

SOLVING $AX=B$

$$\max c^T x$$

$$Ax \leq b \rightarrow A'x = b$$

$$x \geq 0$$

$$x \in \mathbb{R}^n \Rightarrow \text{int sol.}$$

if A is TU

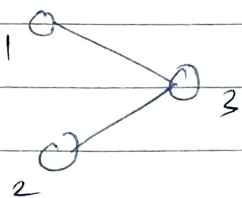
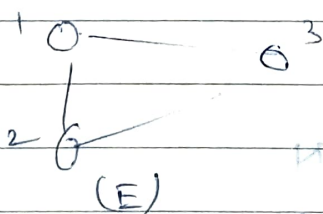
& b is int.

$$Ax = b$$

$$x = A^{-1} b = \frac{1}{|A|} \text{Cof}(A) [b]$$

$$T \rightarrow TU \Rightarrow$$

$$-1, 0, 1$$



$$(V) \begin{bmatrix} 1 & 1 & 0 \\ 2 & 1 & 1 \\ 3 & 0 & 1 \end{bmatrix}$$

$$\begin{bmatrix} 1 & 0 \\ 2 & 1 \\ 1 & 1 \end{bmatrix}$$

$$|A|$$

$$\rightarrow 2$$

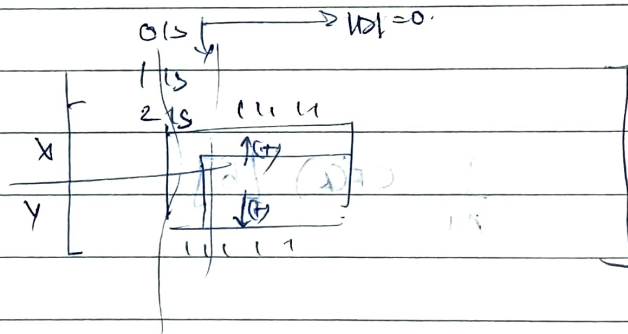
A for BPG is TU.

X Y

all elements either 0 or 1

all submatrices of X are TU.

if every $n \times n$ submatrices is TU
all $(n+1) \times (n+1)$ matrices is TU.



rows of this matrices are linearly independent

A

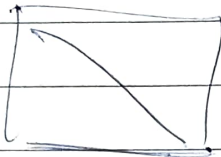
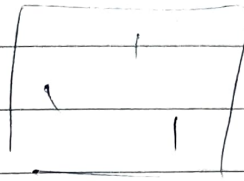
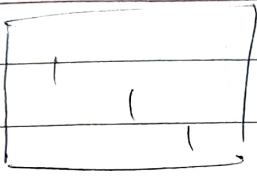
least sq.

$$Ax = b$$

$L \times N$

sq. + non sq.

$$Xx = A^{-1}b.$$



$$\begin{bmatrix} a_{11} & 0 \\ A_{12} & A_{22} \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \end{bmatrix} = \begin{bmatrix} b_1 \\ B_2 \end{bmatrix}$$

\downarrow \downarrow
 $n-1 \times 1$ $(n-1) \times (n-1)$ $(n-1) \times 1$ $(n-1) \times 1$

$$x_1 = \frac{b_1}{a_{11}}$$

$$A_{12} x_1 + A_{22} x_2 = B_2$$



lower triangular matrix.

PD - positive definite.

$$Ax = b$$



costly step.

$$LL^T x = b.$$

$$Lv = b$$

$$L^T x = v$$

$$A \begin{bmatrix} x_i & x_i \\ 1 & 1 \end{bmatrix} = \begin{bmatrix} p_i & p_i \\ 1 & 1 \end{bmatrix}$$

$$A [x_i] = [b_i]$$

iq lhz (b) (c)

$$MIS + MVC = |V|$$