

Santa Clara University



School of Engineering

**Digital Image Processing I:
Project Part 3**

ELEN 640
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1. Best Methods Used to Identify the Coins

1.1. Image Set #1

The images presented in the set #1 are grayscale images with only coins of different sizes and different types of contrast and illuminations as shown in Figure 1.1

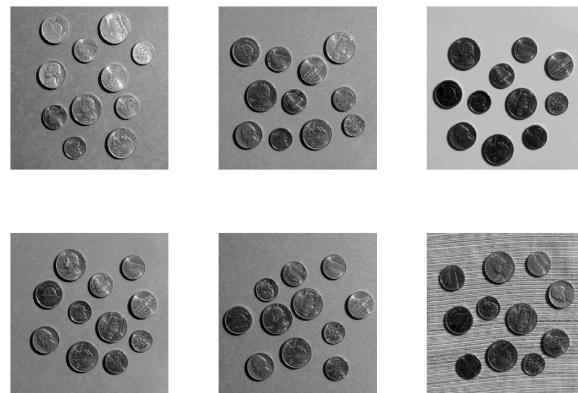


Figure 1.1. Images of Set #1

1.1.1. Best Method for Set #1

For Image set #1, the best method found to find the coins in the image is using **Hough Transform on the edges of the gray scaled image**, because there is no distractors elements in the image we can easily perform a hough transform after applying an appropriated edge filter to get the centers and the radii of the coins. The process is illustrated in the block diagram in Figure 1.2.

We picked this method because we do not have distraction elements and only circular elements

a. Block Diagram

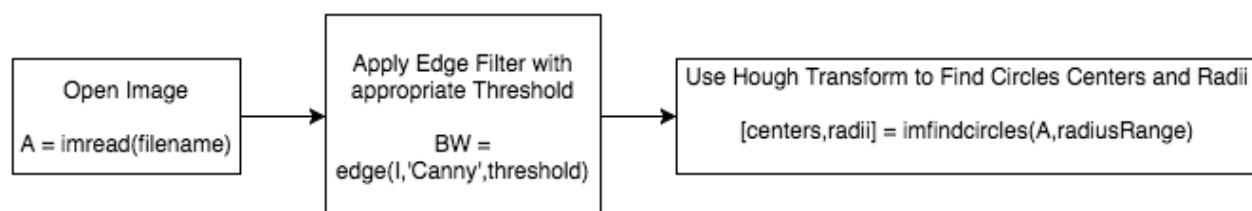


Figure 1.2. Hough Transform Process for Image Set #1

b. Selected Images Result

For image 563 and Image 579 the following table summarize the result using the procedure of Table 1.1

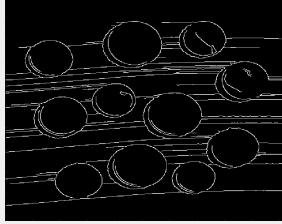
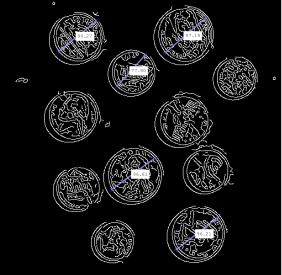
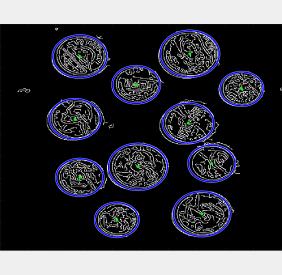
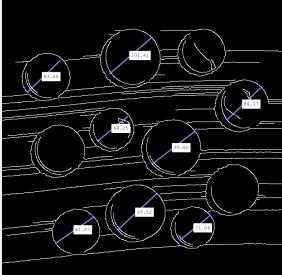
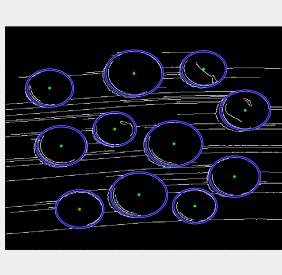
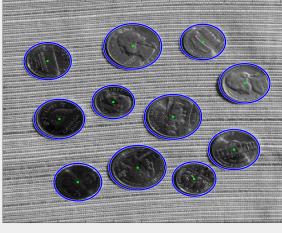
Original Image	Edges of the Image	Original Image	Edges of the Image																																																																		
																																																																					
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Table 1.1 Result for selected images on set #1

1.2. Image Set #2

The images presented in the set #2 are the color version of the images presented in image set #1, as shown in Figure 1.2. We can see now the different colors of the coins and the color of the backgrounds allowing us to perform a better segmentation of the image based on the color information for some of the images.



Figure 1.2. Images of Set #2

1.2.1. Best Method for Set #2

Image Set #2 are the colored images of set #1 therefore we can use the same method as in set #1 to find the coins centers and radii but first we need to obtain the grayscale version of the images.

