Computer Organisation and Architecture Course Code: C0206

Objective

To provide knowledge about the principles, concepts and applications of Computer Organization and Architecture.

Course Description(Module-wise)

Module No	Title of Module	Number of Lectures
1	Introduction	8
2	Control Unit	8
3	Central Processing Unit	9
4	Input / Output Organisation	4
5	Modes of Data Transfer	5
6	Memory	8

Detailed Syllabus

S.No.	Contents	Contact Hours
1.	Introduction: Digital computer generation, computer types and classifications, functional units and their interconnections, bus architecture, types of buses and bus arbitration. Register, bus and memory transfer. REGISTER TRANSFER LANGUAGE: Data movement around registers. Data movement from/to memory, arithmetic and logic micro operations. Concept of bus and timing in register transfer.	8
2.	Control Unit: Instruction types, formats, instruction cycles and subcycles (fetch and execute etc.), micro-operations, execution of a complete instruction. Hardwired and microprogrammed control: microprogrammed sequencing, wide branch addressing, and micro-instruction with next address field, pre-fetching microinstructions, concept of horizontal and vertical microprogramming.	8
3.	Central Processing Unit: Addition and subtraction of signed numbers look ahead carry adders. Multiplication: Signed operand multiplication, Booths algorithm and array multiplier. Division and logic operations. Floating point arithmetic operation, Processor organization, general register organization, stack organization and addressing modes.	9
4.	Input/Output organization: Peripheral devices, I/O interface, I/O ports, Interrupts: interrupt hardware, types of interrupts and exceptions.	4
5	Modes of Data Transfer: Programmed I/O, interrupt initiated I/O and Direct Memory Access. I/O channels and processors. Serial Communication: Synchronous & asynchronous communication, standard communication interfaces.	5
6.	Memory: Basic concept and hierarchy, Main memory, Auxiliary memory, Associative memory, Cache memories: concept and design issues, associative mapping, direct mapping, set-associative mapping, cache writing and initialization.	8
TOTAL		

Recommended Reading Material

Text Books:

- 1. Patterson, Computer Organization and Design, Elsevier Pub, 2009
- 2. Morris Mano, Computer System Architecture, PHI
- 3. William Stalling, Computer Organization, PHI

Reference Books:

- 1. Vravice, Hamacher&Zaky, Computer Organization, TMH
- 2. Tannenbaum, Structured Computer Organization, PHI

Evaluation Criteria

Component	Description
Credits	4
Contact Hours	Theory: 3 Hours Tutorial: 1 Hours
Relative Weightage	CWS: 25 MTE: 25ETE: 50
Total	100

Component	Sub Components
Class Work Sessional(CWS)	Presentation, Seminar, Viva, Attendance
Mid Term Examination(MTE)	Innovative Project
End Term Examination(ETE)	CT1,CT2,CT3, Minor Test1, Minor Test 2

Contents of Module 1

- Digital computer generation
- Computer types and classifications
- Functional units and their interconnections
- Bus architecture
- Types of buses and bus arbitration
- Register transfer language
- Data movement around registers
- Data movement from/to memory
- ☐ Arithmetic and logic micro-operations
- Concept of bus and timing in register transfer

Prefac

Who is generally known as "Father of Digital Computers"? Charles Babbage. Which is World's first general purpose electronic digital computer? **ENIAC: Electronic Numerical Integrator and Computer(1946).** What is a Computer? It is an electronic device that takes some input, process it and gives some output. What is Computer Architecture? It refers to those attributes that have a direct impact on the logical execution of a program. What is Computer Organization? Itrefers the operational units and their interconnections that * to realize the architectural specifications

Difference between Computer Organisation & Architecture

Computer Architecture	Computer Organisation
What does the system do?	How does the system do?
Deals with High level design issue	Deals with Low level design issue
Describes the functional behaviour	Describes the structural relationship
While designing a computing system, computer architecture is approached first	Computer organisation is approached after we have finalised the computer architecture
It involves instruction sets, addressing modes and data types	It involves the circuit design, signals, ALU, CPU and memory

Digital Computer Generation

	Approxima		Typical Speed
Generati	te	Technolo	(operations per
on 1	194 6ade \$57	Vacuum tube 40,000	second)
2	1958–1964	Transistor 200,000	
3	1965–1971	Small and medium scale integration	1,000,000
4	1972–1977	Large scale integration 10,0	000,000
5	1978–1991	Very large scale integration	100,000,000
6	1991-	Ultra large scale integration	1,000,000,000

First Generation-Vacuum Tubes (1946-1957)

- It had more than 1800 Vacuum tubes and 1500 relays
 Able to perform nearly 5000 additions or subtraction per second
 It was a decimal rather than a binary machine
 It had memory of 20 accumulators, each capable of storinga ten digit decimal number.
 It had weight of 30 tons covering area of 15000 sq. ft with power consumption of 140kW.
- □ John Von Neumann introduced concept of stored program to design computer- EDVAC(Electronic Discrete Variable Computer)
- → Assembly language was used to prepare programs and was translated into machine language for execution

Second Generation-Transistors (1958-1964)

transistors (semiconductor device which are smaller, Used cheaper and dissipates less heat) Greater **speed**, Larger **memory capacity**, smaller **size** than first generation Magnetic disks were used for secondary memory They had **separate I/O processors** having direct access to main memory It could handle both floating point and fixed point operations. Support **higher level programming languages**(Fortran) Provision of **system software**(compilers) 12 **Concept of multiprogramming was developed** in systems

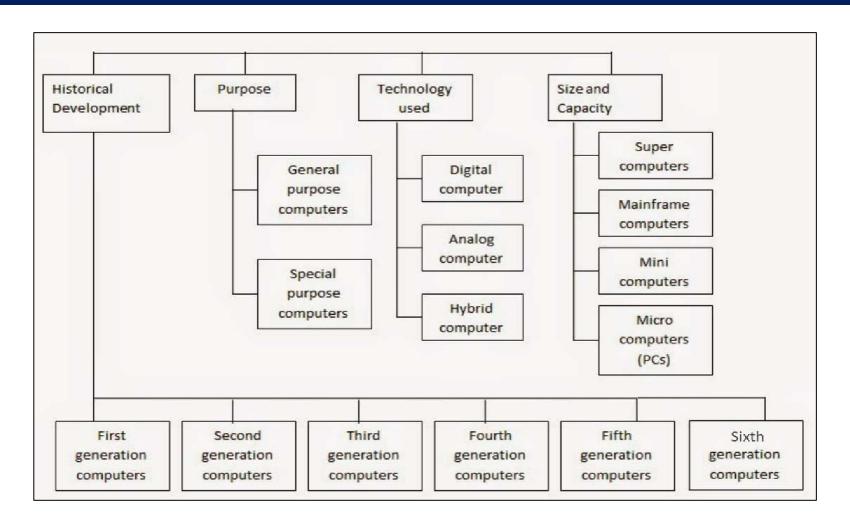
Third Generation-Small and Medium Scale Integration (1965-1971)

- Used Integrated circuits(ICs)
- ICs enabled lower cost, faster processors and development of chips
- Magnetic core memories were replaced by ICs memories
- Various techniques introduced
 - Microprogramming
 - Parallel Processing
 - Sharing resources

Later Generation

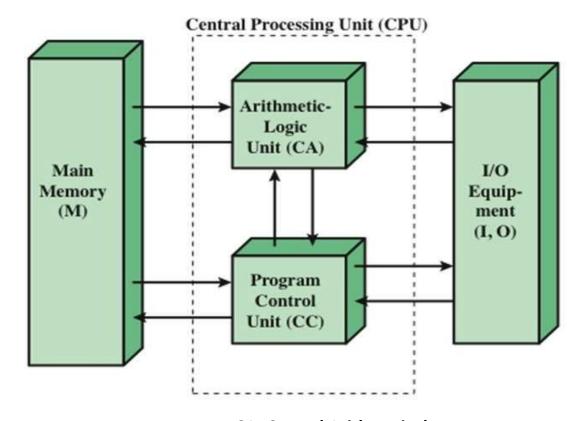
- Beyond the third generation there is less general agreement on defining generations of computers.
- Large Scale Integration(1972-1977)
 - ☐ More than 1000 components can be placed on a single integrated circuit chip
- Very Large Scale Integration(1978-1991)
 - ☐ More than 10,000 components per chip
- ☐ Ultra Large Scale Integration(1991-..)
 - ☐ More than one billion components

Computer types and classification



Von Neumann Architecture

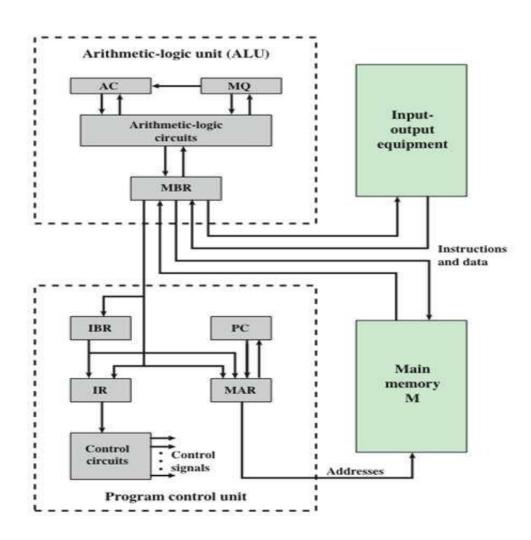
- In 1946, von Neumann and his colleagues began the design of a new stored program Computer
- Also referred to as the IAS computer, at the Princeton Institute for Advanced Studies.
- The IAS computer, although not completed until 1952, prototype is the of all general-purpose southers.



