ASSIGNMENT No. 1

Simplify the following expressions using Boolean algebra.

$$\mathbf{a}$$
. $A + AB$

b.
$$AB + AB'$$

$$\mathbf{d}$$
. $A'B + ABC' + ABC$

Simplify the following expressions using Boolean algebra.

a.
$$AB + A(CD + CD')$$

b.
$$(BC' + A'D)(AB' + CD')$$

Using DeMorgan's theorem, show that:

a.
$$(A + B)'(A' + B')' = 0$$

b.
$$A + A'B + A'B' = 1$$

Simplify the following Boolean functions using three-variable maps.

a.
$$F(x,y,z) = \sum_{i=1}^{n} (0,1,5,7)$$

b.
$$F(x,y,z) = \sum (1,2,3,6,7)$$

c.
$$F(x, y, z) = \sum (3, 5, 6, 7)$$

d.
$$F(A, B, C) = \sum_{i=1}^{n} (0, 2, 3, 4.6)$$

Simplify the following Boolean functions using four-variable maps.

a.
$$F(A, B, C, D) = \sum (4, 6, 7, 15)$$

b.
$$F(A, B, C, D) = \sum (3, 7, 11, 13, 14, 15)$$

c.
$$F(A, B, C, D) = \sum_{i=1}^{n} (0, 1, 2, 4, 5, 7, 11, 15)$$

d.
$$F(A, B, C, D) = \sum_{i=1}^{n} (0, 2, 4, 5, 6, 7, 8, 10, 13, 15)$$

Simplify the following expressions in (1) sum-of-products form and (2) product-of-sums form.

a.
$$x'z' + y'z' + yz' + xy$$

b. $AC' + B'D + A'CD + ABCD$

Simplify the following Boolean function in sum-of-products form by means of a four-variable map. Draw the logic diagram with (a) AND-OR gates; (b) NAND gates.

$$F(A, B, C, D) = \sum_{i=1}^{n} (0, 2, 8, 9, 10, 11, 14, 15)$$

Simplify the following Boolean function in product-of-sums form by means of a four-variable map. Draw the logic diagram with (a) OR-AND gates; (b) NOR gates.

$$F(w, x, y, z) = \sum (2, 3, 4, 5, 6, 7, 11, 14, 15)$$

Simplify the Boolean function F together with the don't-care conditions d in (1) sum-of-products form and (2) product-of-sums form.

$$F(w, x, y, z) = \sum (0, 1, 2, 3, 7, 8, 10)$$

$$d(w, x, y, z) = \sum (5, 6, 11, 15)$$