

SELARU modelling framework

Technical documentation

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1 Overview

SELARU (Spatially-explicit Energy and LAnd system InfrastRucture) modelling framework is a high-resolution spatially explicit analytical tool for integrated assessments of energy and land systems using Mixed-Integer Linear Programming (MILP) optimization approach. The main feature of SELARU is its capability to address economies of scale that occur from geographical expansion of energy and land system infrastructures. This allows a more accurate system depiction to facilitate scientific investigations concerning long term infrastructure sitting/deployment in a highly complex and geographically diverse environment.

In this version, the application of SELARU is limited to Indonesia's electricity sector (**Figure 1**) to demonstrate the impact of spatially explicit representation for energy system optimization. SELARU generates optimal configuration of technology application for power generation, transmission lines and substations that minimises total system cost throughout the planning horizon. The optimisation is achieved through minimising total system costs while guaranteeing security of supply, ensuring technically feasible operation. SELARU endogenously determines the capacity expansion decisions in every 20-year timestep from 2020 to 2100.

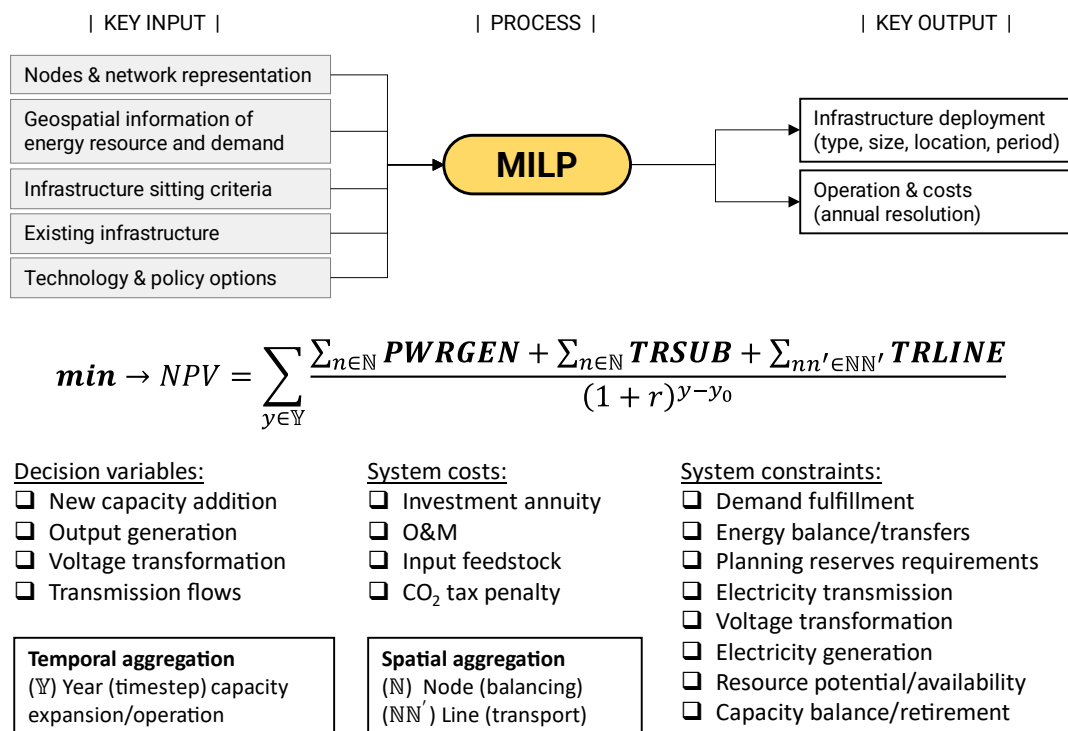


Figure 1 | Schematic overview of SELARU modelling framework for Indonesia's electricity sector.

The modelled energy system is represented as a network of interconnecting nodes. A node in the network represents a region in which energy can be utilized, converted, stored, or send-in or -out. The lines connecting different nodes represent the connections or transmission corridors along which energy can be transported. Consequently, the basic framework of the energy system model is given by the energy balance and transfers at and from or to nodes in all times.

The required capacity deployment, generation, voltage-transformation, transmission flows, reserve capacity, and primary energy feedstock are endogenously determined by ensuring the nodal supply-

demand balances are satisfied all the time. The modelled energy system is formulated using sets of equations defining the costs and technical constraints of capacity deployment and operation. The objective of optimization is to minimise the system's costs while guaranteeing security of supply, ensuring technically feasible operation, and considering region-specific resource availability and environmental restriction. Spatial-explicit information of resource, supply, and demand, as well as region-specific policy interventions are exogenously considered for each modelled timestep.