CA: Central Arithmetical

CC: Control Center

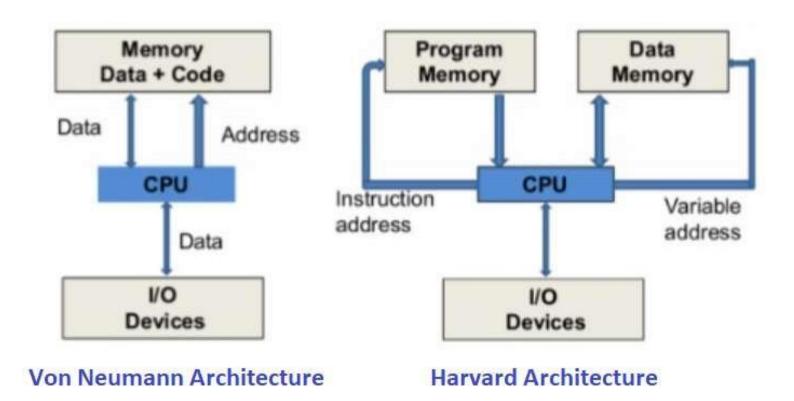
Internal Structure of Von Neumann Architecture



Components in Von Neumann Architecture

Accumulator (AC) and Multiplier quotient (MQ)	• Employed to temporarily hold operands and results of ALU operations
Memory buffer register (MBR)	 Contains a word to be stored in memory or sent to the I/O unit It is used to receive a word from memory or from the I/O unit
Instruction buffer register (IBR)	Employed to temporarily hold the right-hand instruction from a word in memory
Program counter (PC)	Contains the address of the next instruction pair to be fetched from memory
Memory address register (MAR)	• Specifies the address in memory of the word to be written from or read into the MBR
Instruction register (IR)	It is used to hold the instructions that is currently being executed

Von Neumann Architecture Vs. Harvard Architecture



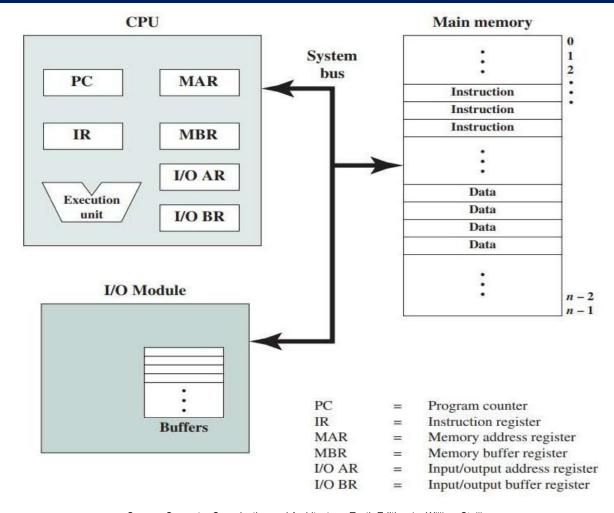
Von Neumann Architecture Vs. Harvard Architecture

von Neumann Architecture	Harvard Architecture
Only one main memory	Two memory units i.e. one for data and another for program
System with one bus design is simpler	System with two bus is complex
Free memory space can be used for data or program	Free memory space in data cant be used for program or vice versa
Economical design	Costlier design
Commonly used in PCs, Laptops, workstations	Used primarily for small embedded systems and signal processing

Von Neumann Bottleneck/Memory Wall

- Because of the stored program architecture of the Von-Neumann Machine, the processor performance is tightly bound to the memory performance.
- ☐ We need to access memory at least once per cycle to read an instruction, the processor can only operate as fast as the memory.
- This is sometimes known as Von Neumann bottleneck or Memory wall.

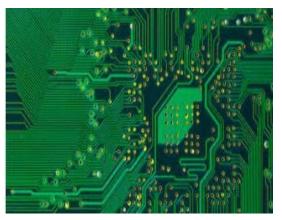
Functional Units and their Interconnections



Bus

- A group of wires that connects two or more communication is called a BUS. It can be a cable or printed in circuit. hardware
- ☐ It reduces the number of pathways between interconnecting hardware components
- ☐ A bus that connects the major components with CPU i.e. memory & I/O is called System Bus.
- ☐ The term "width" is used to refer the number of bits that a bus can transmit at once

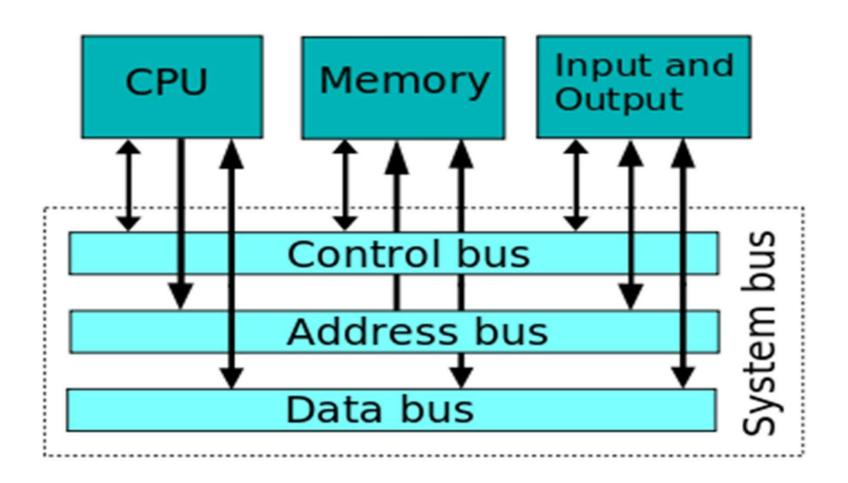




Some major functions of Bus in Computers

- □ Data transfer
- Addressing
- □ Timing/Synchronization
- Power

Bus Architecture



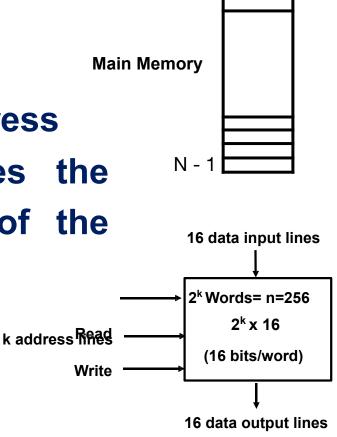
Types of Bus(on the basis of contents)

- Data Bus
- Address Bus
- Control Bus

Memory Components

Main Memory

- -Each word has a unique address
- -Access to a word requires the same time, independent of the location of the word



Data Bus (Data Lines)

- Carries data throughout the system
- These are bi-directional lines
- Width is a key factor.
 - ☐ It determines the number of bytes that can be transferred in one cycle and hence the overall performance of the system.

