Inference for numerical data

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North Carolina births

In 2004, the state of North Carolina released a large data set containing information on births recorded in this state. This data set is useful to researchers studying the relation between habits and practices of expectant mothers and the birth of their children. We will work with a random sample of observations from this data set.

Exploratory analysis

Load the nc data set into our workspace.

load("more/nc.RData")

We have observations on 13 different variables, some categorical and some numerical. The meaning of each variable is as follows.

variable	description	
fage	father's age in	
	years.	
mage	mother's age in	
	years.	
mature	maturity status	
	of mother.	
weeks	length of	
	pregnancy in	
	weeks.	
premie	whether the	
	birth was	
	classified as	
	premature	
	(premie) or	
	$\operatorname{full-term}$.	
visits	number of	
	hospital visits	
	during	
	pregnancy.	
marital	whether mother	
	${ m is}$ married ${ m or}$	
	$\verb"not married" at$	
	birth.	
gained	weight gained by	
	mother during	
	pregnancy in	
	pounds.	

variable	description		
weight	weight of the		
	baby at birth in		
	pounds.		
lowbirthweight	whether baby		
	was classified as		
	low birthweight		
	(low) or not		
	(not low).		
gender	gender of the		
	baby, female or		
	male.		
habit	status of the		
	mother as a		
	nonsmoker or a		
	smoker.		
whitemom	whether mom is		
	white or not		
	white.		

1. What are the cases in this data set?

The cases in this data sets are the births.

How many cases are there in our sample?

There are 1,000 cases in this data set.

dim(nc)

[1] 1000 13

As a first step in the analysis, we should consider summaries of the data. This can be done using the summary command:

summary(nc)

##	fage	mage	mature	weeks
##	Min. :14.00	Min. :13	mature mom :133	Min. :20.00
##	1st Qu.:25.00	1st Qu.:22	younger mom:867	1st Qu.:37.00
##	Median:30.00	Median :27		Median :39.00
##	Mean :30.26	Mean :27		Mean :38.33
##	3rd Qu.:35.00	3rd Qu.:32		3rd Qu.:40.00
##	Max. :55.00	Max. :50		Max. :45.00
##	NA's :171			NA's :2
##	premie	visits	marital	gained
##	full term:846	Min. : 0.0	married :386	Min. : 0.00
##	premie :152	1st Qu.:10.0	not married:613	1st Qu.:20.00
##	NA's : 2	Median :12.0	NA's : 1	Median :30.00
##		Mean :12.1		Mean :30.33

```
##
                     3rd Qu.:15.0
                                                          3rd Qu.:38.00
##
                             :30.0
                                                                  :85.00
                     Max.
                                                          Max.
##
                     NA's
                             :9
                                                          NA's
                                                                  :27
##
        weight
                       lowbirthweight
                                          gender
                                                            habit
##
    Min.
           : 1.000
                       low
                               :111
                                       female:503
                                                     nonsmoker:873
    1st Qu.: 6.380
                       not low:889
                                       male :497
                                                               :126
##
                                                     smoker
    Median: 7.310
                                                     NA's
##
                                                               : 1
            : 7.101
##
    Mean
##
    3rd Qu.: 8.060
##
    Max.
           :11.750
##
##
         whitemom
##
    not white: 284
##
    white
              :714
##
    NA's
              : 2
##
##
##
##
```

As you review the variable summaries, consider which variables are categorical and which are numerical. For numerical variables, are there outliers? If you aren't sure or want to take a closer look at the data, make a graph.

Categrical: mature, premie, marital, lowbirthweight, gender, habit and whitemom.

Numerical: fage, mage, weeks, visits, gained and weight.

head(nc)

