

#### FACULTY OF COMPUTING

## SEMESTER 1

2023/2024

## SECI 1013 - DISCRETE STRUCTURE

# **SECTION 2**

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#### Question 1

- a) In order to know the habits of the FC students about social networks we have asked 150 students if they have an active account in some of the most famous social networks: Facebook, Instagram or Twitter. Considering the positive answers, we obtain that 25 people have only Facebook account, 30 have only Instagram account, and 20 have only Twitter account. 15 of them have Facebook and Instagram accounts, but not a Twitter one. Only 5 people have an account in the three social networks. After the experiment, we obtain 65 Facebook users, 55 Instagram users and 50 Twitter users.
  - i) Draw a Venn diagram to represent to above problem. (2 marks)
  - ii) How many students do not have an account in any of the three social networks?

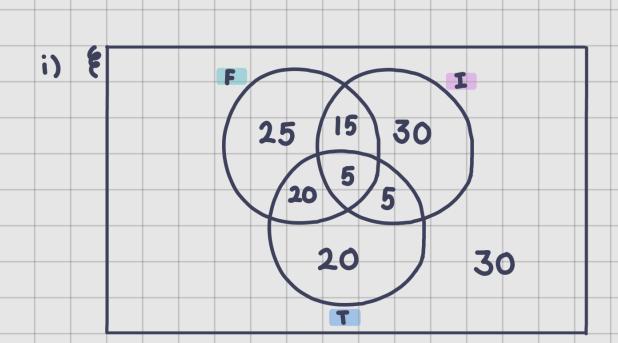
(2 marks)

iii) How many students have exactly two social networks?

(2 marks)

iv) How many students have social media account other than Facebook?

(2 marks)