2 Spatial representation

SELARU uses nodes and lines to represent the spatial context of energy systems. The nodes represent geographic areas within which selection of technologies for power generations, storages, transmission lines and substations will be solved as decision variables. The nodes also contain information such as potential of renewables, energy demand, and area of exclusion zones originating from spatial aggregation within the regions that the nodes represent. The lines connecting different nodes represent eligible connections or transmission corridors along which electricity can be transported. The default mode of SELARU Indonesia application comprises 776 nodes and 1768 lines that connect the nodes (**Figure 2**). The nodes are generated through clustering villages as the lowest administrative unit in Indonesia. This selection assumes that village map is a suitable proximation for the geographic distribution of socio-economic activities. 83,458 villages are aggregated to 500 clusters using k-Clusters algorithm¹ performed in QGIS software. Under the algorithm, mean coordinates of villages that belong to a unique cluster—weighted using their population density and distances to neighbouring villages—are used as the basis for Voronoi Tessellation² to generate polygons describing the clusters' bounding area. Clustered zones that include different islands or separated by water body are further divided, resulting in 776 nodes that represent areas ranging from 0.01-20,300 km², with an average of 217 km² which is comparable to 0.14° geographic grid resolution. International electricity trade with neighbouring countries is not considered.

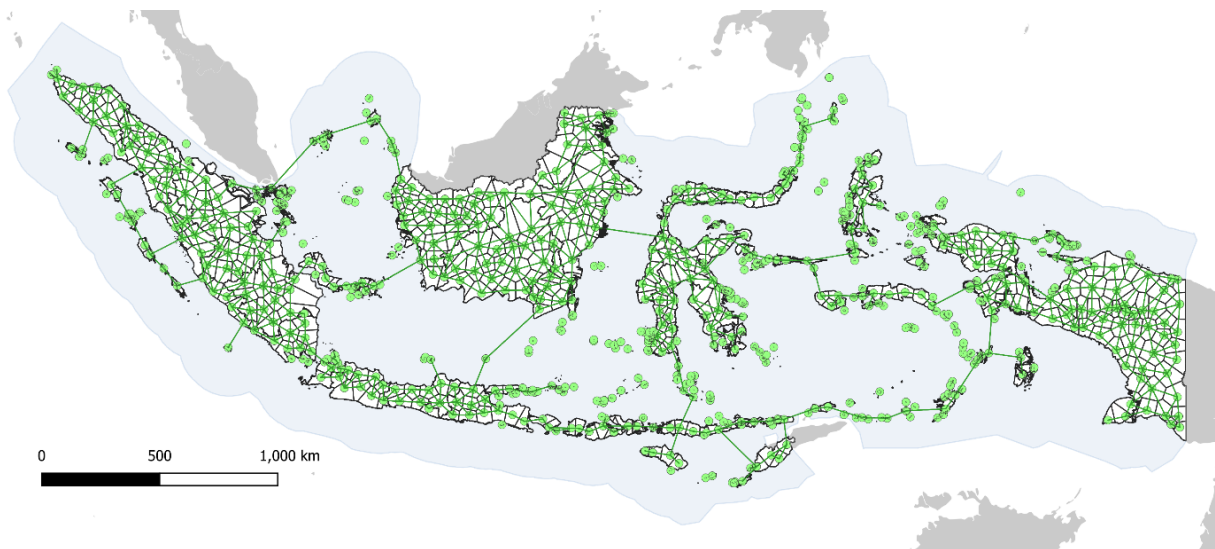


Figure 2 | Spatial representation for SELARU Indonesia application.

¹ Hartigan, J. A. & Wong, M. A. Algorithm AS 136: A K-Means Clustering Algorithm. *J. R. Stat. Soc. Ser. C Appl. Stat.* **28**, 100–108 (1979)

² Boots, B., Sugihara, K., Chiu, S. N. & Okabe, A. *Spatial Tessellations: Concepts and Applications of Voronoi Diagrams*. (John Wiley & Sons, 2009)

3 Input data

The input data that are used in this SELARU version were compiled from the following sources:

Geographical context

Includes administrative boundaries, land cover and topography:

<https://data.humdata.org/dataset/cod-ab-idn>

<https://www.indonesia-geospasial.com/2020/09/download-shp-tutupan-lahan-tahun-2019.html>

https://www.restoreplus.org/uploads/1/0/4/5/104525257/restore_technical_report_land_cover_mapping_july2022.pdf

<https://www.earthenv.org/topography>

Renewable energy resources

Geothermal, hydropower, solar, and wind resources:

<https://geoportal.esdm.go.id/potensiebtke/>

<https://datacatalog.worldbank.org/search/dataset/0042082>

<https://globalsolaratlas.info/map>

Fuel related parameters

Covers fossil fuel and biomass assumed to be abundantly available due to maturity of supply chain:

<https://world-nuclear.org/information-library/facts-and-figures/heat-values-of-various-fuels.aspx>

https://www.engineeringtoolbox.com/fuels-higher-calorific-values-d_169.html

https://www.ipcc-nggip.iges.or.jp/public/2006gl/pdf/2_Volume2/V2_2_Ch2_Stationary_Combustion.pdf

