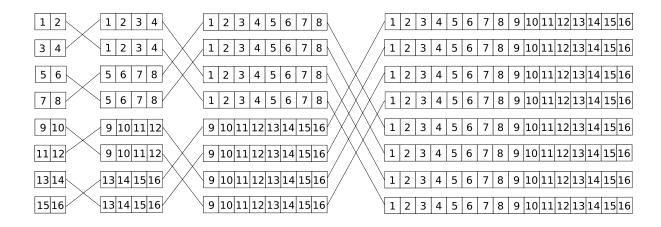


Figura 3: Allgather em comunicação butterfly

2.15 Questão 3.17

MPI_Type_contiguous can be used to build a derived datatype from a collection of contiguous elements in an array. Its syntax is

```
int MPI_Type_contiguous(
int count /* in */,
MPI_Datatype old_mpi_t /* in */,
MPI_Datatype* new_mpi_t_p /* out */);
```

Modify the Read_vector and Print_vector functions so that they use an MPI datatype created by a call to MPI_Type_contiguous and a count argument of 1 in the calls to MPI_Scatter and MPI_Gather.

```
void Read_vector(
         double
                     local_a[]
                                   /* out */,
                     local n
                                      in
         int
                                            */,
                                       in
         int
                     n
                                            */,
4
                     vec_name[]
         char
                                       in
                                            */,
         int
                     my_rank
                                   /* in
                                            */,
```

```
*/) {
         MPI Comm comm
                                 /* in
7
      double* a = NULL;
9
      int i;
10
      int local_ok = 1;
11
      char* fname = "Read vector";
12
13
      MPI_Datatype CONTIGUOUS;
14
      MPI_Type_contiguous(local_n, MPI_DOUBLE, &CONTIGUOUS);
15
      MPI_Type_commit(&CONTIGUOUS);
16
      if (my_rank == 0) {
18
         a = malloc(n*sizeof(double));
19
         if (a == NULL) local_ok = 0;
20
         Check_for_error(local_ok, fname, "Can't allocate temporary
21
            vector",
               comm);
22
         printf("Enter the vector %s\n", vec_name);
23
         for (i = 0; i < n; i++)
24
            scanf("%lf", &a[i]); // reads a double (long float)
25
         MPI_Scatter(a, 1, CONTIGUOUS, local_a, 1, CONTIGUOUS, 0, comm);
26
         free(a);
27
      } else {
28
         Check_for_error(local_ok, fname, "Can't allocate temporary
29
            vector",
               comm);
30
         MPI_Scatter(a, 1, CONTIGUOUS, local_a, 1, CONTIGUOUS, 0, comm);
31
      }
32
      /* Read_vector */
33
  void Print_vector(
         double
                    local_b[]
                                /* in */,
                    local_n
                                /* in */,
         int
         int
                                /* in */,
                    title []
                                /* in */,
         char
                    my_rank
                                /* in */,
         int
                                /* in */) {
         MPI_Comm
                    comm
      double* b = NULL;
      int i;
10
      int local_ok = 1;
11
      char* fname = "Print_vector";
12
13
      MPI_Datatype CONTIGUOUS;
14
      MPI\_Type\_contiguous (\ local\_n \ , \ MPI\_DOUBLE, \ \&CONTIGUOUS) \ ;
15
```

```
MPI_Type_commit(&CONTIGUOUS);
16
17
      if (my_rank == 0) {
18
         b = malloc(n*sizeof(double));
19
         if (b == NULL) local_ok = 0;
20
         Check_for_error(local_ok, fname, "Can't allocate temporary
21
            vector",
               comm);
22
         MPI_Gather(local_b, 1, CONTIGUOUS, b, 1, CONTIGUOUS, 0, comm);
23
         printf("%s\n", title);
24
         for (i = 0; i < n; i++)
            printf("%f ", b[i]);
26
         printf("\n");
27
         free(b);
28
      } else {
29
         Check_for_error(local_ok, fname, "Can't allocate temporary
30
            vector",
               comm);
         MPI_Gather(local_b, 1, CONTIGUOUS, b, 1, CONTIGUOUS, 0, comm);
32
      }
      /* Print vector */
```

2.16 Questão 3.19

MPI_Type_indexed can be used to build a derived datatype from arbitrary array elements. Its syntax is

```
int MPI_Type_indexed(
      int
                     count
                                                   /* in */,
      int
                     array_of_blocklengths[]
                                                   /* in */,
3
                     array_of_displacements[]
                                                   /* in */,
      int
                                                   /* in */,
      MPI_Datatype
                     old_mpi_t
      MPI_Datatype* new_mpi_t_p
                                                   /* out */);
```

