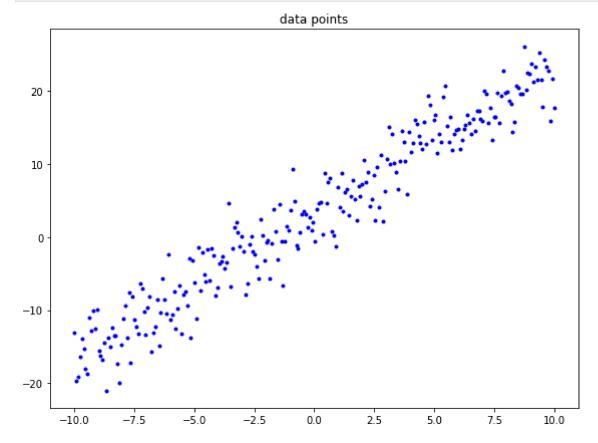
# Linear regression

## import library

```
In [ ]: import numpy as np
  import matplotlib.image as img
  import matplotlib.pyplot as plt
  import matplotlib.colors as colors
  from mpl_toolkits.mplot3d import Axes3D
```

## load data points

 $\bullet \quad \{(x_i,y_i)\}_{i=1}^n$ 



#### compute the residual

#### compute the loss

• useful functions: np.inner

## compute the gradient with respect to $heta_0$

• useful functions: np.inner

## compute the gradient with respect to $heta_1$

• useful functions: np.inner

#### gradient descent for the optimization

```
In [ ]: number_iteration = 500
        learning_rate = 0.01
        theta0
                         = 0
        theta1
        list_theta0 = np.zeros(number_iteration)
list_theta1 = np.zeros(number_iteration)
list_loss = np.zeros(number_iteration)
        for i in range(number_iteration):
           # complete the blanks
           theta0 = list_theta0[i - 1] - (learning_rate * compute_gradient_theta0(x, y, li
           theta1 = list_theta1[i - 1] - (learning_rate * compute_gradient_theta1(x, y, li
           loss = compute_loss(x, y, theta0, theta1)
           list_theta0[i] = theta0
           list\_theta1[i] = theta1
           list_loss[i] = loss
```

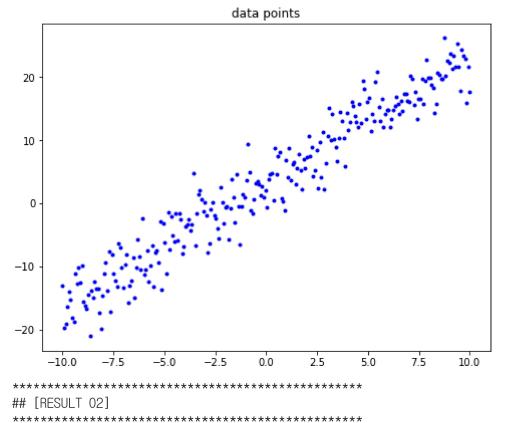
```
In [ ]: def function_result_01():
             plt.figure(figsize=(8,6))
             plt.plot(x, y, '.', color='blue')
             plt.title('data points')
             plt.show()
In [ ]: def function_result_02():
             plt.figure(figsize=(8,6))
             ax = plt.gca()
             plt.plot(list_theta0, '-', color='blue', label=r'$\text{\text{Wtheta_0$}'}
             plt.plot(list_theta1, '-', color='red', label=r'$\text{\psi}theta_1$')
             plt.title('model parameters')
             ax.legend()
             plt.show()
In [ ]: def function_result_03():
             plt.figure(figsize=(8,6))
            plt.plot(list_loss, '-', color='blue')
             plt.title('loss curve')
             plt.show()
In [ ]: def function_result_04():
             f = theta0 + theta1 * x
             plt.figure(figsize=(8,6))
             ax = plt.gca()
             plt.plot(x, y, '.', color='blue', label='data point')
             plt.plot(x, f, '-', color='red', label='regression')
             plt.title('regression')
             ax.legend()
             plt.show()
In [ ]: def function_result_05():
             XO = np.arange(-10, 10, 0.1)
             X1 = np.arange(-10, 10, 0.1)
             grid_theta0, grid_theta1 = np.meshgrid(X0, X1)
             grid_loss = np.zeros(grid_theta0.shape)
             for i, t0 in enumerate(X0):
                 for j, t1 in enumerate(X1):
                     grid_loss[j, i] = compute_loss(x, y, t0, t1)
             fig = plt.figure(figsize=(8,6))
             ax = fig.add_subplot(111, projection='3d')
             plt.title('loss surface')
             ax = plt.axes(projection='3d')
```

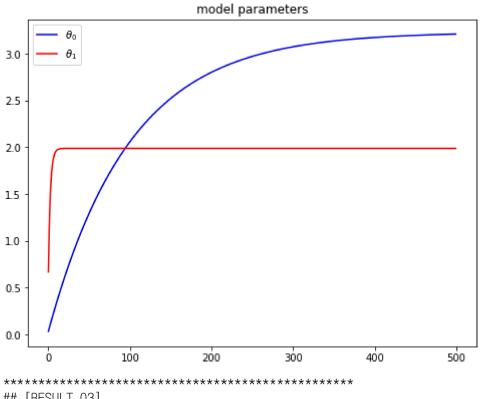
```
ax.set_xlabel(r'$\text{\text{wtheta}_0$')
ax.set_ylabel(r'$\text{\text{\text{wtheta}_1$'}})
ax.set_zlabel('loss')

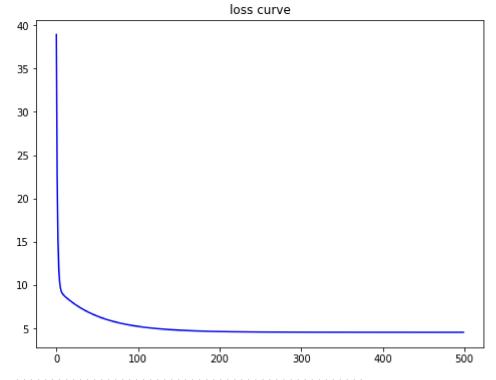
ax.plot_surface(grid_theta0, grid_theta1, grid_loss, rstride=1, cstride=1, cmap=

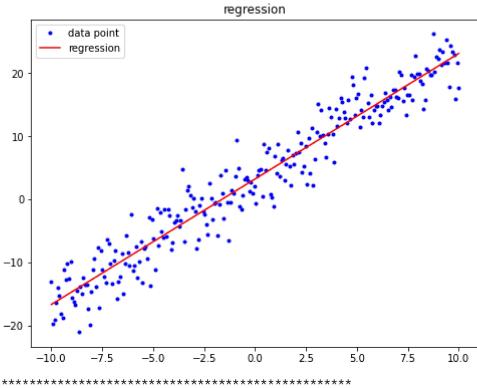
plt.tight_layout()
plt.show()
```

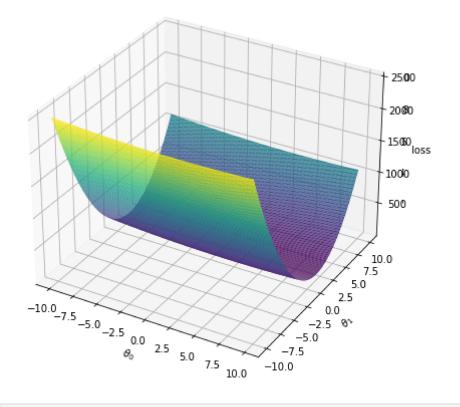
### results











In [ ]: