Introduction to Programming

Week – 5, Lecture – 1 **Iterative Operations on Arrays**

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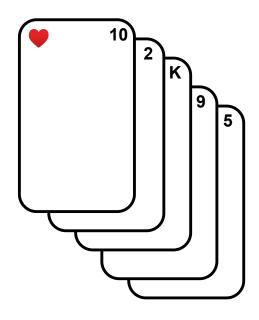
We will now have a look at two most common operations performed through loops on an array

- Sorting the values in an array
- Searching for a value in an array

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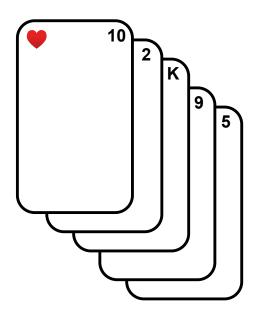
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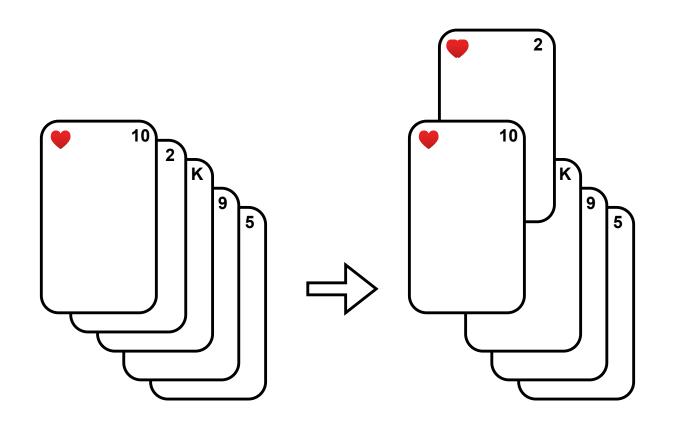
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How do they usually do it?

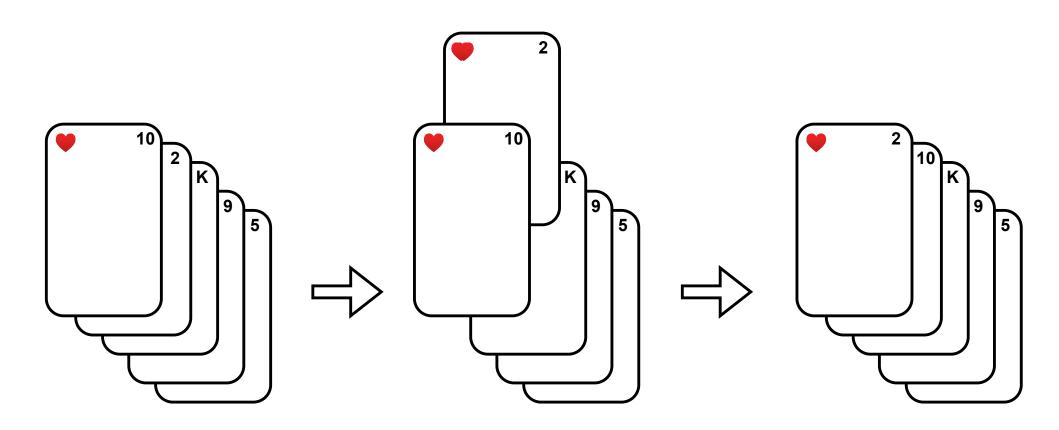
A common approach to get the cards in order (assuming the smallest card is on top) is this:

Browse though the cards, and find the smallest card in the hand



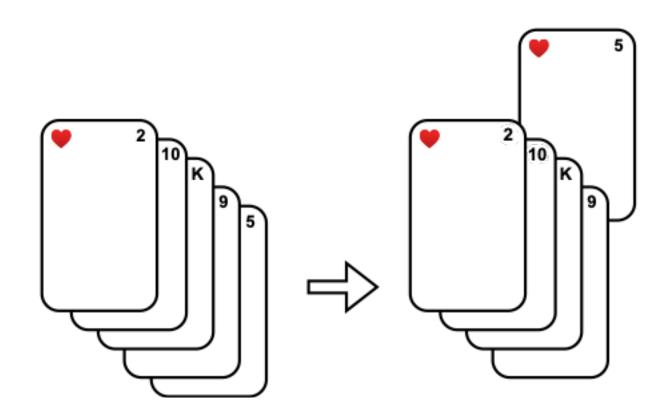
A common approach to get the cards in order (assuming the smallest card is on top) is this:

- Browse though the cards, and find the smallest card in the hand
- Pick out the card, and bring it on top



