

# **Curse of Dimensionality**

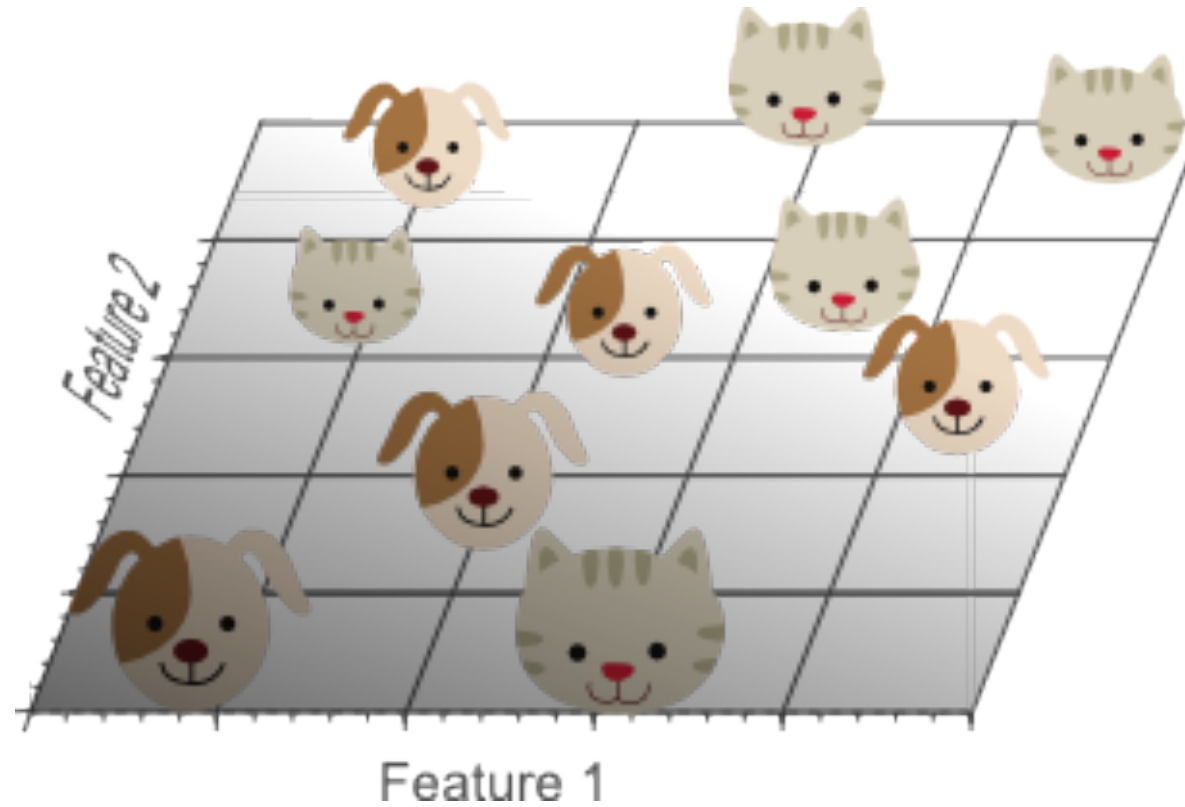
## **Or the mysteries of highly-dimensional spaces**

**Mauricio Araya**

<https://www.visiondummy.com/2014/04/curse-dimensionality-affect-classification/>

