# Computer Organization and Architecture

### Chapter 4

Cache Memory

Note: Appendix 4A will not be covered in class, but the material is interesting reading and may be used in some homework problems.

# **Characteristics of Memory Systems**

Location
Processor
Internal (main)
External (secondary)

Capacity
Word size
Number of words
Unit of Transfer
Word
Block

Word Block Access Method Sequential Direct Random Associative Performance
Access time
Cycle time
Transfer rate
Physical Type

Physical Type
Semiconductor
Magnetic
Optical
Magneto-Optical
Physical Characteristics
Volatile/nonvolatile
Erasable/nonerasable
Organization

### Location

- CPU
  - Registers and control unit memory
- Internal
  - Main memory and cache
- External
  - Storage devices (paper tape, cards, tapes, discs, flash cards, etc.)

# Capacity

- Word size
  - The natural unit of organisation
  - Typically number of bits used to represent an integer in the processor
- · Number of words
  - Most memory sizes are now expressed in bytes
  - Most modern processors have byte-addressable memory but some have word addressable memory
  - Memory capacity for A address lines is 2<sup>A</sup> addressable units

# Unit of Transfer

- Internal
  - Usually governed by data bus width
- External
  - Usually a block which is much larger than a word (typical disk 512 - 4096 bytes)
- · Addressable unit
  - Smallest location which can be uniquely addressed
  - Some systems have only word addressable memory while many have byte addressable memory
  - A block or even cluster of blocks on most disks

### Access Methods (1)

- Sequential
  - Start at the beginning and read through in order
  - Access time depends on location of data and previous location
  - e.g. tape
- Direct
  - Individual blocks have unique address
  - Access is by jumping to vicinity plus sequential search
  - Access time depends on location and previous location
  - -e.g. disk

### Access Methods (2)

- Random
  - Individual addresses identify locations exactly
  - Access time is independent of location or previous access
  - e.g. RAM
- Associative
  - Data is located by a comparison with contents of a portion of the store
  - Access time is independent of location or previous access
  - All memory is checked simultaneously; access time is constant
  - -e.g. cache

### **Performance**

- From user's perspective the most important characteristics of memory are capacity and performance
- Three performance parameters:
  - Access time
  - Cycle Time
  - Transfer Rate
- Access time (latency)
  - For RAM access time is the time between presenting an address to memory and getting the data on the bus
  - For other memories the largest component is positioning the read/write mechanism

### **Performance**

- Cycle Time
  - Primarily applied to RAM; access time + additional time before a second access can start
  - Function of memory components and system bus, not the processor
- Transfer Rate the rate at which data can be transferred into or out of a memory unit
  - For RAM TR = 1 / (cycle time)

# Transfer rate for other memories

- $T_n = T_a + (n/r)$  where
- T<sub>n</sub>=Average time to read or write N bits
- T<sub>a</sub>=Average access time
- n = number of bits
- r = transfer rate in bits / second

# Physical Types of Memory

- Semiconductor
  - RAM (volatile or non-volatile)
- Magnetic Surface Memory
  - Disk & Tape
- Optical
  - CD & DVD
- Others
  - Magneto-optical
  - Bubble
  - Hologram

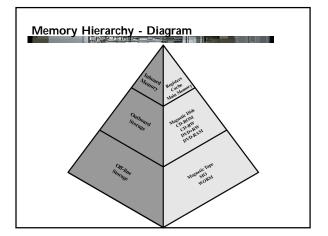
# Physical Characteristics

- Volatility
  - Does the memory retain data in the absence of electrical power?
- Decay
  - Ranges from tiny fractions of a second (volatile DRAM) to many years (CDs, DVDs)
- Erasable
  - Can the memory be rewritten? If so, how fast? How many erase cycles can occur?
- Power consumption

- Physical arrangement of bits into words
- Not always obvious, e.g., interleaved memory (examples later)

### Memory Hierarchy

- · For any memory:
  - How fast?
  - How much?
  - How expensive?
- Faster memory => greater cost per bit
- Greater capacity => smaller cost / bit
- Greater capacity => slower access
- Going down the hierarchy:
  - Decreasing cost / bit
  - Increasing capacity
  - Increasing access time
  - Decreasing frequency of access by processor