Unlike MPI_Type_create_struct, the displacements are measured in units of old_mpi_t - not bytes. Use MPI_Type_indexed to create a derived datatype that corresponds to the upper triangular part of a square matrix. For example, in the 4×4 matrix

$$\left(\begin{array}{ccccc}
0 & 1 & 2 & 3 \\
4 & 5 & 6 & 7 \\
8 & 9 & 10 & 11 \\
12 & 13 & 14 & 15
\end{array}\right)$$

the upper triangular part is the elements 0, 1, 2, 3, 5, 6, 7, 10, 11, 15. Process 0 should read in an n x n matrix as a one-dimensional array, create the derived datatype, and send the upper triangular part with a single call to MPI_Send. Process 1 should receive the upper triangular part with a single call to MPI_Recv and then print the data it received.

```
#include <stdio.h>
2 #include < stdlib.h>
  #include <mpi.h>
  int main(int argc, char *argv[])
6
       int rank, size, i;
       MPI_Datatype type;
       int n = 4;
10
       int blocklen[n], displacement[n];
       for (int i = n, j = 0;
12
            i > 0 \&\& i < n; i--, i++)
13
            \{ blocklen[j] = i; \}
14
15
       for (int i = 0, j = 0;
16
            i < n, j < n; i+=5, j++
17
            { displacement[j] = i;}
19
       int buffer[n*n];
20
       MPI_Init(&argc , &argv);
21
       MPI_Comm_rank(MPI_COMM_WORLD, &rank);
22
       MPI_Comm_size(MPI_COMM_WORLD, &size);
23
24
       if (size < 2)
25
26
           printf("Please run with 2 processes.\n");
27
           MPI_Finalize();
28
           return 1;
       }
30
31
       MPI_Type_indexed(n, blocklen, displacement, MPI_INT, &type);
32
       MPI_Type_commit(&type);
33
34
       if (rank == 0)
35
       {
           printf("Enter the matrix: ");
37
           fflush (stdout);
           for (int i = 0; i < n*n; i++){
39
                scanf("%d", &buffer[i]);
           }
41
           MPI_Send(buffer, 1, type, 1, 123, MPI_COMM_WORLD);
43
       }
44
45
```

```
if (rank == 1)
46
47
            for (i=0; i < n * n; i++)
48
                 buffer[i] = -1;
49
            MPI_Recv(buffer, 1, type, 0, 123, MPI_COMM_WORLD,
50
               MPI STATUS IGNORE);
            for (i=0; i < n * n; i++)
51
                 printf("buffer[%d] = %d \ n", i, buffer[i]);
52
            fflush (stdout);
       }
54
       MPI_Finalize();
56
       return 0;
57
  }
58
```

2.17 Questão 3.20

The functions MPI_Pack and MPI_Unpack provide an alternative to derived datatypes for grouping data. MPI_Pack copies the data to be sent, one block at a time, into a user-provided buffer. The buffer can then be sent and received. After the data is received, MPI_Unpack can be used to unpack it from the receive buffer. The syntax of MPI_Pack is

```
int MPI_Pack(
                void*
                                in_buf
                                                /* in
                                                            */,
                int
                                in buf count
                                                   in
3
                MPI_Datatype
                                datatype
                                                            */,
                                                /* in
                void*
                               pack_buf
                                                /* out
                                                            */,
                                pack_buf_sz
                int
                                                /* in
                                                            */,
                int*
                                position_p
                                                /* in/out */,
                MPI Comm
                                                            */);
                                comm
                                                /* in
```

We could therefore pack the input data to the trapezoidal rule program with the following code:

```
char pack_buf[100];
int position = 0;

MPI_Pack(&a, 1, MPI_DOUBLE, pack_buf, 100, &position, comm);
MPI_Pack(&b, 1, MPI_DOUBLE, pack_buf, 100, &position, comm);
MPI_Pack(&n, 1, MPI_INT, pack_buf, 100, &position, comm);
```

The key is the position argument. When $\texttt{MPI_Pack}$ is called, position should refer to the first available slot in pack buf . When $\texttt{MPI_Pack}$ returns, it refers to the first available slot after the data that was just packed, so after process 0 executes this code, all the processes can call $\texttt{MPI_Bcast}$:

```
MPI_Bcast(pack_buf, 100, MPI_PACKED, 0, comm);
```