1.3. Image Set #3

The images presented in the set #3 are color images with coins of different sizes and non circular distractions objects with different shapes, colors of contrast and illuminations as shown in Figure 1.3.

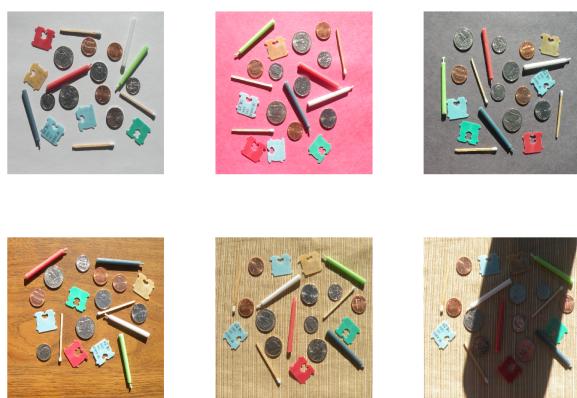


Figure 1.3. Images of Set #3

1.3.1. Best Method for Set #3

For Image set #3, the best method found to find the coins in the image is using **Hough Transform on a BW image** we were able to separate almost all of the images using a combination of RGB or HSV color segmentation and thresholding, combined with morphological operation in order to eliminate the non circular distracting element and then performing a hough transform to find the centers and the radii of the coins. The process is illustrated in the block diagram in Figure 1.4.

We picked this method because we were able to separate the foreground and the background and eliminate the distraction element based in the shaped of the distractor objets.

c. Block Diagram

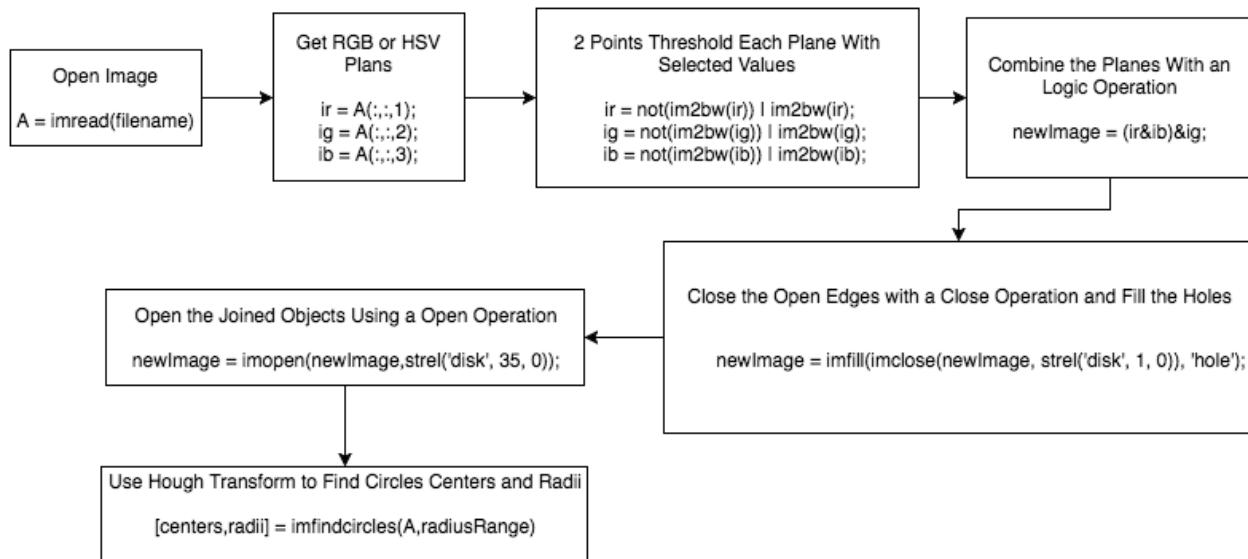


Figure 1.4. BW Hough Transform Process for Image Set #3

d. Selected Images Result

For image 616 and 619 the following table summarize the result using the procedure of Table 1.2

