

Lesson 2: Stated Annual Interest Rates, Compounding Frequency, Effective Annual Rates and Illustrations of TVM Problems





Example 2-1: Compute the FV after 5 years of \$5,000 invested at 13% assuming quarterly compounding.







Continuous Compounding and Future Values

Example 2-2: Calculate the FV after 3 years of an investment of \$5,000 at an interest rate of 7% assuming continuous compounding.





Effective Annual Rates







Compounding and Present Value

Example 2-3: Calculate the PV of a payment of \$7,000 that will be received after 9 years if the interest rate is 6% compounded monthly.





Continuous Compounding and Present Value

Example 2-4: Calculate the PV of a payment of \$7,000 that will be received after 9 years if the interest rate is 5% compounded continuously.





Calculate the PV of \$100 to be received in one year using different compounding frequencies.







Loan Payments and Amortization

Example 2-5: Loan Payment Calculations with Annual Payments

A company borrows \$75,000 at a rate of 10%. The loan will be paid off in three equal end-of-year instalments. Calculate the amount of the annual payment.









Example 2-6: Loan Payment Calculations with Monthly Payments

A company borrows \$75,000 at a rate of 10%. The loan will be paid off through equal monthly instalments over three years. Calculate the monthly payment required to pay off the loan.







Example 2-7: Constructing and Amortization Schedule

Ben Company borrows \$25,000 at an interest rate of 7%. The amount will be paid back in semiannual instalments over 14 years. Calculate the outstanding balance of the loan after the second payment is made.







Example 2-10: Computing the Number of Periods in an Annuity

Jack needs to accumulate at least \$1,000 with annual deposits of \$80 into his bank account. If the annual interest rate is 10%, how many end-of-year payments are required?







Example 2-13: Computing the Discount Rate for an Annuity

What rate of return will we earn on an ordinary annuity that requires a \$900 deposit today and promises to pay \$150 at the end of every year for the next 10 years?







Funding a Future Obligation

Example 2-14: Computing the Required Payment to Fund an Annuity Due

Suppose we have to make 5 annual payments of \$1,500 starting at the beginning of Year 5. To accumulate the money to meet these obligations, we want to make 4 equal annual deposits beginning at the end of Year 1. Assuming a 12% rate of return, what amount must be deposited for 4 years to satisfy the eventual payment obligations?





Example 2-15: Funding a Retirement Plan

Assume that 20-year old Janet wants to retire in 40 years at the age of 60. She expects to earn 10% on deposits prior to retirement and 8% thereafter. How much must she deposit at the end of each of the next 40 years in order to be able to withdraw \$15,000 every year at the beginning of each year for 30 years from the age of 60 to 90?







The Cash Flow Additivity Principle

Example 2-16: Additivity Principle

Robin will make the following payments in the next 4 years: \$150, \$500, \$150 and \$150. Calculate the PV of the cash flows using the concept of present value of an annuity assuming that the discount rate equals 8%.