Note that the MPI datatype for a packed buffer is MPI_PACKED. Now the other processes can unpack the data using: MPI_Unpack:

```
int MPI_Unpack(
              void*
                              pack_buf
                                               /* in
                                                           */,
2
              int
                              pack_buf_sz
                                                  in
                                                           */,
3
                              position_p
                                                          */,
              int*
                                               /*
                                                  in/out
                              out_buf
              void*
                                               /*
                                                  out
                                                           */,
                              out_buf_count /*
              int
                                                  in
                                                           */,
              MPI_Datatype
                              datatype
                                               /* in
                                                           */,
              MPI_Comm
                              comm
                                               /*
                                                  in
                                                           */);
```

This can be used by "reversing" the steps in MPI_Pack , that is, the data is unpacked one block at a time starting with position = 0. Write another Get input function for the trapezoidal rule program. This one should use MPI_Pack on process 0 and MPI_Unpack on the other processes.

```
void Get_input(int my_rank, int comm_sz, double* a_p, double* b_p,
         int * n_p)  {
2
      //int dest;
     MPI_Comm comm = MPI_COMM_WORLD;
     char pack_buf[100];
     int position = 0;
     if (my rank == 0) {
         printf("Enter a, b, and n\n");
10
         scanf("%lf %lf %d", a_p, b_p, n_p);
11
12
         printf("rank %d: %d\n", my_rank, *n_p);
13
         printf("rank %d: %lf\n", my_rank, *b_p);
         printf("rank %d: %lf\n", my_rank, *a_p);
15
16
         MPI_Pack(a_p, 1, MPI_DOUBLE, pack_buf, 100, &position, comm);
17
         MPI_Pack(b_p, 1, MPI_DOUBLE, pack_buf, 100, &position, comm);
18
         MPI_Pack(n_p, 1, MPI_INT, pack_buf, 100, &position, comm);
19
20
         MPI_Bcast(pack_buf, 100, MPI_PACKED, 0, comm);
21
     }
22
     else { /* my rank != 0 */
23
         MPI_Bcast(pack_buf, 100, MPI_PACKED, 0, comm);
24
25
         MPI_Unpack(pack_buf, 100, &position, a_p, 1, MPI_DOUBLE, comm);
26
         MPI_Unpack(pack_buf, 100, &position, b_p, 1, MPI_DOUBLE, comm);
27
        MPI_Unpack(pack_buf, 100, &position, n_p, 1, MPI_INT, comm);
28
29
     /* Get_input */
```

2.18 Questão 3.21

How does your system compare to ours? What run-times does your system get for matrix-vector multiplication? What kind of variability do you see in the times for a given value of $comm_sz$ and n? Do the results tend to cluster around the minimum, the mean, or the median?

	Ordem da Matriz									
comm_sz	1024	2048	4096	8192	16384					
1	3.7561	12.8853	52.0139	210.4686	846.9655					
2	2.0700	10.2071	41.1858	107.3081	438.0811					
4	1.7275	6.8219	25.0998	64.2229	245.5204					
8	1.7007	4.1896	14.3932	56.5015	219.8544					
16	2.1960	6.0016	20.8711	76.8699	236.1451					

A medida que o comm_sz aumenta, é possível ver que o tempo de execução diminui. Contudo, a execução nem sempre tem um comportamento constante. Isso pode ser observado na Figura 4.

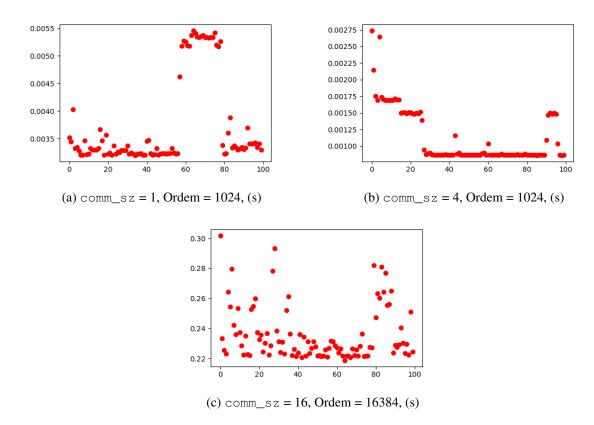


Figura 4: Comportamento dos tempos de execução

2.19 Questão 3.22

Time our implementation of the trapezoidal rule that uses MPI Reduce. How will you choose n, the number of trapezoids? How do the minimum times compare to the mean and median times? What are the speedups? What are the efficiencies? On the basis of the data you collected, would you say that the trapezoidal rule is scalable?