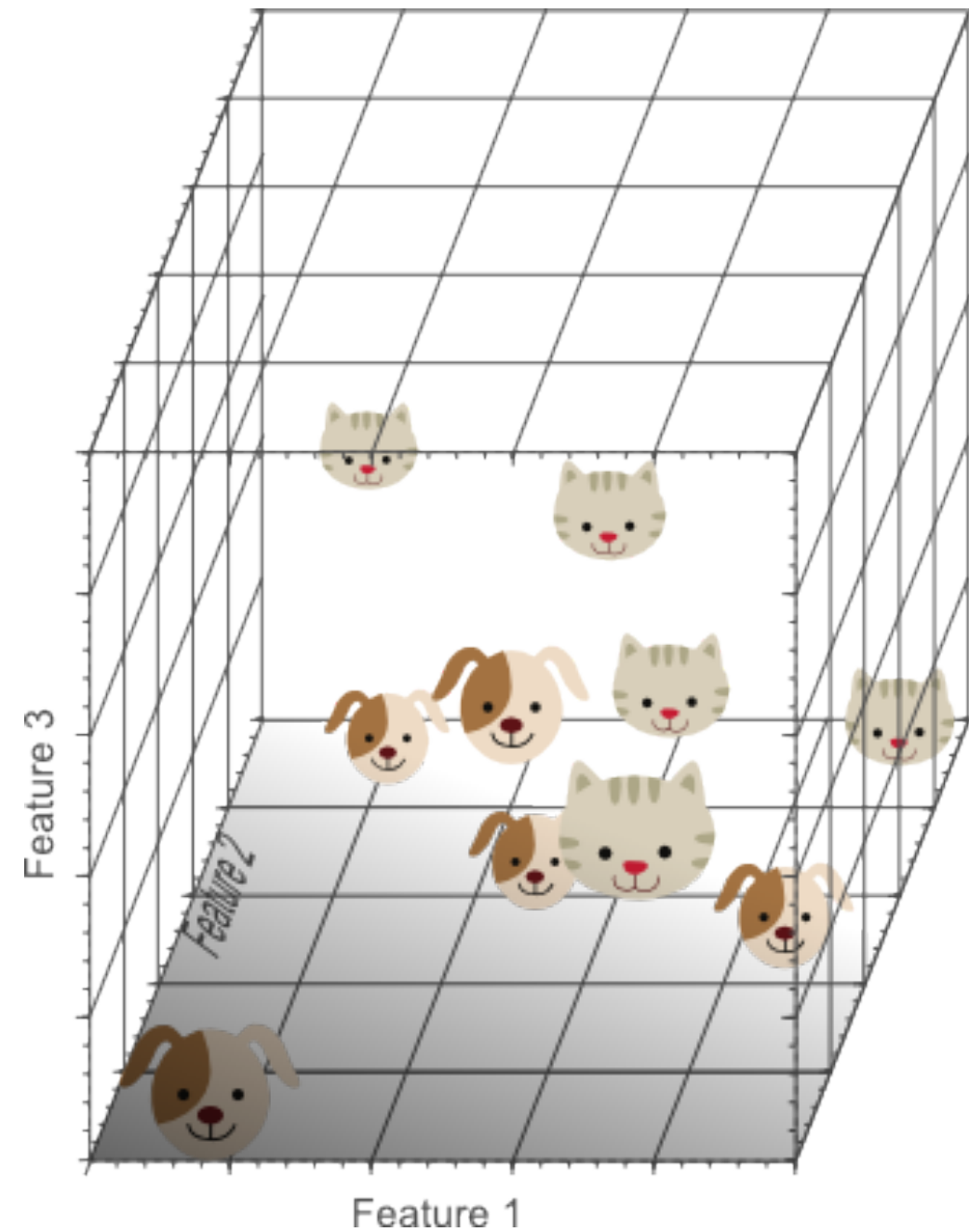
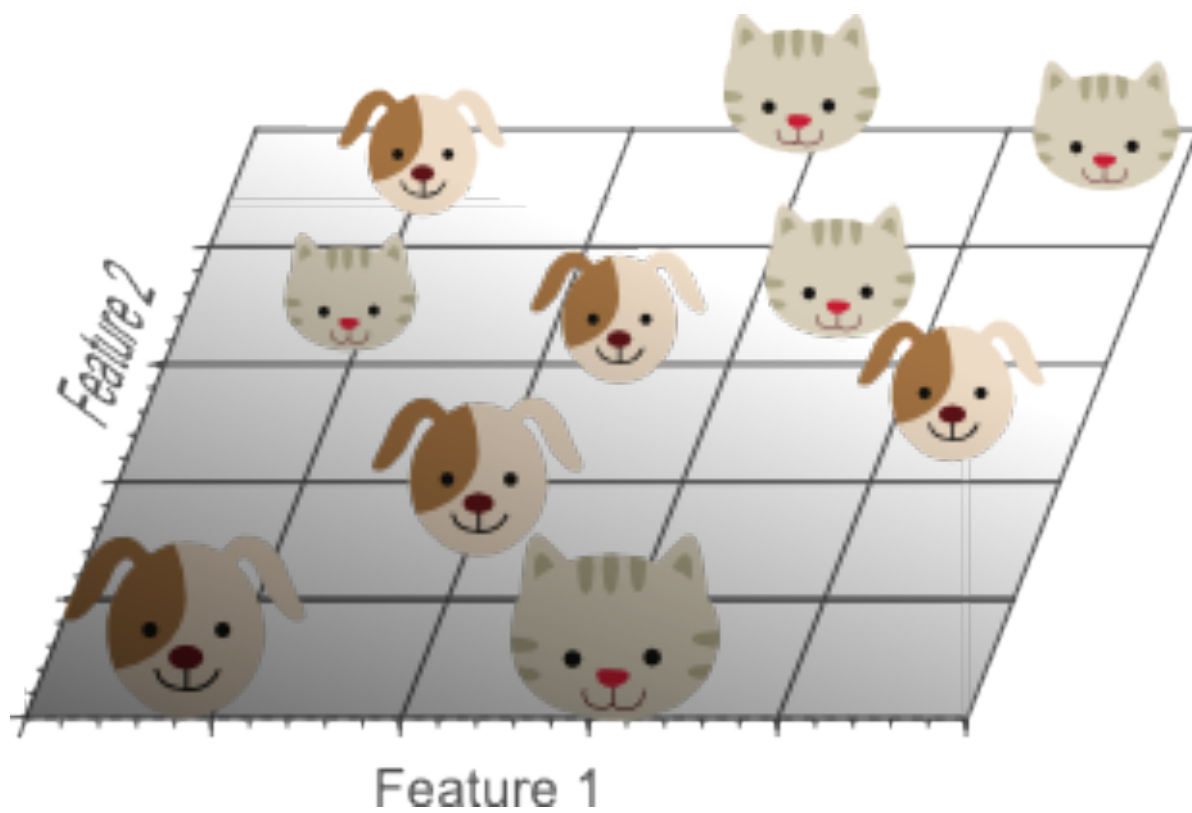
# Cats and Dogs