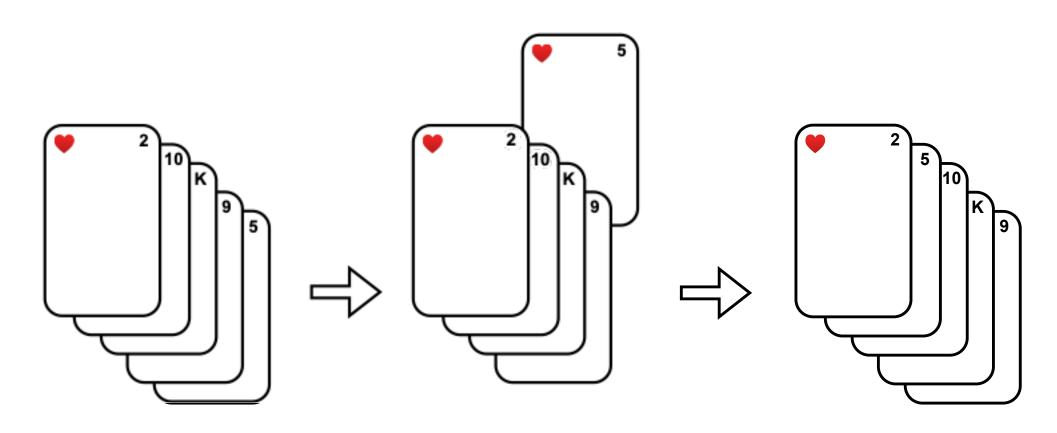
A common approach to get the cards in order (assuming the smallest card is on top) is this:

- Browse though the cards, and find the smallest card in the hand
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- Browse through the rest of the cards, and find the smallest card among them



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- Browse though the cards, and find the smallest card in the hand
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- Pick out the card, and place it just below the card that was picked previously



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- ... sorting an array involves re-shuffling of the values that the array stores
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What we just saw included examples of two common array operations

• "inserting" a value and "deleting" the value at a given index (in this case, it was the same value)

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- Shifting elements at index i and and all "valid" indices greater than i, to the right

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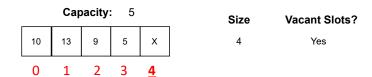
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- Inserting the new value at index i

Capacity: 5						Size	Vacant Slots
	10	13	9	5	х	4	Yes

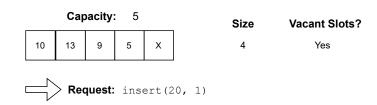


Assume that we have an array of capacity 5 and current size as 4

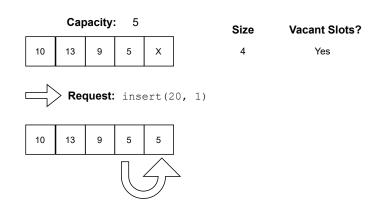


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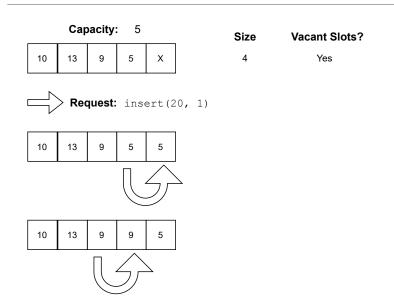
Here, there is no "recognized" value at index 4 (i.e., it could be some random value, that we don't care)



Assume that we now get a request to insert a new value, 20, at index 1 of the array

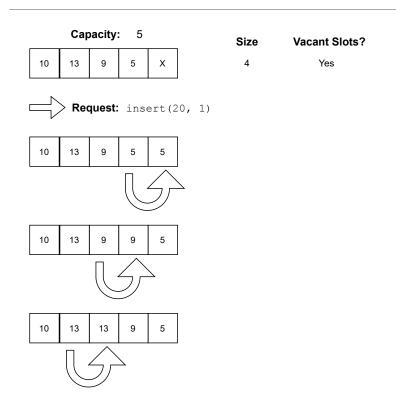


We copy the value at last occupied index, i.e., index $\,3\,$ to the next index, i.e., index $\,4\,$



We copy the value at last occupied index, i.e., index 3 to the next index, i.e., index 4

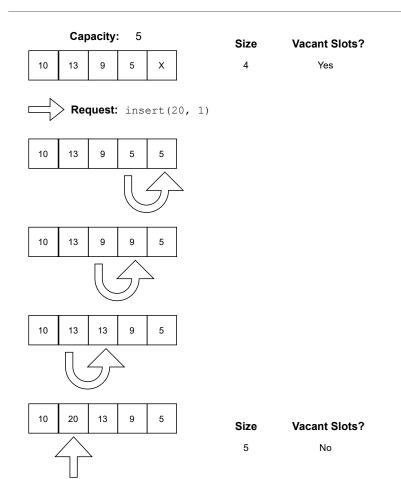
... then we copy the value at index 2 to index 3