F: Facebook users

I: Instagram users

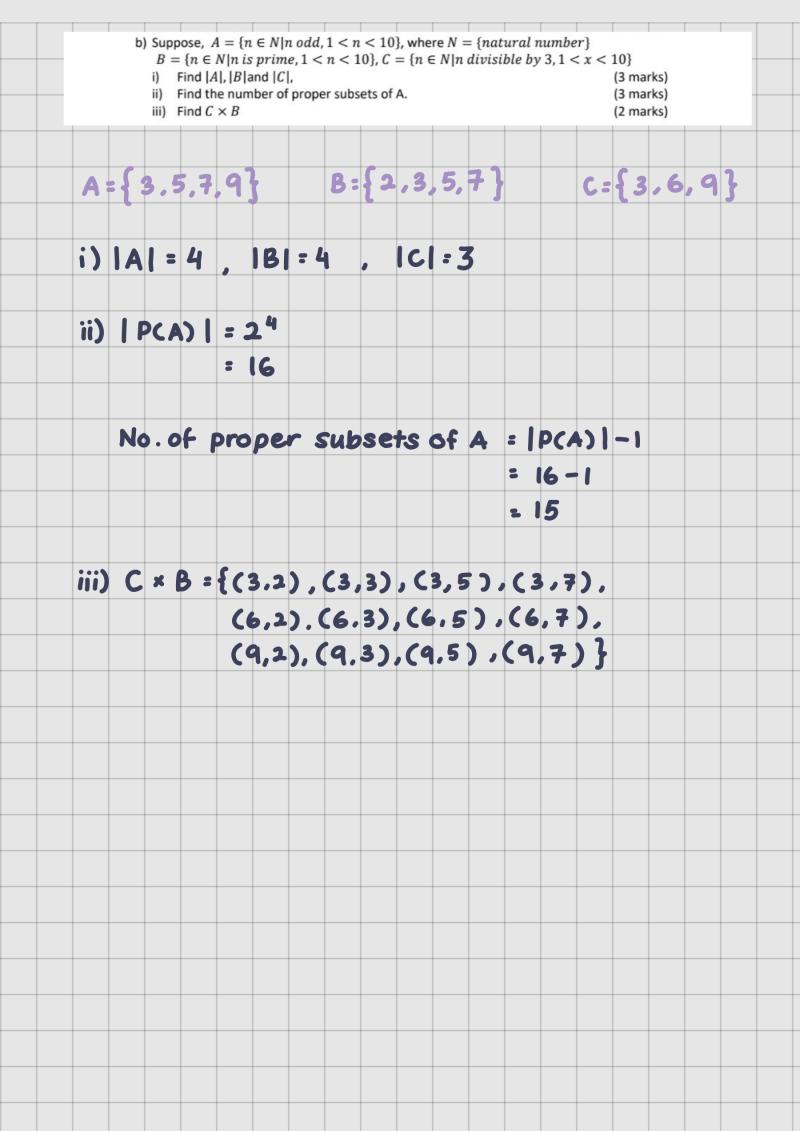
T: Twitter users

\$ : FC Students

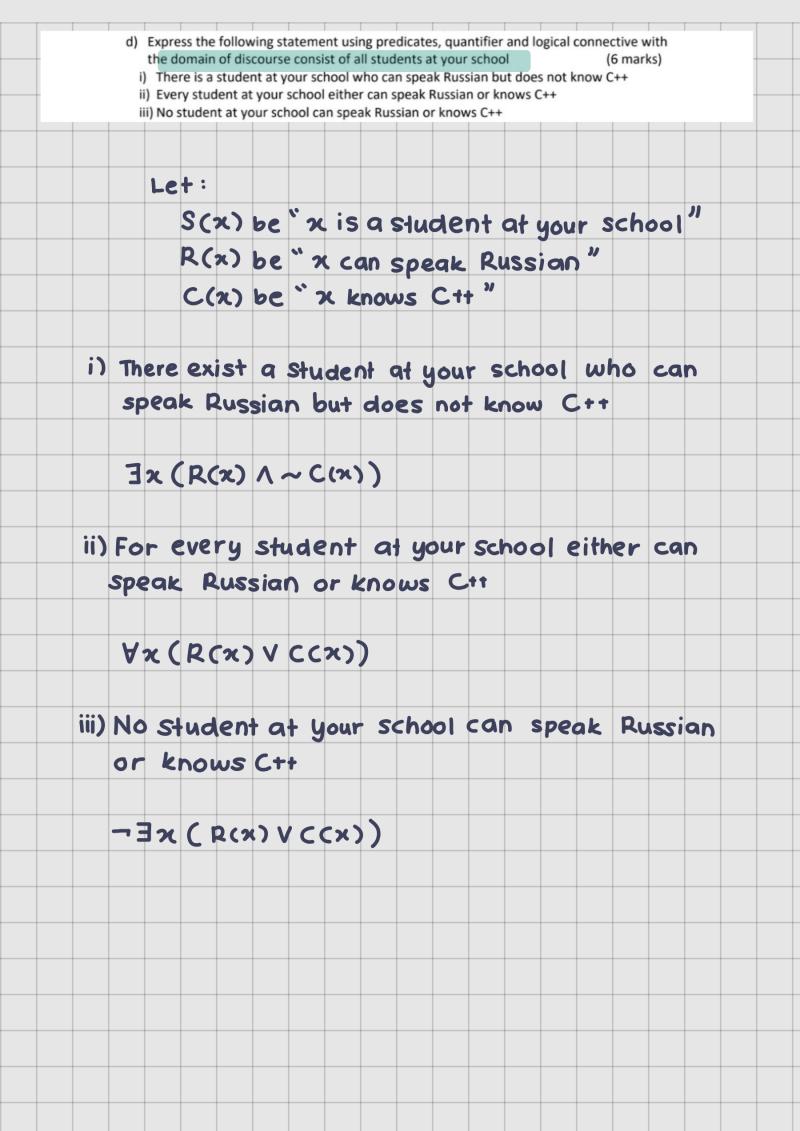
ii) (FUIUT)' = 30 students

iii) ((FnI) U(FNT) U (INT)) n (FNINT) = 40 student

iv) (FUIUT) - F = 55 students



| P         | 9                           | ~(P  | Vq)   | ~   | ρ  | (~                         | p/q)                                   | ~(p   | Vq)V                               | (~P/     | 19)    |                  |    |    |
|-----------|-----------------------------|--|---|---|--|----------------------------|--|---|------------------------------------|----------|--------|------------------|----|----|
| T         | T                           |  | F   | F   |  |                            | F                                      |   | F                                  |          |        |                  |    |    |
| T         | F                           |  | F   | F   |  |                            | F                                      |   | F                                  |          |        |                  |    |    |
| F         | 7                           |  | F   | I   |  |                            | T                                      |   | T                                  |          |        |                  |    |    |
| F         | F                           | •  | 7   | 7   |  |                            | F                                      |   | T                                  |          |        |                  |    |    |
|           |                             |  |   |   |  |                            |  |   |                                    |          |        |                  |    |    |
| ( p       | Vq.                         | ) v (·   | νPΛ   | <b>q.</b> )   | <b>=</b> (                               | <b>`~</b> ρ                | 1~q                                    | v (·  | ~P ^                               | q. ) D   | 2 Ma   | rgan             | 's | La |
|           |                             |  |   |   |  |                            | 1 (~q                                  |   |                                    |          | Stri   |                  |    |    |
|           |                             |  |   |   | = ~                                      | •                          |  |   |                                    | C        | omp    | eme              | nt | L  |
|           |                             |  |   |   |  | •                          |  |   |                                    |          |        |                  |    |    |
|           |                             |  | p: I go to<br>q: it is a<br>r: it is S  | o the be<br>a sunny<br>unday  | each<br>sumn                             | ner da                     |  |   |                                    |          | (2 ma  | irks)            |    |    |
|           | i)   {<br>ii)   f           | go to the  | p: I go to<br>q: it is a<br>r: it is Si<br>beach weither Su   | o the be<br>a sunny<br>unday<br>wheneve<br>unday or                             | each<br>sumn<br>er it is<br>r sunn       | mer da<br>Sund             |  | ny summ<br>nen I do r                         | er day<br>not go to t              |          | . (2 m | arks)            |    |    |
|           | i)   {<br>ii)   f           | go to the  | p: I go to<br>q: it is a<br>r: it is Si<br>beach weither Su   | o the be<br>a sunny<br>unday<br>wheneve<br>unday or                             | each<br>sumn<br>er it is<br>r sunn       | mer da<br>Sund             | ay<br>lay and suni<br>nmer day th      | ny summ<br>nen I do r                         | er day<br>not go to t              |          | . (2 m | arks)            |    |    |
