

belief_mean init.

ii loop

mobility init:
$$\begin{cases} q_j(t) = x_j + \frac{1}{2} N(0, \sigma_d) + v_j \Delta t \\ \psi_{q_j}(t) = \sigma_d + \begin{bmatrix} 0.1 \\ 1.0 \end{bmatrix} \end{cases}$$

belief_variance

movement variation

sum-product init:
$$\begin{cases} \hat{x}_j(l) = q_j(t) \\ \psi_j^{\hat{x}}(l) = \psi_{q_j}(t) \end{cases}$$

measurement init:
$$\begin{cases} \Delta_{kj}(l) = 0 \\ \psi_{kj}^{\Delta}(l) = 0 \end{cases}$$

$$\begin{cases} d_{kj} = \|x_k - x_j\|_2 \\ \theta_{kj} = \tan^{-1} \left(\frac{x_{1k} - x_{1j}}{x_{2k} - x_{2j}} \right) \end{cases}$$

i.e. from j to k

$$\Rightarrow x_k = x_j + d_{kj} \begin{bmatrix} \cos \theta_{kj} \\ \sin \theta_{kj} \end{bmatrix}$$

iter loop

j loop

$$\sum \frac{\Delta_{hj}}{\psi_{hj}^{\Delta}} = 0, \quad \sum \frac{1}{\psi_{hj}^{\Delta}} = 0 \quad \text{init}$$

k loop, if $k \neq j$:

$$\Delta_{kj}(l) = \hat{x}_k(l-1) - d_{kj} \begin{bmatrix} \cos \theta_{kj} \\ \sin \theta_{kj} \end{bmatrix}$$

$$\psi_{kj}^{\Delta}(l) = \psi_k^{\hat{x}}(l-1) + \begin{bmatrix} \sigma_d^2 \cos^2 \theta_{kj} + d_{kj}^2 \sigma_{\theta}^2 \sin^2 \theta_{kj} \\ \sigma_d^2 \sin^2 \theta_{kj} + d_{kj}^2 \sigma_{\theta}^2 \cos^2 \theta_{kj} \end{bmatrix}$$

$$\sum \frac{\Delta_{hj}}{\psi_{hj}^{\Delta}} += \frac{\Delta_{kj}}{\psi_{kj}^{\Delta}}, \quad \sum \frac{1}{\psi_{hj}^{\Delta}} += \frac{1}{\psi_{kj}^{\Delta}}$$

end

$$\begin{aligned} \psi_j^{\hat{x}}(l) &= \left(\frac{1}{\psi_{q_j}(t)} + \sum \frac{1}{\psi_{hj}^{\Delta}} \right)^{-1} \\ \hat{x}_j(l) &= \psi_j^{\hat{x}}(l) \cdot \left(\frac{q_j(t)}{\psi_{q_j}(t)} + \sum \frac{\Delta_{hj}}{\psi_{hj}^{\Delta}} \right) \end{aligned}$$

end

end

belief_mean = $q_j(t)$, belief_var = $\psi_j^{\hat{x}}(t)$

end