### Memory Hierarchy

- Registers
  - In CPU
- · Internal or Main memory
  - May include one or more levels of cache
  - "RAM"
- · External memory
  - Backing store

# Hierarchy List

- Registers
- L1 Cache
- L2 Cache
- Main memory
- Disk cache
- Magnetic Disk
- Optical
- Tape
- (and we could mention punch cards, etc at the very bottom)

### Locality of Reference

- Two or more levels of memory can be used to produce average access time approaching the highest level
- · The reason that this works well is called "locality of reference"
- In practice memory references (both instructions and data) tend to cluster
  - Instructions: iterative loops and repetitive subroutine calls
  - Data: tables, arrays, etc. Memory references cluster in short run

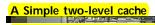
### Cache

- A small amount of fast memory that sits between normal main memory and CPU
- May be located on CPU chip or module
- Intended to allow access speed approaching register speed
- When processor attempts to read a word from memory, cache is checked first

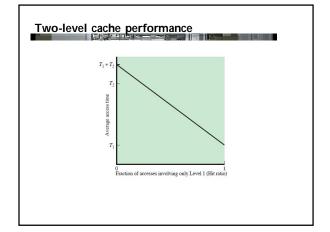
# Cache Memory Principles

- If data sought is not present in cache, a block of memory of fixed size is read into the cache
- Locality of reference makes it likely that other words in the same block will be accessed soon

# Cache and Main Memory Block Transfer Word Transfer Word Transfer Word Transfer Word Transfer Word Transfer Word Transfer Wain Memory (a) Single cache (b) Transfer (c) Cache (c) Single cache (d) Cache (e) Single cache (d) Transferition

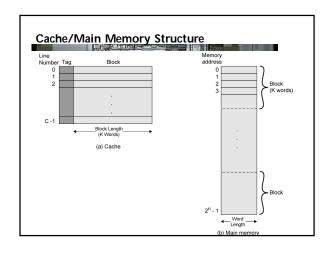


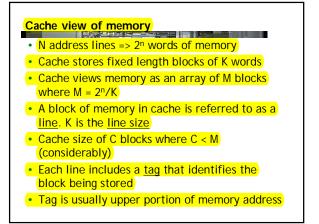
- Level 1: 1000 words, 0.01μs
- Level 2: 100,000 words 0.1μs
- If word in L1 processor has direct access else word copied from L2 into L1
- Av Access Time as function of hit ratio H: H \* 0.01µs + (1-H)\* 0.11µs
- With H near 1 access time approaches 0.01 µs



# Two-level disk access

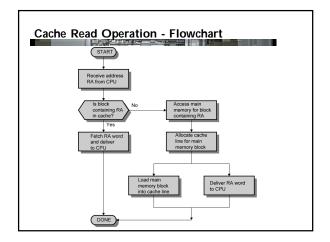
- Principles of two-level memories can be applied to disk as well as RAM
- A portion of main memory can be used as a disk cache
  - Allows disk writes to be clustered; largest component of disk access time is seek time
  - Dirty (modified) datamay be requested by the program before it is even written back to disk

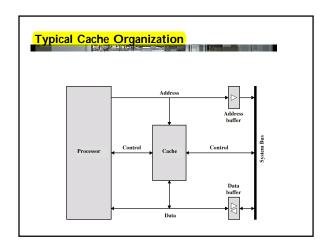




# Cache operation – overview

- CPU requests contents of memory location
- Check cache for this data
- If present, get from cache (fast)
- If not present, read required block from main memory to cache
- · Then deliver from cache to CPU
- Cache includes tags to identify which block of main memory is in each cache slot





# Cache organization The preceding diagram illustrates a shared connection between the processor, the cache and the system bus (look-aside cache) Another way to organize this system is to interpose the cache between the processor and the system bus for all lines (look-through cache)

# Elements of Cache Design

- Addresses (logical or physical)
- Size
- Mapping Function (direct, associative, set associative)
- Replacement Algorithm (LRU, LFU, FIFO, random)
- Write Policy (write through, write back, write once)
- Line Size
- Number of Caches (how many levels, unified or split)

Note that cache design for High Performance Computing (HPC) is very different from cache design for other computers Some HPC applications perform poorly with typical cache designs