The good thing



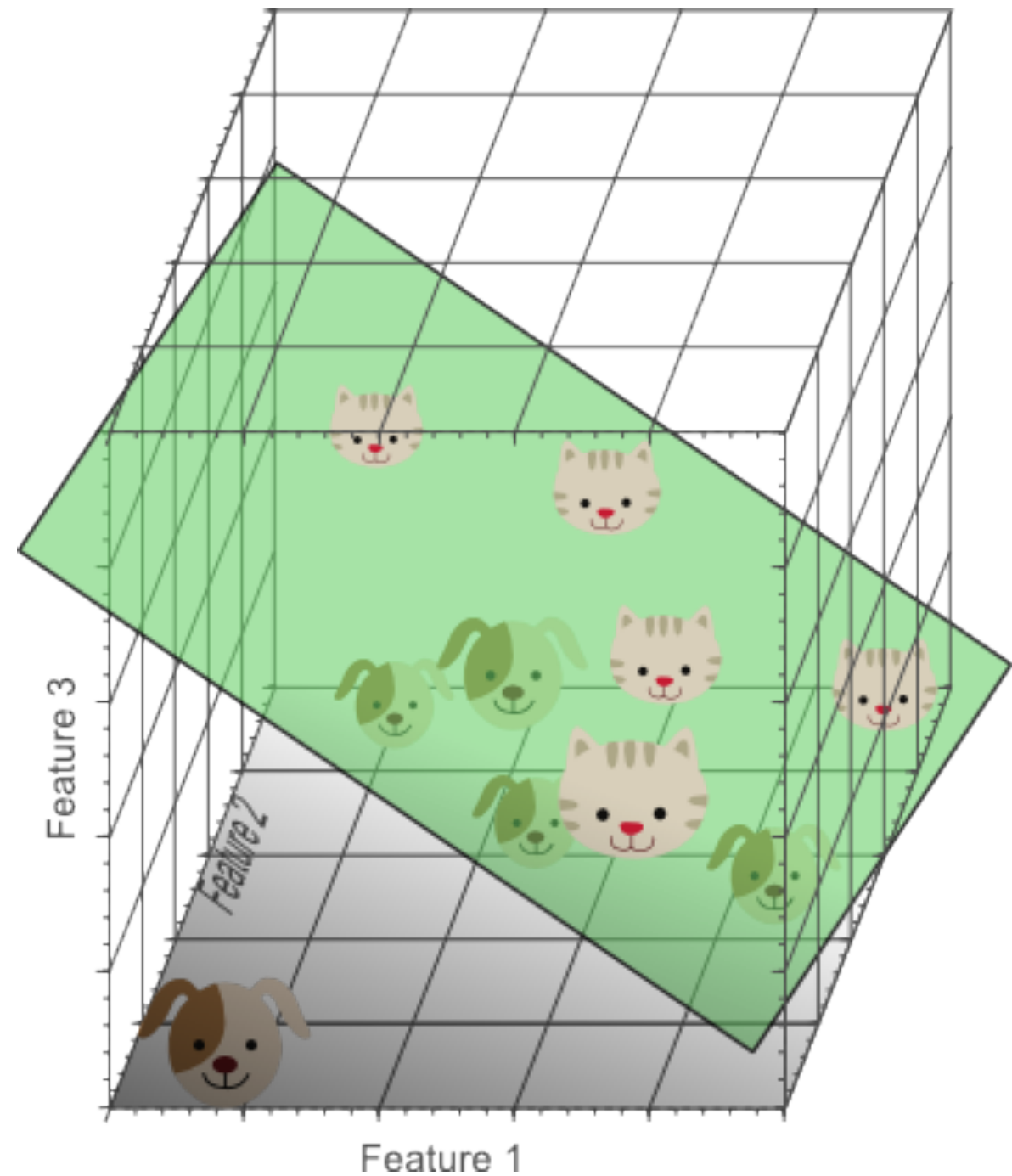