Original Image	Segmented Image	Original Image	Segmented Image																																																																					
Selecting Range for Radii	Results	Selecting Range for Radii	Results																																																																					
Results on Original Image	Centers and Radii	Results on Original Image	Centers and Radii																																																																					
	<table> <tbody> <tr><td>519.7953</td><td>200.4177</td><td>52.3256</td></tr> <tr><td>683.1419</td><td>601.5355</td><td>53.5093</td></tr> <tr><td>582.9936</td><td>348.0584</td><td>54.8359</td></tr> <tr><td>686.6015</td><td>225.9459</td><td>52.8018</td></tr> <tr><td>687.7254</td><td>584.9032</td><td>54.5342</td></tr> <tr><td>609.5259</td><td>463.1647</td><td>53.8162</td></tr> <tr><td>391.0323</td><td>485.0418</td><td>62.2220</td></tr> <tr><td>358.0248</td><td>266.6106</td><td>61.4776</td></tr> <tr><td>358.6938</td><td>253.2327</td><td>61.5957</td></tr> <tr><td>256.9178</td><td>499.4723</td><td>50.4310</td></tr> <tr><td>801.2699</td><td>414.7685</td><td>49.7150</td></tr> <tr><td>395.9131</td><td>470.3646</td><td>61.1877</td></tr> </tbody> </table>	519.7953	200.4177	52.3256	683.1419	601.5355	53.5093	582.9936	348.0584	54.8359	686.6015	225.9459	52.8018	687.7254	584.9032	54.5342	609.5259	463.1647	53.8162	391.0323	485.0418	62.2220	358.0248	266.6106	61.4776	358.6938	253.2327	61.5957	256.9178	499.4723	50.4310	801.2699	414.7685	49.7150	395.9131	470.3646	61.1877		<table> <tbody> <tr><td>547.4355</td><td>177.6980</td><td>64.3624</td></tr> <tr><td>252.9359</td><td>321.8691</td><td>53.4492</td></tr> <tr><td>686.8374</td><td>112.6636</td><td>51.8688</td></tr> <tr><td>718.8634</td><td>590.0446</td><td>53.1336</td></tr> <tr><td>385.3520</td><td>336.6177</td><td>49.8606</td></tr> <tr><td>549.4195</td><td>427.6463</td><td>54.0613</td></tr> <tr><td>713.7194</td><td>606.5444</td><td>52.0350</td></tr> <tr><td>390.2278</td><td>558.1761</td><td>62.9726</td></tr> <tr><td>386.4999</td><td>569.9432</td><td>63.1255</td></tr> <tr><td>507.9907</td><td>666.3561</td><td>54.2486</td></tr> <tr><td>692.7375</td><td>269.5300</td><td>49.1694</td></tr> </tbody> </table>	547.4355	177.6980	64.3624	252.9359	321.8691	53.4492	686.8374	112.6636	51.8688	718.8634	590.0446	53.1336	385.3520	336.6177	49.8606	549.4195	427.6463	54.0613	713.7194	606.5444	52.0350	390.2278	558.1761	62.9726	386.4999	569.9432	63.1255	507.9907	666.3561	54.2486	692.7375	269.5300	49.1694
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Table 1.2 Result for selected images on set #3

1.4. Image Set #4

The images presented in the set #4 are color images with coins of different sizes and circular distractions objects with different colors and sizes, contrast and illumination as we can see in Figure 1.5.



Figure 1.5. Images of Set #4

1.4.1. Best Method for Set #4

For Image set #4, the best method found to find the coins in the image is using **Matching Filters** performing a normalized cross correlation with a different templates for each of the coins and finding the respective peaks. The process is illustrated in the block diagram of Figure 1.6.

We picked this method because if we try to separate the foreground and the background there is no way to differentiate what was a coin and what is not a coin only based in the shape of the object as the distractor elements are also circular.

a. Block Diagram

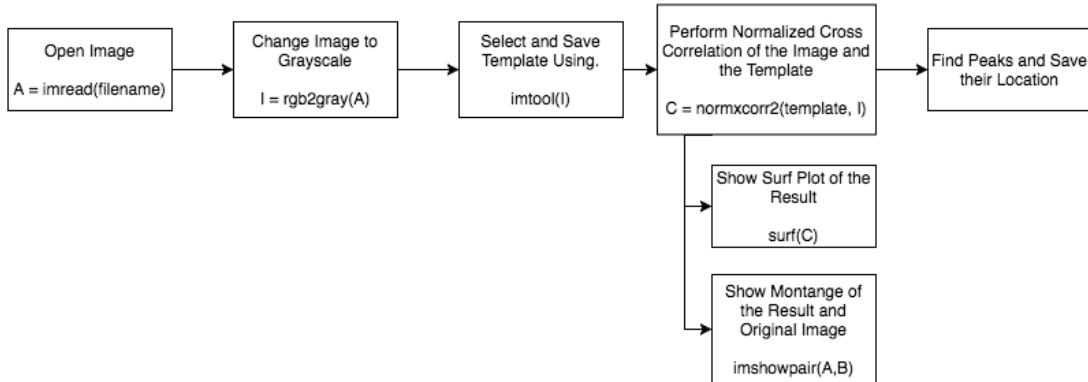


Figure 1.6. Match Filter process for Image Set #4

b. Selected Images Result

For image 582 using the following table summarize the result using the procedure of Table 1.3.

