

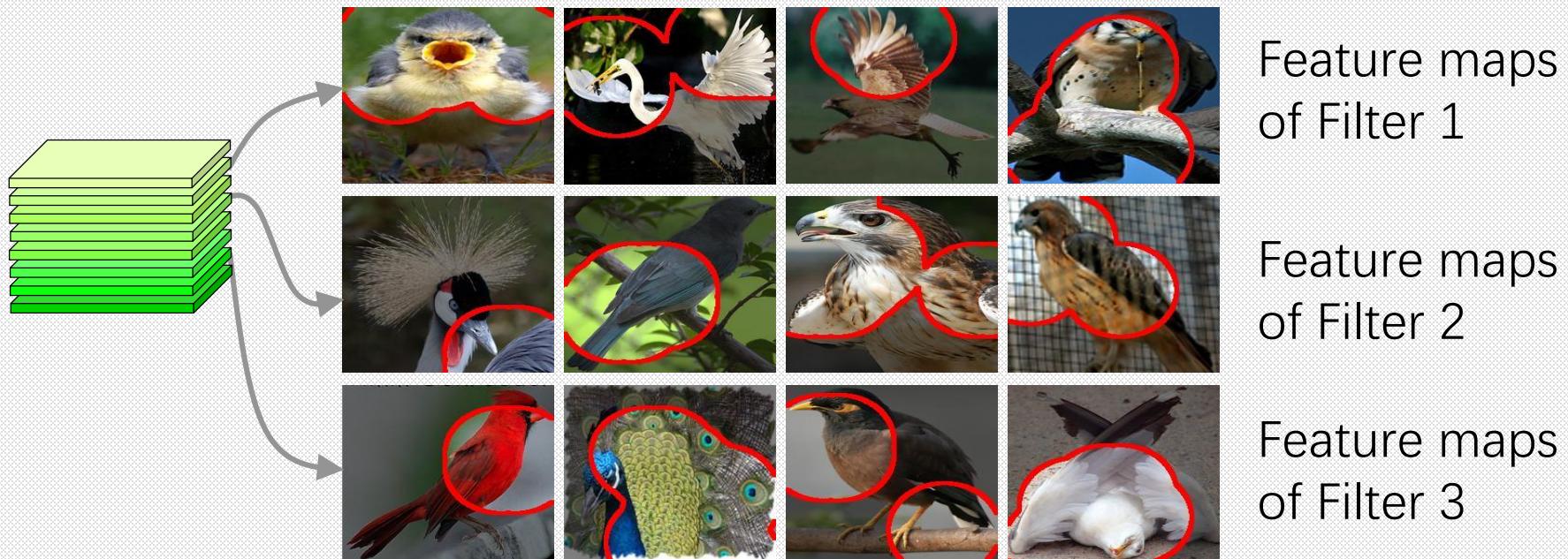
What is the relationship between interactions and visual concepts? —— Learning compositional and interpretable features.



Wen Shen, Quanshi Zhang

Background

- Neural activations of filters in traditional CNNs



**Feature maps of a filter in traditional CNNs
are usually chaotic.**

Strongly interacted filters → meaningful concepts



Wen Shen Quanshi Zhang

Disentangling visual concepts from chaotic feature maps

Learning interpretable features

Build an **explanatory graph** to explain the semantic hierarchy^[1]

The **interpretable CNN**, where each filter represents a specific object part^[2]

The **compositional CNN**, where each filter represents a specific object part/image region^[3]

[1] Quanshi Zhang et al. "Interpreting CNN Knowledge via an Explanatory Graph" in AAAI 2018

[2] Quanshi Zhang et al. "Interpretable Convolutional Neural Networks" in CVPR 2018

[3] Wen Shen et al. "Interpretable Compositional Convolutional Neural Networks" in IJCAI 2021

Strongly interacted filters → meaningful concepts



Wen Shen Quanshi Zhang

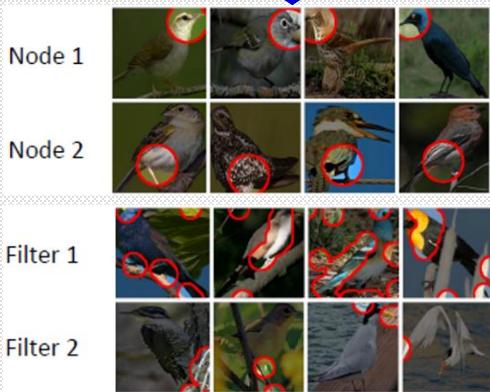
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Each node represents a pattern of an object part. A filter may encode multiple patterns (nodes).

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A filter only encode a specific pattern of an object part.

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A filter only encode a specific pattern of an object part.



A filter can encode a specific pattern of an object part or image region.

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- The interpretability of filters is gradually enhanced.
A filter may encode multiple patterns [1] → A filter only encodes a specific pattern [2][3].
- The representation power of filters is gradually enhanced.
A filter can only encodes an object part in ball-like areas [2] → A filter can encodes an object part with a specific shape or the image region without a specific structure [3].

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Wen Shen Quanshi Zhang



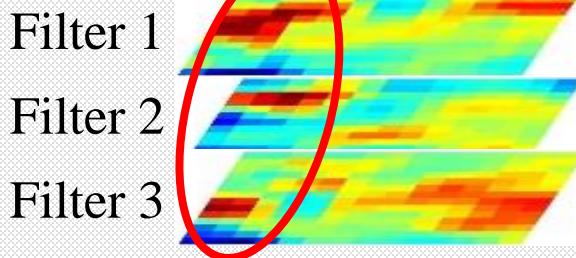
The relationship between interactions and visual concepts

Learning interpretable features

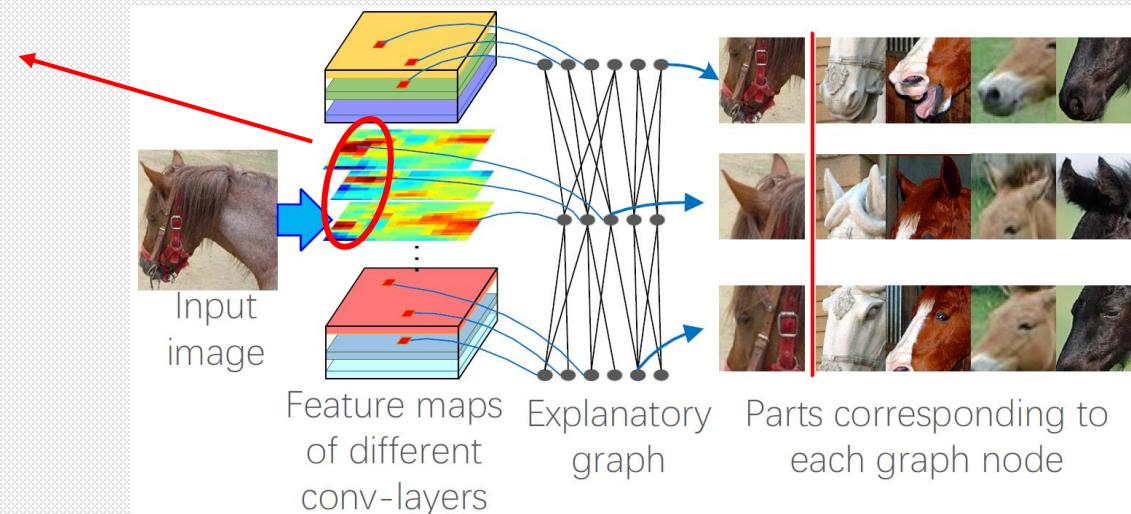
Build an **explanatory graph to explain the semantic hierarchy^[1]**

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A node of the explanatory graph is encoded as the **highly interacted activations** of a few filters.



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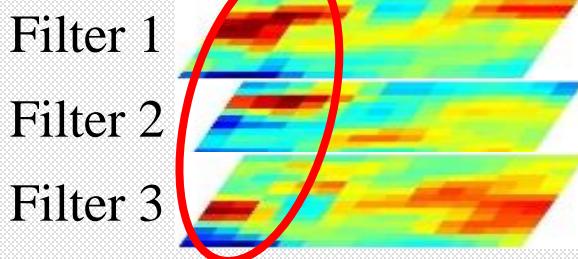
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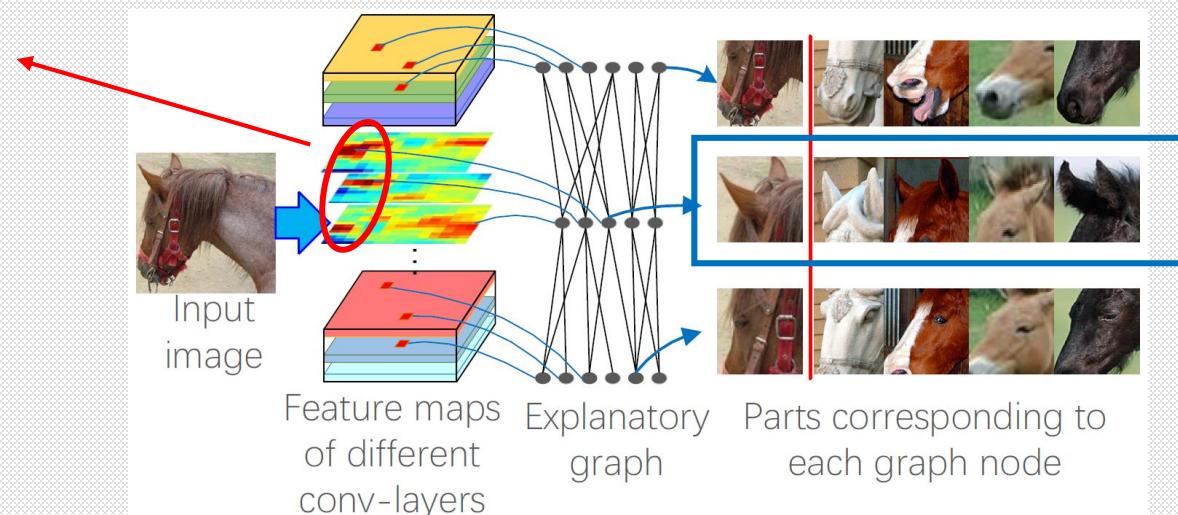
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A node of the explanatory graph is encoded as the **highly interacted activations** of a few filters.



E.g., these filters with highly interacted activations in certain area represent the head of a horse.

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The relationship between interactions and visual concepts

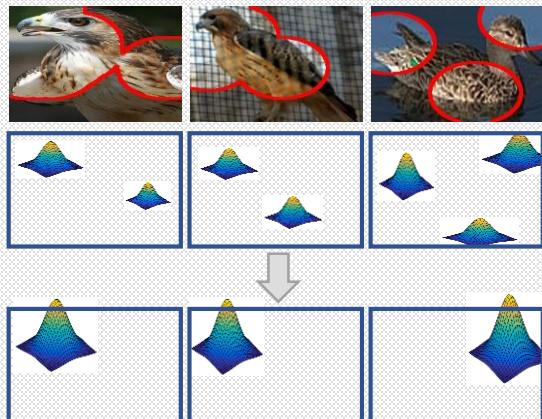
Learning interpretable features

Build an explanatory graph to explain the semantic hierarchy^[1]

The **interpretable CNN**, where each filter represents a specific object part^[2]

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A filter



Interpretable filters

Use **regional interaction activations** of a filter to represent object parts.

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Strongly interacted filters → meaningful concepts



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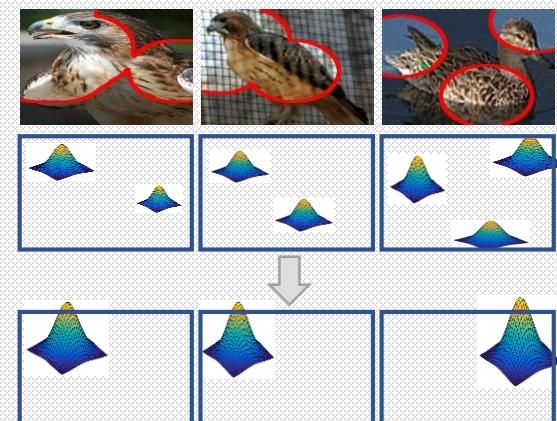
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A filter

Interpretable filters



Use **regional interaction activations** of a filter to represent object parts.

Each filter represents a specific part through different objects.

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The relationship between interactions and visual concepts

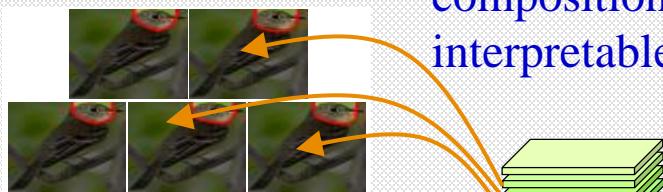
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Group 1



compositional and interpretable filters

Group 2



A group of filters **cooperate with each other** to make inferences.

The cooperative features have strong interactions.