Address Bus (Address Lines)

- Designate source or destination of data on the bus
- It is an unidirectional bus.
- Width determines the maximum possible memory capacity of the system.
- ☐ Also used to address I/O ports
 - ☐ High order bits selects a particular module
 - ☐ Lower order bits select a memory location or I/O port within the memory

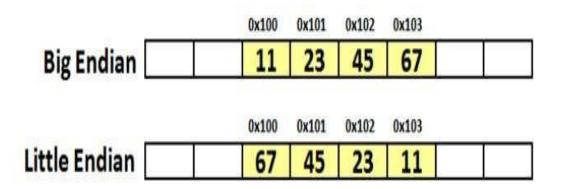
Control Bus (Control Lines)

- ☐ Usedto provide synchronization between CPU and system components other
- Control lines include
 - Memory read and Memory write
 - ☐ I/O read and I/O write
 - □ Transfer Acknowledgment
 - Bus request and bus grant
 - ☐ Interrupt request and interrupt acknowledgement
 - □ Clock
 - ☐ Reset

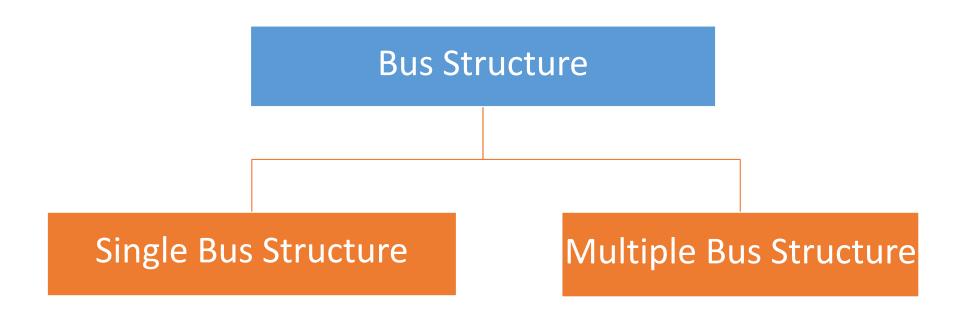
Representation of Data in Memory

- If we need to store a data=11234567 in memory then the representation can be done its in two ways
- □ Big Endian
 - ☐ MSB will be stored first
 - ☐ Intel, ARM processors
- Little Endian
 - ☐ LSB will be stored first
 - ☐ Motorola, PowerPC, SPARK



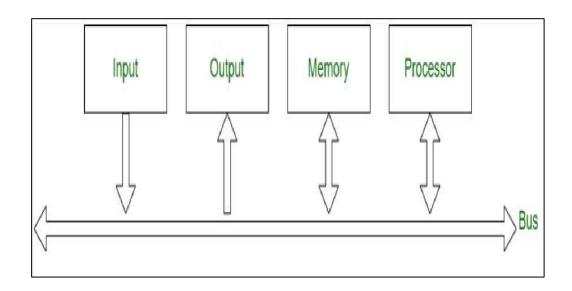


Types of Bus (on the basis of number of bus)



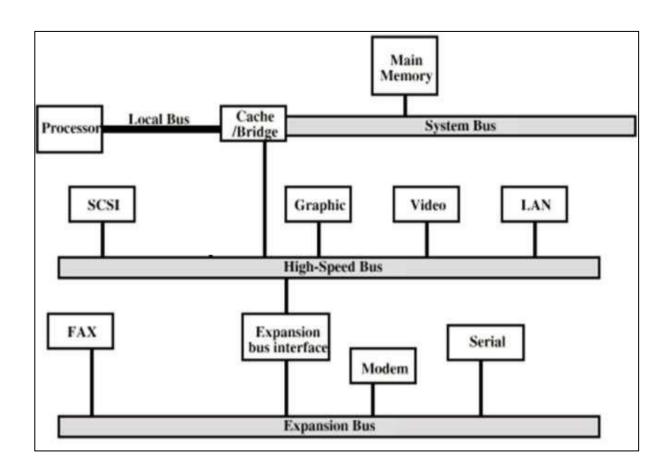
Single Bus Structure

- Pros and Cons
 - ✓ Cheaper
 - ✓ Easier design
 - ✓ Low performance
 - ✓ Limited Capacity
 - ✔ Propagation delay



Multiple Bus Structure

- Pros and Cons
 - ✓ High performance
 - ✓ Complex design
 - ✓ Scalable
 - ✓ Faster access
 - ✓ Costlier



Bus Arbitration

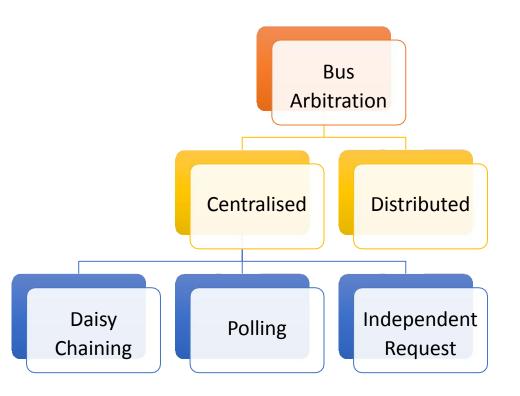
- □ The device which is allowed to initiate the data transfer on the bus at any given point of time is called the BUS MASTER.
- □ In computer system, there may be more than one bus master such as processor, DMA controller etc. They share the system bus.
- □When **one master relinquish control** of the bus, **another bus master can acquire the control** of the Bus.
- □ Bus Arbitration refers to the transfer of control of bus from one master to another.

Important terminology in Bus Arbitration

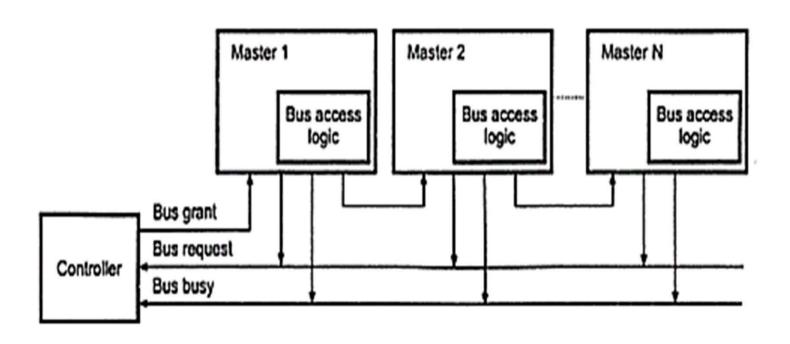
- Bus Master
 - A controller who has currently access to the bus
- Bus Arbiter
 - It decides who would become the next bus master
- Bus Request(BRQ)
 - It is used by a module to request the control of the bus
- Bus Grant(BGT)
 - •It is signal which indicates that theaccess to the bus is granted

Types of Bus Arbitration

- Centralised Arbitration
 - ☐ Single hardware device controlling the bus access.
 - ☐ May be part of CPU or separate
- Distributed Arbitration
 - ☐ Any module may claim the bus
 - Access control logic is on all modules
 - Modules work together to control bus



Daisy Chaining method



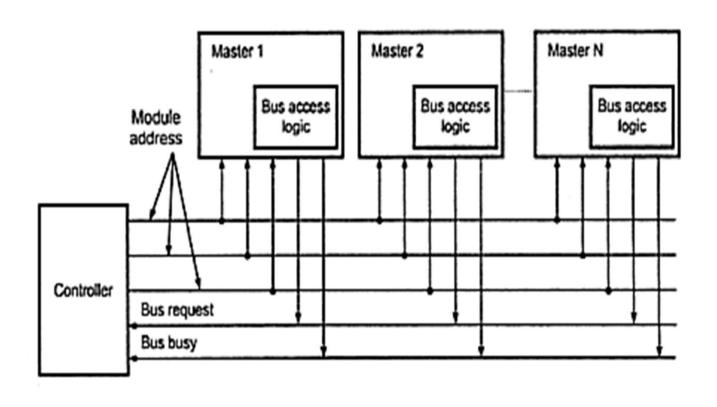
Daisy Chaining method

- ☐ It is **simple and cheaper** method
- ☐ All masters make use of the same line for bus request
- □ In response to a bus request, the controller sends a bus grant signal if the bus is free.
- ☐ The bus grant signal propagates through each master until it reaches the device which has requested the access to the bus.
- ☐ The requesting master blocks the propagation of the bus grant signal, activates the busy line and gains control of the bus.
- □ Any other master requesting module will not receive the grant signal and hence cannot get bus access.

Daisy Chaining method

- Advantages
 - It is simple and cheaper method
 - It requires least number of lines
 - •Independent of the number of masters in the system
- Disadvantages
 - •Propagation delay is proportional to number of masters in the system
 - Slow arbitration time
 - Priority is based on the physical location
 - Failure of any one master may cause the failure of whole system

Polling or Rotating Priority Method



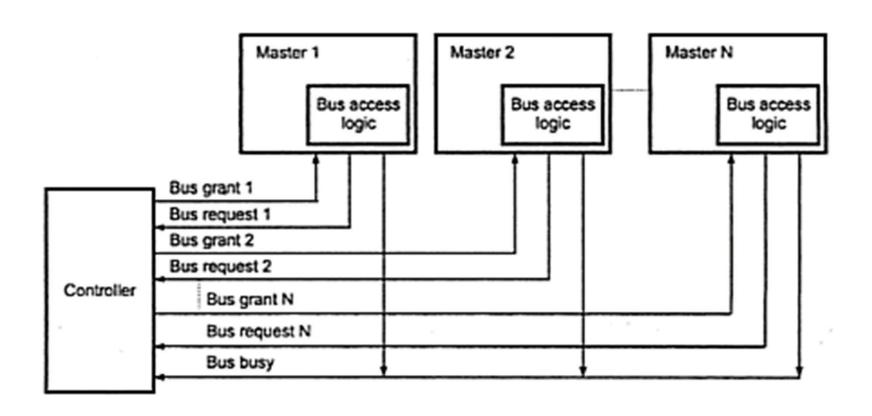
Polling or Rotating Priority Method

- ☐ The controller is used to generate the addresses for the master.
- ☐ The number of address line required depends on the number of master connected in the system.
- ☐ For example, if there are **8 masters connected** in the system, at least **three address lines are required**.
- ☐ In response to the bus request, controller generates a sequence of master address.
- When the requesting master recognizes its address, it activates the busy line and begins to use the bus.