### Cache Size does matter

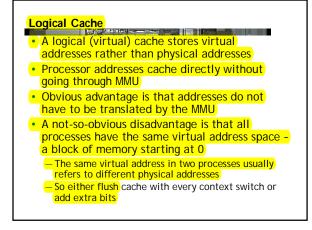
- Cost
  - More cache is expensive
  - Would like cost/bit to approach cost of main memory
- Speed
  - But we want speed to approach cache speed for all memory access
  - More cache is faster (up to a point)
  - Checking cache for data takes time
  - Larger caches are slower to operate

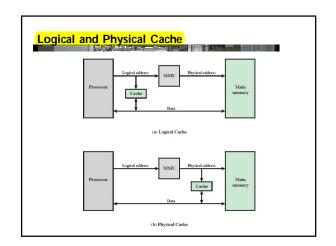
### Comparison of Cache Sizes L1 Cache<sup>a</sup> L2 cache 64 kB 128 to 256 kB 8 kB 8 kB/8 kB 32 kB 32 kB/32 kB 32 kB/32 kB 32 kB/32 kB 32 kB 256 to 512 KB IBM SP 2000 64 kB/32 kB 8 MB CRAY MTAb 4 MB 32 kB/32 kB 32 kB 256 KB Itanium 64 kB 1.9 MB 36 MB 2004 64 kB/64 kB 1MB 32 MB

## Virtual Memory

 Almost all modern processors support virtual memory (Ch 8)

- Virtual memory allows a program to treat its memory space as single contiguous block that may be considerably larger than main memory
- A memory management unit takes care of the mapping between virtual and physical addresses





# Look-aside and Look-through

- Look-aside cache is parallel with main memory
- Cache and main memory both see the bus cycle
  - Cache hit: processor loaded from cache, bus cycle
  - Cache miss: processor AND cache loaded from memory in parallel
- Pro: less expensive, better response to cache
- Con: Processor cannot access cache while another bus master accesses memory

### Look-through cache

- Cache checked first when processor requests data from memory
  - Hit: data loaded from cache
  - Miss: cache loaded from memory, then processor loaded from cache
- Pro:
  - Processor can run on cache while another bus master uses the bus
- - More expensive than look-aside, cache misses slower

### Mapping Function

- There are fewer cache lines than memory blocks so we need
  - —An algorithm for mapping memory into cache lines
  - A means to determine which memory block is in which cache line
- Example elements:
  - Cache of 64kByte
  - Cache block of 4 bytes
    - i.e. cache is 16k (2<sup>14</sup>) lines of 4 bytes
  - 16MBytes main memory
  - -24 bit address (2<sup>24</sup>=16M)

(note: Pentium cache line = 32 bytes until Pentium 4 (128 bytes))

- Direct Mapping Each block of main memory maps to only one cache
  - i.e. if a block is in cache, it must be in one specific place
- Mapping function is i = j modulo m

(i = j % m) where

- i = cache line number
- j = main memory block number
- m = number of cache lines
- Address is in two parts
- Least Significant w bits identify unique word
- Most Significant s bits specify one memory block
- The MSBs are split into a cache line field r and a tag of s-r bits (most significant)

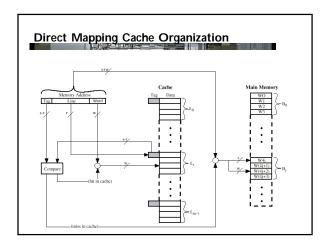
## **Direct Mapping Address Structure**

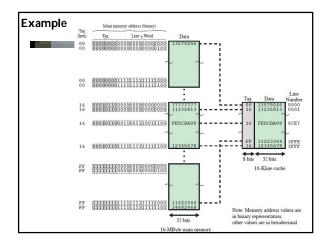
Line or Slot r Word w Tag s-r 14 2

- 24 bit address, 2 bit word identifier (4 byte block)
- 22 bit block identifier (s)
  - 8 bit tag (=22-14) and 14 bit slot or line
  - Example: AB1402 tag=AB line=0500 word=2
    - Remove I.s. 2 bits = 0001 0100 0000 00 = 00 0101 0000 0000 = 0500
- There are 2<sup>s</sup> blocks in memory
- · No two blocks with the same line number can have the same Tag field
- AC1400, 041403, C71401
- · Check contents of cache by finding line and checking Tag - Line is 0500 for all of these If mem request is AB1402 tag at 0500 must = AB