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Strongly interacted filters → meaningful concepts



Wen Shen Quanshi Zhang



The relationship between interactions and visual concepts

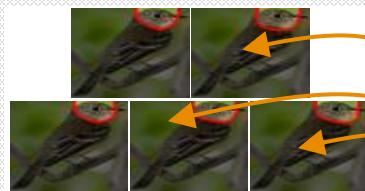
Learning interpretable features

Build an explanatory graph to explain the semantic hierarchy^[1]

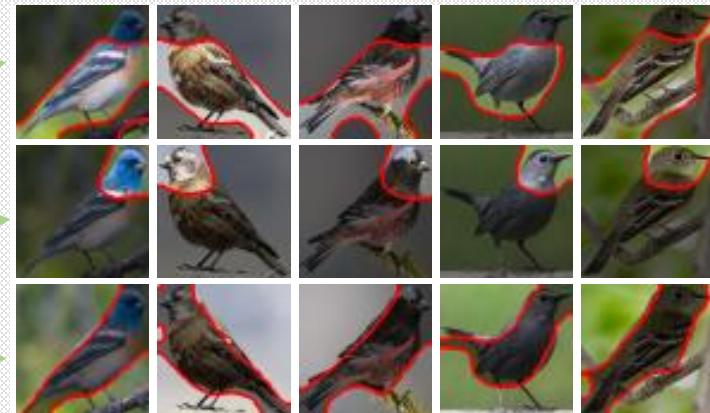
The interpretable CNN, where each filter represents a specific object part^[2]

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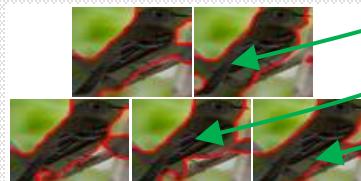
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Strongly interacted filters → meaningful concepts



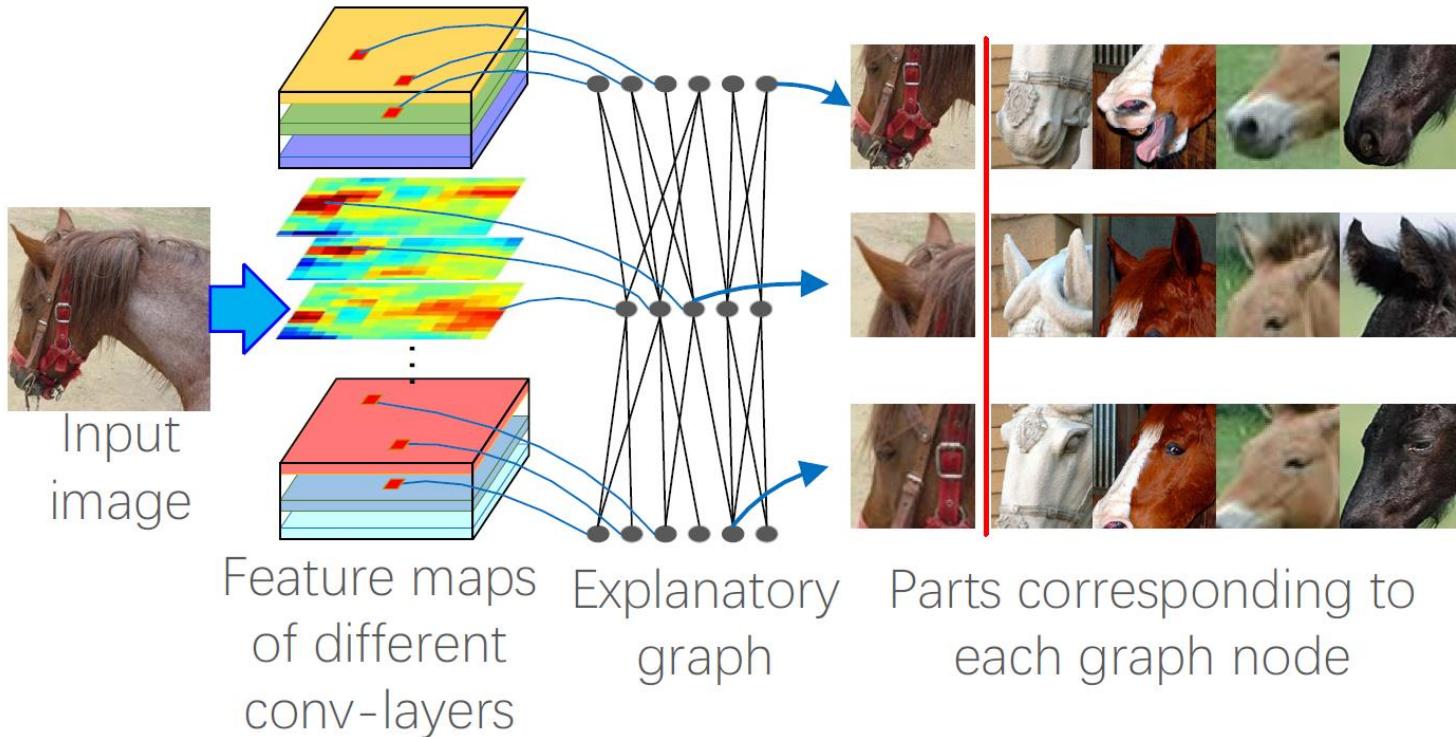
Wen Shen Quanshi Zhang

Quanshi Zhang et al. “Interpreting CNN Knowledge via an Explanatory Graph” in AAAI 2018



Wen Shen Quanshi Zhang

Object

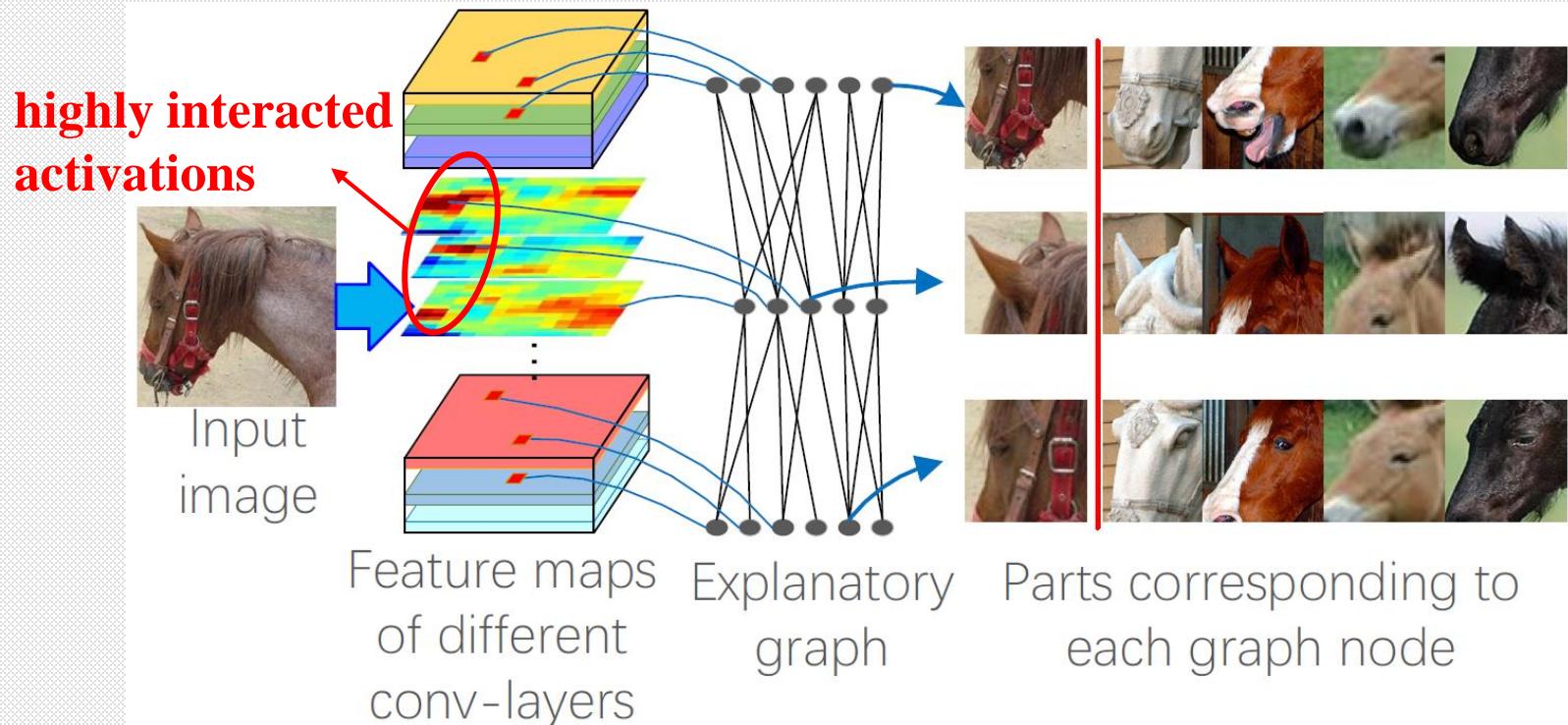


**Build an explanatory graph to explain
the semantic hierarchy hidden inside the network.**



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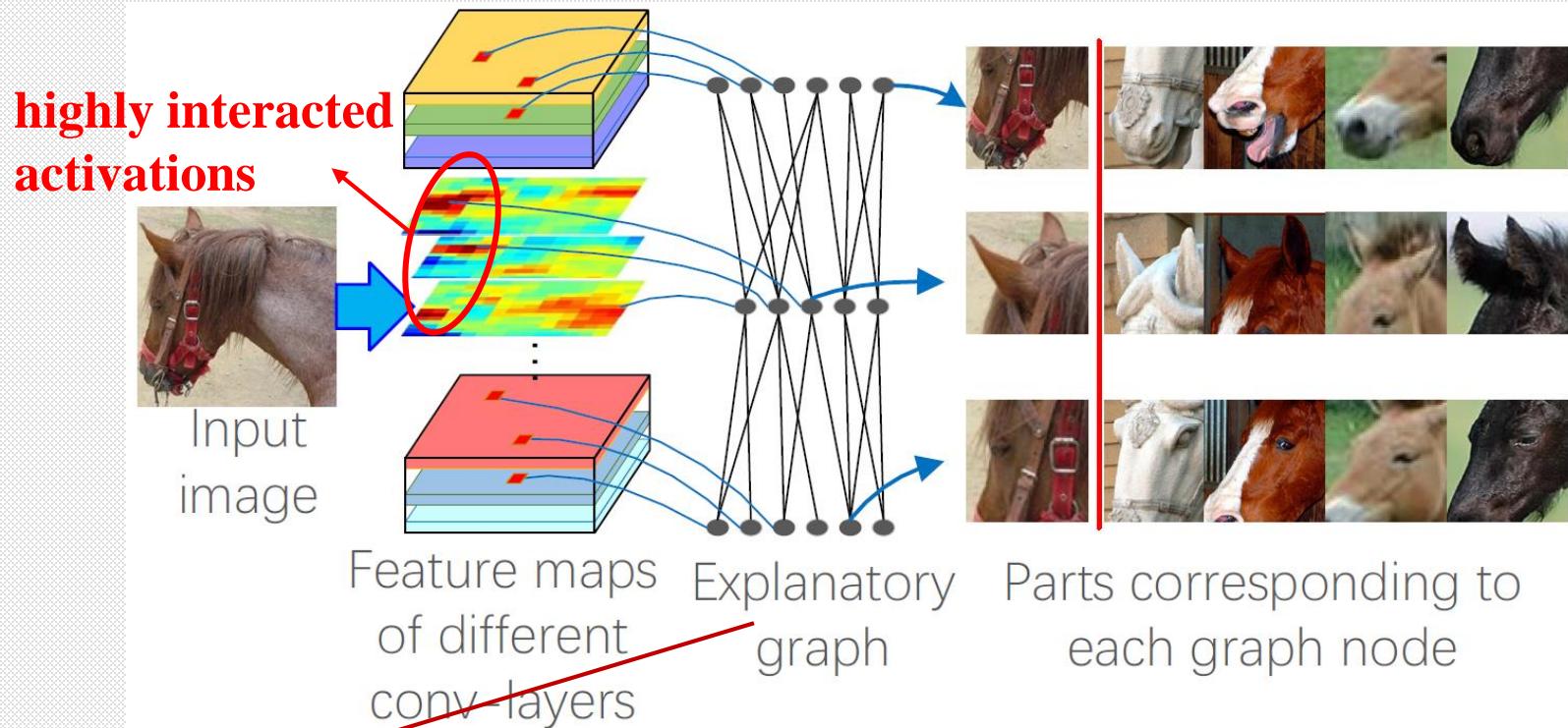
Objective