Polling or Rotating Priority Method

- Advantages
 - The priority can be changed by altering the polling sequence stored in the controller
 - Fast arbitration
 - •If one of the module fails, entire system does not fail
- Disadvantages
 - •Increasing the size will require more number of address
 - lines

Independent Request or Fixed Priority method



Independent Request or Fixed Priority method

- □ In this scheme each master has a separate pair of bus request and bus grant lines
- ☐ Each pair has a priority assigned to it.
- □ The built in priority decoder within the controller selects the highest priority request and provides the corresponding bus grant signal

Independent Request or Fixed Priority method

- Advantages
 - Due to separate pairs of bus request and bus grant signals, arbitration is fast and is independent of the masters in the system
 - Very less chance of failure
- Disadvantages
 - It requires more bus request and grant signals
 - Costlier
 - Chance of starvation

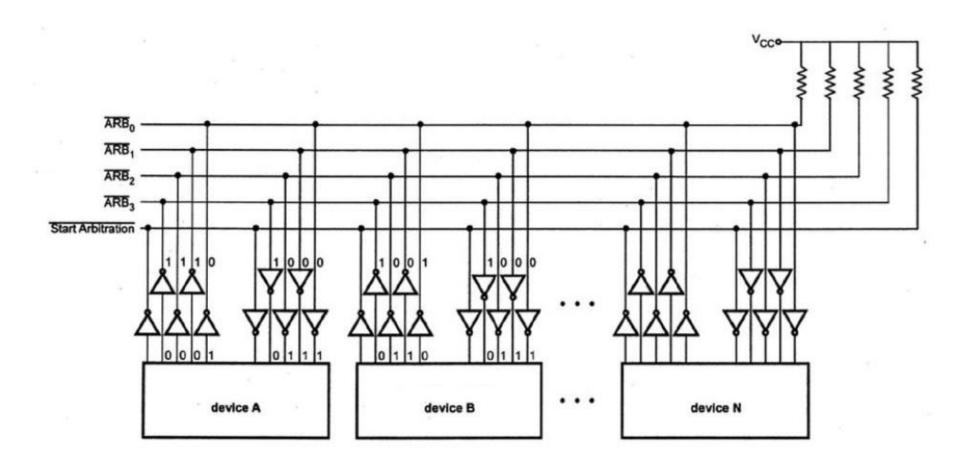
Distributed Arbitration

In distributed arbitration, all devices participate in the selection of the next bus
master.
In this scheme each device on the bus is assigned a 4-bit identification number.
When one or more devices request for the control of bus, they assert the start-
arbitration signal and place their 4-bit ID numbers on arbitration lines, ARBO through
ARB3.
These four arbitration lines are all open-collector. Therefore, more than one device
can place their 4-bit ID number to indicate that they need to control of bus.
In this method, the device having highest ID number has highest priority.
When two or more devices place their ID number on bus lines then it is necessary to
identify the highest ID number from the status of bus line.
The decentralized arbitration offers high reliability because operation of the bus is not
dependent on any single device

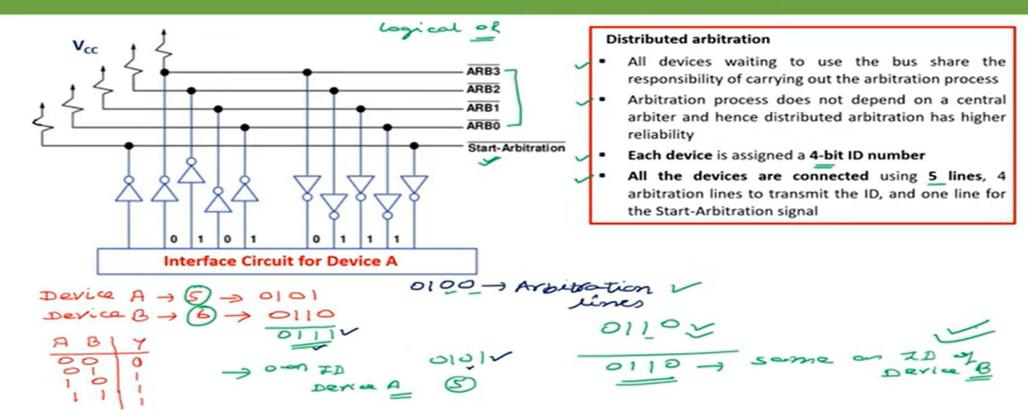
Distributed Arbitration example

- ☐ Consider that two devices A and B, having ID number 1 (0001) and 6(0110), respectively are requesting the use of the bus.
- □ Device A puts the bit pattern 0001, and device B puts the bit pattern 0110. With this combination the status of bus-line will be 1000(for instance, XNOR of the bits); however because of inverter buffers, code seen by both devices is 0111.
- ☐ Each device compares the code formed on the arbitration line to its own ID, starting from the most significant bit. If there is a match, the output bit remains same but If it finds the difference at any bit position, it disables its drives by placing a 0 at that bit position as well as for all following lower-order bits
- ☐ In our example, device A detects a difference on line ARB2 and hence it disables its drives on line ARB2, ARB1 and ARB0. Thus, it's codes becomes 0000. Device B detects a difference on line ARB0 and hence it disables its drives on line ARB0. This causes the code on the arbitration lines to change to 0110. Device B is having highest number which means that device B has won the race.

Distributed Arbitration example



Distributed Bus Arbitration



To request the bus a device:

- Asserts the Start-Arbitration signal
- Places its 4-bit ID number on the arbitration lines
- The pattern that appears on the arbitration lines is the logical-OR of all the 4-bit device IDs placed on the arbitration lines
- Device A has the ID 5 and wants to request the bus:- Transmits the pattern 0101 on the arbitration lines
- Device B has the ID 6 and wants to request the bus:- Transmits the pattern 0110 on the arbitration lines
- Pattern that appears on the arbitration lines is the logical OR of the patterns:- Pattern 0111 appears on the arbitration lines

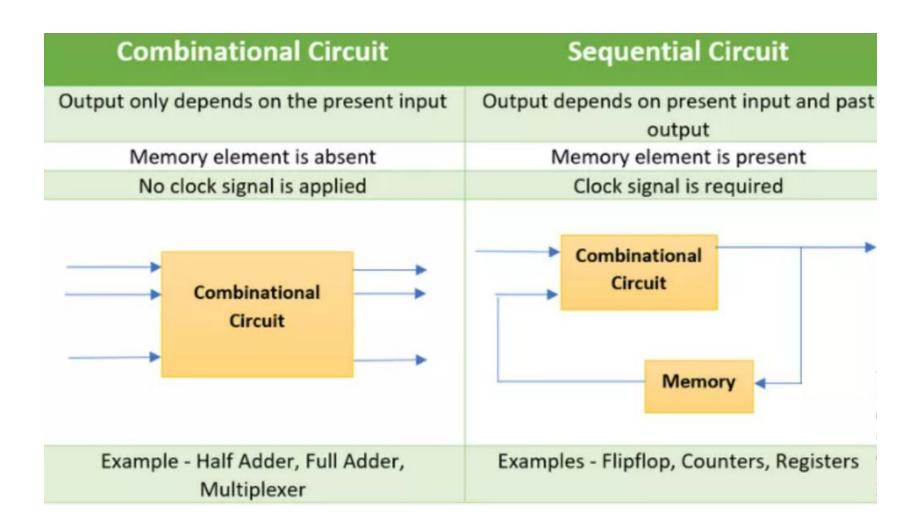
Arbitration process:

- Each device compares the pattern that appears on the arbitration lines to its own ID, starting with MSB
- If it detects a difference, it transmits 0s on the arbitration lines for that and all lower bit positions
- Device A compares its ID 5 with a pattern 0101 to pattern 0111
- It detects a difference at bit position 0, as a result, it transmits a pattern 0100 on the arbitration lines
- The pattern that appears on the arbitration lines is the logical-OR of 0100 and 0110, which is 0110
- This pattern is the same as the device ID of B, and hence B has won the arbitration

Digital Systems

- ☐ Combinational and sequential circuits can be used to create simple digital systems
- ☐ The combinational circuit is time-independent. The output it generates does not depend on any of its previous inputs.
- □ Sequential circuits are the ones that depend on clock cycles. They depend entirely on the past as well as the present inputs for generating output.
- ☐ Simple digital system or module is frequently characterized in terms of
 - Set of registers and their functions
 - Set of Micro-operations
 - Control signals that initiate the sequence of micro-operations
- □ Such digital system or module are interconnected with common data and control path to form a digital computer system.