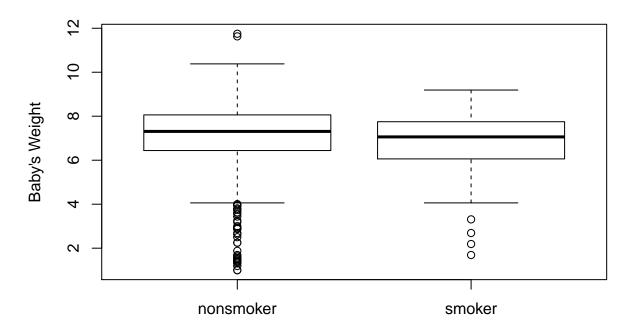
```
##
     fage mage
                     mature weeks
                                      premie visits marital gained weight
## 1
       NA
            13 younger mom
                               39 full term
                                                 10 married
                                                                 38
                                                                      7.63
## 2
                                                                 20
                                                                      7.88
       NA
            14 younger mom
                               42 full term
                                                 15 married
## 3
       19
            15 younger mom
                               37 full term
                                                 11 married
                                                                 38
                                                                      6.63
## 4
       21
            15 younger mom
                               41 full term
                                                  6 married
                                                                 34
                                                                      8.00
## 5
       NA
            15 younger mom
                                                                 27
                                                                      6.38
                               39 full term
                                                  9 married
## 6
       NA
            15 younger mom
                               38 full term
                                                 19 married
                                                                 22
                                                                      5.38
##
     lowbirthweight gender
                                habit
                                       whitemom
## 1
            not low
                       male nonsmoker not white
## 2
            not low
                       male nonsmoker not white
## 3
            not low female nonsmoker
                                           white
## 4
            not low
                       male nonsmoker
                                           white
## 5
            not low female nonsmoker not white
## 6
                 low
                       male nonsmoker not white
```

Consider the possible relationship between a mother's smoking habit and the weight of her baby. Plotting the data is a useful first step because it helps us quickly visualize trends, identify strong associations, and develop research questions.

2. Make a side-by-side boxplot of habit and weight. What does the plot highlight about the relationship between these two variables?

```
# Boxplot of habit and weight
boxplot(weight~habit,data=nc, main="Relation Between Mother's Habit and Baby's Weight",
    ylab="Baby's Weight", xlab="Mother Smoker/Non-Smoker")
```

Relation Between Mother's Habit and Baby's Weight



Mother Smoker/Non-Smoker

The box plots show how the medians of the two distributions compare, but we can also compare the means of the distributions using the following function to split the weight variable into the habit groups, then take the mean of each using the mean function.

There is an observed difference, but is this difference statistically significant? In order to answer this question we will conduct a hypothesis test.

Inference

3. Check if the conditions necessary for inference are satisfied. Note that you will need to obtain sample sizes to check the conditions. You can compute the group size using the same by command above but replacing mean with length.

```
by(nc$weight, nc$habit, length)
```

```
## nc$habit: nonsmoker
## [1] 873
## -----
## nc$habit: smoker
## [1] 126
```

4. Write the hypotheses for testing if the average weights of babies born to smoking and non-smoking mothers are different.

```
H0: \mu\{\text{nonsmoker}\}\ -\ \mu\{\text{smoker}\}\ =\ 0, There is no difference in the mean of the weight of babies born to smoking and to nonsmoking mothers.
```

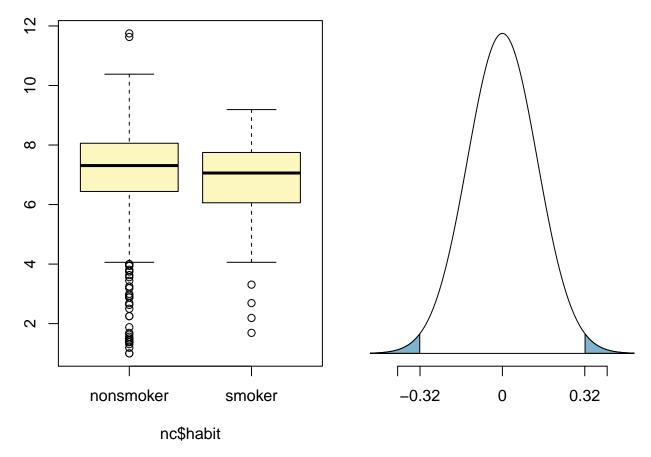
HA: $\mu\{nonsmoker\}$ - $\mu\{smoker\}$!= 0, There is a difference in the mean of the birth weight of babies born to smoking and to nonsmoking mothers.

Next, we introduce a new function, inference, that we will use for conducting hypothesis tests and constructing confidence intervals.

```
## Warning: package 'BHH2' was built under R version 3.5.3

## Response variable: numerical, Explanatory variable: categorical
## Difference between two means
## Summary statistics:
## n_nonsmoker = 873, mean_nonsmoker = 7.1443, sd_nonsmoker = 1.5187
## n_smoker = 126, mean_smoker = 6.8287, sd_smoker = 1.3862

## Observed difference between means (nonsmoker-smoker) = 0.3155
##
## H0: mu_nonsmoker - mu_smoker = 0
## HA: mu_nonsmoker - mu_smoker != 0
## Estandard error = 0.134
## Test statistic: Z = 2.359
## p-value = 0.0184
```

