

1.3 SUM OF SQUARES OF DISTINCT COUNTS

Question:

You are given a 0-indexed integer array `nums`. The distinct count of a subarray of `nums` is defined as: Let `nums[i..j]` be a subarray of `nums` consisting of all the indices from `i` to `j` such that $0 \leq i \leq j < \text{nums.length}$. Then the number of distinct values in `nums[i..j]` is called the distinct count of `nums[i..j]`. Return the sum of the squares of distinct counts of all subarrays of `nums`. A subarray is a contiguous non-empty sequence of elements within an array.

AIM:

To compute the sum of the squares of distinct counts of all possible subarrays of a given integer array.

ALGORITHM:

1. Initialize total sum = 0.
2. Generate all possible subarrays:
 - Outer loop for starting index `i`.
 - Inner loop for ending index `j`.
3. For each subarray `nums[i..j]`:
 - Use a set to find the distinct elements.
 - Let `count` = size of set.
 - Add `count * count` (square of distinct count) to total sum.
4. Return total sum after processing all subarrays.

PROGRAM:

```
def sum_of_squares(nums):
    total = 0
    for i in range(len(nums)):
        seen = set()
        for j in range(i, len(nums)):
            seen.add(nums[j])
            total += len(seen) ** 2
    return total

nums = list(map(int, input("Enter nums: ").split()))
print("Sum of squares of distinct counts:", sum_of_squares(nums))
```

Input:

nums = [1,2,1]

Output:

```
>>> Enter nums: 1 2 1
Sum of squares of distinct counts: 15
>>> |
```

RESULT:

Thus the program is successfully executed, and the output is verified.

PERFORMANCE ANALYSIS:

Time Complexity:

- Generating all subarrays = $O(n^2)$
- Counting distinct using set (up to $O(n)$ each)
- Worst case = $O(n^3)$
- For small n this is fine.

Space Complexity:

- Temporary set of size up to $O(n)$
- So overall = $O(n)$