<https://www2.deloitte.com/content/dam/Deloitte/ca/Documents/energy-resources/ca-en-energy-resources-industrials-o-g-price-forecast-report-Q4-aoda.pdf?icid=commentaryEN>

<https://www.eia.gov/outlooks/steo/report/prices.php>

<https://migas.esdm.go.id/uploads/harga-indek-pasar-/2020-hip/hip-solar-dalam-rangka-perhitungan-selisihtahun-2020.pdf>

https://www.minerba.esdm.go.id/harga_acuan

<https://jdih.esdm.go.id/index.php/web/result/2355/detail>

<https://www.liputan6.com/bisnis/read/4401992/menengok-harga-keekonomian-biomassa-bahan-bakucofiring-pltu>

<https://winrock.org/wp-content/uploads/2016/05/CIRCLE-Handbook-2nd-Edition-EN-25-Aug-2015-MASTER-rev02-final-new02-edited.pdf>

<https://www.iea.org/reports/outlook-for-biogas-and-biomethane-prospects-for-organic-growth/sustainable-supply-potential-and-costs>

[https://world-nuclear.org/information-library/economic-aspects/economics-of-nuclear-power.aspx#:~:text=Its%202020%20report%2C%20Capital%20Cost,%2FkWe%20\(overnight%20cost\).](https://world-nuclear.org/information-library/economic-aspects/economics-of-nuclear-power.aspx#:~:text=Its%202020%20report%2C%20Capital%20Cost,%2FkWe%20(overnight%20cost).)

<https://www.eia.gov/opendata/v1/qb.php?category=40290&sdid=SEDS.NUETD.WI.A>

[https://www.eia.gov/uranium/marketing/#:~:text=During%202021%2C%2019%25%20of%20the,per%20pound%20\(Table%207\).](https://www.eia.gov/uranium/marketing/#:~:text=During%202021%2C%2019%25%20of%20the,per%20pound%20(Table%207).)

<https://www.world-nuclear.org/uploadedfiles/org/info/pdf/economicsnp.pdf>

Electricity generation parameters

Technoeconomic parameters related to plant-sitting investment decisions:

<https://www.irena.org/publications/2021/Jun/Renewable-Power-Costs-in-2020>

https://www.eia.gov/analysis/studies/powerplants/capitalcost/pdf/capital_cost_AEO2020.pdf
<https://atb.nrel.gov/>
https://atb.nrel.gov/electricity/2021/equations_&_variables#equations
<https://www.nrel.gov/docs/fy19osti/74184.pdf>
<https://www.nrel.gov/docs/fy21osti/77324.pdf>
<https://www.nrel.gov/docs/fy13osti/56290.pdf>
<https://globalwindatlas.info/about/ReleaseNotes>
<https://www.nrel.gov/docs/fy21osti/78882.pdf>
<https://www.nrel.gov/analysis/tech-size.html>
https://www.gem.wiki/Concentrating_solar_power_land_use
<https://ourworldindata.org/land-use-per-energy-source>
<https://docs.wind-watch.org/US-footprints-Strata-2017.pdf>
[https://ens.dk/sites/ens.dk/files/Globalcooperation/technology_data_for_the_indonesian_power_sector -
final.pdf](https://ens.dk/sites/ens.dk/files/Globalcooperation/technology_data_for_the_indonesian_power_sector_-_final.pdf)

Grid related parameters

Substation, transmissions and basis for assumptions on planning reserve margin:

https://iea-etsap.org/E-TechDS/PDF/E12_el-t&d_KV_Apr2014_GSOK.pdf
<https://www.adb.org/sites/default/files/linked-documents/47296-001-ea.pdf>
https://www.wecc.org/Administrative/TEPPC_TransCapCostCalculator_E3_2019_Update.xlsx
<https://web.pln.co.id/statics/uploads/2021/10/ruptl-2021-2030.pdf>

Socio-economic data for demand projection

Spatially explicit projections of electricity demand are exogenous input to the model. Demand information is obtained from national demand projection and its downscaling to take into account regional disparities in accordance with the spatial resolution of the analysis. Projection is based on linear regression throughout the modelling time horizon with dependent variables including historical data for electricity consumption³, population⁴, gross domestic product (GDP) at corresponding spatial resolutions (i.e. national, provincial and district levels)⁵, and population projection from the Shared Socioeconomic Pathways “Middle of the road” scenario (SSP2)⁶.

4 MILP formulation

Optimization in SELARU is formulated as an MILP model using the General Algebraic Modelling System (GAMS).