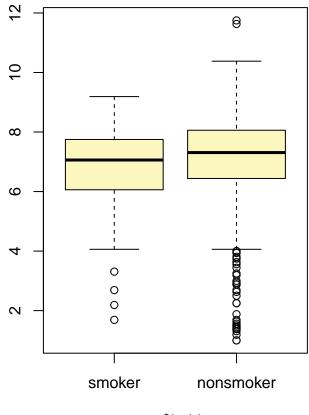


Let's pause for a moment to go through the arguments of this custom function. The first argument is y, which is the response variable that we are interested in: nc\$weight. The second argument is the explanatory variable, x, which is the variable that splits the data into two groups, smokers and non-smokers: nc\$habit. The third argument, est, is the parameter we're interested in: "mean" (other options are "median", or "proportion".) Next we decide on the type of inference we want: a hypothesis test ("ht") or a confidence interval ("ci"). When performing a hypothesis test, we also need to supply the null value, which in this case is 0, since the null hypothesis sets the two population means equal to each other. The alternative hypothesis can be "less", "greater", or "twosided". Lastly, the method of inference can be "theoretical" or "simulation" based.

5. Change the type argument to "ci" to construct and record a confidence interval for the difference between the weights of babies born to smoking and non-smoking mothers.

By default the function reports an interval for $(\mu_{nonsmoker} - \mu_{smoker})$. We can easily change this order by using the order argument:

```
## Response variable: numerical, Explanatory variable: categorical
## Difference between two means
## Summary statistics:
## n_smoker = 126, mean_smoker = 6.8287, sd_smoker = 1.3862
## n_nonsmoker = 873, mean_nonsmoker = 7.1443, sd_nonsmoker = 1.5187
```



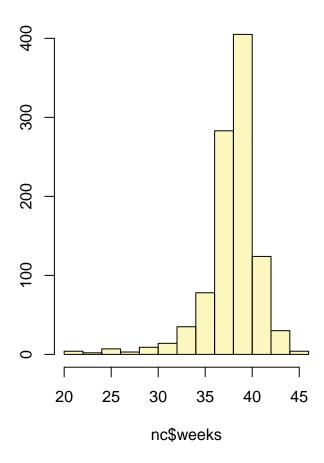
nc\$habit

```
## Observed difference between means (smoker-nonsmoker) = -0.3155 ## ## Standard error = 0.1338 ## 95 % Confidence interval = (-0.5777, -0.0534)
```

On your own

• Calculate a 95% confidence interval for the average length of pregnancies (weeks) and interpret it in context. Note that since you're doing inference on a single population parameter, there is no explanatory variable, so you can omit the x variable from the function.

```
## Single mean
## Summary statistics:
```



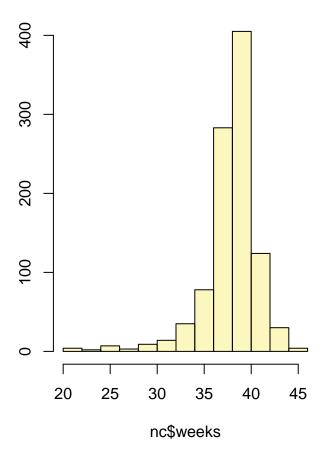
```
## mean = 38.3347; sd = 2.9316; n = 998 ## Standard error = 0.0928 ## 95 % Confidence interval = ( 38.1528 , 38.5165 )
```

Based on our computation We are 95% confident that the population mean falls between (38.1528 , 38

• Calculate a new confidence interval for the same parameter at the 90% confidence level. You can change the confidence level by adding a new argument to the function: conflevel = 0.90.

```
## Single mean
```

Summary statistics:



```
## mean = 38.3347 ; sd = 2.9316 ; n = 998
## Standard error = 0.0928
## 90 % Confidence interval = ( 38.182 , 38.4873 )
```

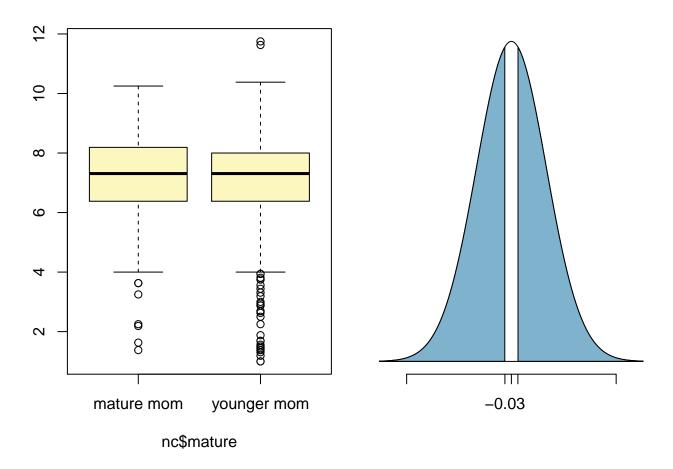
Based on our computation We are 90% confident that the population mean falls between (38.182 , 38.

