

3.9 FINDING THE K CLOSEST POINTS TO ORIGIN

Question:

Given an array of points where $\text{points}[i] = [x_i, y_i]$ represents a point on the X-Y plane and an integer k , return the k closest points to the origin $(0, 0)$.

AIM

To design a program that returns the k closest points to the origin using Euclidean distance.

ALGORITHM

1. Start with the given list of points and the integer k .
2. Compute the Euclidean distance of each point from the origin using the formula:

$$\text{Distance} = \sqrt{x^2 + y^2}$$

3. Sort the points based on their distance from the origin.
4. Return the first k points from the sorted list

PROGRAM

```
def k_closest(points, k):
    points.sort(key=lambda x: x[0]**2 + x[1]**2)
    return points[:k]

def run_k_closest():
    points = eval(input("Enter list of points (e.g. [[1,3],[-2,2]]): "))
    k = int(input("Enter k: "))
    print("Closest points:", k_closest(points, k))

run_k_closest()
```

Input:

Points = [(4,3), (-9,5), (1,-7)]

Output:

```
>>> Enter list of points (e.g. [[1,3],[-2,2]]): [[4,3],[-9,5],[1,-7]]
Enter k: 6
Closest points: [[4, 3], [1, -7], [-9, 5]]
```

RESULT:

Thus the program is successfully executed and the output is verified.

PERFORMANCE ANALYSIS:

- Time Complexity: Sorting takes $O(n \log n)$, where n is the number of points.
- Space Complexity: Uses only a few variables, so $O(1)$ (constant extra space).