We copy the value at last occupied index, i.e., index $\,3\,$ to the next index, i.e., index $\,4\,$

... then we copy the value at index 2 to index 3

... and finally, we copy value at index 1 to index 2



Finally, we can now insert new value at index 1

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- Checking if the array has any vacant slots; if there are, we can accommodate a new value
- Picking an index in the array to "insert" the new value; let the index be i
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Here, we are explicitly maintaining the size of an array

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Here, we are explicitly maintaining the size of an array

It can range from 0 to the array capacity

Array capacity is essentially its declared size

```
// Check for vacancy
if(size == CAPACITY)
       printf("The array is full; remove some elements first !\n");
        break;
printf("Enter the index where you would like to insert the value: ");
scanf("%d", &op1);
// Check if the index is valid
if(op1 < 0 || op1 >= CAPACITY)
       printf("Invalid insertion index\n");
       break;
else if(op1 > size)
       printf("WARNING: The element will be added at the end, i.e. index %d\n",size);
       op1 = size;
printf("Enter the value to insert: ");
scanf("%d", &op2);
// Shift elements to the right
for(i = size; i > op1; i--)
       arr[i] = arr[i-1];
// Insert the new element
arr[op1] = op2;
// Update the size
size++;
```

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for(i = size; i > op1; i--)
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This is C code for inserting a value in an array

```
printf("Enter the index where you would like to insert the value: ");
scanf("%d", &op1);
```

op1 contains the index of insertion

```
printf("Enter the value to insert: ");
scanf("%d", &op2);
```

op2 contains the value to be inserted

```
// Shift elements to the right
for(i = size; i > op1; i--)
       arr[i] = arr[i-1];
// Insert the new element
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```

Focus on this part, and convince yourself that it performs the insertion

In the card sorting example, we also *deleted* a card every time (before we inserted it back again)

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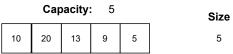
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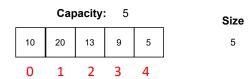
- Checking if the array has any elements; if there are, we can remove any one of them
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In the card sorting example, we also *deleted* a card every time (before we inserted it back again)

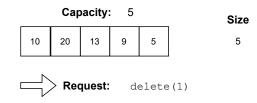
Deletion involves

- Checking if the array has any elements; if there are, we can remove any one of them
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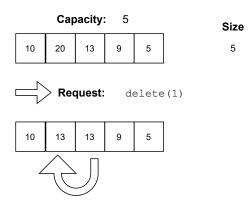




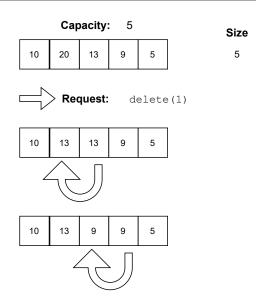
Let us go back to the array where we inserted the value



Assume that we now get a request to delete the value at index $\ensuremath{\mathbb{1}}$ of the array

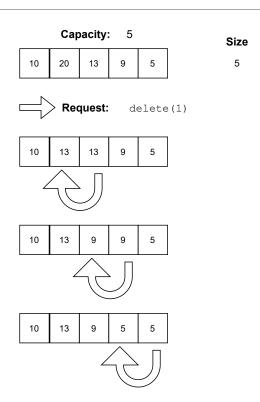


We copy the value at index i+1 to i, i.e., index 2 to the previous index, i.e., index 1



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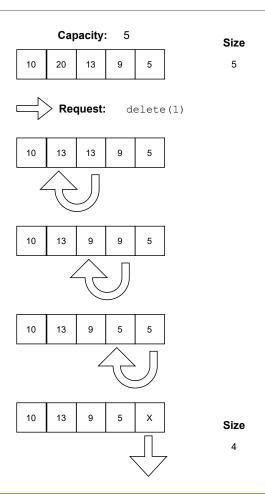
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We copy the value at index i+1 to i, i.e., index 2 to the previous index, i.e., index 1

... then we copy the value at index 3 to index 2

... and finally, we copy value at index 4 to index 3



We don't really need to "delete" the value at last index... we just reduce the size, and "ignore" the stored value