Wen Shen Quanshi Zhang

Object

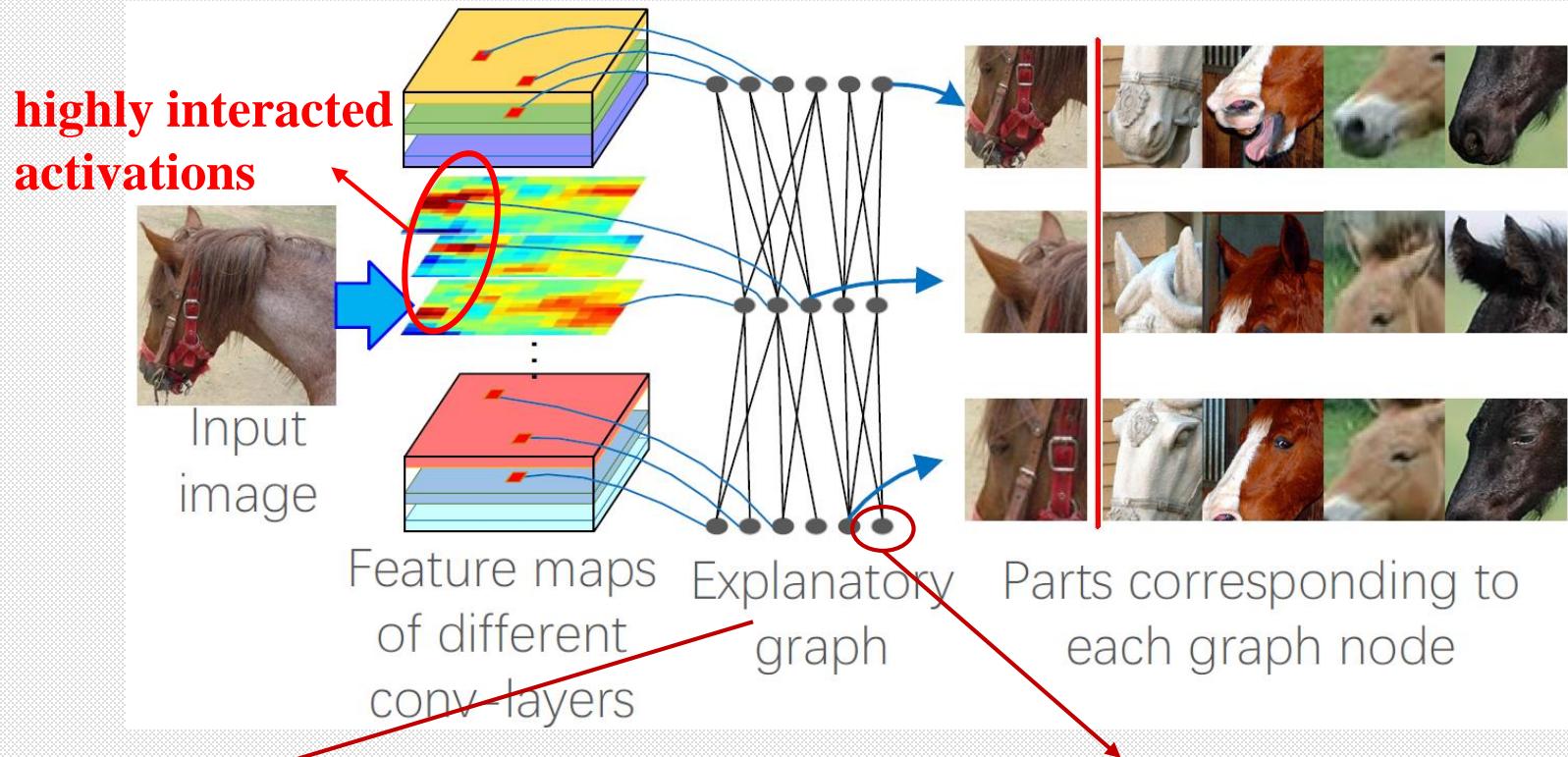


The graph has multiple layers →
multiple conv-layers of the CNN



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Object



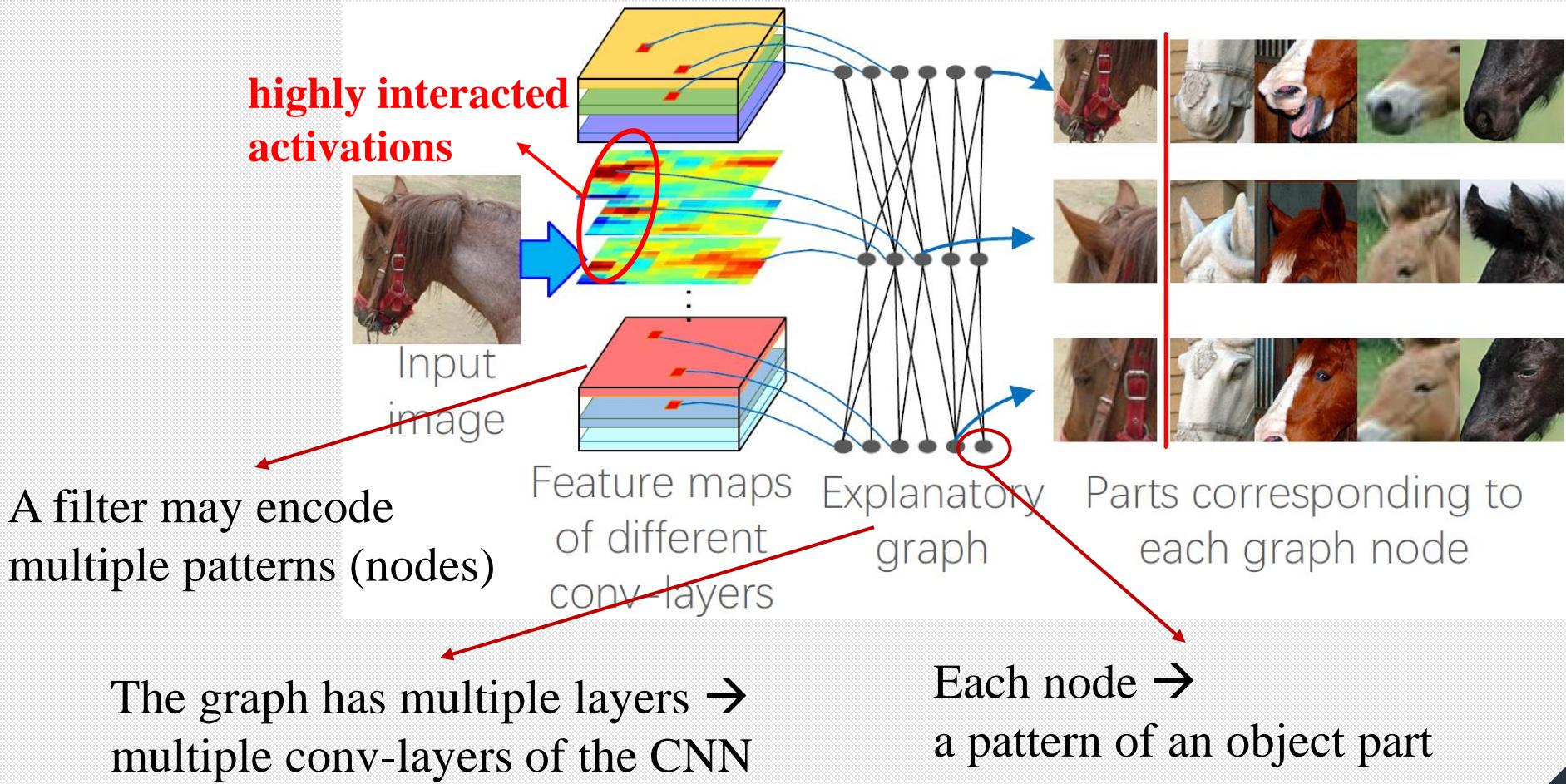
The graph has multiple layers →
multiple conv-layers of the CNN

Each node →
a pattern of an object part



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Object



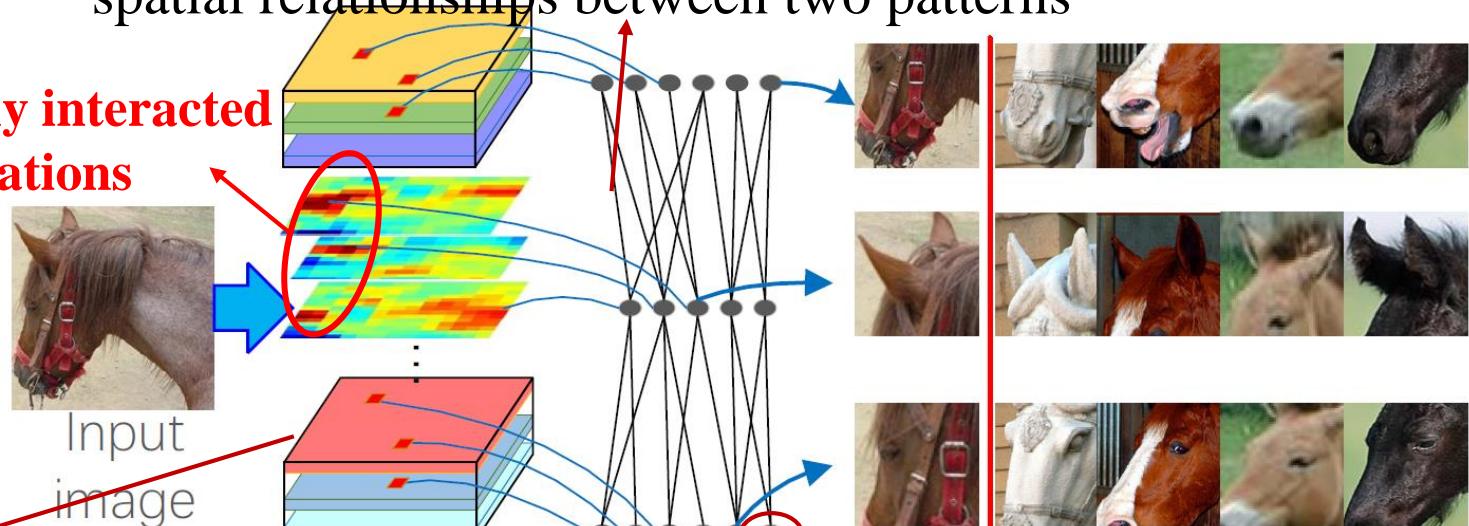


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Object

Each edge → co-activation relationships and spatial relationships between two patterns

highly interacted activations



A filter may encode multiple patterns (nodes)

The graph has multiple layers → multiple conv-layers of the CNN

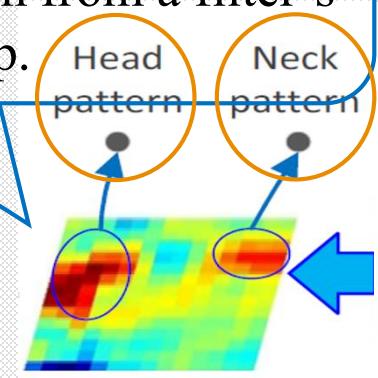
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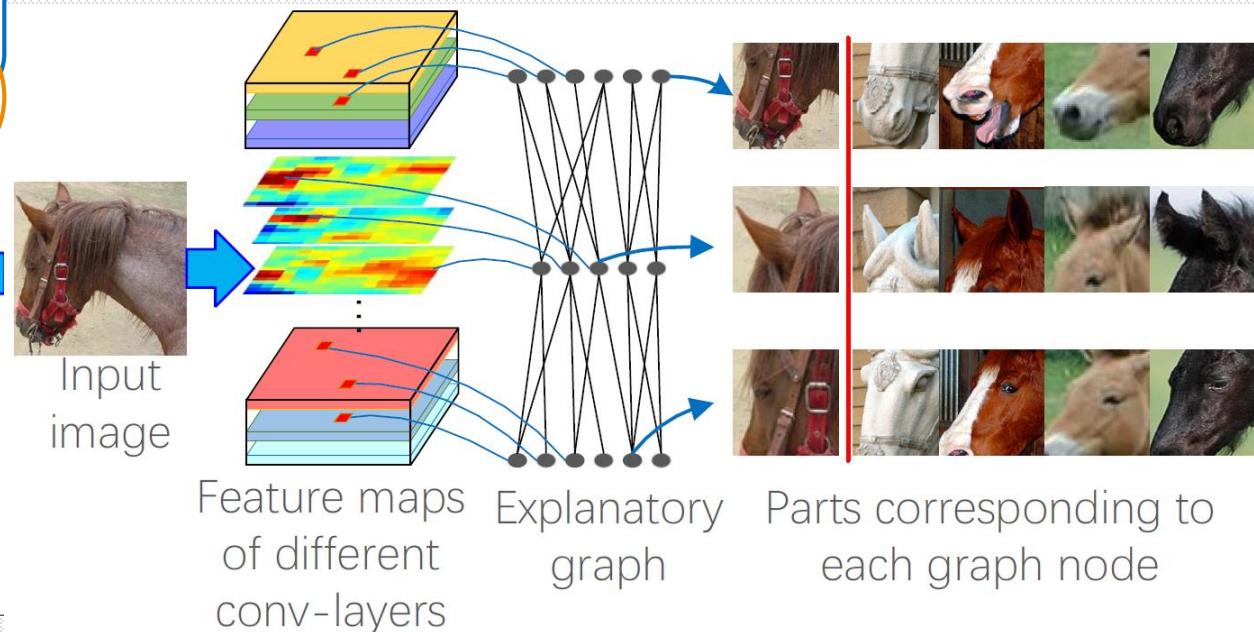
Wen Shen Quanshi Zhang

The explanatory graph

Disentangle the mixture of the head pattern and the neck pattern from a filter's feature map.



Mixture of patterns in a feature map of a channel

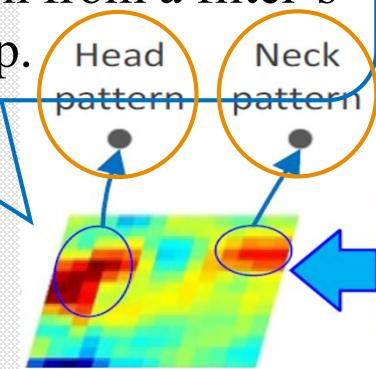




Wen Shen Quanshi Zhang

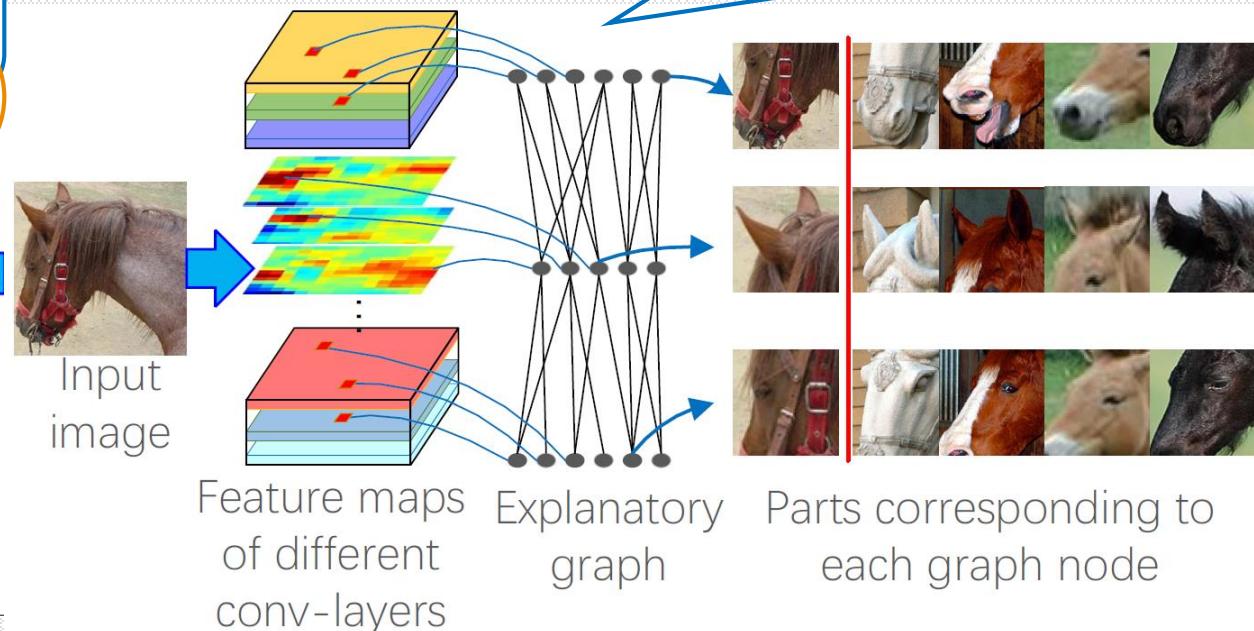
The explanatory graph

Disentangle the mixture of the head pattern and the neck pattern from a filter's feature map.



Mixture of patterns in a feature map of a channel

Summarize complex distributions of neural activations into a few patterns (nodes).

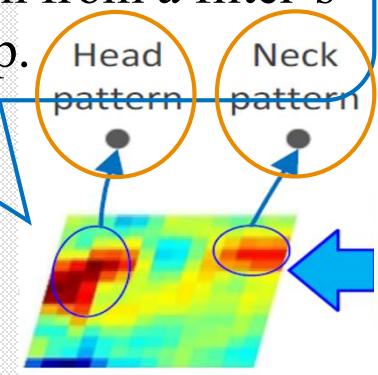




Wen Shen Quanshi Zhang

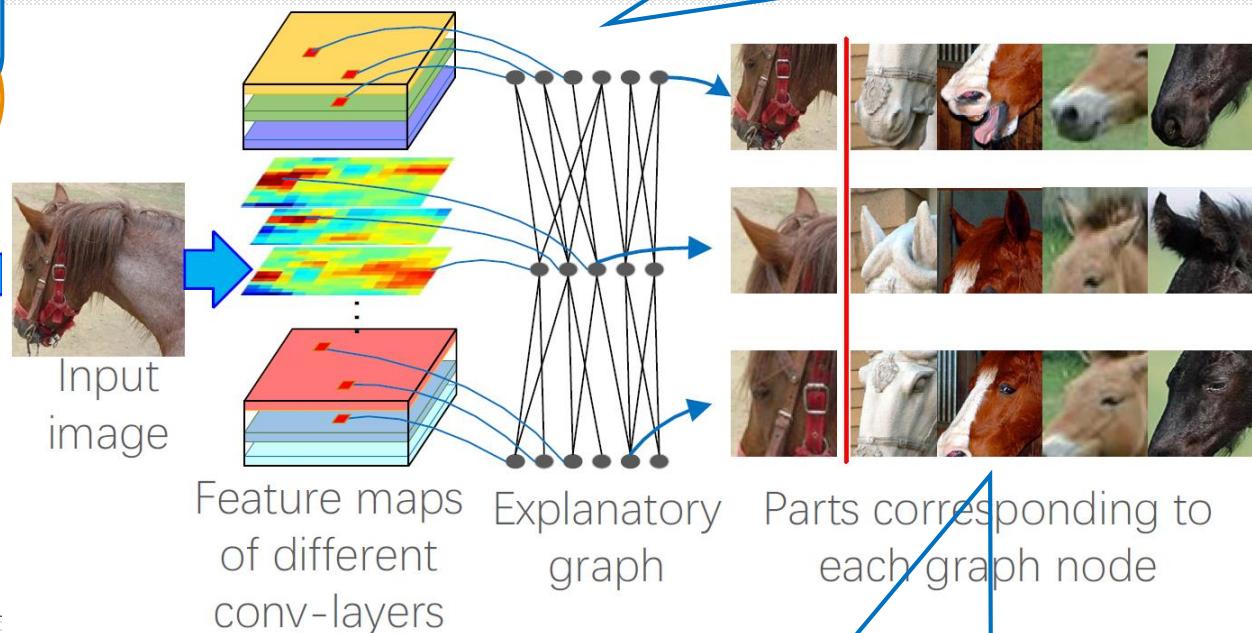
The explanatory graph

Disentangle the mixture of the head pattern and the neck pattern from a filter's feature map.