• Conduct a hypothesis test evaluating whether the average weight gained by younger mothers is different than the average weight gained by mature mothers.

```
## Response variable: numerical, Explanatory variable: categorical
## Difference between two means
## Summary statistics:
## n_mature mom = 133, mean_mature mom = 7.1256, sd_mature mom = 1.6591
## n_younger mom = 867, mean_younger mom = 7.0972, sd_younger mom = 1.4855

## Observed difference between means (mature mom-younger mom) = 0.0283
##
## HO: mu_mature mom - mu_younger mom = 0
## HA: mu_mature mom - mu_younger mom != 0
## Standard error = 0.152
## Test statistic: Z = 0.186
## p-value = 0.8526
```

inference(y = nc\$weight, x = nc\$mature, est = "mean", type = "ht", null = 0,



Based on statistical data, we cannot reject the null hypothesis since the p-value of 0.8526 is grea

• Now, a non-inference task: Determine the age cutoff for younger and mature mothers. Use a method of your choice, and explain how your method works.

We can use the range to find teh cutoff age between the young mothers and mature mothers. From this

• Pick a pair of numerical and categorical variables and come up with a research question evaluating the relationship between these variables. Formulate the question in a way that it can be answered using a hypothesis test and/or a confidence interval. Answer your question using the inference function, report the statistical results, and also provide an explanation in plain language.

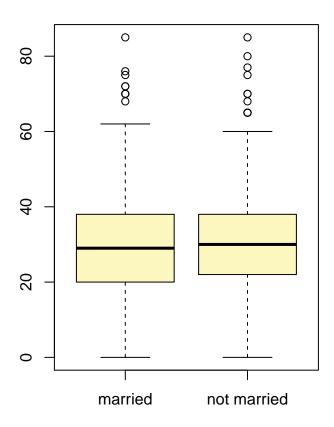
Research question: Does marital status affect weight gained by mothers during pregnancy?

H0: $\mu\{\text{married}\}\ - \mu\{\text{not married}\}\ = 0$, There is no difference in the mean of the weight gained during pregnancy of between married and single mothers.

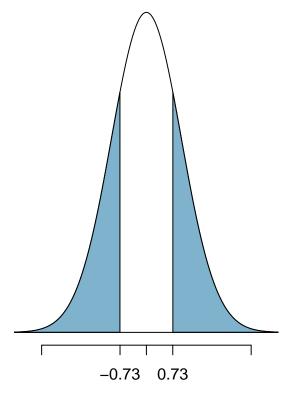
HA: $\mu\{\text{married}\}\ - \mu\{\text{not married}\}\ != 0$, There is a difference in the mean of the weight gained during pregnancy between married and single mothers.

```
## Response variable: numerical, Explanatory variable: categorical
## Difference between two means
## Summary statistics:
## n_married = 370, mean_married = 29.873, sd_married = 15.2721
## n_not married = 603, mean_not married = 30.6036, sd_not married = 13.5757

## Observed difference between means (married-not married) = -0.7307
##
## HO: mu_married - mu_not married = 0
## HA: mu_married - mu_not married != 0
## Standard error = 0.967
## Test statistic: Z = -0.755
## p-value = 0.4502
```

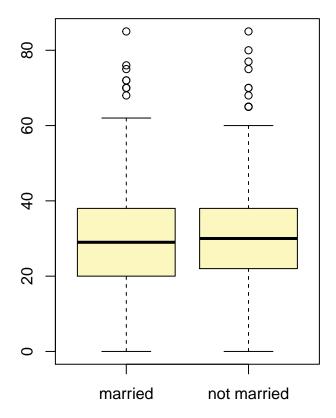


nc\$marital



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```
## Response variable: numerical, Explanatory variable: categorical
## Difference between two means
## Summary statistics:
## n_married = 370, mean_married = 29.873, sd_married = 15.2721
## n_not married = 603, mean_not married = 30.6036, sd_not married = 13.5757
```



nc\$marital

```
## Observed difference between means (married-not married) = -0.7307 ## ## Standard error = 0.9675 ## 95 % Confidence interval = ( -2.6269 , 1.1655 )
```

Based on the hypothesis test the p-value of 0.4502 is greater than alpha of 0.05 and thus w