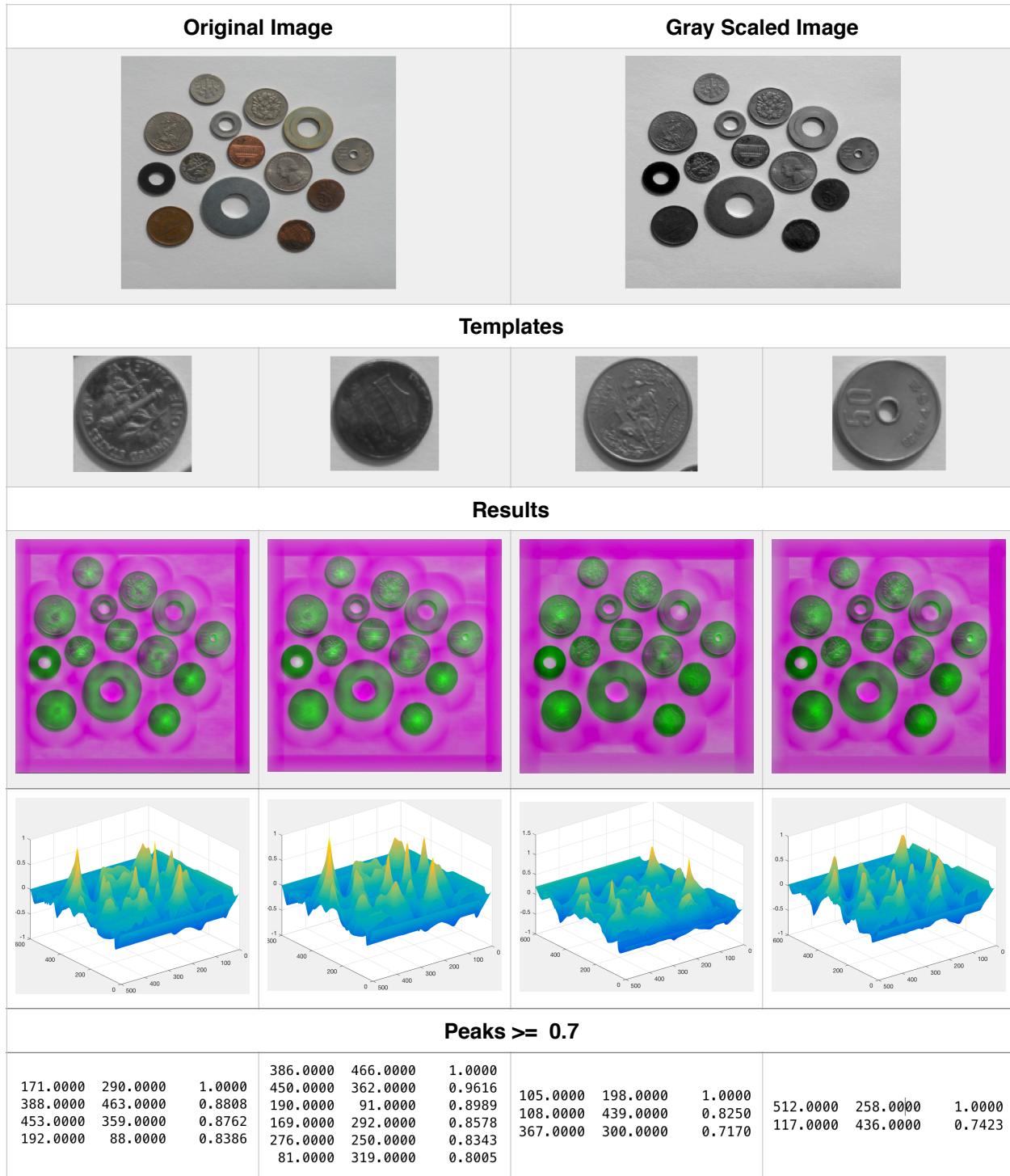


Table 1.3 Result for selected images on set #4

For image 582 using the following table summarize the result using the procedure of Table 1.4