Mixture of patterns in a feature map of a channel

Summarize complex distributions of neural activations into a few patterns (nodes).



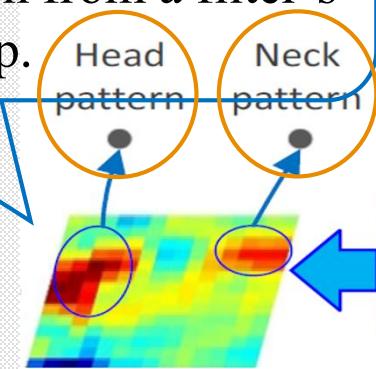
Each pattern consistently represents the same part among different images.



Wen Shen Quanshi Zhang

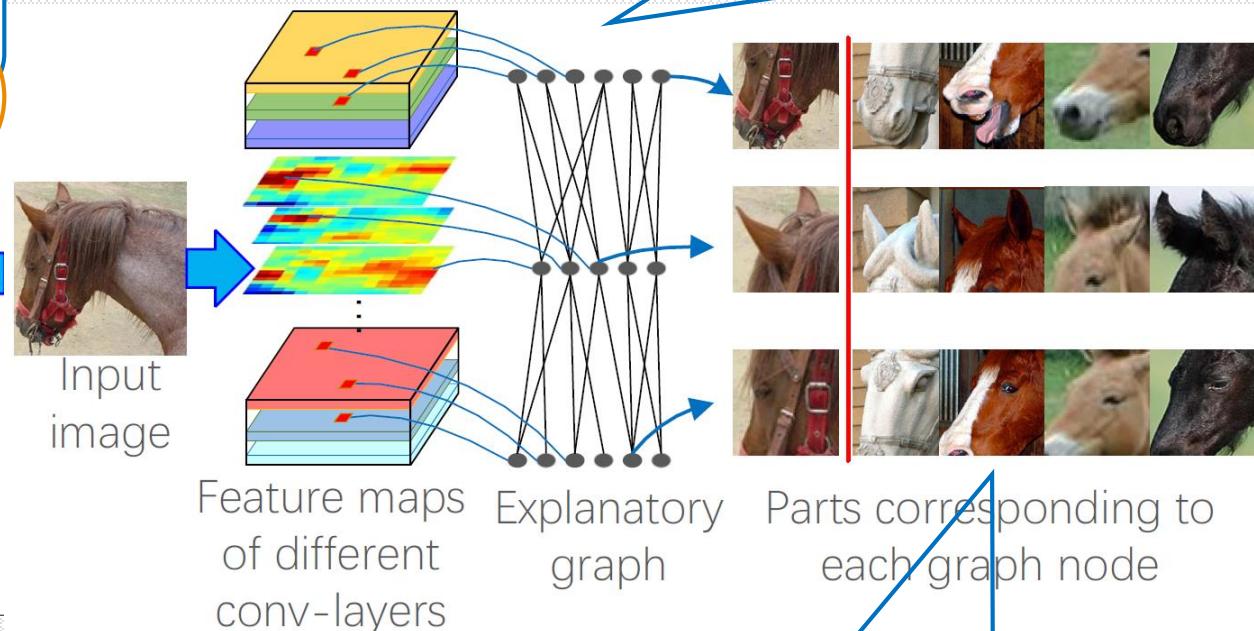
The explanatory graph

Disentangle the mixture of the head pattern and the neck pattern from a filter's feature map.



Mixture of patterns in a feature map of a channel

Summarize complex distributions of neural activations into a few patterns (nodes).



Filter out noisy activations on background from each feature map.

Each pattern **consistently** represents the same part among different images.



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Input & Output

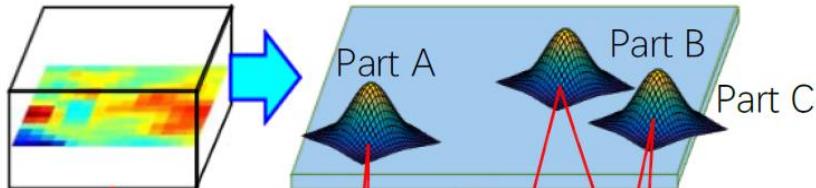
- Input:
 - A pre-trained CNN
 - trained for classification, segmentation, or ...
 - AlexNet, VGG-16, ResNet-50, ResNet-152, and etc.
 - Its training images with object bounding boxes
- Output: an explanatory graph



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Mining an explanatory graph

The $(L+2)$ -th conv-layer



Use a mixture of patterns to fit activation distributions of a feature map (just like GMM)

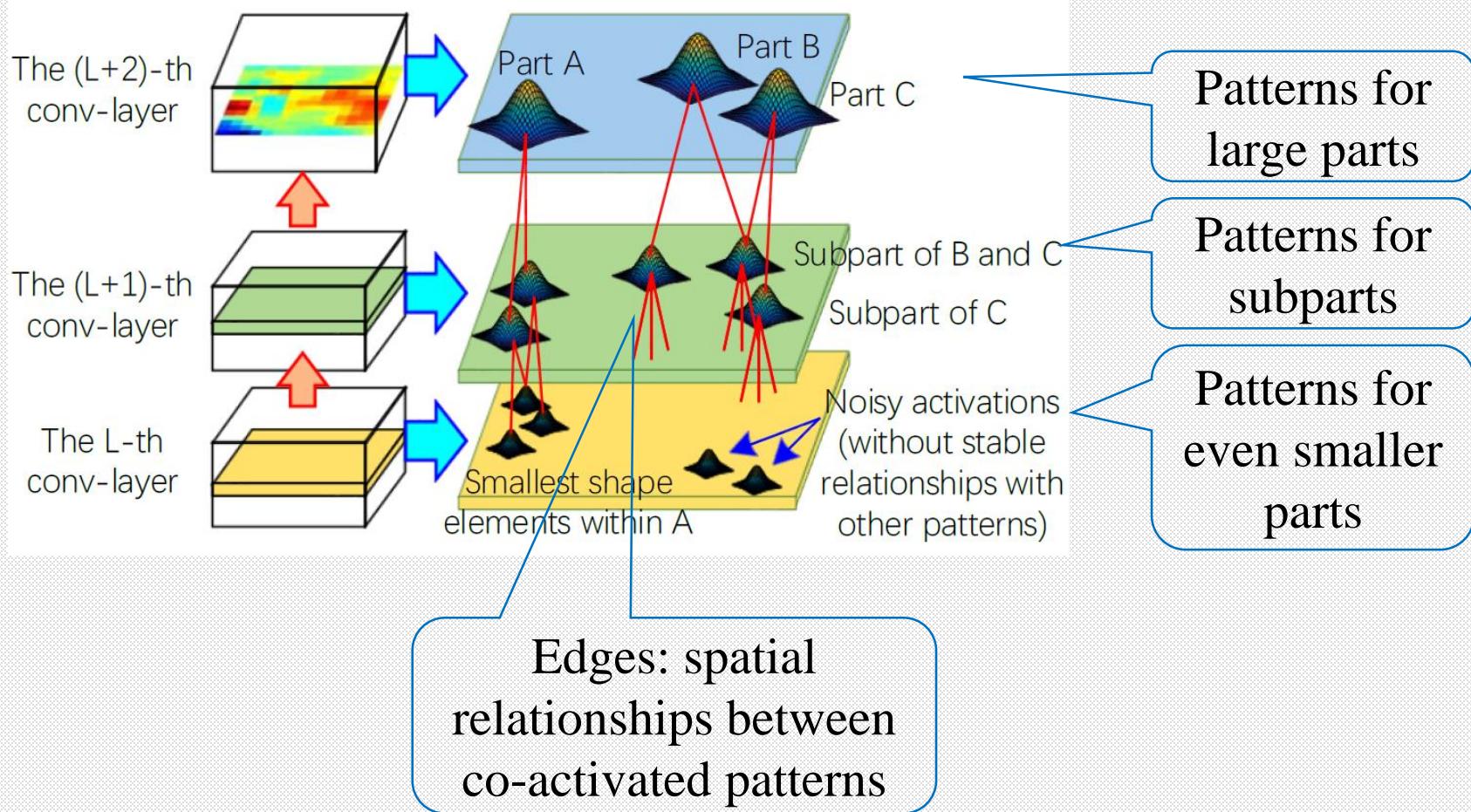
a feature map of a filter

→ a distribution of “activation entities”



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Mining an explanatory graph

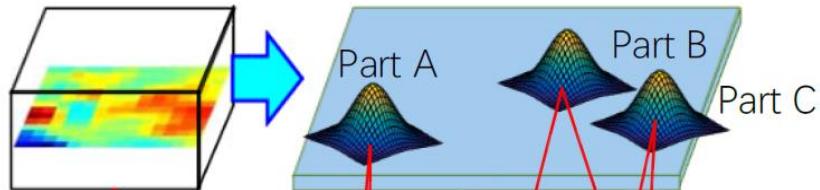




Wen Shen Quanshi Zhang

Mining an explanatory graph

The $(L+2)$ -th conv-layer



Use a mixture of patterns to fit activation distributions of a feature map (just like GMM)

Need to learn

1. Connections between nodes
2. Spatial relationships between connected nodes

Use such spatial relationships to disentangle feature maps of conv-layers.

Strongly interacted filters → meaningful concepts



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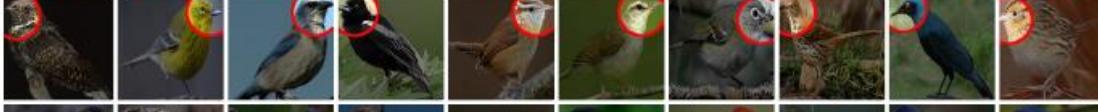
Node 1



Node 2



Node 3



Node 4



Node 5



Filter 1



Filter 2



Filter 3



Filter 4



Filter 5



Performance of nodes in the explanatory graph

Disentangle each pattern component from each filter's feature map.

Performance of raw filters in the CNN

Strongly interacted filters → meaningful concepts



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Quanshi Zhang et al. “Interpretable Convolutional Neural Networks” in CVPR 2018



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Object

Without additional part annotations, learn a CNN, where each filter represents a specific part through different objects.



Neural activations of 3 interpretable filters



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Input & Output

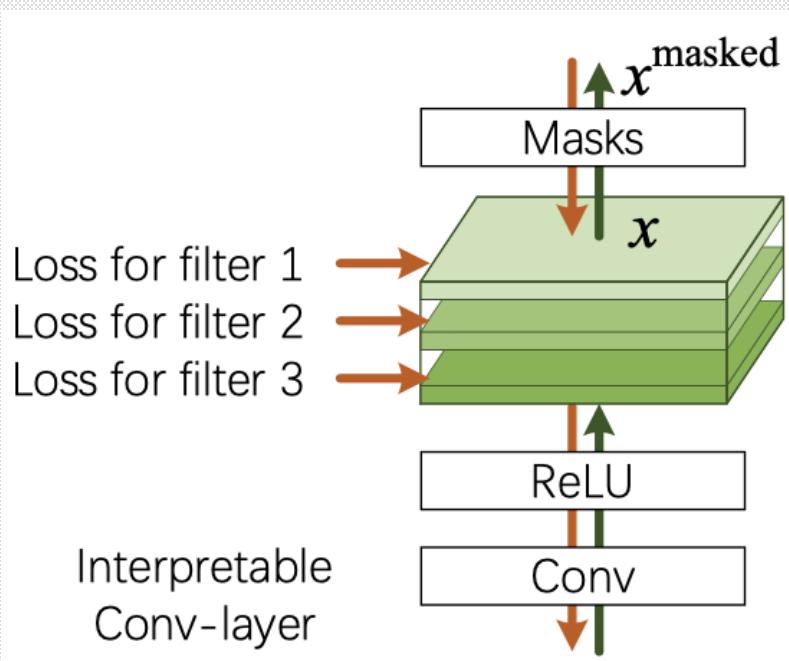
- Input
 - Training samples (X_i, Y_i) for a certain task
 - **No annotations of parts or textures are used.**
- Output
 - An interpretable CNN with disentangled filters



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Network structure

Add a loss to each channel to construct an interpretable layer



$$\text{Loss} = \underbrace{\text{Loss}(\hat{y}, y^*)}_{\text{task loss}} + \sum_f \underbrace{\text{Loss}_f(x)}_{\text{filter loss}}$$

The filter loss boosts the mutual information between feature maps X and a set of pre-defined templates T .