### Direct Mapping

- Parking lot analogy: think of the cache as a parking lot, with spaces numbered 0000-9999
- With a 9 digit student id, we could assign parking spaces based on the middle 4 digits: xxx PPPP yy
- Easy to find your parking space
- · Problem if another student is already there!
- Note that with memory addresses, the middle bits are used as a line number
  - Locality of reference suggests that memory references close in time will have the same highorder bits





Address length = (s + w) bits where w = log<sub>2</sub>(block size)
Number of addressable units = 2<sup>s+w</sup> words or bytes
Block size = line size = 2<sup>w</sup> words or bytes
Number of blocks in main memory = 2<sup>s+w</sup>/2<sup>w</sup> = 2<sup>s</sup>
Size of line field is r bits - Number of lines in cache = m = 2<sup>r</sup> - Size of tag = (s - r) bits
Size of cache 2<sup>r+w</sup> bytes or words

 Direct Mapping Cache Line Table

 Cache line
 Main Memory blocks held

 0
 0, m, 2m, 3m...2s-m

 1
 1,m+1, 2m+1...2s-m+1

 ...
 m-1

 0
 000000,010000,...,FF0000

 1
 0000004,010004,...,FF0004

 ...
 m-1

 0 m-1
 00FFFC,01FFFC,...,FFFFFC

Pro
Simple
Inexpensive
Con
Fixed location for given block
If a program accesses 2 blocks that map to the same line repeatedly, cache misses are very high (thrashing)
Victim cache
A solution to direct mapped cache thrashing
Discarded lines are stored in a small "victim" cache (4 to 16 lines)
Victim cache is fully associative and resides between L1 and next level of memory

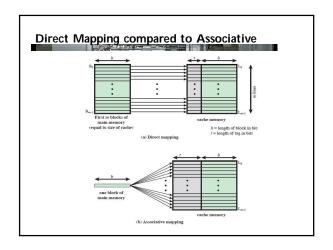
A main memory block can load into any line of cache
Memory address is interpreted as 2 fields: tag and word
Tag uniquely identifies block of memory
Every line's tag is examined simultaneously for a match
Cache searching gets expensive because a comparator must be wired to each tag
A comparator consists of XNOR gates (true when both inputs are true)
Complexity of comparator circuits makes fully associative cache expensive

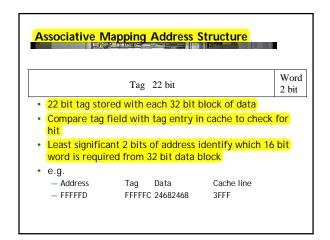
Associative Mapping

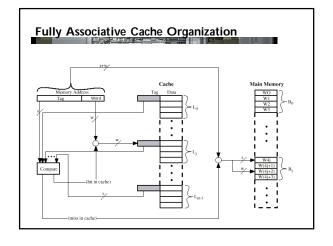
XNOR, this is the logical complement of the exclusive OR (XOR) gate

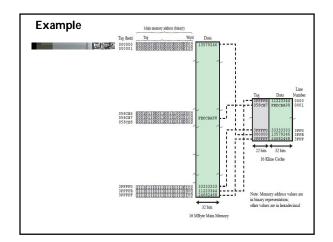
IN	PUT	OUTPUT		
A	В	A XNOR B		
0	0	1		
0	1	0		
1	0	0		
1	1	1		

# Associative Mapping Because no bit field in the address specifies a line number the cache size is not determined by the address size Associative-mapped memory is also called "content-addressable memory." Items are found not by their address but by their content Used extensively in routers and other network devices Corresponds to associative arrays in Perl and other languages Primary disadvantage is the cost of circuitry









# Parking lot analogy: there are more permits than spaces Any student can park in any space Makes full use of parking lot With direct mapping many spaces may be unfilled Note that associative mapping allows flexibility in choice of replacement blocks when cache is full Discussed below

