# Automated Verification of Cyber-Physical Systems A.A. 2024/2025

Basic Notions

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#### General Info for This Class

- Automated Verification of Cyber-Physical Systems is an elective course for the Master Degree in Computer Science
- Lecturer: Igor Melatti
- Where to find these slides and more:
  - https://igormelatti.github.io/aut\_ver\_cps/ 20242025/index\_eng.html
  - also on MS Teams: "DT0759: Automated Verification of Cyber-Physical Systems (2024/25)", code ramh3r4
- 2 classes every week, 2 hours per class





#### Rules for Exams

- The exam consists in either reviewing a research paper or working on a project
- Each student may choose one between the two options
- Project: perform verification of a given cyber-physical system
  - also in small teams (max 3 students)
  - each team may choose one among the ones selected by lecturer
  - or may propose one (but wait for lecturer approval!)
  - each team will have to discuss its project with slides
- Paper: read a conference or journal paper and present it with slides
  - each student may choose one among the ones selected by lecturer
  - or may propose one (but wait for lecturer approval!)



# Model Checking Problem

- ullet Input: a system  ${\cal S}$  and (at least) a property arphi
  - ullet more precisely, a *model* of  ${\mathcal S}$  must be provided
  - ullet that is,  ${\cal S}$  must be described in some suitable language
- Output:

PASS 
$$S$$
 satisfies  $\varphi$ , i.e.,  $S \models \varphi$ 

- ullet the system  ${\cal S}$  is correct w.r.t. the property arphi
- mathematical certification, much better than, e.g., testing

FAIL 
$$S$$
 does not satisfy  $\varphi$ , i.e.,  $S \not\models \varphi$ 

- ${\color{blue} \bullet}$  the system  ${\mathcal S}$  is buggy w.r.t. the property  $\varphi$
- a counterexample providing evidence of the error is also returned



# Model Checking vs. Other Verification Techniques

- Model checking is fully automatic
  - $\bullet$  a model checker only needs the description of  ${\mathcal S}$  and the property  $\varphi$
  - "press button and go"
  - this is not true for other verification tools such as proof checkers, which require human intervention in the process
- Model checking is correct for both PASS and FAIL
  - ullet unless the description of  ${\mathcal S}$ , or the property  ${arphi}$ , are wrong
  - this is not true for other verification techniques such as testing,
     which only guarantees the FAIL result
  - a buggy system may pass all tests, because the error is in some corner case





# Model Checking Shortcomings

- Only works for finite-state systems
  - typical example: you may verify a system with 3, 4 or 5 processes, but not with *n* processes, for a generic *n*
- Requires skilled personnel to write descriptions (and properties)
  - must know both the model checker language and the system
  - however, less skilled than a proof checker user
  - very few exceptions in which the model is automatically extracted from the system
  - also direct translations from digital circuits to NuSMV are available
- Very resource demanding
  - besides PASS and FAIL, also OutOfMem and OutOfTime are expected results...
  - bounded model checking: PASS is limited to execution up to a given number of steps



# Model Checking Algorithms

#### Two main categories:

Explicit visit the graph induced by the description of  ${\cal S}$ 

- very good for invariants and LTL model checking of communication protocols
- ullet on-the-fly generation of the graph: only the reachable states are stored, the adjacency matrix is implicitly given by the description of  ${\cal S}$
- Murphi, SPIN

Symbolic represent sets of states and transition relations as OBDDs

- very good for LTL and CTL model checking of hardware-like systems
- all translated into a boolean formula
- also SAT tools may be used (bounded mode)

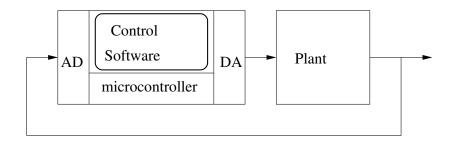
# Cyber-Physical Systems

- A Cyber-Physical System (CPS) is a system where a physical system is controlled and/or monitored by a software
- They are either partially or fully autonomous
  - we will mainly deal with fully autonomous CPSs
- Examples are everywhere:
  - Internet of Things devices
  - Unmanned Autonomous Vehicles
  - Drones
  - Medical Devices
  - Embedded Systems
  - ..