$$\text{Loss}_f = -MI(\mathbf{X}; \mathbf{T}) \quad \text{for filter } f$$

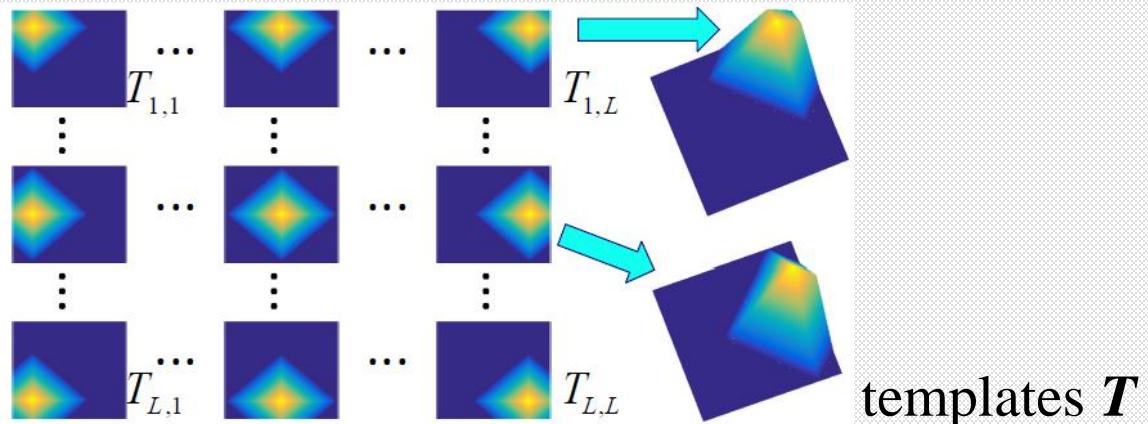


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Network structure

Understanding the filter loss: the filter loss boosts the mutual information between feature maps X and a set of pre-defined templates T .

$$Loss_f = -MI(\mathbf{X}; \mathbf{T})$$



$$Loss_f = -H(\mathbf{T}) + H(\mathbf{T}' = \{\mathbf{T}^-, \mathbf{T}^+\} | \mathbf{X}) + \sum_x p(\mathbf{T}^+, x) H(\mathbf{T}^+ = \{T_\mu\} | X=x)$$

A constant

Entropy of inter-category activations

Entropy of the spatial distribution of activations

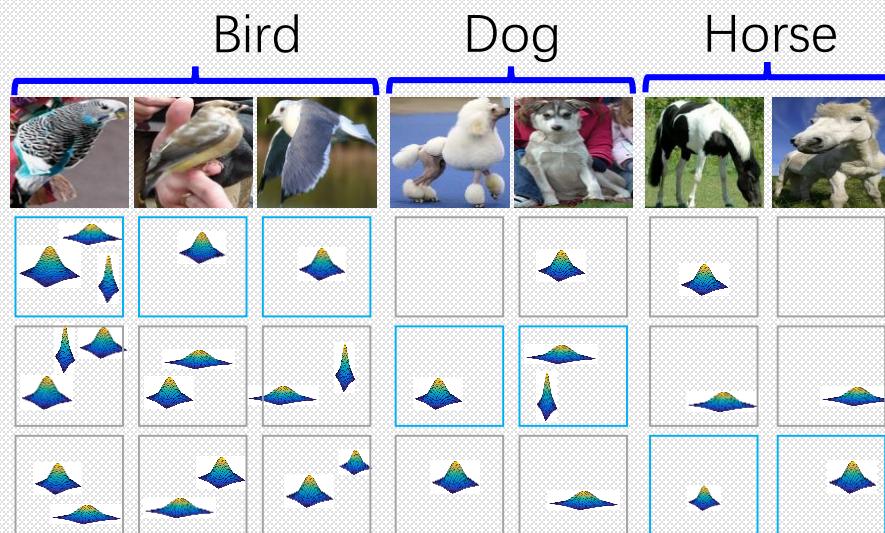


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Learning

From chaotic feature maps to the disentangled maps of object parts

$$Loss_f = \underbrace{-H(\mathbf{T})}_{\text{A constant}} + \underbrace{H(\mathbf{T}' = \{T^-, \mathbf{T}^+\} | \mathbf{X})}_{\text{Entropy of inter-category activations}} + \sum_x p(\mathbf{T}^+, x) H(\mathbf{T}^+ = \{T_\mu\} | X=x) \underbrace{\quad}_{\text{Entropy of the spatial distribution of activations}}$$



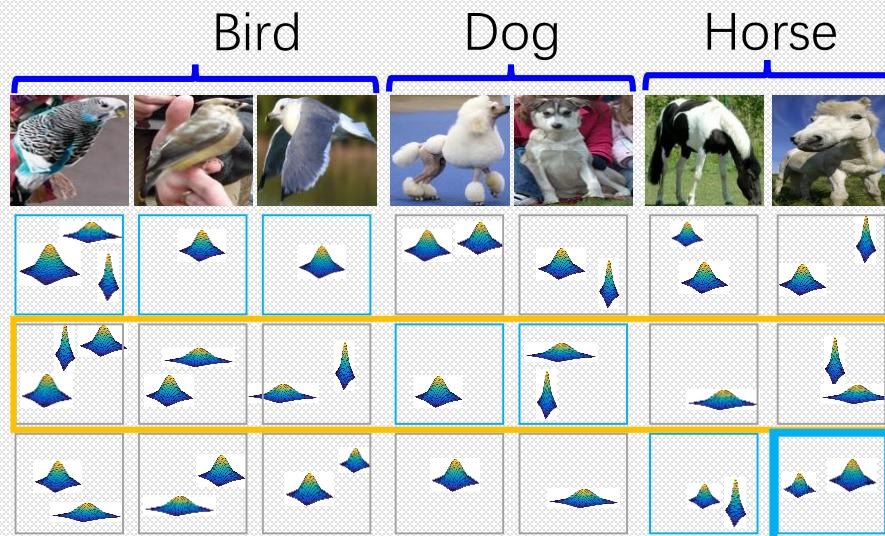


Wen Shen Quanshi Zhang

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The loss encourages a low inter-class entropy, i.e., **increasing regional activations with strong interactions.**

The loss encourages a low spatial entropy.

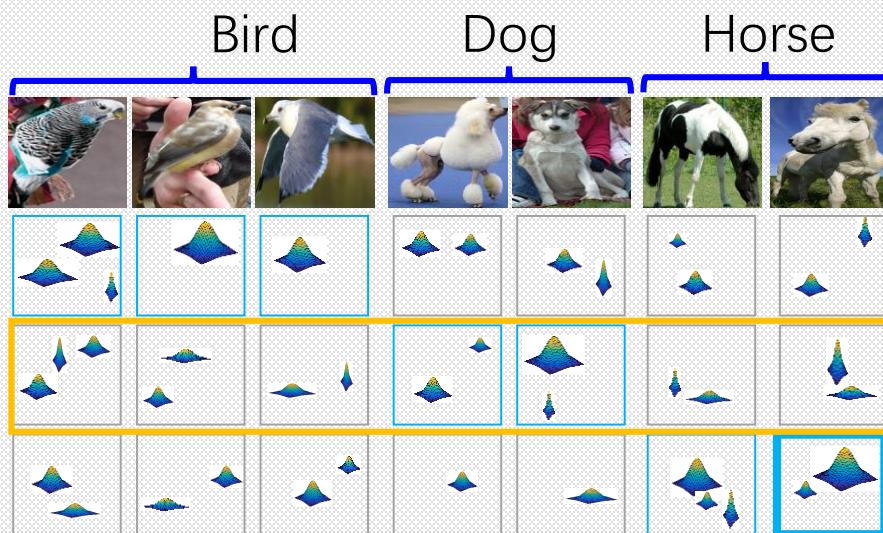


Wen Shen Quanshi Zhang

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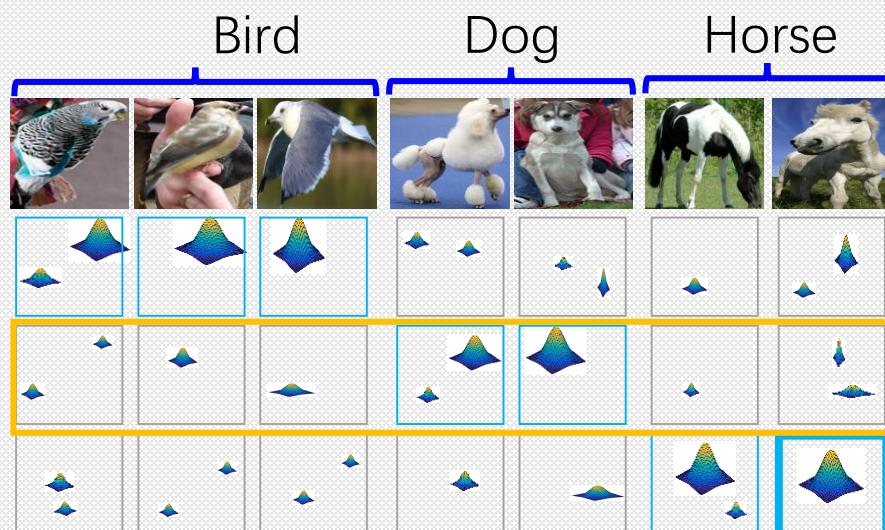


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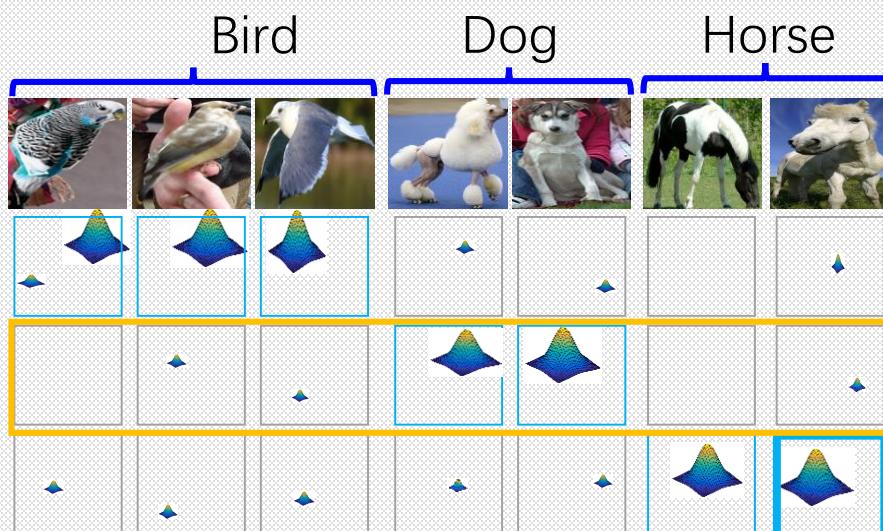


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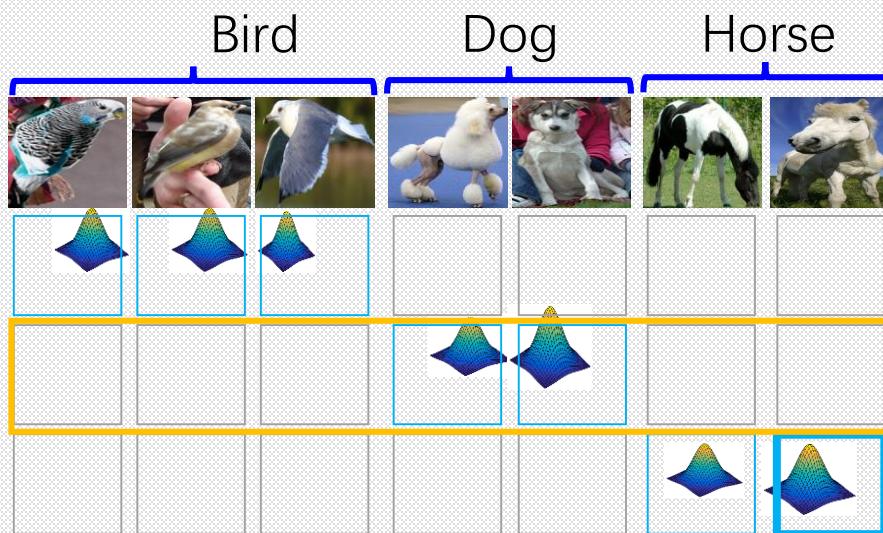


Wen Shen Quanshi Zhang

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The loss encourages a low inter-class entropy, i.e., **increasing regional activations with strong interactions.**

The loss encourages a low spatial entropy.



Activation regions of interpretable filters.

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	Filter 1	Filter 2	Filters 3 & 4	
Filter				
Filter				
Filter				

Strongly interacted filters → meaningful concepts



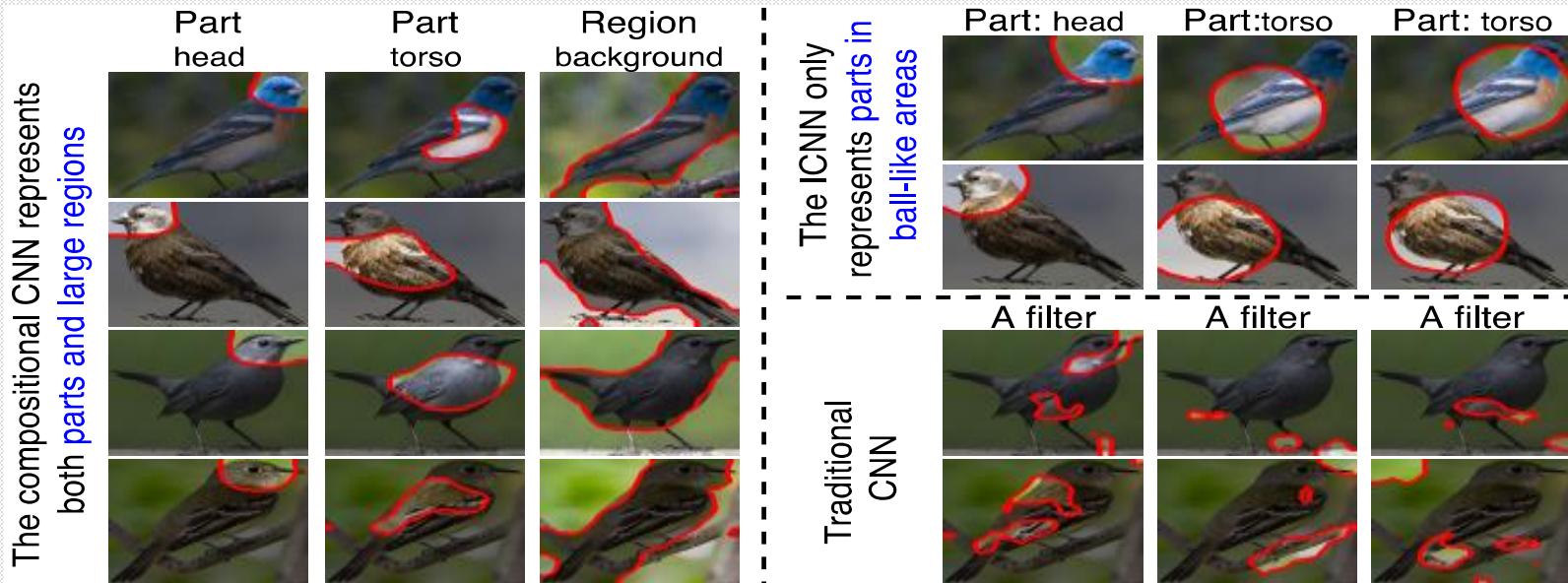
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Wen Shen et al. “Interpretable Compositional Convolutional Neural Networks” in IJCAI 2021