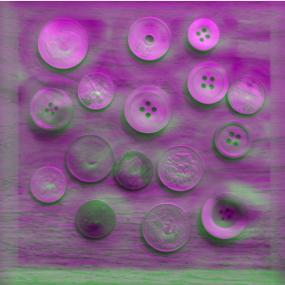
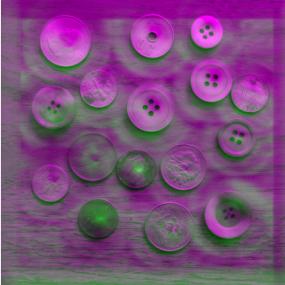
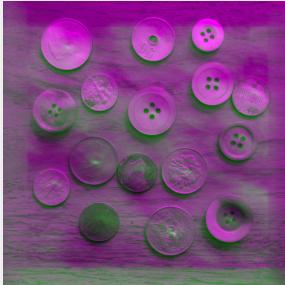
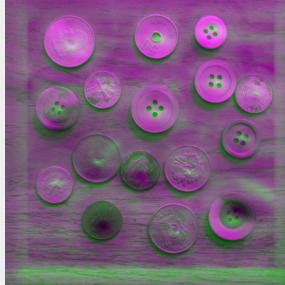
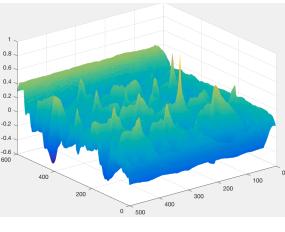
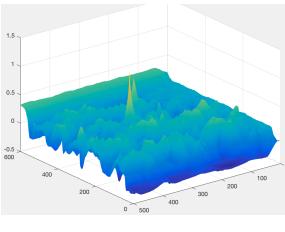
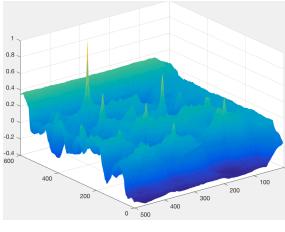
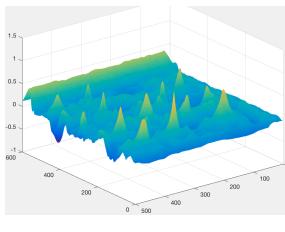
Original Image	Gray Scaled Image		
			
Templates			
			
Results			
			
			
Peaks >= 0.7			
205.0000 193.0000 1.0000	285.0000 356.0000 1.0000	352.0000 479.0000 1.0000	317.0000 83.0000 1.0000 439.0000 174.0000 0.7012

Table 1.4 Result for selected images on set #4

2. The Ideal Image (Most Robust)

The Image 569 shown in Figure 2.1 was identified as the most robust image across all the methods. The Image is the image number 3 from the image set #1, and therefore is also image number 3 from the set #2



Figure 2.1. Most Robust Image

2.1. Characteristic

The image defined as most robust presented a high contrast between the background and foreground, as shown in the histogram in Figure 2.2 and the background is a solid light gray color, the coins have enough space in between and there is no overlapping even in the minimum shadow it presents.

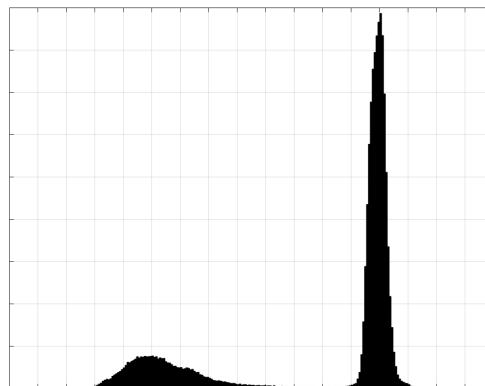


Figure 2.2. Histogram of most robust Image

Most of the features of the inside the coins are not underexposed, but for this case we only care about the size thus these features are not needed.

2.2. Processing Steps

In order to find the circles on this image we didn't require a lot of prepossessing as most of the methods worked very well as we see below.

2.2.1. Segmentation

Using simple thresholding, because the high contrast of the background and foreground we found a range of value that worked well from 0.5 to 0.73.

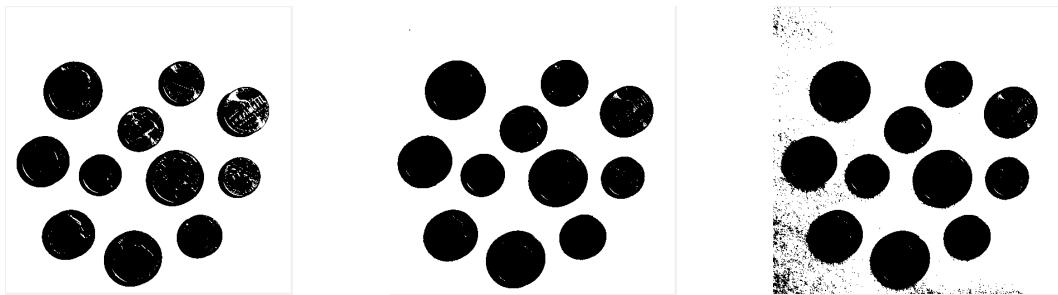


Figure 2.3 Range of values for Thresholding

We also start noticing some detail of the background start to appear and is at this point the process would not work anymore.

