# Package 'fitOU'

October 30, 2023

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R topics documented:				
bivariate_ou				
Index				

2 FitOU

bivariate\_ou

Bivariate Ornstein-Uhlenbeck Model Data

#### Description

Bivariate Ornstein-Uhlenbeck Model Data

#### Usage

```
bivariate_ou
```

#### **Format**

A dataframe with 10000 rows and 4 columns (y1, y2, id, and time) generated from the bivariate Ornstein–Uhlenbeck model from Chow et al. (2023).

#### References

Chow, S.-M., Losardo, D., Park, J., & Molenaar, P. C. M. (2023). Continuous-time dynamic models: Connections to structural equation models and other discrete-time models. In R. H. Hoyle (Ed.), Handbook of structural equation modeling (2nd ed.). The Guilford Press.

FitOU

Fit the Ornstein-Uhlenbeck Model

#### **Description**

This is a wrapper function that makes fitting the Ornstein–Uhlenbeck model convenient using the dynr package.

#### Usage

```
FitOU(
  data,
  observed,
  id,
  time,
  mu0 = NULL,
  sigma0 = NULL,
  mu_start = NULL,
  phi_start = NULL,
  sigma_start = NULL,
  theta_start = NULL,
  sigma_diag = FALSE,
  center = FALSE,
  lb = NULL,
```

FitOU 3

```
ub = NULL,
rerun = NULL,
...
)
```

## Arguments

data	Data frame. A data frame object of data for potentially multiple subjects that contain a column of subject ID numbers (i.e., an ID variable), a column indicating subject-specific measurement occasions (i.e., a TIME variable), at least one column of observed values.
observed	Character vector. A vector of character strings of the names of the observed variables in the data.
id	Character string. A character string of the name of the ID variable in the data.
time	Character string. A character string of the name of the TIME variable in the data.
mu0	Numeric vector. Mean of initial latent variable values $(\mu_{\eta 0})$ . If mu0 = NULL, a vector of zeros is used.
sigma0	Numeric matrix. Covariance matrix of initial latent variable values $(\Sigma_{\eta 0})$ . If sigma0 = NULL, an identity matrix is used.
mu_start	Numeric vector. Starting values of the mu vector, that is, the long-term mean or equilibrium level. If mu_start = NULL, a vector means of the observed variables is used.
phi_start	Numeric matrx. Starting values of the phi matrix, that is, the rate of mean reversion, determining how quickly the variable returns to its mean. If phi_start = NULL, a matrix of zeros is used.
sigma_start	Numeric matrx. Starting values of the sigma matrix, that is, the matrix of volatility or randomness in the process. If sigma_start = NULL, an identity matrix is used.
theta_start	Numeric matrx. Starting values of the theta matrix, that is, the measurement error covariance matrix $(\Theta)$ . If theta_start = NULL, an identity matrix is used.
sigma_diag	Logical. If sigma_diag = TRUE, estimate only the diagonals of $\Sigma$ .
center	Logical. If center = TRUE, mean center by id.
1b	Numeric vector. Optional. The lower bounds for $\Phi$ .
ub	Numeric vector. Optional. The upper bounds for $\Phi$ .
rerun	Positive integer. Number of times to rerun model fitting with a slight change to starting values when exit code is 2 to 6.
	Additional arguments to pass to dynr::dynr.cook().

## Details

The measurement model is given by

4 FitOU

where  $\mathbf{y}_{i,t}$ ,  $\eta_{i,t}$ , and  $\varepsilon_{i,t}$  are random variables and  $\boldsymbol{\nu}$ ,  $\boldsymbol{\Lambda}$ , and  $\boldsymbol{\Theta}$  are model parameters.  $\mathbf{y}_{i,t}$  is a vector of observed random variables at time t and individual i,  $\eta_{i,t}$  is a vector of latent random variables at time t and individual i, while  $\boldsymbol{\nu}$  is a vector of intercept,  $\boldsymbol{\Lambda}$  is a matrix of factor loadings, and  $\boldsymbol{\Theta}$  is the covariance matrix of  $\varepsilon$ .

The dynamic structure is given by

$$\mathrm{d}\boldsymbol{\eta}_{i,t} = \boldsymbol{\Phi}\left(\boldsymbol{\mu} - \boldsymbol{\eta}_{i,t}\right) \mathrm{d}t + \boldsymbol{\Sigma}^{\frac{1}{2}} \mathrm{d}\mathbf{W}_{i,t}$$

where  $\mu$  is the long-term mean or equilibrium level,  $\Phi$  is the rate of mean reversion, determining how quickly the variable returns to its mean,  $\Sigma$  is the matrix of volatility or randomness in the process, and dW is a Wiener process or Brownian motion, which represents random fluctuations.

#### Author(s)

Ivan Jacob Agaloos Pesigan

#### References

Chow, S.-M., Losardo, D., Park, J., & Molenaar, P. C. M. (2023). Continuous-time dynamic models: Connections to structural equation models and other discrete-time models. In R. H. Hoyle (Ed.), Handbook of structural equation modeling (2nd ed.). The Guilford Press.

Ou, L., Hunter, M. D., & Chow, S.-M. (2019). What's for dynr: A package for linear and nonlinear dynamic modeling in R. *The R Journal*, 11(1), 91. doi:10.32614/rj2019012

Uhlenbeck, G. E., & Ornstein, L. S. (1930). On the theory of the brownian motion. *Physical Review*, 36(5), 823–841. doi:doi.org/10.1103/physrev.36.823

#### See Also

Other Fit Ornstein-Uhlenbeck Model Functions: FitOUID()

#### **Examples**

```
## Not run:
FitOU(
   data = bivariate_ou,
   observed = c("y1", "y2"),
   id = "id",
   time = "time",
   verbose = FALSE
)
## End(Not run)
```

FitOUID 5

FitOUID

Fit the Ornstein-Uhlenbeck Model for Each Individual

#### Description

This is a wrapper function that makes fitting the Ornstein-Uhlenbeck model for each individual convenient using the dynr package.