4.1 Nomenclature

Sets and indices

$y \in \mathbb{Y}$	year in parameterised time-step
v	technology vintage
$n n' \in \mathbb{N}$	nodes of energy supply and demand balancing
$nn' \in \mathbb{NN}$	lines of connection from node (n) to another node (n')

³ PLN (2022), <https://web.pln.co.id/statics/uploads/2022/08/Statistik-PLN-2021-29-7-22-Final.pdf>

⁴ BPS (2022), <https://www.bps.go.id/pressrelease/2021/01/21/1854/hasil-sensus-penduduk-2020.html>

⁵ BPS (2019), <https://www.bps.go.id/publication/2019/10/04/9812a1c4ea25298004839596/produkt-domestik-regional-bruto-kabupaten-kota-di-indonesia-2014-2018.html>

⁶ Riahi, K. et al. The Shared Socioeconomic Pathways and their energy, land use, and greenhouse gas emissions implications: An overview. Glob. Environ. Change 42, 153–168 (2017)

$i \in \mathbb{I}$	type of technology
$eg \in \mathbb{EG}$	type of electricity generation technology
$greg \in \mathbb{GREG}$	group of electricity generation technology
$ts \in \mathbb{TS}$	type of electricity transformer-substation technology
$tl \in \mathbb{TL}$	type of electricity transmission line technology
$kv kv' \in \mathbb{KV}$	type of voltage
$f \in \mathbb{F}$	type of fuel

Parameters

r	system-wide discount rate
$length_y^{\text{years}}$	(years) length of years of the modelled time-step (y)
$d_{n,n2}$	(km) total distance in km of corridor (n,n')
$D_{n,y}^{\text{ely}}$	(MWh) annual demand of electricity at spatial unit (j) in year (y)
$typcap_i$	(MW) typical capacity (size) of technology (i)
$life_i^{\text{tech}}$	(years) technical lifetime of technology (i)
$life_i^{\text{econ}}$	(years) economic lifetime of technology (i)
$CAPEX_{n nn',i,y}$	(\$) overnight capital costs per unit capacity of technology (i) at node (n) or at corridor (n,n2) in year (y)
OMF_i	factor of fixed operating and maintenance costs towards capital expenditure of technology (i)
VOM_i	(\$) variable operating and maintenance costs per unit of output of technology (i)
\widehat{CF}_i	maximum capacity factor of technology (i)
\overline{CF}_i	minimum capacity factor of technology (i)
η_i	rate of energy efficiency by technology (i)
$loss_{nn',tl}$	(per 10 km) rate of energy losses of transmission line (tl) at corridor (n,n')
$\widehat{fmx}_{eg,f}$	maximum share of fuel type (f) in input aggregate of electricity generation (eg)
$landuse_{eg}$	(km ² MW ⁻¹) area of land-use per unit of capacity of electricity generation (eg)
$P_{n,f,y}$	(\$ GJ ⁻¹) energy price of fuel (f) at node (n) in year (y)
$emsf_f^{\text{CO}_2}$	(tCO ₂ GJ ⁻¹) CO ₂ emissions factor of fuel type (f)
$potential_{n,greg}^{\text{MW}}$	(MW) potential capacity of deploying electricity generation types that belong to group (greg) at node (n)
GHI_n	(kWh m ⁻² y ⁻¹) annual global horizontal irradiance at node (n)
DNI_n	(kWh m ⁻² y ⁻¹) annual direct normal irradiance at node (n)
$CF_{n,eg}^{\text{WIND}}$	(unitless) wind resource capacity factor at node (n) for electricity generation (eg)
$stock_{n,eg,v,y}$	(MW) existing stock capacity of electricity generation (eg) that was built in year (v) at node (n) in year (y)
$stock_{n,ts,y}$	(MW) existing stock capacity of transformer substation (ts) at node (n) in year (y)
$stock_{nn',tl,y}$	(MW) existing stock capacity of transmission line (tl) at corridor (n,n') in year (y)

Variables

Costs

NPV	(\$ y ⁻¹) net-present value of the whole planning horizon
TSC_y	(\$ y ⁻¹) annual cost of the total system in year (y)
$TSC_{n,eg,v,y}^{\text{Generation}}$	(\$ y ⁻¹) annual costs of electricity generation by technology (eg) that was built in year (v) at node (n) in year (y)
$TSC_{nn',tl,y}^{\text{Transmission}}$	(\$ y ⁻¹) annual costs of electricity transmission by technology (tl) at corridor (nn') in year (y)

$TSC_{n,ts,y}^{Substation}$ (\$ y^{-1}) annual costs of voltage transformation by technology (sub) at node (n) in year (y)

Electricity transmission

$CAP_{nn',tl,y}$ (units) installed capacity of transmission line (tl) at corridor (nn') in year (y)
 $NEW_{nn',tl,y}$ (MW) new addition units of transmission line (tl) at corridor (nn') in year (y)
 $FLOW_{nn',tl,y}^{ely}$ (MWh y^{-1}) flow of electricity in transmission line (tl) at corridor (nn') in year (y)
 $FLOW_{nn',tl,y}^{plrsv}$ (MW y^{-1}) flow of planning reserve capacity in transmission line (tl) that was built in year (v) at corridor (n,n') in year (y)