Also because of this high contrast we can easily detect the edges using the different method, Sobel, Prewitt, Roberts, LoG and Canny, with the automatic thresholding, being Canny with manual thresholding the most reliable one

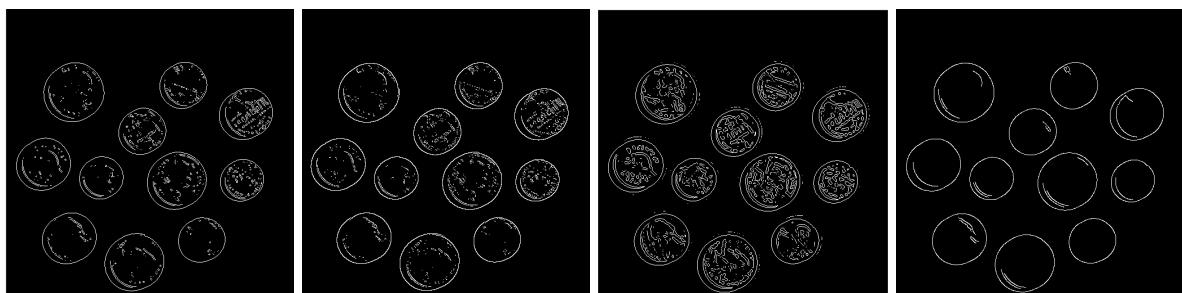


Figure 2.4 Range of values for Thresholding

2.3. System Design

2.3.1. Image Resolution

According to the theory we need at least 2 pixel in the smallest feature in this case a smaller image should work as well, as see in Figure 2.5 with a lower resolution image.

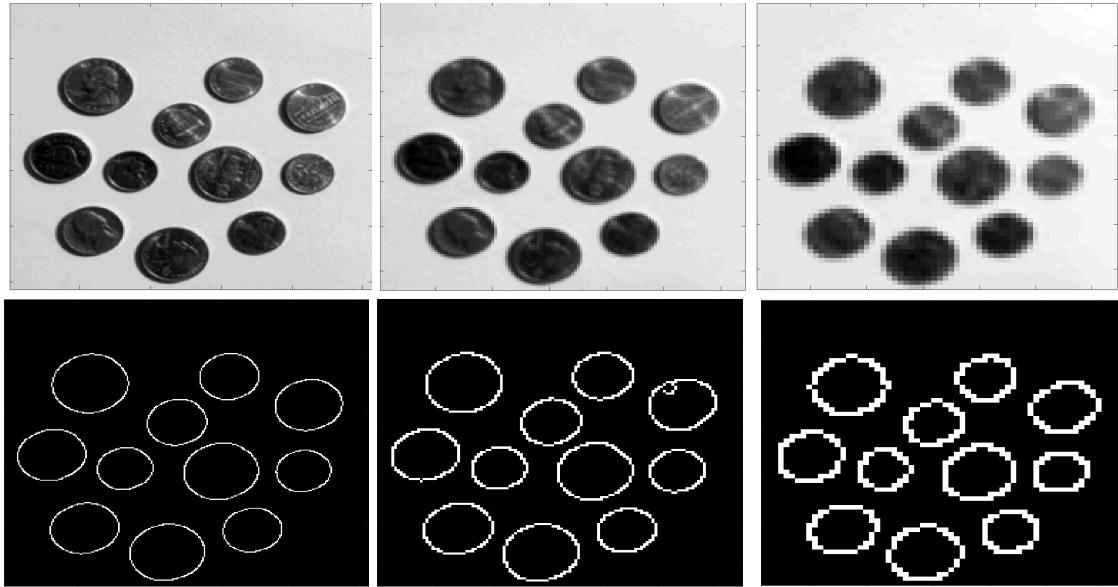


Figure 2.5. Lower resolution Images and their detected edges

As we can see using lower resolution image we can still detect the edges of the images and therefore we would be able to find the center and the radii of the images as seen in Figure 2.6. and the computational complexity decrease.

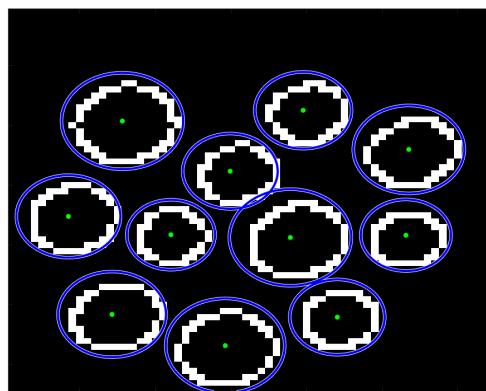


Figure 2.6 Centers and radii of low resolution Image

2.3.2. Illumination Source

I would recommend a system a diffuse illumination right above the coins to reduce the shadows and detect the radii with more accuracy.

2.3.3. Background

I would use a solid and uniform background with such as it would produce a high contrast between the foreground and the background.

Because the algorithm we are using depend on the edges of the image, a patterned background would create edges other than the coins, making it harder to detect the circles.

3. The Image 632

The Image 632 shown in Figure 3.1 was identify as the most complex image across all the methods. The Image is the image number 6 from the image set #3.



Figure 3.1. Image 632

3.1. Characteristics

The image defined as most complex presented a noticeably bad illumination due to the big shadow in the middle of the image, also with a patterned background and with non circular distraction element.

We can see that the simpler processing method of the most robust image will fail here, as we don't have a very well define high contrast between the background and the foreground objects, so the simple two point thresholding will fail, as well as the edge detection.