Associative Mapping

# Associative Mapping Summary

- Address length = (s + w) bits where w = log<sub>2</sub>(block size)
- Number of addressable units = 2<sup>s+w</sup> words or bytes
- Block size = line size = 2<sup>w</sup> words or bytes
- Number of blocks in main memory
  = 2<sup>s+ w</sup>/2<sup>w</sup> = 2<sup>s</sup>
- Number of lines in cache = undetermined
- Size of tag = s bits

# Set Associative Mapping

 A compromise that provides strengths of both direct and associative approaches

2---

- Cache is divided into a number of sets of lines
- Each set contains a fixed number of lines
- A given block maps to any line in a given set determined by that block's address
   e.g. Block B can be in any line of set i
- e.g. 2 lines per set
  - 2-way associative mapping
  - A given block can be in one of 2 lines in only one set

### Set Associative Mapping

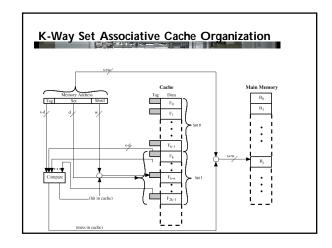
- m = v \* k
  - Where m = number of lines in cache, v = number of sets and k = lines/set
  - Lines in cache = sets \* lines per set
- i = j modulo v
  - Where I = set number and j = main memory block number
  - Set number = block number % number of sets
- This is referred to as a "k-way" set associative mapping
- Block B<sub>i</sub> can be mapped only into lines of set j.

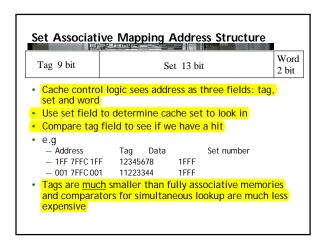
### Set Associative Mapping: Parking Analogy

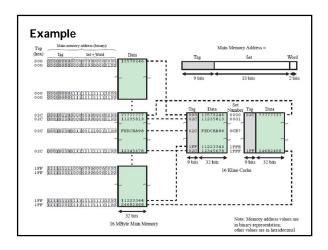
- If we have 10,000 parking spaces we can divide them into 1000 sets of 10 spaces each
- Still use middle digits of id to find your parking place set: xxx PPP yyy
- · You have a choice of any place in your set
- Our parking lots actually work like this, but the sets are fairly large: Fac/Staff; Commuter; Resident; Visitor

### Set Associative Mapping Example

- Assume 13 bit set number
- Block number in main memory is modulo 2<sup>13</sup> (0010 0000 0000 0000 = 2000h
- 000000, 002000, 004000, ... map to same set







## Set Associative Mapping Summary • For a k-way set associative cache with v sets (each set

- contains k lines):
  - Address length = (t+d+w) bits where  $w = log_2(block size)$  and d  $= log_2(v)$
  - Number of addressable units = 2<sup>t+d+w</sup> words or bytes
  - Size of tag = t bits
  - Block size = line size = 2<sup>w</sup> words or bytes
  - Number of blocks in main memory = 2t+d
  - Number of lines in set = k
  - Number of sets = v = 2d
  - Number of lines in cache = kv = k \* 2<sup>d</sup>

Word Tag (t bits) Set (d bits) (w bits)

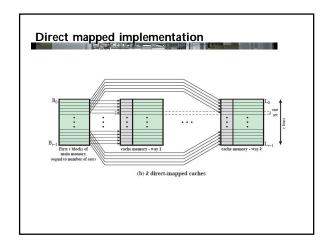
### **Additional Notes**

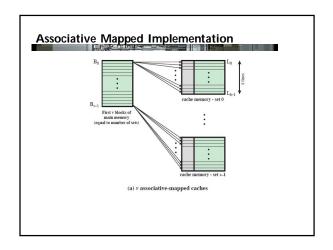
• Where v (# sets) = m (# lines in cache) and k = 1 (one line/set) then set associative mapping reduces to direct mapping

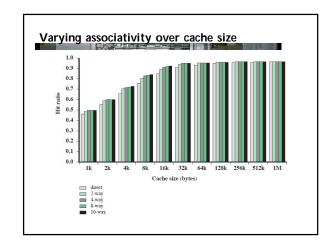
- For v=1 (one set) and k=m (# sets = # lines) it reduces to pure associative mapping
- 2 lines/set; v=m/2, k=2 is quite common.
- Significant improvement in hit ratio over direct mapping
- Four-way mapping v=m/4, k=4 provides further modest improvement

## Set Associative Mapping Implementation

- A set associative cache can be implemented as k direct mapped caches OR as v associative caches
- · With k direct mapped caches each direct mapped cache is referred to as a way
- The direct mapped implementation is used for small degrees of associativity (small k) and the associative mapped implementation for higher degrees.