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Register and micro-operation

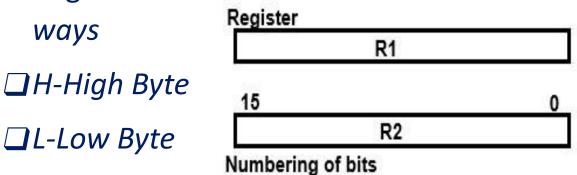
- ☐ A Register is a group of flip flops.
- □ An elementary operation performed (in one clock cycle) on the data stored in one or more registers is called micro-operations.
- ☐ There are **four types of micro-operations** in computer systems
 - Register Transfer micro-operations
 - Arithmetic micro-operations
 - Logic micro-operations
 - Shift micro-operations

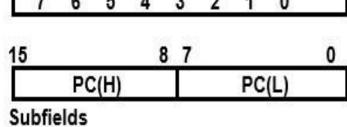
Register Transfer Language (RTL)

- □ Rather than specifying a digital system in words, a specific notation is used which is called Register Transfer Language
- ☐ For any function of the computer, the register transfer language can be used to describe the sequence of microoperations
- □ A Register Transfer Language is
 - A symbolic language
 - a convenient tool for describing the internal organization of digital computers
 - Can also be used to facilitate the design process of digital system

Designation of Registers

- □ Registers are designated by capital letters, sometimes followed by numbers (e.g., A, R13, IR)
- Often the names indicate function:
 - MAR memory address register
 - □ PC- program counter
 - □ IR- instruction register
- ☐ Registers and their contents can be viewed and represented in *various*





Showing individual bits

Registers Transfer

- ☐ Copying the contents of one register to another is a register transfer
- A register transfer is indicated as

R2 ← R1

- ☐ In this case the contents of register R1 are **loaded**(copied) into register R2
- ☐ A **simultaneous transfer** of all bits from the source R1 to the destination register R2, during one clock pulse
- ☐ Note that this is a **non-destructive**; i.e. the contents of R1 are not altered by loading(copying) them to R2

Registers Transfer

□ A register transfer such as

 $R3 \leftarrow R5$

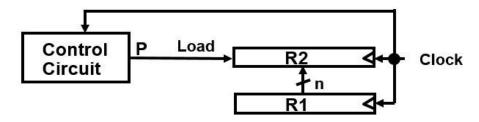
- ☐ Implies that the digital system has
 - the data lines from the source register (R5) to the destination register (R3)
 - Parallel load in the destination register (R3)
 - Control lines to perform the action

Registers Transfer

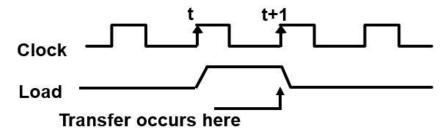
- Often actions need to performed only if a certain condition is true
- ☐ Similar to an "if" statement in a programming language
 - In digital systems, this is often done via a *control signal*, called a *control function*
 - If the signal is 1, the action takes place
- ☐ This is represented as:
 - P: R2 ← R1
 - Which means "if P = 1, then load the contents of register R1 into register R2", i.e., if (P = 1) then $(R2 \leftarrow R1)$

Registers Transfer & Timing Diagram

- Implementation of controlled transfer :
 - P: R2 ← R1
- □ Block diagram



□ Timing diagram



- The same clock controls the circuits that generate the control function and the destination register
- > Registers are assumed to use *positive-edge-triggered* flip-flops

Basic symbols for register transfer

Symbol	Description	Examples
Capital letters & numerals	Denotes a register	MAR, R2
Parentheses ()	Denotes a part of a register	R2(0-7), R2(L)
Arrow ←	Denotes transfer of information	R2 ← R1
Colon :	Denotes termination of control function	P:
Comma,	Separates two micro-operations	A ← B , B ← A

Register Transfer

Basic Symbols used for Register Transfer

	Symbol	Description	Example
¥	Letters and Numbers	Denotes a Register	MAR, R1, R2
,	()	Denotes a part of register	R1(8-bit) R1(0-7)
1	<-	Denotes a transfer of information	R2 <- R1
*	,	Separate two micro-operations	R1 <- R2 , R2 <- R1
	:	Denotes conditional operations	P: R2 <- R1 if P=1
-	Naming Operator (:=)	Denotes another name for an already existing register/alias	Ra := R1

1. Register Transfer

Copying the content of one register to another

2. Control Function

Similar to "if" statement in a programming language

3. Simultaneous Operations

Two or more operations are to occur simultaneously

P:
$$R_3 \leftarrow R_5$$
, MAR \leftarrow IR
$$P = 1$$

Data movement around

- □ In a digital system with many registers, it is impractical to have data and control lines to directly allow each register to be loaded with the contents of every possible other registers
- \square To completely connect n registers \square n(n-1) lines
 - $O(n^2)$ cost
 - This is not a realistic approach to use in a large digital system
- Instead, take a different approach
- Have one centralized set of circuits for data transfer the bus
- ☐ Have control circuits to select which register is the source, and which is the destination

Data movement around registers using Bus

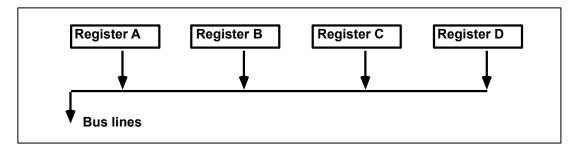
Depending on whether the bus is to be mentioned explicitly or not, register transfer can be indicated as either

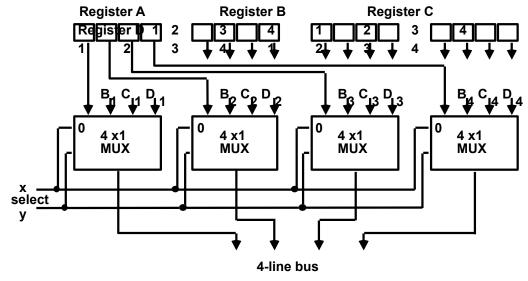
$$R2 \leftarrow R1$$
 or

☐ In the former case the bus is implicit, but in the latter, it is explicitly indicated

Data movement from Register to Bus

☐ From a register to bus: BUS ← R





What is Multiplexer (MUX)?

- ☐ Also called **data selectors**.
- \square Basic function: **select one of 2^n data input lines** and **place** coits esponding information **onto a single output** line.
- lacktriangle n input bits needed as selection to specify which input line is to be

selected. n

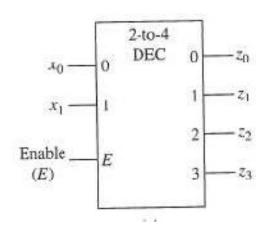
Place binary code for a desired data input line onto its select input lines.

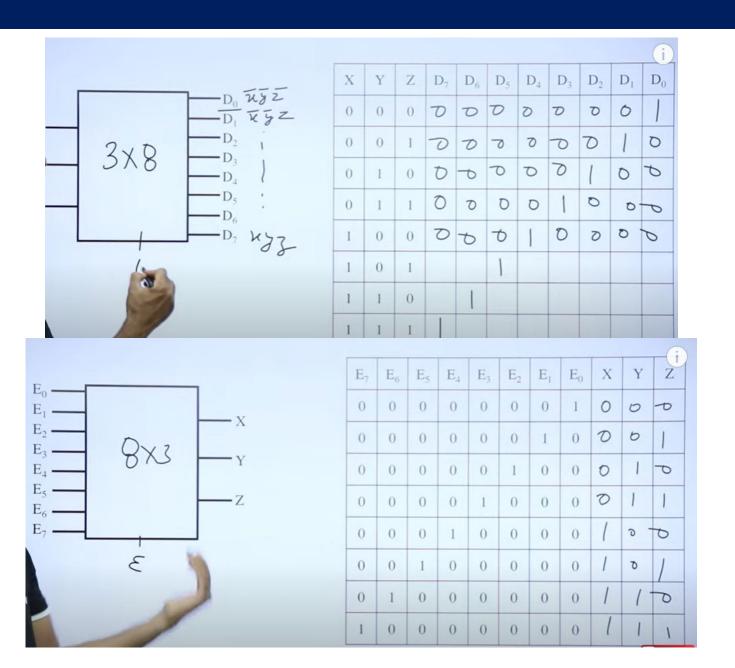
Select		Output		4-t	p-1		
S ₁	So	f	I ₀		JX		
0	0	I ₀	$$ I_1				
0	1	l ₁	I_2			f	
1	0	l ₂	13				
1	1	I_3	E	S_1	S_0		

What is Decoder?