```
// Check if array has any elements
if(size == 0)
       printf("The array is empty; add some elements first !\n");
        break;
printf("Enter the index of the value you wish to delete: ");
scanf("%d", &op1);
// Check if the index is valid
if(op1 < 0 || op1 >= CAPACITY)
       printf("Invalid insertion index\n");
       break;
else if(op1 >= size)
       printf("WARNING: The last element will be deleted, i.e. at index %d\n",size-1);
       op1 = size;
// Shift elements to the left
for(i = op1; i < size - 1; i++)</pre>
       arr[i] = arr[i+1];
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Focus on this part, and convince yourself that it performs the deletion

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The idea behind Insertion Sort is summarised as below

At each step, we divide the array into 2 "imaginary" parts

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- Then, we increase the size of the sorted part by 1 (thus, decreasing the size of unsorted part by 1)
- When the size of unsorted part becomes 0, the whole array has become sorted





Let us do insertion sort on our sample array!!

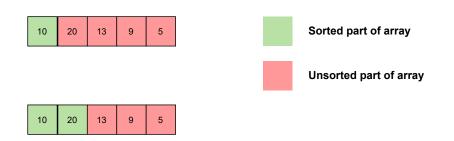


At the start, the sorted part only contains the index $\,0$, while the unsorted part contains indices $\,1$ to $\,4$

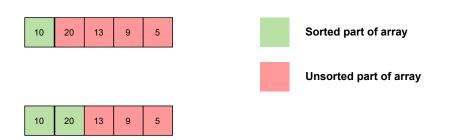


At the start, the sorted part only contains the index 0, while the unsorted part contains indices 1 to 4

We delete the first element of the unsorted part, i.e., 20 at index 1...

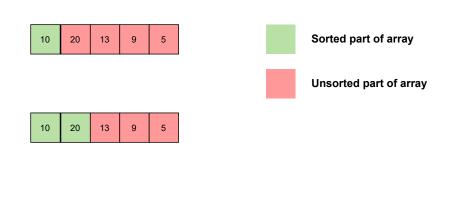


... and insert it in the sorted part at its correct position, i.e., index 1 itself!!

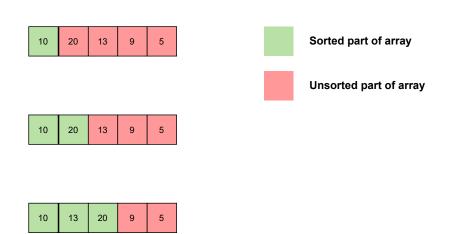


... and insert it in the sorted part at its correct position, i.e., index 1 itself!!

Next, we delete 13 from index 2...

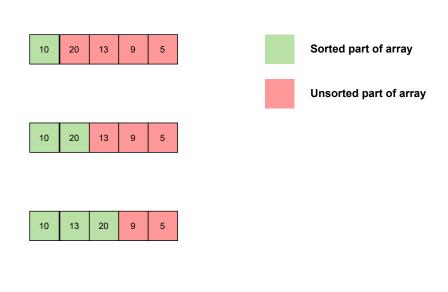


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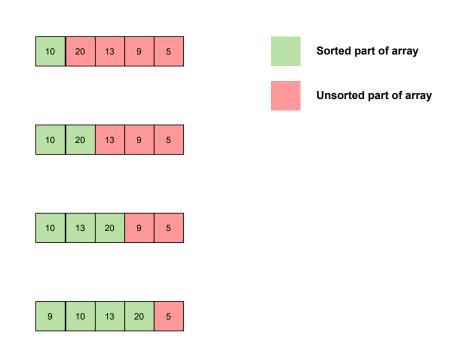
The first element of the unsorted part, i.e., 9 at index 3 is now deleted...



13

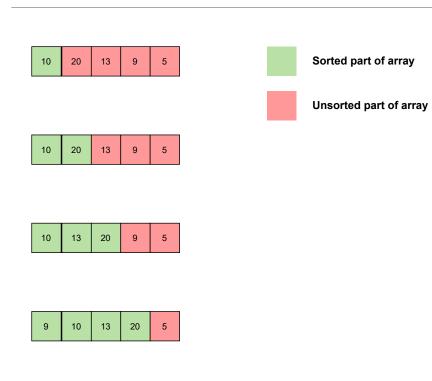
20

 \dots which gets inserted at index 0 in the sorted part of the array !!