Voltage transformation

$CAP_{n,sub,y}$ (units) installed capacity of technology type (sub) that was built in year (v) at node (n) in year (y)
 $NEWi_{n,sub,y}$ (units) new addition of technology type (sub) that was built in year (v) at node (n) in year (y)
 $NEWc_{n,sub,y}$ (MW) new addition of technology type (sub) that was built in year (v) at node (n) in year (y)
 $Vup_{n,kv',kv,y}^{ely}$ (MWh y^{-1}) transformation of electricity from lower (kv') to higher (kv) voltage class at node (n) in year (y)
 $Vdo_{n,kv',kv,y}^{ely}$ (MWh y^{-1}) transformation of electricity from higher (kv') to lower (kv) voltage class at node (n) in year (y)
 $Vup_{n,kv',kv,y}^{plrsv}$ (MW) transformation of planning reserve capacity from lower (kv') to higher (kv) voltage class at node (n) in year (y)
 $Vdo_{n,kv',kv,y}^{plrsv}$ (MW) transformation of planning reserve capacity from higher (kv') to lower (kv) voltage class at node (n) in year (y)

Electricity generation

$CAP_{n,eg,v,y}$ (units) installed capacity of technology type (eg) that was built in year (v) at node (n) in year (y)
 $NEWi_{n,eg,v,y}$ (units) new addition of technology type (eg) that was built in year (v) at node (n) in year (y)
 $NEWc_{n,eg,v,y}$ (MW) new addition of technology type (eg) that was built in year (v) at node (n) in year (y)
 $RET_{n,eg,v,y}$ (units) retired units of technology type (eg) that was built in year (v) at node (n) in year (y)
 $INPUT_{n,eg,v,y}$ (GJ y^{-1}) primary energy input mixture of technology type (eg) that was built in year (v) at node (n) in year (y)
 $OUTPUT_{n,eg,v,y}^{ely}$ (MWh y^{-1}) electricity output for demand fulfilment of technology type (eg) at node (n) in year (y)
 $FUEL_{n,eg,v,f,y}$ (GJ y^{-1}) input feedstock fuel by type (f) bound to technology type (eg) that was built in year (v) at node (n) in year (y)
 $Cems_{n,eg,v,y}$ (tCO₂ y^{-1}) CO₂ emissions from technology type (eg) that was built in year (v) at node (n) in year (y)
 $Cbio_{n,eg,v,y}$ (tCO₂ y^{-1}) CO₂ emissions from bioenergy conversion of technology type (eg) that was built in year (v) at node (n) in year (y)

4.2 Objective function

The objective function of the optimisation model is to minimize the net-present value (NPV) of total annual system costs (TSC_y) along the planning horizon (\mathbb{Y}) that is composed of the total annual costs of all deployed generation \mathbb{EG} , transformer-substation \mathbb{TS} , transmissions \mathbb{TL} . The NPV is defined

$$NPV = \sum_{y \in \mathbb{Y}} \frac{\sum_{n \in \mathbb{N}, eg \in \mathbb{EG}, v} TSC_{n, eg, v, y}^{Generation} + \sum_{n \in \mathbb{N}, ts \in \mathbb{TS}} TSC_{n, sub, y}^{Substation} + \sum_{nn' \in \mathbb{NN}', tl \in \mathbb{TL}} TSC_{nn', tre, y}^{Transmission}}{(1 + r)^{y - y_0}}$$

NPV accounts for the time value of money and can be used to compare investment alternatives. All future cashflows and initial capital investments at period y are discounted by r (set to 5%) to obtain the present-value at y_0 .

4.3 Cost equations

The TSC for each technology class comprises of costs of capacity investment annuities, operation and maintenance, and when applicable costs of input feedstock and CO₂ emissions tax penalty, given for each node n or corridor nn' and planning period y , given by

$$\forall n \in \mathbb{N}, eg \in \mathbb{EG}, y \in \mathbb{Y},$$

$$TSC_{n, eg, v, y}^{Generation} = CAP_{n, eg, v, y} * CAPEX_{n, eg, y} * (CRF_{eg} + OMF_{eg}) + OUT_{n, eg, v, y}^{ely} * VOM_{eg} + \sum_f INPUT_{n, eg, v, f, y} * P_{n, f, y} + (Cems_{n, eg, v, y} - Cbio_{n, eg, v, y}) * tax_y^{Cems}$$

$$\forall n \in \mathbb{N}, ts \in \mathbb{TS}, y \in \mathbb{Y},$$

$$TSC_{n, ts, y}^{Substation} = CAP_{n, ts, y} * CAPEX_{n, ts, y} * (CRF_{ts} + OMF_{ts})$$

$$\forall nn' \in \mathbb{NN}', tl \in \mathbb{TL}, y \in \mathbb{Y},$$

$$TSC_{nn', tl, y}^{Transmission} = CAP_{nn', tl, y} * d_{nn'} * CAPEX_{nn', tl, y} * (CRF_{tre} + OMF_{tl})$$

