

## 4.16 UNIQUE PATHS IN A GRID USING COMBINATORICS

### Question:

There is a robot on an  $m \times n$  grid. The robot is initially located at the top-left corner (i.e., `grid[0][0]`). The robot tries to move to the bottom-right corner (i.e., `grid[m - 1][n - 1]`). The robot can only move either down or right at any point in time. Given the two integers  $m$  and  $n$ , return the number of possible unique paths that the robot can take to reach the bottom-right corner. The test cases are generated so that the answer will be less than or equal to  $2 * 10^9$ .

### AIM

To compute the total number of unique paths from the top-left to the bottom-right corner of an  $m \times n$  grid using combinatorics.

### ALGORITHM

1. Create a 2D DP table `dp[m][n]` where `dp[i][j]` represents the number of ways to reach cell  $(i, j)$ .
2. Initialize the first row and first column with 1, since there is only one way to move straight along them.
3. For each cell  $(i, j)$  with  $i > 0$  and  $j > 0$ :
  - The number of ways = `dp[i-1][j] + dp[i][j-1]` (from top or left).
4. The result will be stored in `dp[m-1][n-1]`.

### PROGRAM

```
def unique_paths(m, n):
    dp = [[1]*n for _ in range(m)]
    for i in range(1, m):
        for j in range(1, n):
            dp[i][j] = dp[i-1][j] + dp[i][j-1]
    return dp[m-1][n-1]

m = int(input("Enter number of rows (m): "))
n = int(input("Enter number of columns (n): "))
print("Number of unique paths:", unique_paths(m, n))
```

Input:

Enter number of rows (m): 3

Enter number of columns (n): 6

Output:

```
>>> | Enter number of rows (m): 3
      | Enter number of columns (n): 6
      | Number of unique paths: 21
      |
```

## RESULT:

Thus the program is successfully executed and the output is verified.

## PERFORMANCE ANALYSIS:

- Time Complexity:  $O(m \times n)$
- Space Complexity:  $O(m \times n)$