- □ A decoder has
 - n inputs
 - \square 2ⁿ outputs
- □ A decoder selects one of 2ⁿ outputs by decoding the binary value on the n inputs
- Exactly one output will be active for each combination of the inputs.

	Inputs		Outputs				
	E	x_1	x_0	₹0	z_1	z_2	Z3
	0	×	×	0	0	0	0
	1	0	0	1	0	0	0
	1	0	1	0	1	0	0
1	1	1	0	0	0	1	0
	1	1	1	0	0	0	1

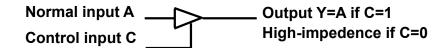




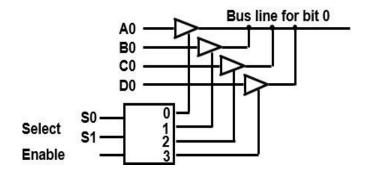
Data movement from Register to Bus

☐ From a bus to register: Bus ← R

Three-State Bus Buffers

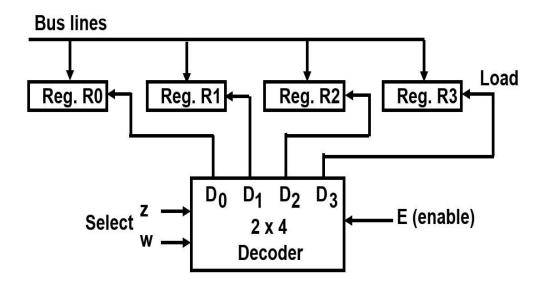


Bus line with three-state buffers



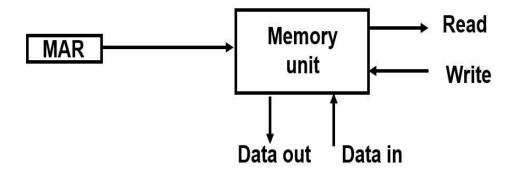
Data movement from Bus to Register

☐ From a bus to register: R ← BUS



Data movement from/to Memory

- ☐ The memory is viewed as a device, M at the register level.
- ☐ Since it contains multiple locations, we must specify which address in memory we will be using
- This is done by indexing memory references
- Memory is usually accessed in computer systems by putting the desired address in a special register, the Memory Address Register (MAR, or AR)
- When memory is accessed, the contents of the MAR is sent to the memory unit's address lines



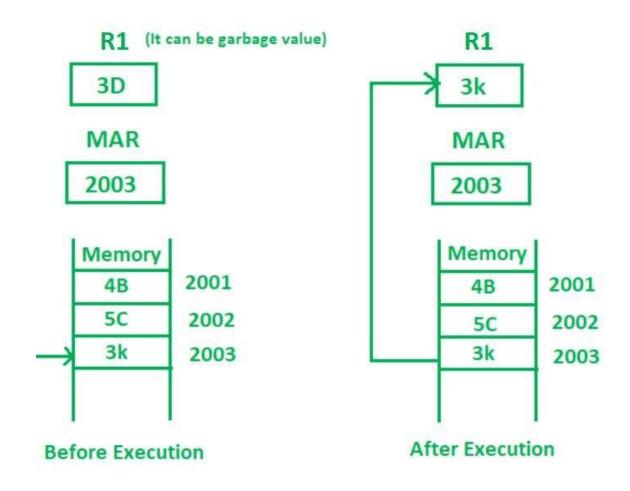
Data Transfer from Memory to Register

☐ To read a value from a location in memory and load it into a register, the register transfer language notation looks like this:

$R1 \leftarrow M[MAR]$

- This causes the following to occur
 - The contents of the MAR is sent to the memory address lines
 - A Read= 1 signal is sent to the memory unit
 - The contents of the specified address are put on the memory's output data lines
 - The contents is sent over the bus to be loaded into register R1

Data Transfer from Memory to Register



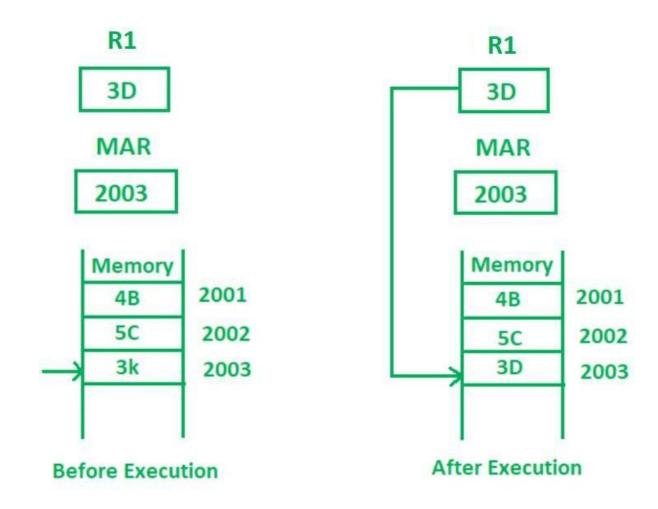
Data Transfer from Register to Memory

☐ To write a value from a register to a location in memory, it is represented in register transfer language as:

$M[MAR] \leftarrow R1$

- This causes the following to occur
 - The contents of the MAR is sent to the memory address lines
 - A Write (= 1) gets sent to the memory unit
 - The values in register R1 is sent over the bus to the data input lines of the memory
 - The values get loaded into the specified address in the memory
 - decoder selects one of 2N outputs by decoding the binary value on the N inputs

Data Transfer from Register to Memory



Summary of Register Transfer micro-operations

A ← B Transfer content of register B into register A

A ← constant Transfer a binary constant into register A

ABUS ← R1, R2 ← ABUS Transfer content of R1 into bus A and, at the same time, Transfer content of bus A into R2

MAR Memory Address register

MDR Memory Data register

M[R] Memory word specified by register R

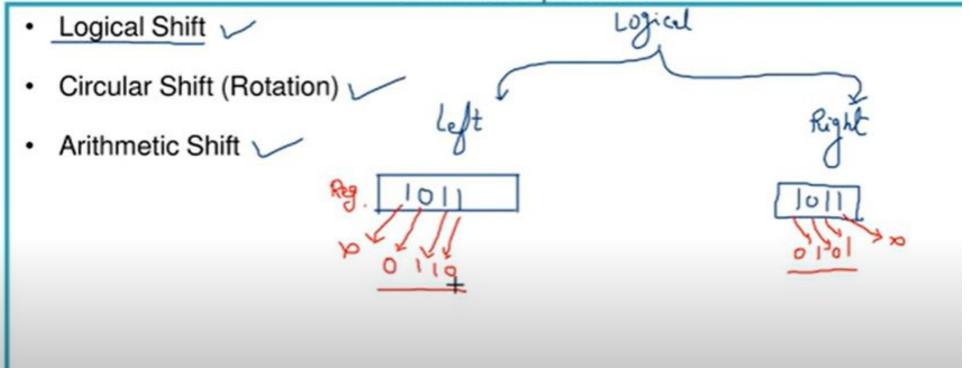
M Equivalent to M[MAR]

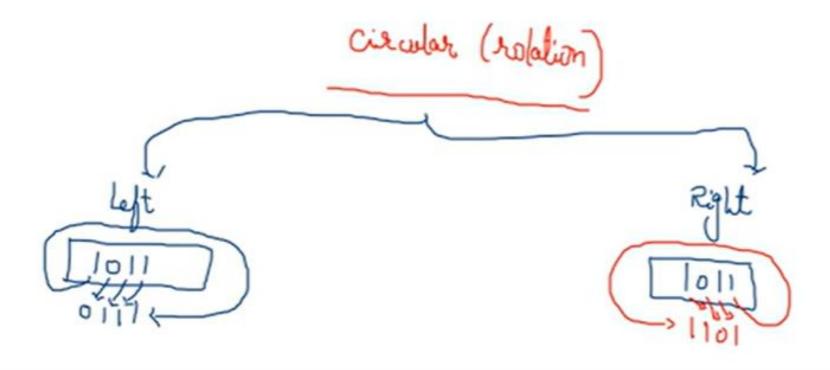
MDR ← M Memory read operation: transfers content of memory word specified by MAR into MDR M ← MDR

Memory write operation: transfers content of MDR into memory word specified by MAR