The annuity of investment for each technology computed by the quantity of deployed capacities CAP , their overnight-capital costs per unit of capacity ($CAPEX$), their capital recovery factor (CRF), and their length (d) of connection of line nn' or from node n to node n' . Technology-specific interest rates and economical lifetime determines the CRF for each technology. The operation and maintenance (O&M) costs are determined by the factor OMF as a fraction of the overall capital costs ($CAPEX$) and by the level of production (OUT) multiplied by the unit variable O&M costs. For fuel-firing power generation technologies, input feedstock costs are determined by the sum of all fuels f multiplied by the price of that fuel $P_{n, f, y}$ at a given node n and in year y . CO₂ emissions tax-penalty are accounted for the net-amount of CO₂ emissions subtracted by CO₂ neutral from the use of sustainably sourced bioenergy, multiplied by the tax on CO₂ emissions tax_y^{Cems} applicable at given year y .

4.4 Electricity supply-demand matching constraints

Electricity supply-demand matching, or energy balance constraints ensure the fulfilment of electricity demand at all nodes \mathbb{N} for all voltage classes \mathbb{KV} in all planning periods \mathbb{Y} , given by

$$\begin{aligned}
D_{n,kv,y}^{ely} = & \sum_{eg \in (kv, eg), v \leq y} OUTPUT_{n, eg, v, y}^{ely} \\
& + \sum_{n' \in n', tre \in (kv, tre)} FLOW_{n'n, tre, y}^{ely} * (1 - loss_{tre} * d_{n'n}) \\
& - \sum_{n' \in nn', tre \in (kv, tre)} FLOW_{nn', tre, y}^{ely} \\
& + \sum_{kv' \leq kv \in (kv, sub)} Vup_{n, kv', kv, y}^{ely} * (1 - loss_{sub}) \\
& + \sum_{kv' \geq kv \in (kv, sub)} Vdo_{n, kv', kv, y}^{ely} * (1 - loss_{sub}) \\
& - \sum_{kv' \geq kv \in (kv, sub)} Vup_{n, kv, kv', y}^{ely} * (1 - loss_{sub}) \\
& - \sum_{kv' \leq kv \in (kv, sub)} Vdo_{n, kv, kv', y}^{ely} * (1 - loss_{sub}) , \quad \forall n \in \mathbb{N}, kv \in \mathbb{kv}, y \in \mathbb{Y}
\end{aligned}$$

Electricity demand at specific node n , voltage class kv , and planning period y (D^{ely}) is fulfilled with the power generated $OUT_{eg \in (kv, eg)}^{ely}$, plus all incoming transmission from all other nodes n' , minus all outgoing transmission to all other nodes n' ($FLOW^{ely}$), and plus net-change of voltage classes step-up Vup^{ely} and step-down Vdo^{ely} to and from other voltage classes kv' with considering transformation and transmissions losses ($loss_{sub}, loss_{tre}$).

4.5 Planning reserve supply-demand matching constraints

Planning reserves is required for the system to have sufficient firm capacity to meet the forecasted demand peak load plus a reserve margin, given by

$$\begin{aligned}
& \widehat{D}_{n,kv,y}^{ely} * (1 + margin_n^{plrsv}) \\
& = \sum_{eg \in (kv, eg), v \leq y} CAP_{n, eg, v, y}^{plrsv} \\
& + \sum_{n' \in n', tre \in (kv, tre)} FLOW_{n'n, tre, y}^{plrsv} * (1 - loss_{tre} * d_{n'n}) \\
& - \sum_{n' \in nn'} FLOW_{nn', tre, y}^{plrsv} + \sum_{kv' \leq kv \in (kv, sub)} Vup_{n, kv', kv, y}^{plrsv} * (1 - loss_{sub}) \\
& + \sum_{kv' \geq kv \in (kv, sub)} Vdo_{n, kv', kv, y}^{plrsv} * (1 - loss_{sub}) \\
& - \sum_{kv' \geq kv \in (kv, sub)} Vup_{n, kv, kv', y}^{plrsv} * (1 - loss_{sub}) \\
& - \sum_{kv' \leq kv \in (kv, sub)} Vdo_{n, kv, kv', y}^{plrsv} * (1 - loss_{sub}) , \quad \forall n \in \mathbb{N}, kv \in \mathbb{kv}, y \in \mathbb{Y}
\end{aligned}$$

$$\text{With } CAP_{n, eg, v, y}^{plrsv} \leq CAP_{n, eg, v, y} * capcredit_{eg}^{plrsv}$$