Cache replacement algorithms
When a line is read from memory it replaces some other line already in cache
Other than direct mapping, there are choices for replacement algorithm
Any given choice can result in a great speedup for one program and slow-down for some other program
There is no "best choice" that works for all programs

Replacement Algorithms (1)
Direct mapping

No choice

Each block only maps to one line

Replace that line

Replacement Algorithms (2)
Associative & Set Associative

• Algorithm is hardware implemented for speed
• Least Recently used (LRU) assumes locality of reference so most recently used is likely to be used again

• LRU is easy for 2-way set associative cache

— Each line has a USE bit

— When a line is referenced, set USE bit to 1 and set the USE bit for the other line to 0

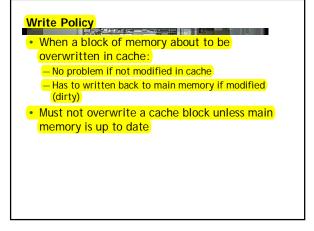
— Replace the block whose USE bit is 0

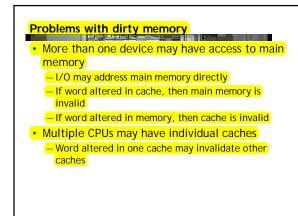
• Implemented in fully-associative caches by keeping list of lines

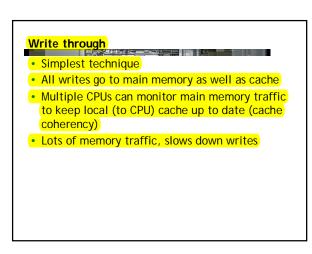
— Most recently referenced lines goes to head of list

MRU replacement
Most Recently Used (MRU) would seem to be an improbable algorithm
It is useful for some specialized caches where the type of code executing is known (example: database index scan)

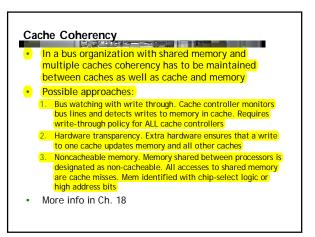
## 







# Write back Updates initially made in cache only Update bit for cache slot is set when update occurs If block is to be replaced, write to main memory only if update bit is set — Other caches can get out of sync I/O must access main memory through cache N.B. Typically 15% of memory references are writes; but can be as high as 50% in some HPC apps



- Line Size • When a cache line is filled it normally includes more than the requested data - some adjacent words are retrieved
- · As block size increases, cache hit ratio will also increase because of locality of reference - to a
- · If block size is too large, possibility of reference to parts of block decreases; there are fewer blocks in cache so more chance of block being overwritten

- Line Size Relationship between block size and hit ratio is complex and program-dependent
- · No optimal formula exists
- General purpose computing uses blocks of 8 to 64 bytes
- In HPC 64 and 128 byte lines are most common

### Number of caches: multilevel caches

- · With increased logic density caches can be on same chip as processor
- · Reduces external bus activity and speeds up execution times
- No bus cycles; shorter data path is faster than 0-wait bus cycles
- Bus is free to do other transfers

### **Multilevel Caches**

- It is usually desirable to have external as well as internal cache
- With only 1 level bus access to memory is slow
- Most contemporary computers have at least 2 **levels** 
  - Internal: Level 1 (L1)
  - External: Level 2 (L2)
- External L2 cache typically built with fast SRAM; uses separate and faster data bus
- Now incorporated on processor chip

- L2 and L3 Cache Performance improvements depend on hit rates
- Complicates replacement algorithms and write
- With L2 cache on-board L3 cache can improve performance just as L2 can improve over L1