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Object



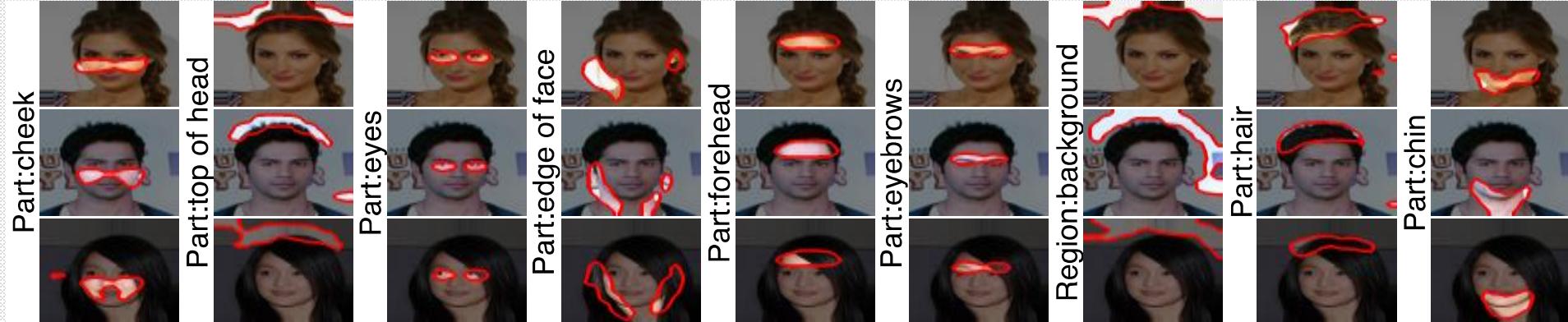
- Traditional CNN: has no self-reflection of its representations.
- ICNN^[1]: only represents object parts in ball-like areas.
- **Our compositional CNN: represents both object parts with specific shapes and image regions without specific structures.**

Strongly interacted filters → meaningful concepts

Object



Wen Shen Quanshi Zhang

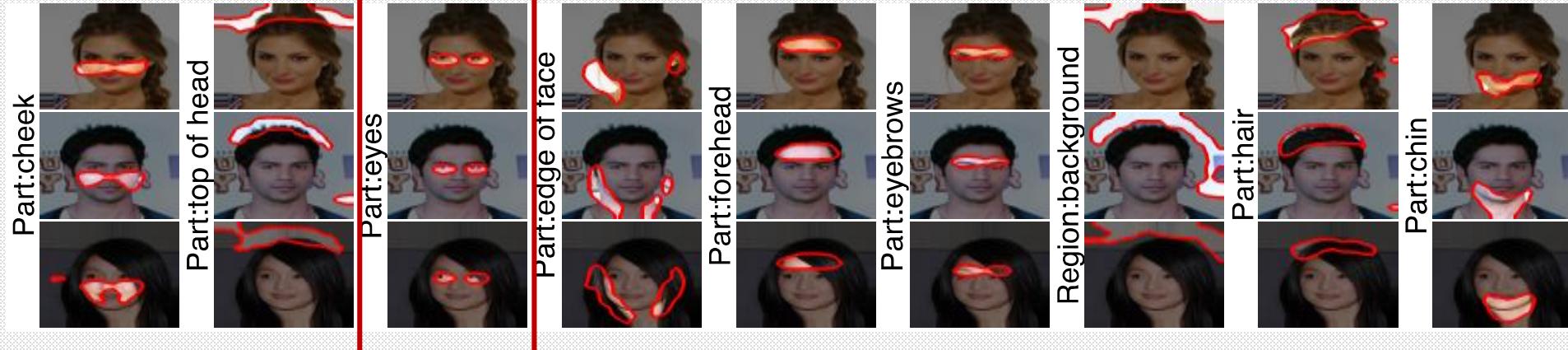


- Compositional interpretable filters should satisfy the following **two properties.**
 - **Consistency.**
 - **Diversity.**

Objective



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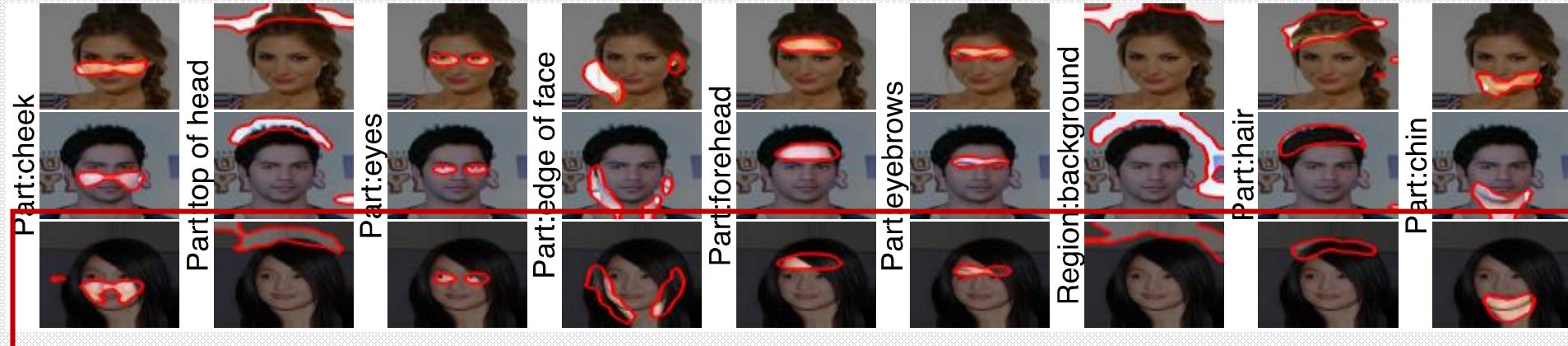


- Compositional interpretable filters should satisfy the following **two properties**.
 - **Consistency.** Each filter is supposed to be consistently activated by **the same object part or the same image region** through different images.
 - **Diversity.**



Wen Shen Quanshi Zhang

Objective



- Compositional interpretable filters should satisfy the following **two properties.**
 - **Consistency.** Each filter is supposed to be consistently activated by the same object part or the same image region through different images.
 - **Diversity.** Different filters are supposed to be activated by different object parts or image regions.



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Input & Output

- Input
 - Training samples (X_i, Y_i) for a certain task.
 - **No** annotations of object parts or image regions are used.
- Output
 - An interpretable compositional CNN with disentangled filters.



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Method

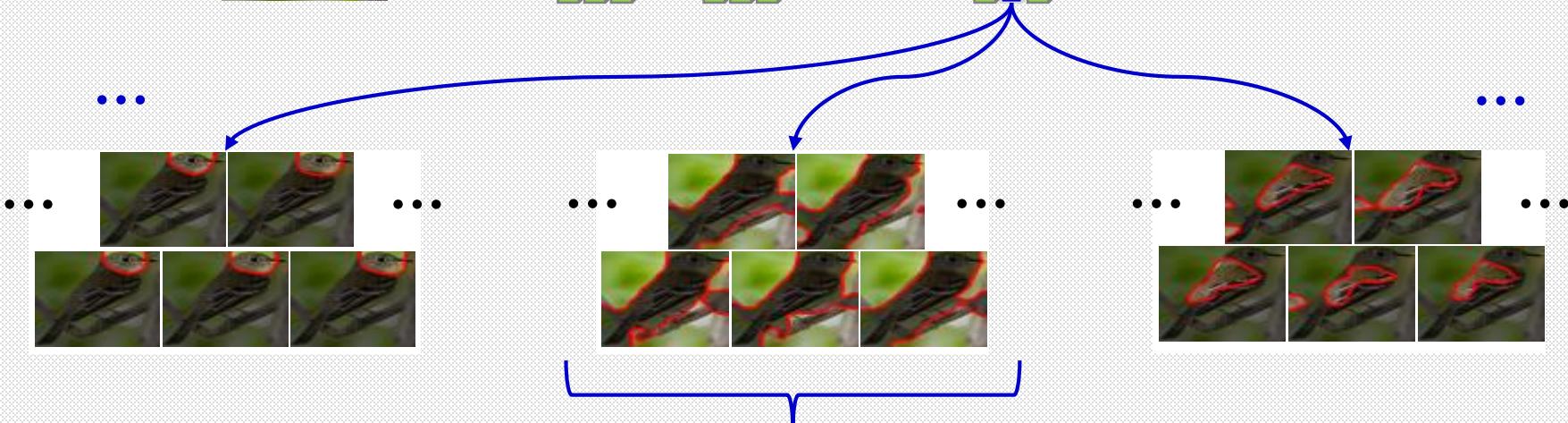
- To satisfy the properties of consistency and diversity
 - use a set of filters to jointly represent a specific part/region, instead of using a single filter → **consistency**



Wen Shen Quanshi Zhang

Method

An interpretable compositional convolutional layer



A group of filters **cooperate with each other** to make inferences



Consistency

The cooperative features have strong interactions.



Wen Shen Quanshi Zhang

Method

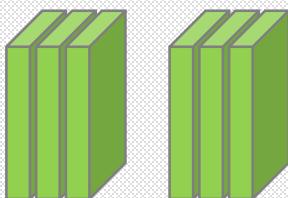
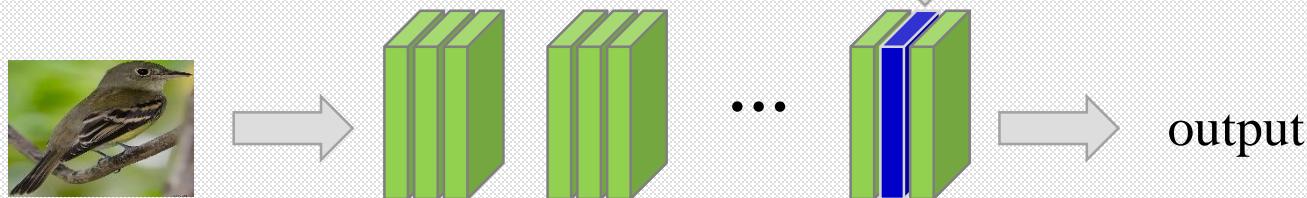
- To satisfy the properties of consistency and diversity
 - use a set of filters to jointly represent a specific part/region, instead of using a single filter → **consistency**
 - use different sets of filters to represent different parts/regions → **diversity**



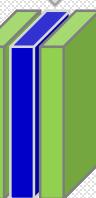
Wen Shen Quanshi Zhang

Method

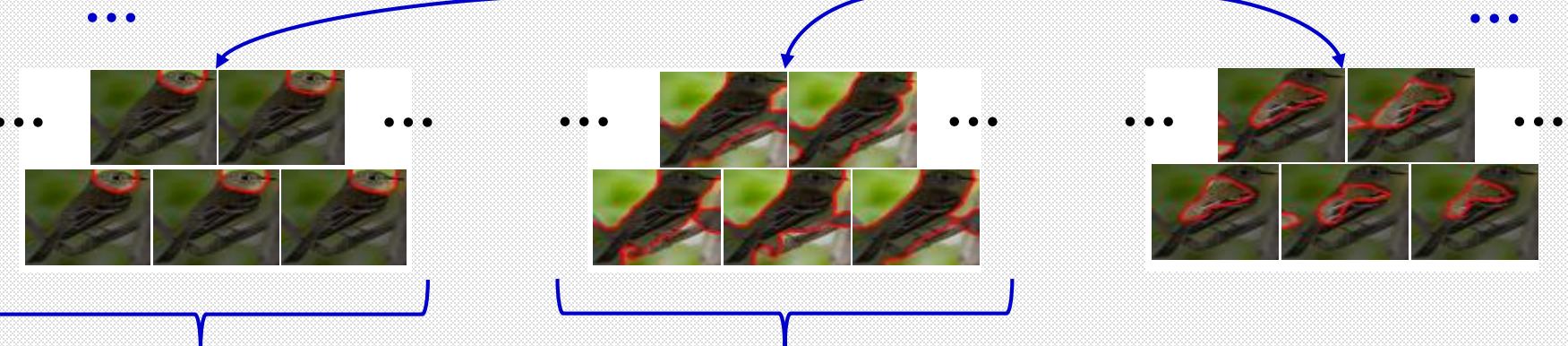
An interpretable compositional convolutional layer



...



output



Different groups of filters represent
different parts/regions.



Diversity

Features of filters in different groups have weak interactions.



Wen Shen Quanshi Zhang

Method

- To satisfy the properties of consistency and diversity
 - use a set of filters to jointly represent a specific part/region, instead of using a single filter → **consistency**
 - use different sets of filters to represent different parts/regions → **diversity**
- We add a loss to the target convolutional layer to construct an compositional interpretable layer

$$L(\theta, \mathbf{A}) = \underbrace{\lambda Loss(\theta, \mathbf{A})}_{\text{filter loss}} + \frac{1}{n} \sum_{I \in \mathbf{I}} \underbrace{L^{\text{cls}}(\hat{y}_I, y_I^*; \theta)}_{\text{task loss}},$$



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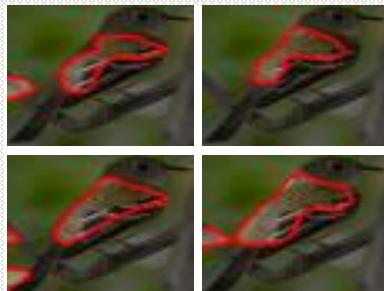
Method

- To satisfy the properties of consistency and diversity
 - use a set of filters to jointly represent a specific part/region, instead of using a single filter → **consistency**
 - use different sets of filters to represent different parts/regions → **diversity**

$$\text{Loss}(\theta, \mathbf{A}) = - \sum_{k=1}^K \frac{S_k^{\text{within}}}{S_k^{\text{all}}} = - \sum_{k=1}^K \frac{\sum_{i,j \in A_k} s_{ij}}{\sum_{i \in A_k, j \in \Omega} s_{ij}}$$

Measure the similarity between filters in the group A_k

These four filters have similar activation regions (i.e. these filters have **strong interactions**)





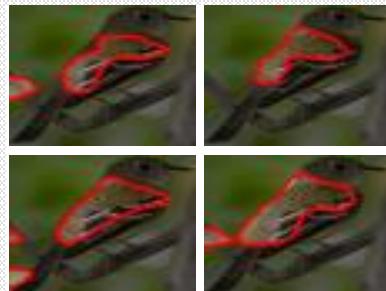
Wen Shen Quanshi Zhang

Method

- To satisfy the properties of consistency and diversity
 - use a set of filters to jointly represent a specific part/region, instead of using a single filter → **consistency**
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Measure the similarity between filters in the group A_k



These four filters have similar activation regions (i.e. these filters have **strong interactions**)

Increase the similarity between filters in the **same** group to ensure the consistency.