The supplied reserve capacities must exceed the peak demand ($\widehat{D}_{n,kv,y}^{ely}$) plus a margin for planning reserve ($margin^{plrsv}$) of respective supply-demand balancing region n . Reserve capacities

($CAP_{n,eg,v,y}^{plrsv}$) are supplied by all generation capacity capped by technology specific capacity reserve credits ($capcredit_{eg}^{plrsv}$), plus net incoming-outgoing flows of planning reserve capacities ($FLOW_{nn',kv,y}^{plrsv}$), plus net-change of voltage class step-up and -down of reserve capacities ($Vup_{n,kv',kv,y}^{plrsv}, Vdo_{n,kv,kv',y}^{plrsv}$), with also taking into account the losses incurred at transformer-substation and transmission line. Each technology is assigned with capacity credit. Reflecting its expected availability when power is needed. For instance, conventional power generating technologies have their maximum availability committed for planning reserve capacity provision.

4.6 Electricity transmission and voltage transformation constraints

Transmission of electricity ($FLOW_{nn',kv,y}^{ely}$) and firm capacities ($FLOW_{nn',kv,y}^{plrsv}$) are capped by the built transmission line capacity (CAP), or maximum transfer limit, given by

$$CAP_{nn',tre \in kvtre,y} * 8760 \geq FLOW_{nn',kv,y}^{ely}$$

$$CAP_{nn',tre \in kvtre,y} \geq FLOW_{nn',kv,y}^{plrsv}$$

Transformer-substation maximum capacity limit determines the maximum voltage transformation and reserves for extra high voltage (EHV) and high voltage (HV) transmission. However, for medium voltage (MV), substation capacity must cover all incoming and outgoing transmission lines' capacity. This ensures a must built MV substation for each MV line-connected neighbouring nodes. Detailed design and analysis of lower voltage (LV) transmissions or distribution are out of the scope of study. The constraints governing how voltage transformation flows and capacities interacts are given by,

$$\forall kv \in \{EHV, HV\},$$

$$CAP_{n,sub \in kvsub,y} * 8760 \geq \sum_{kv > kv'} Vup_{n,kv',kv,y}^{ely}$$

$$CAP_{n,sub \in kvsub,y} * 8760 \geq \sum_{kv > kv'} Vdo_{n,kv,kv',y}^{ely}$$

$$CAP_{n,sub \in kvsub,y} \geq \sum_{kv > kv'} Vup_{n,kv',kv,y}^{plrsv}$$

$$CAP_{n,sub \in kvsub,y} \geq \sum_{kv > kv'} Vdo_{n,kv,kv',y}^{plrsv}$$

$$\forall kv \in \{MV\},$$

$$CAP_{n,sub \in kvsub,y} \geq \sum_{n'} CAP_{nn',tre \in kvtre,y} + \sum_{n'} CAP_{n'n,tre \in kvtre,y}$$

4.7 Electricity generation constraints

For all power generating technologies EG the input-output balance of energy conversion and maximum or minimum generation limits are given by,

$$INPUT_{n,eg,v,y} * \eta_{eg} = OUTPUT_{n,eg,v,y}^{ely}$$

$$CAP_{n,eg,v,y} * \widehat{CF}_{eg} * 8760 \geq OUTPUT_{n,eg,v,y}^{ely}$$

$$CAP_{n,eg,v,y} * \widehat{CF}_{eg} * 8760 \leq OUTPUT_{n,eg,v,y}^{ely}$$

The output electricity generated ($OUTPUT^{ely}$) are influenced by the amount $INPUT$ and the energy conversion efficiency η . Plant productions are capped by \widehat{CF} as a factor of annual production. Minimum production threshold \widehat{CF} are set to ensure economic dispatch of large thermal plants.

Fuel-fired based power generation \mathbb{EG}^{firing} uses fuel ($FUEL$) as primary energy input feedstock ($INPUT$) for energy conversion to electricity. For instance, cofiring biomass-coal use mixture of fuels $f \in \mathbb{F}$ as input feedstock for combustion in generating power and convert to electricity. Moreover, the maximum share of type f feedstock fuel in the input mixture is capped with fractions of \widehat{Fmix} for specific generation technology eg . The input fuel feedstock constraints are given by,

$$INPUT_{n,eg,v,y} = \sum_f FUEL_{n,eg,v,f,y}$$

$$INPUT_{n,eg,v,y} * \widehat{fmix}_{eg,f} \geq FUEL_{n,eg,v,f,y}$$

Plant CO₂ emissions are given by,

$$Cems_{n,eg,v,y} = \sum_f INPUT_{n,eg,v,f,y} * emsf_f^{CO_2}$$

$$Cbio_{n,eg,v,y} = \sum_{f \in bioenergy} INPUT_{n,eg,v,f,y} * emsf_f^{CO_2} * neutral_f^{CO_2}$$

Plant annual CO₂ emissions ($Cems$) are accounted based on CO₂ emissions factor of fuels ($emsf_f^{CO_2}$) used and the respective consumption ($INPUT$). Note that biomass-based fuels are considered with a degree of emissions neutrality ($Cems$), which corresponds to the sustainability of sourced biomass.

