

4.1 DICE THROW PROBLEM

Question:

You are given the number of sides on a die (num_sides), the number of dice to throw (num_dice), and a target sum (target). Develop a program that utilizes dynamic programming to solve the Dice Throw Problem.

AIM

To design a Python program that calculates the number of ways to achieve a target sum using a given number of dice and sides, using dynamic programming.

ALGORITHM

1. Define a 2D DP table $dp[d][t]$ where d is the number of dice used and t is the current sum.
2. Initialize $dp[0][0] = 1$ (1 way to get sum 0 with 0 dice).
3. For each dice from 1 to num_dice:
 - For each sum from 1 to target:
 - For each face value from 1 to num_sides:
 - If $t - \text{face} \geq 0$, add $dp[d-1][t-\text{face}]$ to $dp[d][t]$.
4. Return $dp[\text{num_dice}][\text{target}]$.

PROGRAM

```
def dice_throw(num_dice, num_sides, target):
    dp = [[0] * (target + 1) for _ in range(num_dice + 1)]
    dp[0][0] = 1
    for i in range(1, num_dice + 1):
        for j in range(1, target + 1):
            for k in range(1, num_sides + 1):
                if j - k >= 0:
                    dp[i][j] += dp[i - 1][j - k]
    return dp[num_dice][target]

num_sides = int(input("Enter number of sides on the die: "))
num_dice = int(input("Enter number of dice: "))
target = int(input("Enter target sum: "))
print(f"Number of ways to reach sum {target}: {dice_throw(num_dice, num_sides, target)}")
```

Input:

No. of sides: 6

No. of dice: 2

Target: 7

Output:

```
>>> | Enter number of sides on the die: 6
      | Enter number of dice: 2
      | Enter target sum: 7
      | Number of ways to reach sum 7: 6
```

RESULT:

Thus the program is successfully executed and the output is verified.

PERFORMANCE ANALYSIS:

- Time Complexity: $O(\text{num_dice} \times \text{target} \times \text{num_sides})$
- Space Complexity: $O(\text{num_dice} \times \text{target})$