Wen Shen Quanshi Zhang

Method

- To satisfy the properties of consistency and diversity
 - use a set of filters to jointly represent a specific part/region, instead of using a single filter → **consistency**
 - use **different sets of filters** to represent different parts/regions → **diversity**

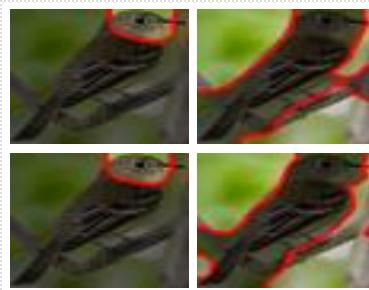
$$\text{Loss}(\theta, \mathbf{A}) = - \sum_{k=1}^K \frac{S_k^{\text{within}}}{S_k^{\text{all}}} = - \sum_{k=1}^K \frac{\sum_{i,j \in A_k} s_{ij}}{\sum_{i \in A_k, j \in \Omega} s_{ij}}$$

Measure the similarity between filters in A_k and *all* filters (Ω) in the target layer.

Filters in A_k



Other filters



These four filters have different activation regions (i.e. these filters have **weak interactions**)



Wen Shen Quanshi Zhang

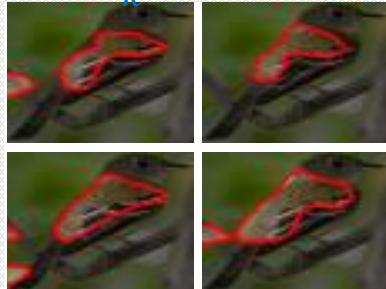
Method

- To satisfy the properties of consistency and diversity
 - use a set of filters to jointly represent a specific part/region, instead of using a single filter → **consistency**
 - use **different sets of filters** to represent different parts/regions → **diversity**

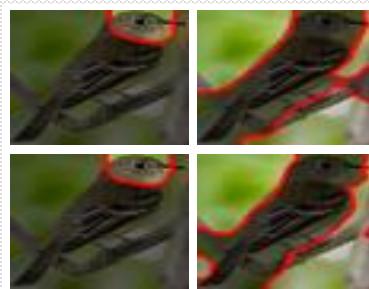
$$\text{Loss}(\theta, \mathbf{A}) = - \sum_{k=1}^K \frac{S_k^{\text{within}}}{S_k^{\text{all}}} = - \sum_{k=1}^K \frac{\sum_{i,j \in A_k} s_{ij}}{\sum_{i \in A_k, j \in \Omega} s_{ij}}$$

Measure the similarity between filters in A_k and *all* filters (Ω) in the target layer.

Filters in A_k



Other filters



These four filters have different activation regions (i.e. these filters have **weak interactions**)

Decrease the similarity between filters in **different** groups to ensure the diversity.



Wen Shen Quanshi Zhang

Method

- We add a loss to the target convolutional layer to construct an compositional interpretable layer, **where filters satisfy the properties of consistency and diversity.**

$$\text{Loss}(\theta, \mathbf{A}) = - \sum_{k=1}^K \frac{S_k^{\text{within}}}{S_k^{\text{all}}} = - \sum_{k=1}^K \frac{\sum_{i,j \in A_k} s_{ij}}{\sum_{i \in A_k, j \in \Omega} s_{ij}}$$

- The similarity between filters i, j is implemented as a kernel function.

$$s_{ij} = \mathcal{K}(X_i, X_j) = \boxed{\rho_{ij}} + 1 = \frac{\text{cov}(X_i, X_j)}{\sigma_i \sigma_j} + 1 \geq 0,$$

The Pearson's correlation coefficient between variables x_i^I and x_j^I through different images.



Wen Shen Quanshi Zhang

Method

- We add a loss to the target convolutional layer to construct an compositional interpretable layer, where filters satisfy the properties of consistency and diversity.

$$\text{Loss}(\theta, \mathbf{A}) = - \sum_{k=1}^K \frac{S_k^{\text{within}}}{S_k^{\text{all}}} = - \sum_{k=1}^K \frac{\sum_{i,j \in A_k} s_{ij}}{\sum_{i \in A_k, j \in \Omega} s_{ij}}$$

Measure the similarity between feature maps of filters i, j .

- The similarity between filters i, j is implemented as a kernel function.

$$s_{ij} = \mathcal{K}(X_i, X_j) = \rho_{ij} + 1 = \frac{\text{cov}(X_i, X_j)}{\sigma_i \sigma_j} + 1 \geq 0,$$

The Pearson's correlation coefficient between variables x_i^I and x_j^I through different images.



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Learning of the filter loss

The minimization of $\text{Loss}(\theta, \mathbf{A})$ is essentially equivalent to the problem of the spectral clustering^[2].

$$\frac{1}{2}(\text{Loss}(\theta, \mathbf{A}) + K) = \frac{1}{2} \sum_{k=1}^K \frac{\sum_{i \in A_k, j \notin A_k} s_{ij}}{\sum_{i \in A_k, j \in \Omega} s_{ij}}$$



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• Broad applicability

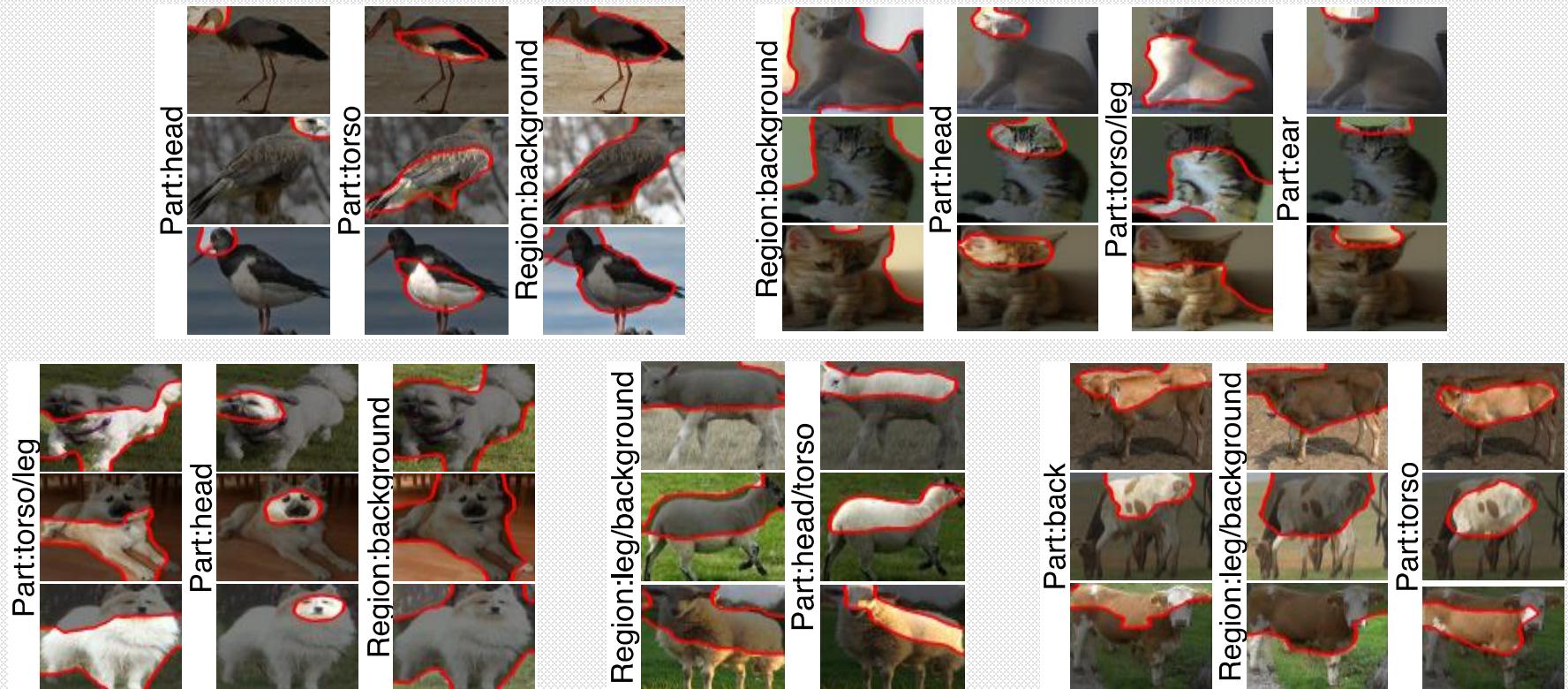
- Can be applied to different task
 - e.g. object classification, segmentation, etc.
- Tested on different CNNs
 - VGG-13
 - VGG-16
 - ResNet-18
 - ResNet-50
 - DenseNet-121
 - DenseNet-161



Activation regions of interpretable filters

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Binary classification of a single category.



Each filter in a compositional CNN consistently represented the same object part or the same image region, while different filters represented different parts and regions.

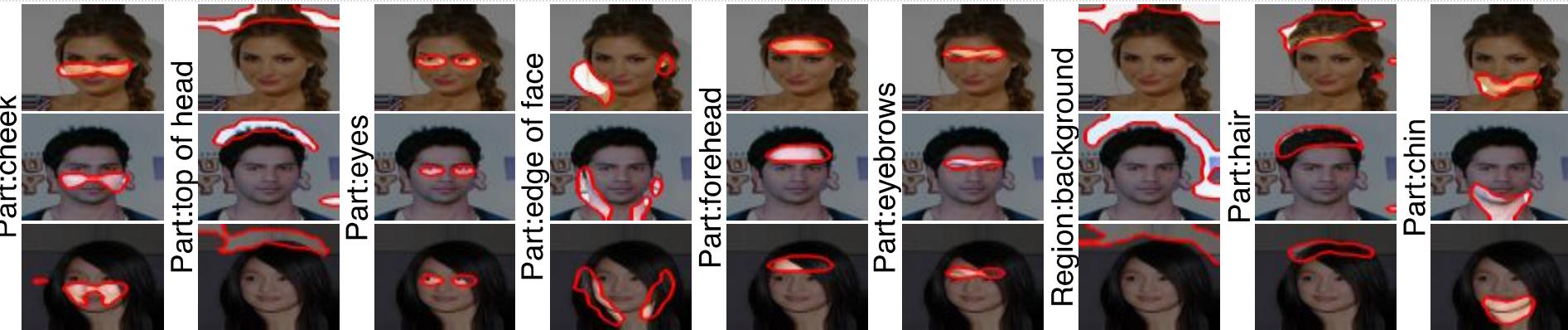


Activation regions of interpretable filters



Wen Shen Quanshi Zhang

Multi-label classification.



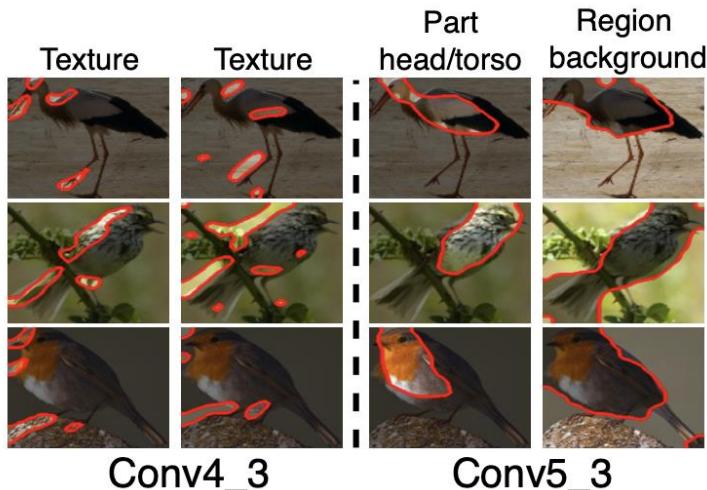
Interpretable filters in a ICNN encoded **very few** types of patterns, which are concentrated in the center of the face.

Interpretable filters in a compositional CNN encoded **diverse** patterns, covering almost all elements of the face image, such as forehead, eyes, nose, etc.



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More visualization



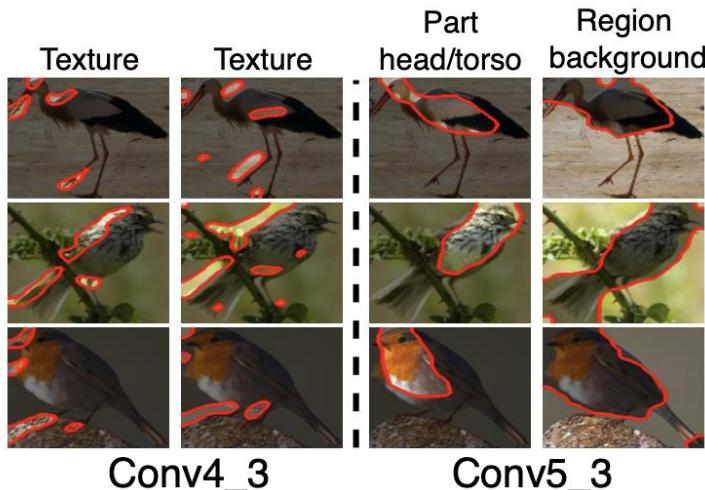
Comparison of interpretable filters of a high convolutional layer and a middle convolutional layer.

High convolutional layer: Interpretable filters usually represent object parts or image regions;
Low convolutional layer: Interpretable filters usually represent local textures or shapes.



Wen Shen Quanshi Zhang

More visualization

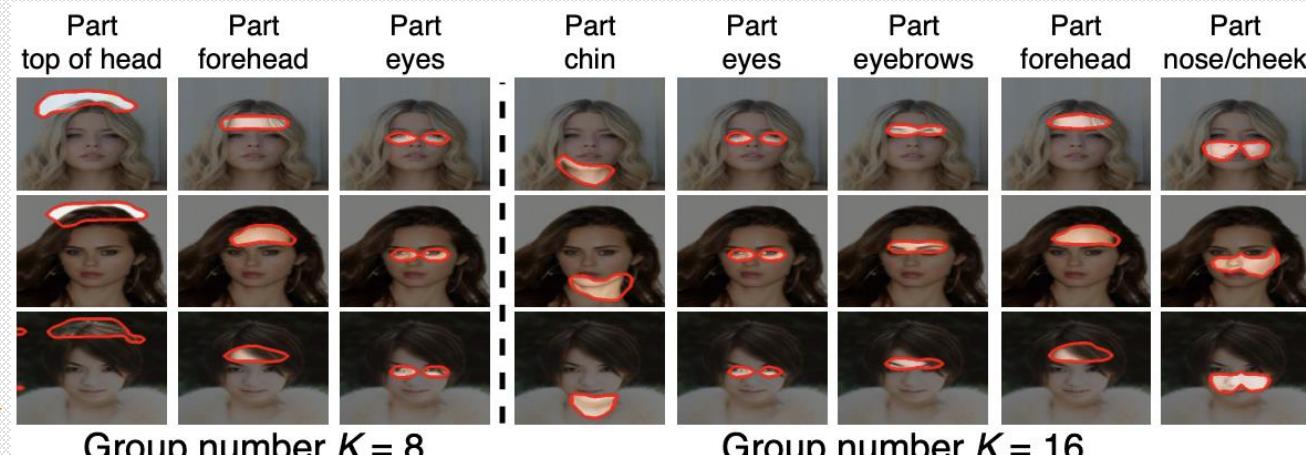


Comparison of interpretable filters of a high convolutional layer and a middle convolutional layer.

