# R-solution: Exercises Day 1

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#### **Exercise 2: Simple regression**

Interpret the Intercept as the level where the predictor is zero, i.e., a person with no work experience earned about 198.8 thousand NOK. The slope is the increase with the predictor, i.e., for each year of work experience, someone will earn 0.88 thousand NOK more.

```
loenn <- haven::read_dta("../data/loenn.dta")</pre>
  summary(lm(loenn ~ erfaring, data=loenn))
Call:
lm(formula = loenn ~ erfaring, data = loenn)
Residuals:
    Min
             1Q Median
                             3Q
                                    Max
-140.27 -79.80 -26.30
                          49.55 779.36
Coefficients:
            Estimate Std. Error t value Pr(>|t|)
(Intercept) 198.7606
                         9.2682 21.445
                                          <2e-16 ***
erfaring
              0.8807
                         0.4310
                                  2.043
                                          0.0416 *
Signif. codes:
                0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Residual standard error: 110.3 on 462 degrees of freedom
  (7 observations deleted due to missingness)
Multiple R-squared: 0.008957, Adjusted R-squared: 0.006812
F-statistic: 4.176 on 1 and 462 DF, p-value: 0.04157
```

```
summary(lm(loenn ~ kvinne, data=loenn))
Call:
lm(formula = loenn ~ kvinne, data = loenn)
Residuals:
    Min
            1Q Median
                            3Q
                                   Max
-142.84 -80.14 -25.30
                         46.06 788.70
Coefficients:
           Estimate Std. Error t value Pr(>|t|)
                        6.694 34.975 < 2e-16 ***
(Intercept) 234.136
kvinne
            -43.832
                        10.074 -4.351 1.66e-05 ***
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Residual standard error: 108.6 on 469 degrees of freedom
Multiple R-squared: 0.0388,
                               Adjusted R-squared: 0.03675
F-statistic: 18.93 on 1 and 469 DF, p-value: 1.663e-05
```

### **Exercise 3: Multiple regression**

When interpreting, it is important to include the "keeping constant" qualifier for all included variables. I.e., For each year in work experience, someone would earn 2400 NOK more controlling for gender and education.

```
loenn <- haven::read_dta("../data/loenn.dta")
summary(lm(loenn ~ erfaring + kvinne + utdann, data=loenn))

Call:
lm(formula = loenn ~ erfaring + kvinne + utdann, data = loenn)

Residuals:
    Min    1Q Median    3Q    Max
-212.47    -55.40    -12.92    38.44   818.33

Coefficients:</pre>
```

```
Estimate Std. Error t value Pr(>|t|)
(Intercept) -58.8169
                        28.7160 -2.048
                                          0.0411 *
erfaring
              2.4172
                         0.4131
                                  5.851 9.41e-09 ***
kvinne
            -50.1182
                         9.2419 -5.423 9.58e-08 ***
utdann
             19.0848
                         1.8722 10.194 < 2e-16 ***
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Residual standard error: 97.68 on 451 degrees of freedom
  (16 observations deleted due to missingness)
Multiple R-squared: 0.2294,
                                Adjusted R-squared: 0.2243
F-statistic: 44.75 on 3 and 451 DF, p-value: < 2.2e-16
  mod <- lm(loenn ~ kvinne + alder + fagfor + gift, data=loenn)</pre>
  predict(mod, newdata=data.frame(kvinne=0, alder=40, fagfor=1, gift=1))
       1
256.9429
```

## **Exercise 4: Brain weight and total sleep across species**

The two "weight" variables are highly correlated (collinear). Individually, they are both related to the total sleep. However, when inputting them simultaneously, the effect disappears.

#### Exercise 5: Random data

When running enough of the regressions, some will be significant (approximately 5% when using the alpha-level of 0.05). The correlation matrix has some pretty large correlations. This is because of the low number of observations (N=20).

```
x1
                         x2
                                     x3
                                                 x4
                                                             x5
                                                                         x6
     1.000000000 \quad 0.11695293 \quad -0.07624683 \quad 0.04819686 \quad -0.339109954 \quad -0.09408270
x1
x2
     0.116952932 1.00000000 0.25331670 -0.29523441 -0.457247484 -0.06376500
x3 - 0.076246825 0.25331670 1.00000000 0.01284676 - 0.420154967 - 0.01864681
     0.048196864 - 0.29523441 \ 0.01284676 \ 1.00000000 - 0.114017442 \ 0.12023231
x4
   -0.339109954 -0.45724748 -0.42015497 -0.11401744 1.000000000 0.29563117
   -0.094082703 -0.06376500 -0.01864681 0.12023231 0.295631170
                                                                1.00000000
x7
   -0.152702852 \quad 0.09020149 \quad -0.10225600 \quad -0.23092627 \quad 0.132059502 \quad 0.06113374
     0.030415870 - 0.31572654 \ 0.10557823 \ 0.15043456 - 0.090024403 \ 0.13995050
8x
x9
     x10 \quad 0.009460436 \quad 0.02845329 \quad -0.04259574 \quad 0.25292105 \quad 0.137002912 \quad 0.06930351
            x7
                        8x
                                     x9
                                                 x10
   -0.15270285 0.03041587 0.019132528 0.009460436
x1
x2
     0.09020149 -0.31572654 0.130022193 0.028453286
xЗ
   -0.10225600 0.10557823 0.277605126 -0.042595739
   -0.23092627 0.15043456 0.295581877 0.252921046
x4
x5
     0.13205950 -0.09002440 0.001988955 0.137002912
     0.06113374 \quad 0.13995050 \quad 0.133412520 \quad 0.069303512
x6
     1.00000000 -0.53114608 -0.081560057 0.333877580
x7
x8 -0.53114608 1.00000000 0.184580080 -0.102162005
   0.33387758 -0.10216200 0.204044226 1.000000000
```