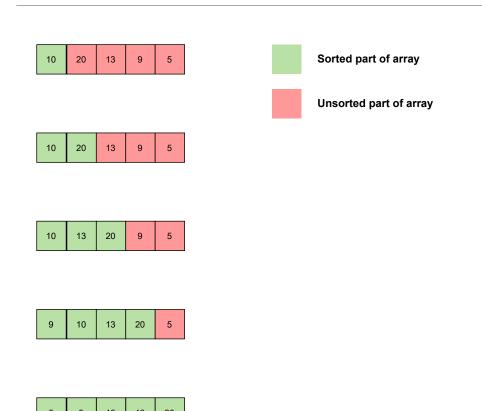


... which gets inserted at index 0 in the sorted part of the array !!

The last element of the unsorted part, i.e., 5 at index 4 is the last value to de deleted...



... which is inserted at the index 0, its correct position in the sorted part



... which is inserted at the index 0, its correct position in the sorted part

With this, the sorted part now contains the whole array... and we can feel proud that we have sorted the array :D

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• We don't have much choice, but to check values at all the array indices, one by one

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But can we do any better if we know that the array is sorted (let us say, in ascending order)?

Assume that you check some random index, i of the array

How can you search for an element in an unsorted array?

We don't have much choice, but to check values at all the array indices, one by one

- Assume that you check some random index, i of the array
- If the element at index i, is the element you were looking for, you've hit the jackpot !!

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- But even if you are not lucky, you have still, essentially, divided the array in two parts...
- The part on the left of i, is sure to only have values smaller than the value at index i...
- ... and the part on the right of i, is sure to only have values larger than the value at index i!!

How can you search for an element in an unsorted array?

We don't have much choice, but to check values at all the array indices, one by one

- Assume that you check some random index, i of the array
- If the element at index i, is the element you were looking for, you've hit the jackpot !!
- But even if you are not lucky, you have still, essentially, divided the array in two parts...
- The part on the left of i, is sure to only have values smaller than the value at index i...
- ... and the part on the right of i, is sure to only have values larger than the value at index i!!
- \circ So based on whether the element you are searching is smaller or larger than the value at index i...

How can you search for an element in an unsorted array?

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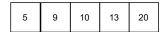
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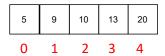
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- If you always pick the mid-point of the array's part you are searching as i, it is called Binary Search





Going back to our array



Assume that we have to search 9 in this sorted array

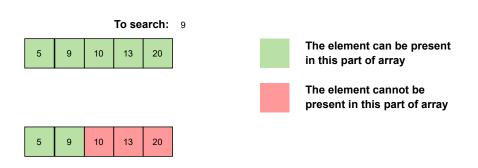


In the beginning, we assume that 9 can be present anywhere in the array

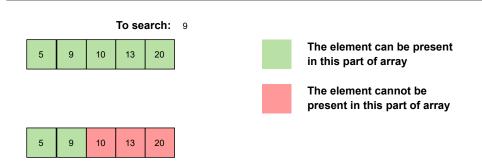


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We compare it with the value at index 2, the mid-point of the part of the array where we must search (i.e., the whole array)

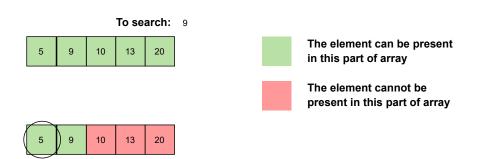


Since 9 is smaller than 10, we can be sure that it cannot be present at indices 2 or higher, so only the left part of the array remains a candidate for further searching



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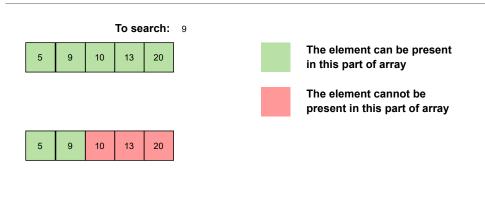
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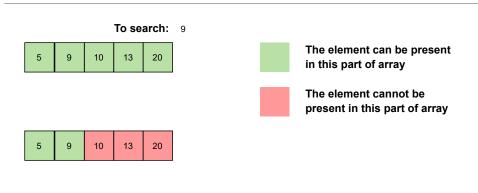
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Let us pick index 0 for the next search



Since 9 is larger than 5, it can only be present to the right of 5 in the array, leaving only index 1 to be searched



... and this is where our element is !!

Homework!!

Go through the Example C file called BasicArrayOperations.c

- Create a new C file called ArrayOperations.c, containing two more operations...
- ... "insertion sort array" operation, with operation code 3
- ... and "binary search in array" operation, with operation code 4
- (assume that the user is "disciplined" enough to sort the array first, and then use binary search)

There are many other searching algorithms, you can easily comprehend at least two of them now

- Bubble Sort
- Selection Sort
- Try to write C code for them as well on your own