High convolutional layer: Interpretable filters usually represent object parts or image regions;
Low convolutional layer: Interpretable filters usually represent local textures or shapes.

Comparison of interpretable filters learned with different values of

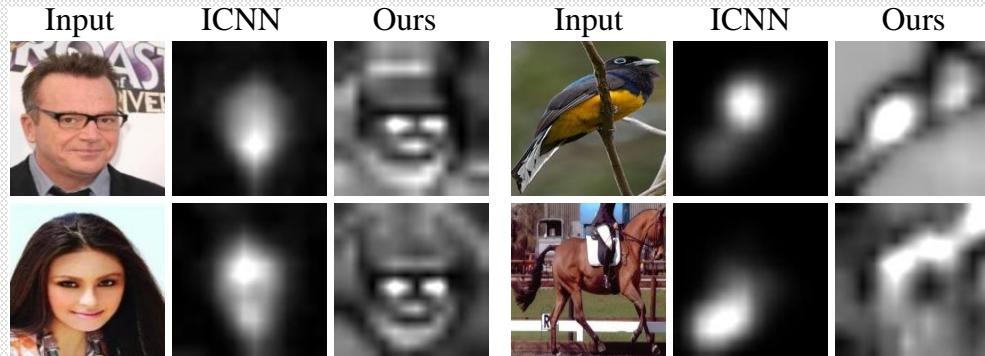
As group number increases, more detailed visual patterns are learned.





Wen Shen Quanshi Zhang

More visualization



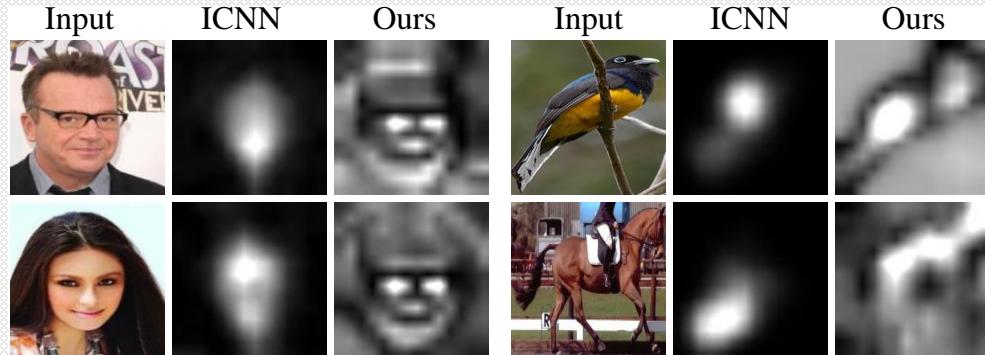
Visualizing distributions of visual patterns that are encoded in interpretable filters.

Interpretable filters of a compositional CNN explain much more regions in an image than those of an ICNN.



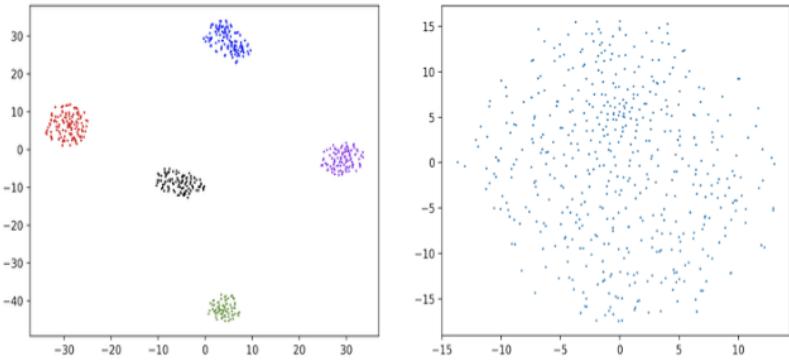
Wen Shen Quanshi Zhang

More visualization



Visualizing distributions of visual patterns that are encoded in interpretable filters.

Interpretable filters of a compositional CNN explain much more regions in an image than those of an ICNN.



(c1) compositional CNN

(c2) traditional CNN

Visualizing filters in a compositional CNN and a traditional CNN using t-SNE

Feature maps of a compositional CNN seem more clustered than those of a traditional CNN.



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Quantitative Evaluation of Filter Interpretability

- **Inconsistency of Visual Patterns** measures the consistency of visual patterns represented by a filter through different images.
 - Ideally, an interpretable filter was supposed to have high consistency.

$$H = - \sum_{j=1}^T P_j \log P_j$$



The entropy of such probabilities over different semantic concepts.

$$P_j = \frac{\sum_{I \in \mathbf{I}^{\text{test}}} \sum_{u=1}^M \min\{\tilde{Q}_u(I), G_u^j(I)\}}{\sum_{I \in \mathbf{I}^{\text{test}}} \sum_{u=1}^M \tilde{Q}_u(I)}$$



The probability of a filter being associated with a ground-truth semantic concept in a specific image.



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Quantitative Evaluation of Filter Interpretability

- **Diversity of Visual Patterns** evaluates whether a CNN learned various visual patterns.

$$Diversity = \frac{1}{M} \mathbb{E}_I \left[\sum_{u=1}^M \mathbb{1} \left(\left(\frac{1}{d} \sum_{i=1}^d \tilde{Q}_u^i(I) \right) \geq \gamma \right) \right]$$



A brace underlines the term $\mathbb{1} \left(\left(\frac{1}{d} \sum_{i=1}^d \tilde{Q}_u^i(I) \right) \geq \gamma \right)$.

A pixel is explained by a CNN, if this pixel was explained by some filters.

The diversity of visual patterns was approximately quantified as the number of pixels which had been explained by a CNN.

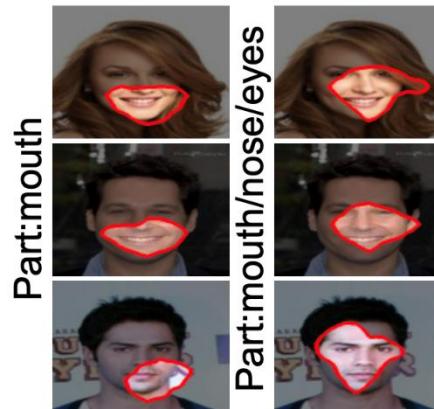
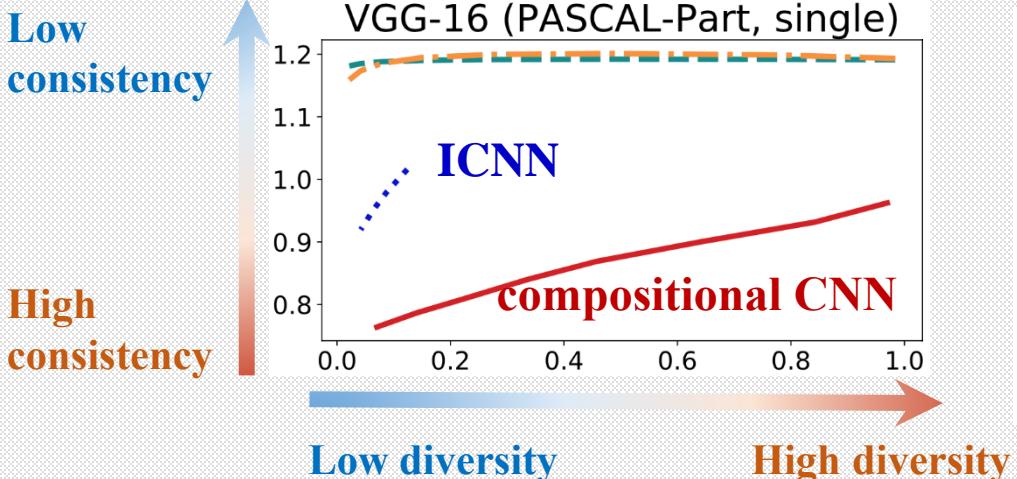
Strongly interacted filters → meaningful concepts



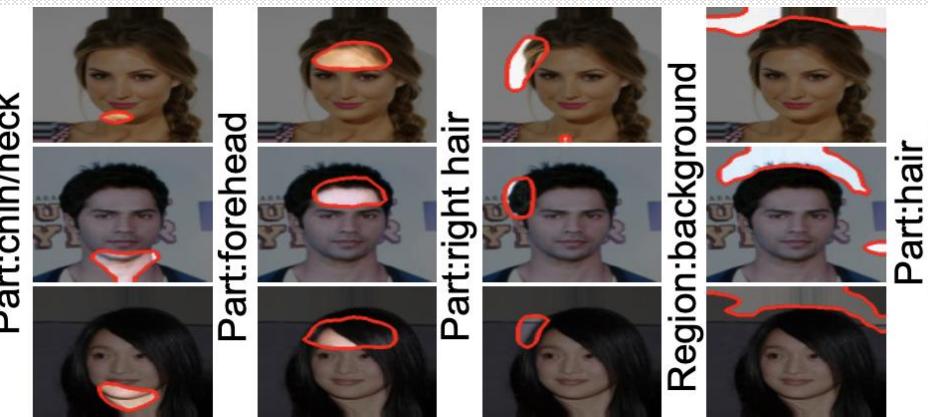
Our method learns filters with much higher consistency and diversity



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Activation regions of interpretable filters in ICNN



Activation regions of interpretable filters in compositional CNN

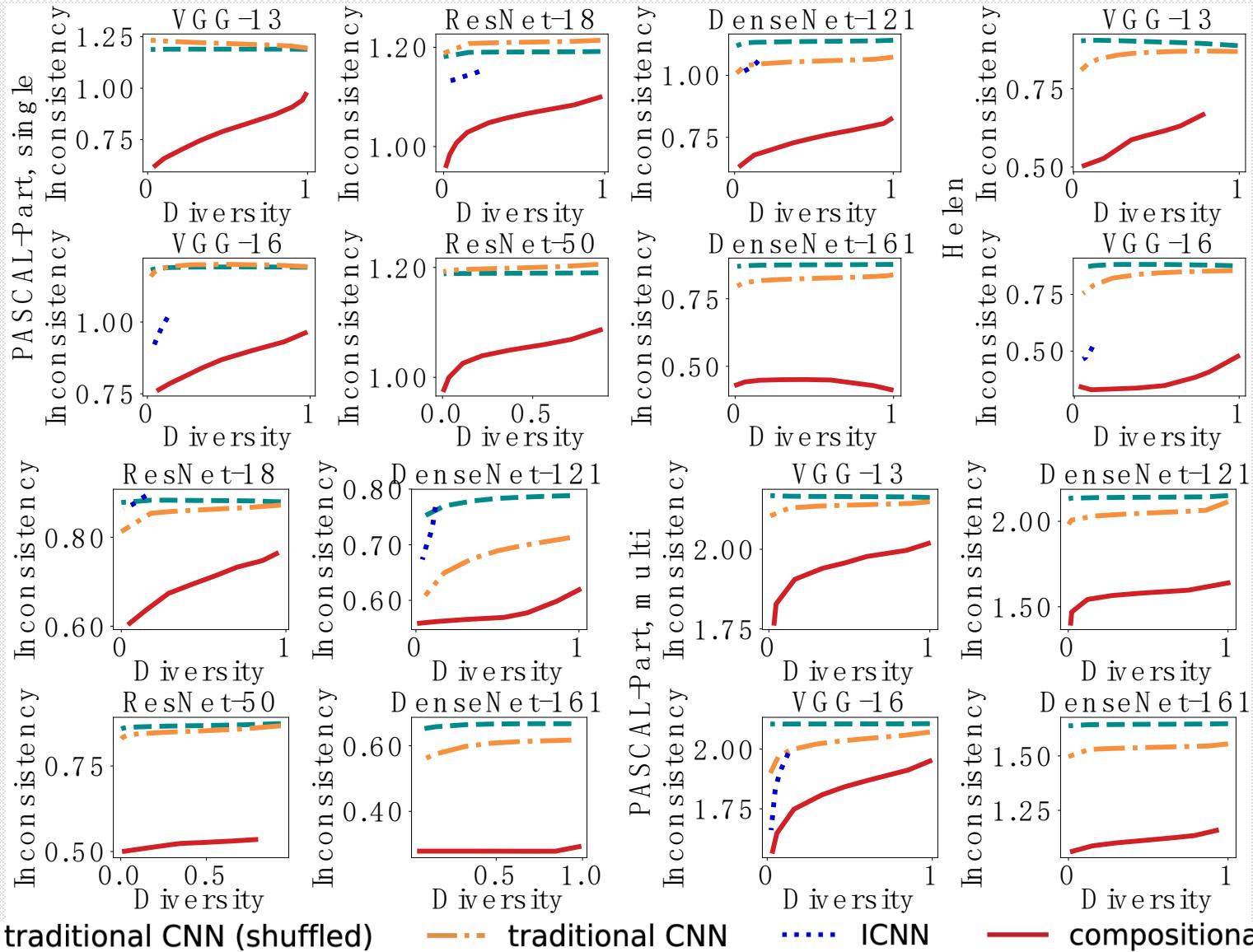
Strongly interacted filters → meaningful concepts



Our method learns filters with much higher consistency and diversity



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Classification performance

	single-category			multi-category
	PASCAL-Part	CUB200	CelebA	PASCAL-Part
VGG-13	97.07	99.76	–	87.51
compositional CNN	96.29	99.41	–	86.37
VGG-16	98.66	99.86	90.47	89.71
ICNN	95.39	96.51	89.11	91.60
compositional CNN	97.12	99.27	90.70	87.51
ResNet-18	97.77	99.81	89.60	–
ICNN	93.30	97.12	–	–
compositional CNN	96.90	98.49	89.76	–
ResNet-50	97.88	99.88	90.21	–
compositional CNN	97.30	99.27	89.63	–
DenseNet-121	98.29	99.92	–	91.28
ICNN	96.55	99.22	–	–
compositional CNN	97.52	98.83	–	91.75
DenseNet-161	98.70	99.96	–	93.48
compositional CNN	98.14	99.61	–	92.66

Compositional CNNs exhibit comparable classification performance with traditional CNNs. Besides, compositional CNNs achieve higher accuracy than ICNNs in most comparisons.