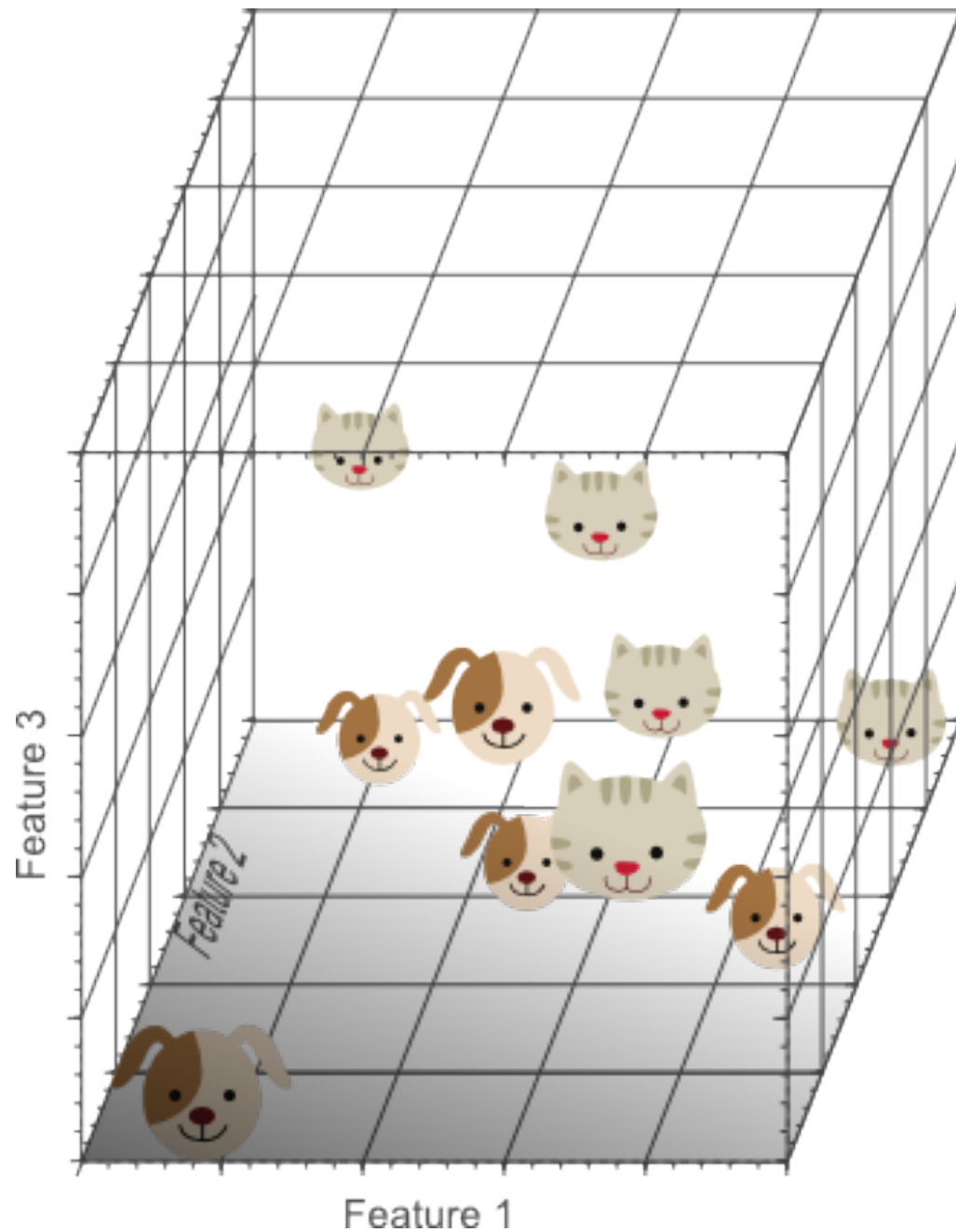
# Cats and Dogs