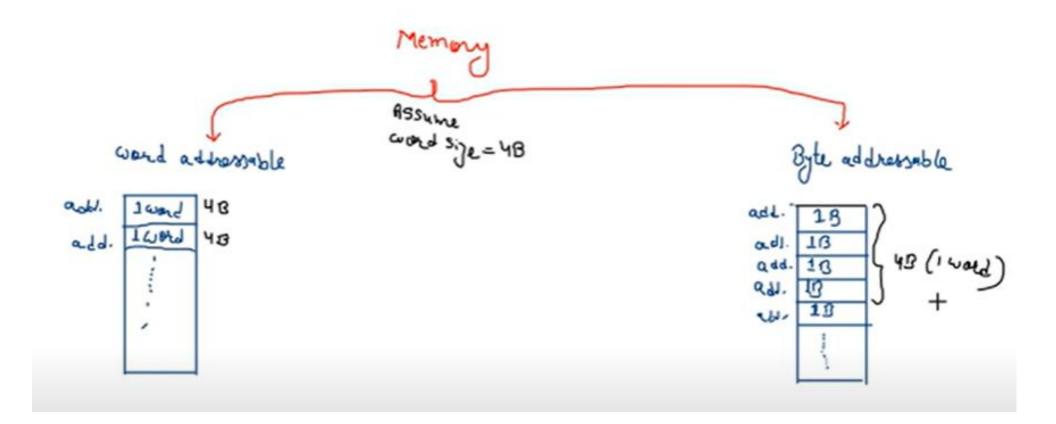
Types of MicroOperations

Shift MicroOperations





Arithmetic shift (Applied on Signed numbers - After the slift sign of the number should remain some. It is some as logical left shift hat it is allowed only when sigh is not going to change. 10 11 =) -ve allowed not-albured Dura - Arithmetic left shift overflow.

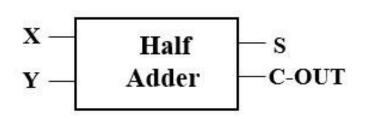


Arithmetic Micro-Operations

- The basic arithmetic micro-operations are
 - Addition
 - Subtraction
 - Increment
 - Decrement
- The additional arithmetic micro-operations are
 - Add with carry
 - Subtract with borrow
 - Transfer/Load

Half Adder

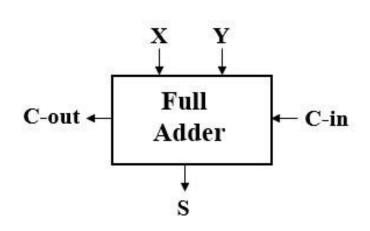
☐ Adding two single-bit binary values, X, Y and produces a sum bit S and a carry out C-out bit.



ıputs	Ou	tputs
\mathbf{Y}	S	C-out
0	0	0
1	1	0
0	1	0
1	0	1
	Y 0 1 0 1	

Full Adder

Adding two single-bit binary values, X, Y along with a carry input bit C-in and produces a sum bit S and a carry out C-out bit.

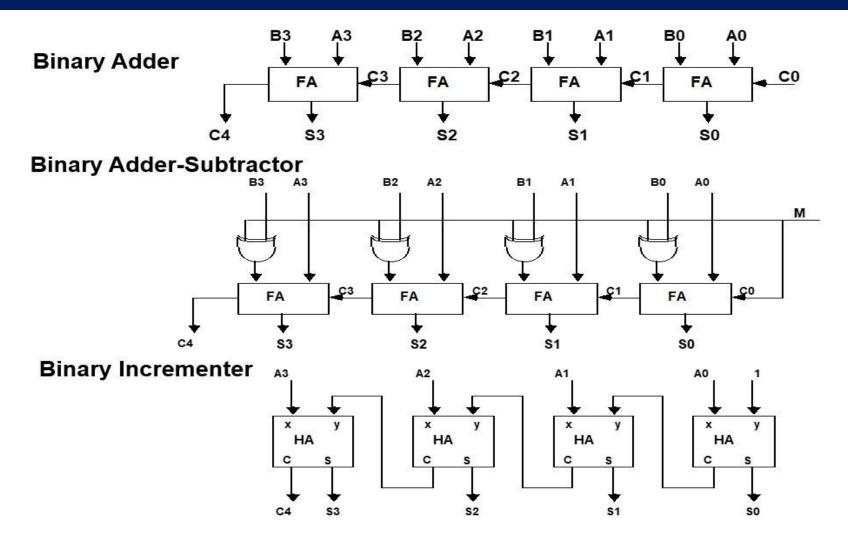


	inputs Outputs			Outputs
X	\mathbf{Y}	C-in	S	C-out
0	0	0	0	0
0	0	1	1	0
0	1	0	1	0
0	1	1	0	1
1	0	0	1	0
1	0	1	0	1
1	1	0	0	1
1	1	1	1	1

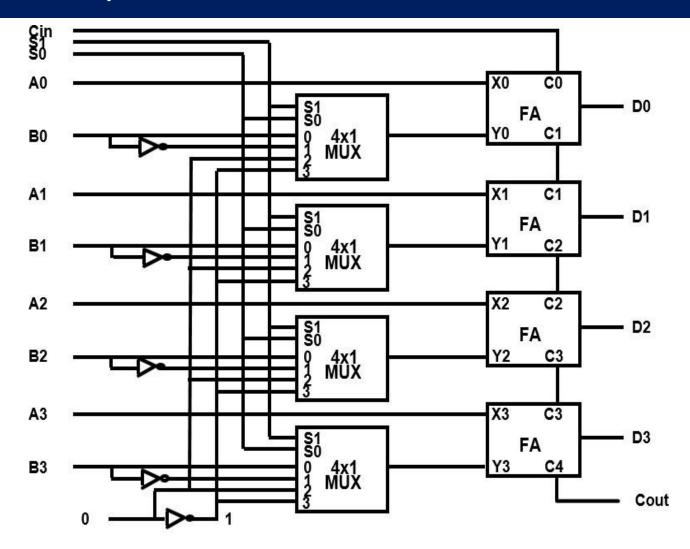
Innuts

Outnuts

Binary Adder/Subtractor/Incrementer



Hardware for Binary Adder/Subtractor/Incrementer/Decrementer



Truth Table for Binary Adder/Subtractor/Incrementer/Decrementer

S 1	S0	Cin	Υ	Output	Microoperation
0	0	0	В	D = A + B	Add
0	0	1	В	D = A + B + 1	Add with carry
0	1	0	B'	D = A + B'	Subtract with borrow
0	1	1	B'	D = A + B' + 1	Subtract
1	0	0	0	D = A	Transfer A
1	0	1	0	D = A + 1	Increment A
1	1	0	1	D = A - 1	Decrement A
1	1	1	1	D = A	Transfer A

Summary of Arithmetic Micro-Operations

R3 ← R1 + R2	Contents of R1 plus R2 transferred to R3	
RZ ← RZ′	Complement the contents of R2	
R2 ← R2'+	2's complement the content of R2	
1	Subtraction	
1 R3 ← R1 + R2'+	Subtraction Increment	

Logic Micro-Operations

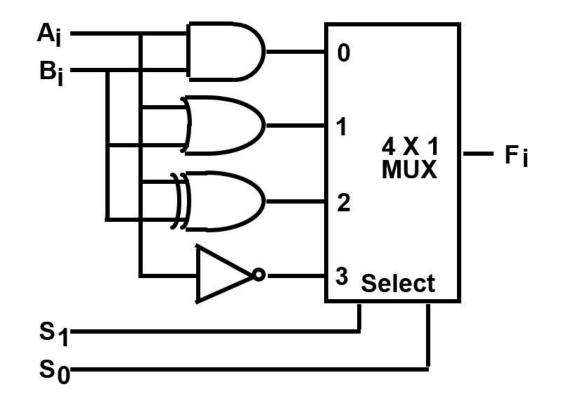
- ☐ Specify **binary operations on the strings of bits** in registers
- Logic micro-operations are bit-wise operations, i.e., they work on the individual bits of data
- ☐ Useful for bit manipulations on binary data
- ☐ Useful for making logical decisions based on the bit value
- ☐ There are, in principle, 16 different logic functions that can be defined

over two binary input variables

Α	В	F ₀	F ₁	F ₂ F ₁₃ F ₁₄ F ₁₅
0	0	0	0	0 1 1 1
0	1	0	0	0 1 1 1
1	0	0	0	1 0 1 1
1	1	0	1	0 1 0 1

- ☐ However, most of the systems only implement four of them
 - □ AND (\land), OR (\lor), XOR (\oplus), Complement/NOT
- ☐ The **others canbe createdfrom combination of these** four operations

Hardware for Logic Micro-Operations



Truth table

S ₁	S ₀	Output	μ-operation
0	0	F=A∧B	AND
0	1	$F = A \vee B$	OR
1	0	F = A ⊕ B	XOR
1	1	F = A'	Complement

Summary of Logic Micro-Operations

Truth tables for 16 functions of 2 variables and the corresponding 16 logic micro-operations

