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Input: sequences  $X, Y, Z$ 
pushdown stack coordinateStack;           /* hold (state, subsequence triplet) pairs */
 $\mathbf{a} \leftarrow \text{Start};$                                /* current ensemble state */
 $n^{(X)} \leftarrow N^{(X)};$            /* current  $X$  subsequence;  $N^{(X)}$  is the outermost subsequence */
 $n^{(Y)} \leftarrow N^{(Y)};$            /* current  $Y$  subsequence;  $N^{(Y)}$  is the outermost subsequence */
 $n^{(Z)} \leftarrow N^{(Z)};$            /* current  $Z$  subsequence;  $N^{(Z)}$  is the outermost subsequence */
clear coordinateStack;
begin main loop:
    output current state  $\mathbf{a}$  and subsequence triplet  $(n^{(X)}, n^{(Y)}, n^{(Z)})$ ;
    if  $\mathbf{a}$  is the End state then                               /* end of a parse subtree */
        if coordinateStack is empty then return ;               /* end of the parse tree */
        pop  $(\mathbf{a}, n^{(X)}, n^{(Y)}, n^{(Z)})$  from coordinateStack ;
        goto main loop ;
    else if  $\mathbf{a}$  is a bifurcation state then                       /* bifurcation  $\mathbf{a} \rightarrow \mathbf{cb}$  */
        select  $(n_L^{(X)}, n_R^{(X)}) \in b_{in}(n^{(X)}), (n_L^{(Y)}, n_R^{(Y)}) \in b_{in}(n^{(Y)}), (n_L^{(Z)}, n_R^{(Z)}) \in b_{in}(n^{(Z)})$ 
        such that
         $\gamma_{\mathbf{a}}(n^{(X)}, n^{(Y)}, n^{(Z)}) = \gamma_{\mathbf{a}}(n_L^{(X)}, n_L^{(Y)}, n_L^{(Z)}) \gamma_{\mathbf{a}}(n_R^{(X)}, n_R^{(Y)}, n_R^{(Z)})$  ;
        push  $(\mathbf{c}, n_R^{(X)}, n_R^{(Y)}, n_R^{(Z)})$  onto coordinateStack ;
         $\mathbf{a} \leftarrow \mathbf{b};$ 
         $n^{(X)} \leftarrow n_L^{(X)};$ 
         $n^{(Y)} \leftarrow n_L^{(Y)};$ 
         $n^{(Z)} \leftarrow n_L^{(Z)};$ 
        goto main loop ;
    else                                                         /* Emit or Null state */
         $m^{(X)} \leftarrow c_{in}(\mathbf{b}; n^{(X)})$  ;
         $m^{(Y)} \leftarrow c_{in}(\mathbf{b}; n^{(Y)})$  ;
         $m^{(Z)} \leftarrow c_{in}(\mathbf{b}; n^{(Z)})$  ;
        select  $\mathbf{b} \in \{\mathbf{b} : \exists \mathbf{a} \rightarrow \mathbf{lbr}\}$ 
        such that
         $\gamma_{\mathbf{a}}(n^{(X)}, n^{(Y)}, n^{(Z)}) = P(\mathbf{a} \rightarrow \mathbf{lbr}) \gamma_{\mathbf{b}}(m^{(X)}, m^{(Y)}, m^{(Z)})$ ;
         $\mathbf{a} \leftarrow \mathbf{b};$ 
         $n^{(X)} \leftarrow m^{(X)};$ 
         $n^{(Y)} \leftarrow m^{(Y)};$ 
         $n^{(Z)} \leftarrow m^{(Z)};$ 
        goto main loop ;
end

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