3.2. Processing Steps

First we used some smoothing filter in all three planes, hoping to make the background pattern more uniform, as well as the different colors. We apply a median filter size 15x15 and then we apply an averaging filter 5x5, the result are shown in Figure 3.2



Figure 3.2 Smoothed Image

Now we proceed to use different color segmentation in order to remove the shadow, and we obtained after several trial is show in Figure 3.3

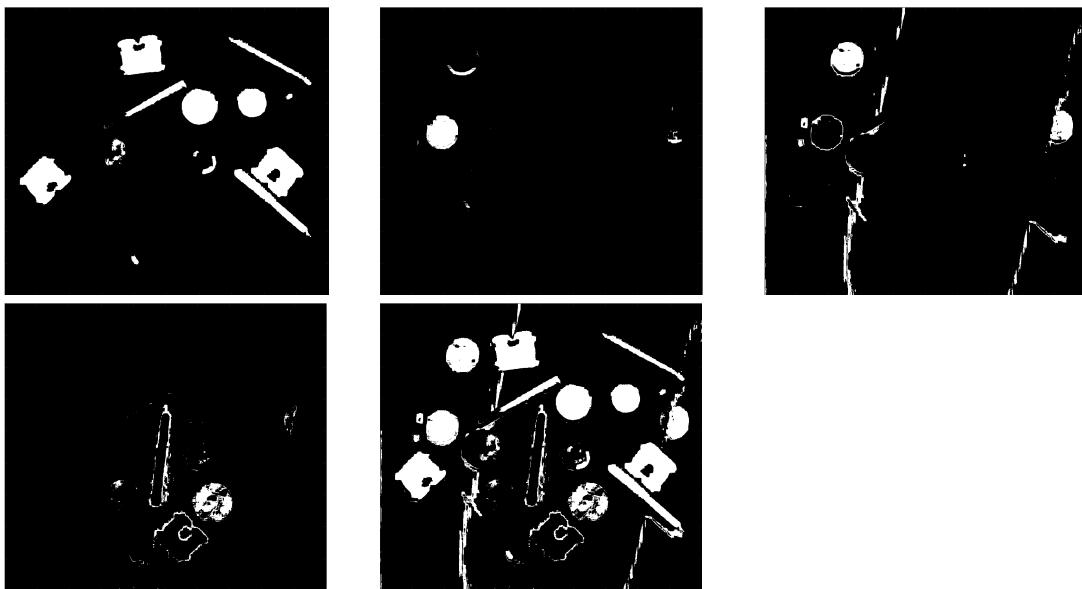


Figure 3.3 Several color segmentation and final result thresholding

As we can see, we were successful in separate some of the objects inside the shadow as well the ones in the well illuminate part.

3.3. Postprocessing

Now we could try to use different types of morphological operation in order to have better circular shapes and then use hough transform to find the centers and radii of the circles. The result of the morphological operation is show in Figure 3.4