#### Usage

```
FitOUID(
   data,
   observed,
   id,
   time,
   mu0 = NULL,
   sigma0 = NULL,
   mu_start = NULL,
   phi_start = NULL,
   sigma_start = NULL,
   theta_start = NULL,
   ...,
   ncores = NULL
)
```

### Arguments

data	Data frame. A data frame object of data for potentially multiple subjects that contain a column of subject ID numbers (i.e., an ID variable), a column indicating subject-specific measurement occasions (i.e., a TIME variable), at least one column of observed values.
observed	Character vector. A vector of character strings of the names of the observed variables in the data.
id	Character string. A character string of the name of the ID variable in the data.
time	Character string. A character string of the name of the TIME variable in the data.
mu0	Numeric vector. Mean of initial latent variable values ( $\mu_{\eta 0}$ ). If mu0 = NULL, a vector of zeros is used.
sigma0	Numeric matrix. Covariance matrix of initial latent variable values $(\Sigma_{\eta 0})$ . If sigma0 = NULL, an identity matrix is used.
mu_start	Numeric vector. Starting values of the mu vector, that is, the long-term mean or equilibrium level. If mu_start = NULL, a vector means of the observed variables is used.
phi_start	Numeric matrx. Starting values of the phi matrix, that is, the rate of mean reversion, determining how quickly the variable returns to its mean. If phi_start = NULL, a matrix of zeros is used.

6 FitOUID

Numeric matrx. Starting values of the sigma matrix, that is, the matrix of volatility or randomness in the process. If sigma\_start = NULL, an identity matrix is used.
 Numeric matrx. Starting values of the theta matrix, that is, the measurement error covariance matrix (Θ). If theta\_start = NULL, an identity matrix is used.
 Additional arguments to pass to dynr::dynr.cook().
 Positive integer. Number of cores to use.

#### **Details**

The measurement model is given by

$$\mathbf{y}_{i,t} = \boldsymbol{\nu} + \boldsymbol{\Lambda} \boldsymbol{\eta}_{i,t} + \boldsymbol{\varepsilon}_{i,t}$$
 with  $\boldsymbol{\varepsilon}_{i,t} \sim \mathcal{N}\left(\mathbf{0}, \boldsymbol{\Theta}\right)$ 

where  $\mathbf{y}_{i,t}$ ,  $\eta_{i,t}$ , and  $\varepsilon_{i,t}$  are random variables and  $\boldsymbol{\nu}$ ,  $\boldsymbol{\Lambda}$ , and  $\boldsymbol{\Theta}$  are model parameters.  $\mathbf{y}_{i,t}$  is a vector of observed random variables at time t and individual i,  $\eta_{i,t}$  is a vector of latent random variables at time t and individual i, and  $\varepsilon_{i,t}$  is a vector of random measurement errors at time t and individual i, while  $\boldsymbol{\nu}$  is a vector of intercept,  $\boldsymbol{\Lambda}$  is a matrix of factor loadings, and  $\boldsymbol{\Theta}$  is the covariance matrix of  $\varepsilon$ .

The dynamic structure is given by

$$\mathrm{d} \boldsymbol{\eta}_{i,t} = \boldsymbol{\Phi} \left( \boldsymbol{\mu} - \boldsymbol{\eta}_{i,t} \right) \mathrm{d} t + \boldsymbol{\Sigma}^{\frac{1}{2}} \mathrm{d} \mathbf{W}_{i,t}$$

where  $\mu$  is the long-term mean or equilibrium level,  $\Phi$  is the rate of mean reversion, determining how quickly the variable returns to its mean,  $\Sigma$  is the matrix of volatility or randomness in the process, and dW is a Wiener process or Brownian motion, which represents random fluctuations.

#### Author(s)

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#### References

Chow, S.-M., Losardo, D., Park, J., & Molenaar, P. C. M. (2023). Continuous-time dynamic models: Connections to structural equation models and other discrete-time models. In R. H. Hoyle (Ed.), Handbook of structural equation modeling (2nd ed.). The Guilford Press.

Ou, L., Hunter, M. D., & Chow, S.-M. (2019). What's for dynr: A package for linear and nonlinear dynamic modeling in R. *The R Journal*, 11(1), 91. doi:10.32614/rj2019012

Uhlenbeck, G. E., & Ornstein, L. S. (1930). On the theory of the brownian motion. *Physical Review*, 36(5), 823–841. doi:doi.org/10.1103/physrev.36.823

#### See Also

Other Fit Ornstein-Uhlenbeck Model Functions: FitOU()

FitOUID 7

## Examples

```
## Not run:
FitOUID(
  data = bivariate_ou,
  observed = c("y1", "y2"),
  id = "id",
  time = "time",
  verbose = FALSE
)
## End(Not run)
```

## **Index**

```
* Fit Ornstein-Uhlenbeck Model Functions
    FitOU, 2
    FitOUID, 5
* data
    bivariate_ou, 2
* fitOU
    {\tt bivariate\_ou, 2}
    FitOU, 2
    FitOUID, 5
* fit
    FitOU, 2
    FitOUID, 5
bivariate_ou, 2
dynr::dynr.cook(), 3, 6
FitOU, 2, 6
FitOUID, 4, 5
```