# Unified and Split Caches

- Split caches have separate caches for instructions and data
  - These tend to be stored in different areas of memory
- Pros of unified cache:
  - Higher rate for given cache size because cache is automatically balanced between instructions and data

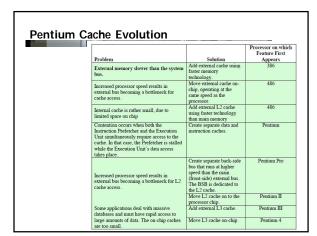
Only one cache needs to implemented

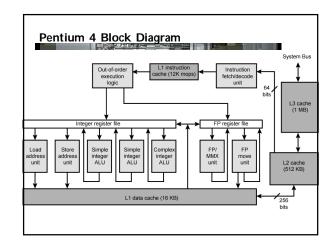
# Split Cache

- Current trend favors split caches
  - Useful for superscalar machines with parallel execution of instructions and prefetching of predicted instructions
  - Split cache eliminates contention for cache between instruction fetch/decode unit and the execution unit (when accessing data)
  - Helps to keep pipeline full because the EU will block (the fetch/decode unit otherwise)

### Pentium Cache Evolution

- 80386 no on chip cache
- 80486 8k using 16 byte lines and four way set associative organization
- Pentium (all versions) two on chip L1 caches
   Data & instructions
- Pentium III L3 cache added off chip
- Pentium 4
  - L1 caches
    - 8k bytes
    - 64 byte lines
    - four way set associative
  - L2 cache
    - Feeding both L1 caches
    - 256k
    - 128 byte lines
  - 8 way set associative
  - L3 cache on chip





### Pentium 4 Core Processor

- · Fetch/Decode Unit
  - Fetches instructions from L2 cache
  - Decode into micro-ops
  - Store micro-ops in L1 cache
- · Out of order execution logic
  - Schedules micro-ops
  - Based on data dependence and resources
  - May speculatively execute
- · Execution units
  - Execute micro-ops
  - Data from L1 cache
- Results in registers
- Memory subsystem
  - L2 cache and systems bus

# Pentium 4 Design Reasoning

- Decodes instructions into RISC like micro-ops before L1 cache
- · Micro-ops fixed length
  - Superscalar pipelining and scheduling
- · Pentium instructions long & complex
- Performance improved by separating decoding from scheduling & pipelining
  - (More later ch14)
- Data cache is write back
  - Can be configured to write through
- L1 cache controlled by 2 bits in register
  - CD = cache disable
  - NW = not write through
  - 2 instructions to invalidate (flush) cache and write back then invalidate
- · L2 and L3 8-way set-associative
  - Line size 128 bytes

### Pentium 4 Cache Operating Modes

Control Bits		Operating Mode			
CD	NW	Cache Fills	Write Throughs	Invalidates	
0	0	Enabled	Enabled	Enabled	
1	0	Disabled	Enabled	Enabled	
1	1	Disabled	Disabled	Disabled	

Note: CD = 0; NW = 1 is an invalid combination.

- ARM3 started with 4KB of cache
- ARM design emphasis on few transistors and small, low-power chips has kept cache fairly

### **ARM Cache Features**

Core	Cache Type	Cache Size (kB)	Cache Line Size (words)	Associativity	Location	Write Buffer Size (words)
ARM720T	Unified	8	4	4-way	Logical	8
ARM920T	Split	16/16 D/I	8	64-way	Logical	16
ARM926EJ-S	Split	4-128/4- 128 D/I	8	4-way	Logical	16
ARM1022E	Split	16/16 D/I	8	64-way	Logical	16
ARM1026EJ-S	Split	4-128/4- 128 D/I	8	4-way	Logical	8
Intel StrongARM	Split	16/16 D/I	4	32-way	Logical	32
Intel Xscale	Split	32/32 D/I	8	32-way	Logical	32
ARM1136-JF-S	Split	4-64/4-64 D/I	8	4-way	Physical	32

# Write Buffer

- Distinctive feature of ARM cache is a FIFO write buffer between cache and main memory
- When data is written to a bufferable area of memory, data are placed in write buffer at CPU clock speed and CPU continues execution
- Write buffer performs memory write in parallel with processor
- If write buffer is full then CPU is stalled until write buffer drains
- · Data from same addresses as write buffer cannot be read until write is complete