## Cyber-Physical Systems with Controllers

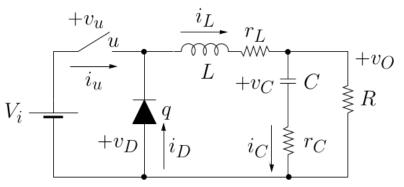




Buck DC/DC Converter



#### Buck DC/DC Converter







#### Continuous time dynamics

$$i_L = a_{1,1}i_L + a_{1,2}v_O + a_{1,3}v_D$$
 (1)

$$\dot{v_O} = a_{2,1}i_L + a_{2,2}v_O + a_{2,3}v_D$$
 (2)

$$q \rightarrow v_D = R_{\rm on} i_D$$
 (3)  $\bar{q} \rightarrow v_D = R_{\rm off} i_D$  (7)  
 $q \rightarrow i_D \ge 0$  (4)  $\bar{q} \rightarrow v_D \le 0$  (8)

$$u \rightarrow v_u = R_{\text{on}}i_u \quad (5) \qquad \qquad \bar{u} \rightarrow v_u = R_{\text{off}}i_u \quad (9)$$

$$v_D = v_U - V_{in}$$
 (6)  $i_D = i_L - i_u$  (10)

where:

- $i_L, v_O$  are state variables
- $u \in \{0, 1\}$  is the action







Discrete time dynamics with sampling time T

$$i_{L}' = (1 + Ta_{1,1})i_{L} + Ta_{1,2}v_{O} + Ta_{1,3}v_{D}$$
 (11)

$$v_{O}' = Ta_{2,1}i_{L} + (1 + Ta_{2,2})v_{O} + Ta_{2,3}v_{D}.$$
 (12)

$$q \rightarrow v_D = R_{\rm on} i_D(13)$$
  $\bar{q} \rightarrow v_D = R_{\rm off} i_D$  (17)

$$q \rightarrow i_D \geq 0$$
 (14)  $\bar{q} \rightarrow v_D \leq 0$  (18)

$$u \rightarrow v_u = R_{\rm on} i_u$$
 (15)  $\bar{u} \rightarrow v_u = R_{\rm off} i_u$  (19)

$$v_D = v_u - V_{in}$$
 (16)  $i_D = i_L - i_u$  (20)







- $\bullet$  Goal: keep  $v_O$  in a desired safe interval
  - typically,  $5 0.01V \le v_O \ge 5 + 0.01V$
- Notwithstanding the input voltage  $V_i$  and the resistance R may vary in some given interval
  - typically,  $R = 5 \pm 25\%\Omega$ ,  $V_i = 15 \pm 25\%V$
- Effectively used in laptops: from battery voltage  $(V_i)$  to laptop processor voltage  $(v_O)$





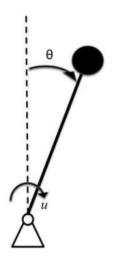
#### Inverted Pendulum







#### Inverted Pendulum







#### Continuous time dynamics

$$\ddot{\theta} = \frac{g}{I}\sin\theta + \frac{1}{mI^2}Fu$$

#### where:

- $\bullet$   $\theta$  is the state variable
- $u \in \{0,1\}$  is the action
- m, l, F are system parameters



#### Continuous time dynamics

$$\dot{x}_1 = x_2 \tag{21}$$

$$\dot{x}_2 = \frac{g}{l} \sin x_1 + \frac{1}{ml^2} Fu$$
 (22)

Discrete time dynamics with sampling time T

$$x_1' = x_1 + Tx_2 (23)$$

$$x'_{1} = x_{1} + Tx_{2}$$

$$x'_{2} = x_{2} + T\frac{g}{I}\sin x_{1} + T\frac{1}{mI^{2}}Fu$$





(24)



#### In This Course

#### To deal with cyber-physical systems:

- Probabilistic Model Checking
  - rather than "are there errors?", it is "is the error probability low enough?"
  - which entails "what is the error probability?"
  - the system is probabilistic, i.e., a Markov Chain
- Statistical Model Checking
  - rather than "are there errors?", it is "is the error probability low enough?"
  - which entails "what is the error probability?"
  - the system may be a non-probabilistic simulator
  - the answer is given with some statistical confidence
  - bridge between testing and verification





#### In This Course

#### To deal with cyber-physical systems:

- System Level Formal Verification
  - directly use a simulator instead of describing the system within the model checker
  - this will also need some background on systems simulation
  - bridge between testing and verification
- Automatic Synthesis of Controllers
  - rather than "are there errors in this system?", it is "generate a controller so that errors are avoided"