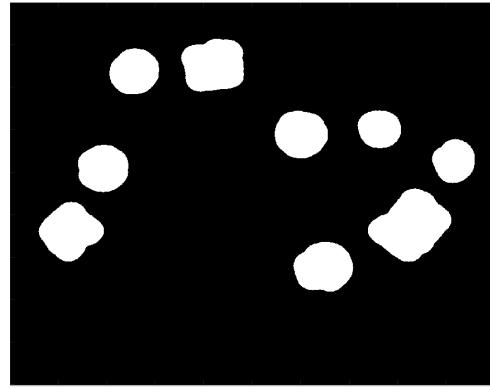


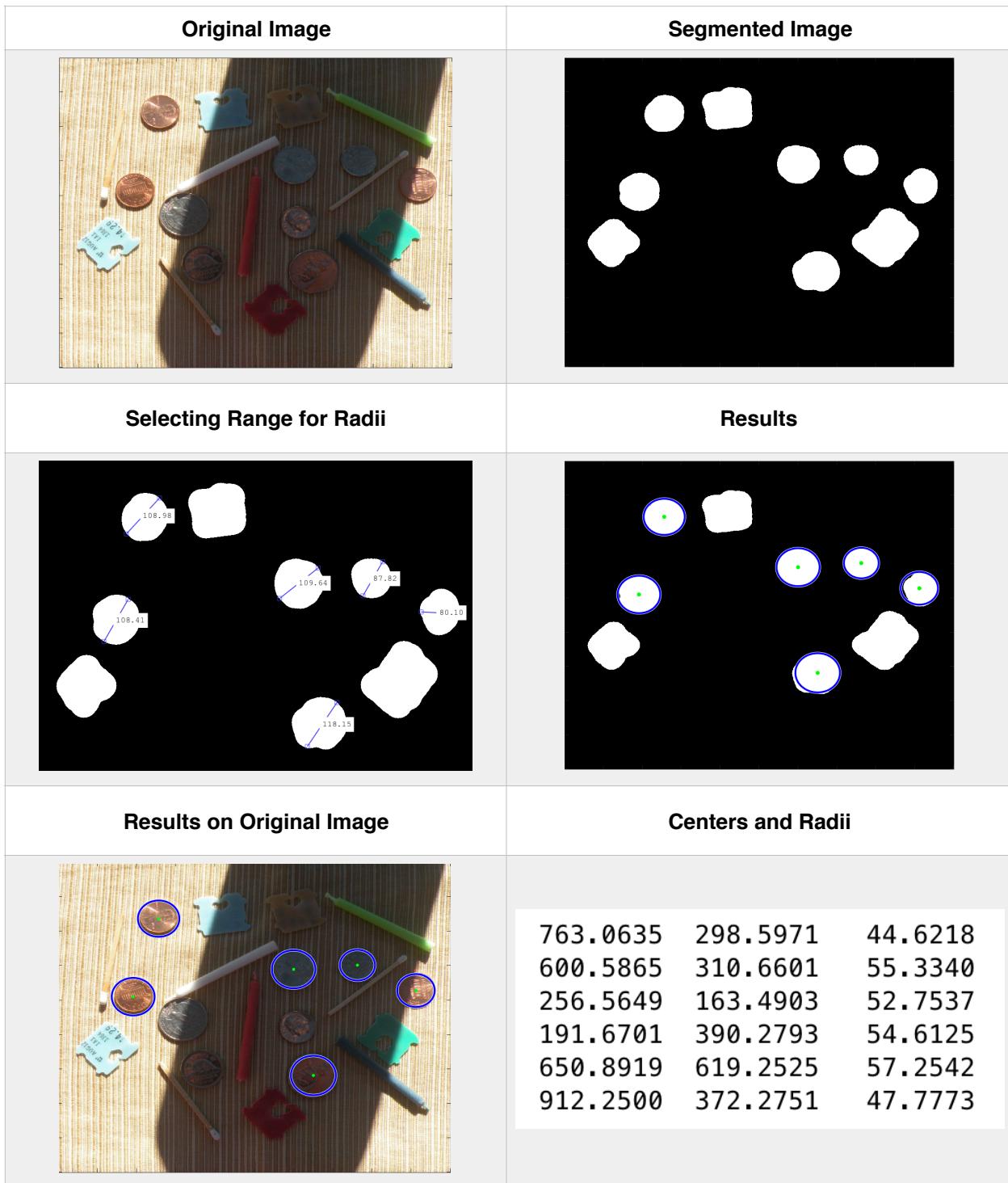
Figure 3.4 Image after Morphological Operation

As we can see of the original 9 coins in the image we can distinguish 6 circular objects, most likely the radii will not be accurate but the centers may be.

We can see that in order of getting some result the simpler step for the ideal image had to be modified starting with the used of smoothing and medial filters and performing several segmentation base on the color of the image, increasing the complexity and the time use in order to get some result.

3.4. Result

Using the Hough Transform in this new Image we get:



At the end with our methods we manage to find 6 out of the 9 coins in the image :)

4. Matlab Functions

`A = imread(filename)`

Reads the image from the file specified by filename, inferring the format of the file from its contents. If filename is a multi-image file, then imread reads the first image in the file.

`I = rgb2gray(RGB)`

Converts the truecolor image RGB to the grayscale intensity image I. The rgb2gray function converts RGB images to grayscale by eliminating the hue and saturation information while retaining the luminance.

`C = normxcorr2(template, A)`

Computes the normalized cross-correlation of the matrices template and A. The matrix A must be larger than the matrix template for the normalization to be meaningful. The values of template cannot all be the same. The resulting matrix C contains the correlation coefficients, which can range in value from -1.0 to 1.0.

`surf(Z)`

Creates a three-dimensional shaded surface from the z components in matrix Z, using x = 1:n and y = 1:m, where [m,n] = size(Z). The height, Z, is a single-valued function defined over a geometrically rectangular grid. Z specifies the color data, as well as surface height, so color is proportional to surface height. The values in Z can be numeric or datetime or duration values.

`[centers,radii] = imfindcircles(A,radiusRange)`

Finds circles with radii in the range specified by radiusRange. The additional output argument, radii, contains the estimated radii corresponding to each circle center in centers.

`BW = edge(I,'Canny',threshold)`

Return all edges that are stronger than threshold. If you do not specify threshold, or if you specify empty brackets ([]), edge chooses the value automatically. threshold is a two-element vector in which the first element is the low threshold, and the second element is the high threshold. If you specify a scalar, edge uses this value for the high value and uses threshold*0.4 for the low threshold.

`B = impyramid(A,direction)`

Computes a Gaussian pyramid reduction or expansion of A by one level, where direction determines whether it's a reduction or an expansion.

5. References

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