Note: Number of Logic Micro-operations
- n binary variables → 22 functions

				2
	0011	Boolean	Micro-	Name
У	0101	Function	Operations	
	0000	F0 = 0	F ← 0	Clear
	0001	F1 = xy	$F \leftarrow A \wedge B$	AND
	0010	F2 = xy'	$F \leftarrow A \wedge B'$	
	0011	F3 = x	$F \leftarrow A$	Transfer A
	0100	F4 = x'y	$F \leftarrow A' \land B$	
	0101	F5 = y	F ← B	Transfer B
	0110	$F6 = x \oplus y$	$F \leftarrow A \oplus B$	Exclusive-OR
	0111	F7 = x + y	$F \leftarrow A \lor B$	OR
	1000	F8 = (x + y)'	$F \leftarrow (A \lor B)'$	NOR
	1001	$F9 = (x \oplus y)'$	F ← (A ⊕ B)'	Exclusive-NOR
	1010	F10 = y'	F ← B'	Complement B
	1011	F11 = x + y'	$F \leftarrow A \lor B$	***
	1100	F12 = x'	F ← A'	Complement A
	1101	F13 = x' + y	$F \leftarrow A' \lor B$	STORY
	1110	F14 = (xy)'	$F \leftarrow (A \land B)'$	NAND
	1111	F15 = 1	F ← all 1's	Set to all 1's

Applications of Logic Micro-Operations

- □ Logic micro-operations can be used to manipulate individual bits or a portions of a word in a register
- Consider the data in a register A. Another register, B will be used to modify the contents of A
 - ☐ Selective-set
 - ☐ Selective-complement
 - ☐ Selective-clear
 - ☐ Mask (Delete)
 - ☐ Clear
 - □ Insert

- $A \leftarrow A \lor B$
- $A \leftarrow A \oplus B$
- $A \leftarrow A \wedge$
 - $B' A \leftarrow A$
 - **∧** B A ←
 - $A \oplus B$
 - $A \leftarrow (A \land B) \lor$

Selective

In a selective set operation, the bit pattern in B is used to set certain bits in A

☐ If a bit in B is set to 1, that same position in A gets set to 1,

otherwise that bit in A keeps its previous value

Selective

In a selective complement operation, the bit pattern in B is used
 to complement certain bits in A

If a bit in B is to1, that same position in A gets semplemented from its original value, otherwise it is unchanged

Selective Clear

In a selective clear operation, the bit pattern in B is used to clear certain bits in A

☐ If a bit in B is set to 1, that same position in A gets set to 0, otherwise it is unchanged

Mask Operation

In mask operation, the bit pattern in B is used to clear certain bits in A

☐ If a bit in B is set to 0, that same position in A gets set to 0, otherwise it is unchanged

Clear Operation

In a clear operation, if the bits in the same position in A and B are the same, they are cleared in A, otherwise they are set in A

Insert Operation

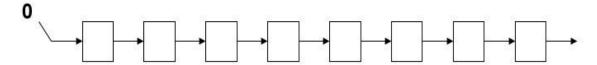
- An insert operation is used to introduce a specific bit pattern into A register, leaving the other bit positions unchanged
- This is done as
 - A mask operation to clear the desired bit positions, followed by
 - An OR operation to introduce the new bits into the desired positions
- **Example:** Suppose you wanted to introduce 1010 into the low order four bits of A:

```
1101 1000 1011 0001 A (Original)
1101 1000 1011 1010 A (Desired)
```

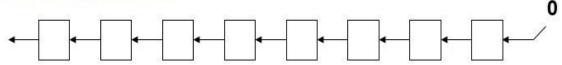
1101 1000 1011 0001	A (Original)
1111 1111 1111 0000	Mask
1101 1000 1011 0000	A (Intermediate)
0000 0000 0000 1010	OR Operation(new bits)
1101 1000 1011 1010	A (Desired)

Logical Shift

- ☐ In a logical shift the serial input to the shift is a 0.
- ☐ A right logical shift operation:



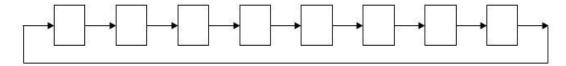
☐ A left logical shift operation:



- ☐ In a Register Transfer Language, the following notation is used
 - shl for a logical shift left
 - shr for a logical shift right
 - Examples:
 - » R2 ← shr R2
 - » R3 ← shl R3

Circular Shift

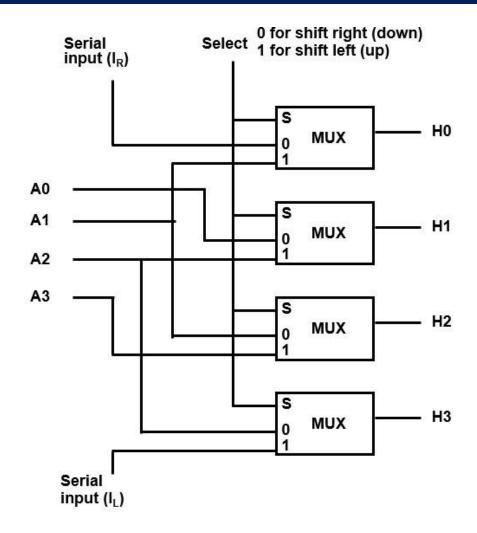
- ☐ In a circular shift the serial input is the bit that is shifted out of the other end of the register.
- ☐ A right circular shift operation:



☐ A left circular shift operation:

- □ In a RTL, the following notation is used
 - cil for a circular shift left
 - cir for a circular shift right
 - Examples:
 - » R2 ← cir R2
 - » R3 ← cil R3

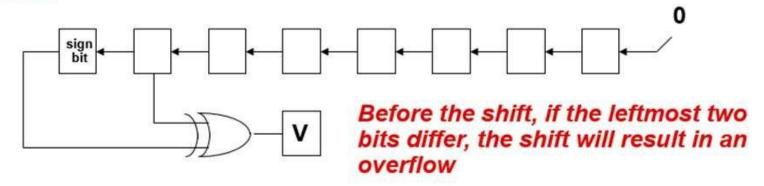
Hardware for Shift Micro-Operation



Functional table				
Select		Out	put	
S	H_0	H_1	H_2	H_2
0	I_R	A_0	A_1	A_2
1	A_1	A_2	A_3	I_L

Arithmetic Shift

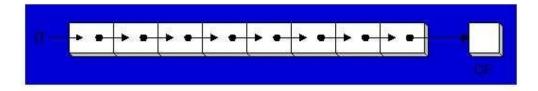
□ A left arithmetic shift operation must be checked for the overflow



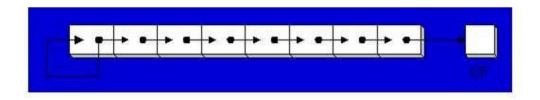
- □ In a RTL, the following notation is used
 - ashl for an arithmetic shift left
 - ashr for an arithmetic shift right
 - Examples:
 - » R2 ← ashr R2
 - » R3 ← ashl R3

Logical Vs. Arithmetic Shift

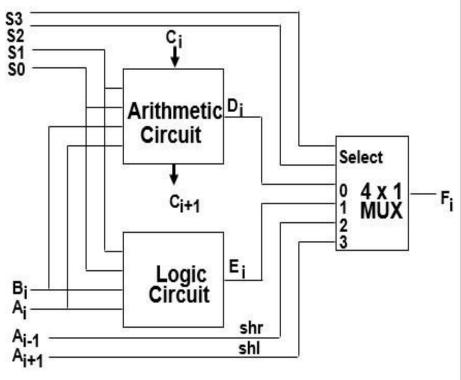
☐A logical shift fills the newly created bit position with zero:



☐ An arithmetic shift fills the newly created bit position with a copy of the number's sign bit:



Hardware for Arithmetic –Logic Shift Micro-Operation



S 3	S2	S 1	SO	Cin	Operation	Function
0	0	0	0	0	F = A	Transfer A
0	0	0	0	1	F = A + 1	Increment A
0	0	0	1	0	F = A + B	Addition
0	0	0	1	1	F = A + B + 1	Add with carry
0	0	1	0	0	F = A + B'	Subtract with borrow
0	0	1	0	1	F = A + B'+ 1	Subtraction
0	0	1	1	0	F = A - 1	Decrement A
0	0	1	1	1	F = A	Transfer A
0	1	0	0	Х	$F = A \wedge B$	AND
0	1	0	1	Х	$F = A \vee B$	OR
0	1	1	0	Х	$F = A \oplus B$	XOR
0	1	1	1	Х	F = A'	Complement A
1	0	X	X	Х	F = shr A	Shift right A into F
1	1	X	X	X	F = shl A	Shift left A into F