4.8 Resource constraints

Maximum potential-built capacity and availability of RES power generation \mathbb{EG}^{RES} at given location n is limited by the potential built capacity of RES group (potential^{RES}), given by

$$\forall n \in \mathbb{N}, y \in \mathbb{Y}, \quad \sum_{eg \in \mathbb{EG}^{RES}, v \leq y} CAP_{n,eg,v,y} \leq potential_n^{RES}$$

The potential RES capacities in MW are estimated using a factor of capacity-land density for each RES technology groups: 39 MW/km² for Solar-RES, i.e., Photovoltaic (PV) and Concentrated Solar Power (CSP); and 5 MW/km² for Wind turbines. The area considered for RES-PV and RES-Wind power generation excludes urban developed areas, water bodies, and protected areas. Geothermal and hydropower potential resource are given at distributed point coordinates in MW terms.

The availability of wind and solar resource is given by,

$$INPUT_{n,eg,v,y} \leq N_{n,eg,v,y} * CF_{n,eg}^{WIND}, \quad \forall eg \in \mathbb{EG}^{WIND}$$

$$INPUT_{n,eg,v,y} \leq N_{n,eg,v,y} * surface_{eg}^{PV} * GHI_n, \quad \forall eg \in \mathbb{EG}^{PV}$$

$$INPUT_{n,eg,v,y} \leq N_{n,eg,v,y} * surface_{eg}^{CSP} * DNI_n, \quad \forall eg \in \mathbb{EG}^{CSP}$$

For wind power electricity generation $\mathbb{EG}^{\text{WIND}}$, annual wind generation inputs are capped by the capacity factor of wind resource ($\text{CF}^{\text{Wind IEC}}$) that are geographically distributed and at different levels depending on the class of wind turbine technology suited for in situ wind speed and turbine heights. The classification of wind turbine technology refers to IEC 61400, the International Standard published by the International Electrotechnical Commission regarding wind turbines. Solar energy input is calculated based on by the size of irradiated-surface area multiplied by the average of annual Global Horizontal Irradiance (GHI) for PV \mathbb{EG}^{PV} , or Direct Normal Irradiance (DNI) measured in kWh/m^2 for CSP \mathbb{EG}^{CSP} .

4.9 Capacity balance constraints

Capacity balance constraints ensure the planned capacity deployment with considering previously built, retired, and newly added capacities given by

$$\begin{aligned} \text{CAP}_{n,eg,v,y} = & \sum_{(y-v) \leq \text{life}_{eg}} \text{CAP}_{n,eg,v,y-1} + (\text{NEW}_{i_{n,eg,y}} * \text{typcap}_{eg} + \text{NEW}_{c_{n,eg,y}}) \\ & + \text{Stock}_{n,eg,v,y}[\text{start}(y)], \quad \forall n \in \mathbb{N}, eg \in \mathbb{EG}, v \leq y, y \in \mathbb{Y}, \end{aligned}$$

with $\text{NEW}^{\text{int}} \in \mathbb{Z} \geq 0$, and $\text{NEW}^{\text{cont}} \in \mathbb{R} \geq 0$

In all locations \mathbb{N} , deployed generation capacity (CAP) of technology type eg in current period y includes the deployed capacities in previous period ($y - 1$), minus capacities that vintages v exceed their economic lifetime, and plus new capacity additions (NEW). The quantity of installed and retired capacities is defined in real numbers. New capacity additions are defined in both integers ($\text{NEW}^{\text{int}} \in \mathbb{Z}$) and real numbers ($\text{NEW}^{\text{cont}} \in \mathbb{R}$), respective to larger or smaller capacity numeration. Stock capacities (STK) are taken into account in the initial period of the planning horizon to avoid double counting.

Electricity transformer-substation (sub), transmission line (tre), and CO_2 transport (trc) capacities are assumed to have no retirement and the only way is to expand, given by

$$\begin{aligned} \text{CAP}_{n,sub,y} &= \sum_{v \leq y} \text{NEW}_{n,sub,v} * \text{typcap}_{sub} + \text{STK}_{n,sub,y} \\ \text{CAP}_{nn',tre,y} &= \sum_{v \leq y} \text{NEW}_{nn',tre,v} * \text{typcap}_{tre} + \text{STK}_{nn',tre,y} \\ \text{CAP}_{nn',trc,y} &= \sum_{v \leq y} \text{NEW}_{nn',trc,v} * \text{typcap}_{trc} + \text{STK}_{nn',trc,y}, \end{aligned}$$

with $\text{NEW}^{\text{int}} \in \mathbb{Z} \geq 0$, and $\text{NEW}^{\text{cont}} \in \mathbb{R} \geq 0$