| i)        | i) 1 g<br>ii) 1f<br>iii) 1f | go to the it is not f I do not   | p: I go to q: it is s r: it is S e beach weither Su e go to th                                      | the bear sunny unday whenever unday or the beach                                | each<br>summer it is<br>r sunn<br>h then | mer da<br>Sund             | ay<br>lay and suni<br>nmer day th      | ny summ<br>nen I do r                         | er day<br>not go to t              |          | . (2 m | arks)            |    |    |
| i)<br>ii) | i)   [8 ii)   If iii)   If  | go to the it is not I do not   | p: I go to q: it is s r: it is S e beach w either Su e go to th                                     | the bear sunny unday whenever unday or the beach                                | each<br>summer it is<br>r sunm<br>h then | mer da<br>Sund             | ay<br>lay and suni<br>nmer day th      | ny summ<br>nen I do r                         | er day<br>not go to t              |          | . (2 m | arks)            |    |    |
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| i)<br>ii) | i)   g ii)   f iii)   f     | go to the it is not it is not if I do not it is not it is not if I do not it is not if I | p: I go to q: it is s r: it is S beach weither Su go to th  | of $\forall x(x)$   | each summer it is r sunrh then           | mer da Sunda Sunda it is n | lay and suninmer day the not either So | ny summ<br>nen I do r<br>unday or<br>determin | er day<br>not go to t<br>sunny sui | mmer day | . (2 m | arks) arks) n is |    |    |
| i)<br>ii) | i)   g ii)   f iii)   f     | go to the it is not it is not if I do not it is not it is not if I do not it is not if I | p: I go to q: it is s r: it is S beach weither Su go to th  | of $\forall x(x)$   | each summer it is r sunrh then           | mer da Sunda Sunda it is n | ay and suninmer day the                | ny summ<br>nen I do r<br>unday or<br>determin | er day<br>not go to t<br>sunny sui | mmer day | . (2 m | arks)<br>arks)   |    |    |
| i) ii)    | i)   [8 ii)   If            | go to the it is not it is not if I do not it is not it is not if I do not it is not if I do not it is not it is not if I do not it is not it is not if I do not it is not it is not if I do not it is not it i | p: I go to q: it is s r: it is S beach weither Su go to th  | of $\forall x(x)$ the document of $\forall x(x)$ the document of $\forall x(x)$ | each summer it is r sunming the then     | mer da Sunda Sunda it is n | lay and suninmer day the not either So | ny summ<br>nen I do r<br>unday or<br>determin | er day<br>not go to t<br>sunny sui | mmer day | . (2 m | arks) arks) n is |    |    |
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|        | Prove the following theorem using indirect proof method. (5 marks)   |
|--------|--|
|        | For all integers, if $a^2 - 3b$ is even then a is even and b is even   |
|        | Tot an integers, if a so is even then a seven and a seven  |
|        |  |
| Le     | <i>†</i> :   |
|        | P(a,b): 92-3b is even  |
|        | A(a): a is even  |
|        | B(b): b is even  |
|        |  |
| Va     | Vb (P(a,b) → (A(a) 1 B(b)))  |
|        |  |
| = ¬(A  | (a) $\wedge$ B(b)) $\rightarrow \neg$ P(a,b) contrapositive  |
|        | Tell / Cell / Ce |
| 4/     |  |
| = 7A(  | (a) V ¬B(b) → ¬P(a,b) De morgan's Laws   |
|        |  |
| ·if    | 9 is odd or b is odd then a <sup>2</sup> -3b is odd  |
|        |  |
| ① · 16 | et a be odd and b even   |
| . 0    | 1 = 2n + 1 and b = 2m  |
|        | $(2n+1)^2 - 3(2m)$   |
|        | $= 4n^2 + 4n + 1 - 6m$   |
|        |  |
|        | $= 2(2n^2 + 2n - 3m) + 1$ $k = 2n^2 + 2n - 3m$   |
|        | = 2 k + 1 → odd TRUE   |
|        |  |
| ② · 1e | t a be even and b odd.   |
| . 0    | 1 - 2n and b - 2m + 1  |
|        | $(2^2 - 3b) = (2n)^2 - 3(2m + 1)$  |
|        | = 4n <sup>2</sup> -6m -3   |
|        |  |

 $= 2(2n^2-3m-2)+1$ 

= 2h +1 → odd TRUE

 $h = 2n^2 - 3m - 2$ 