The good thing



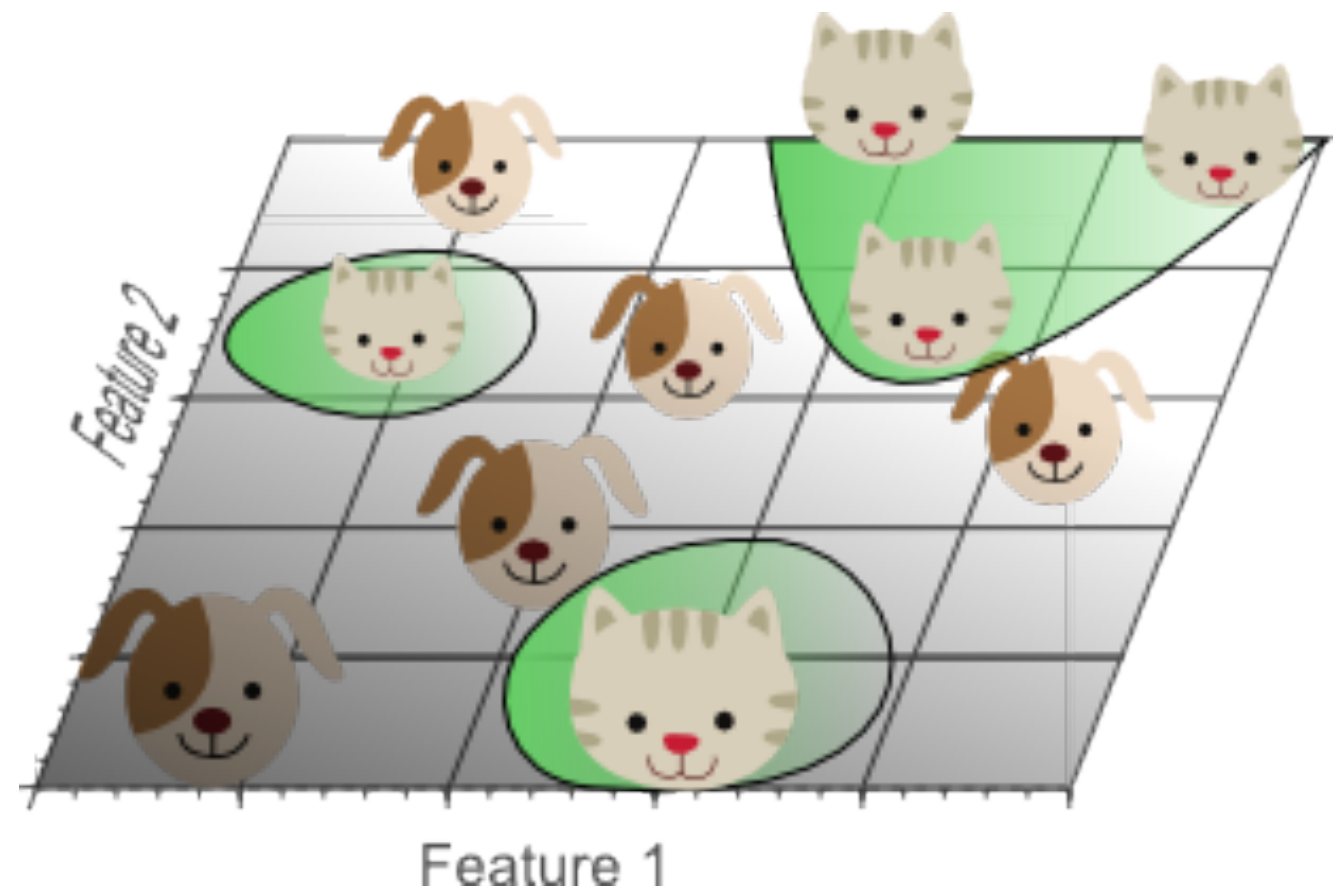
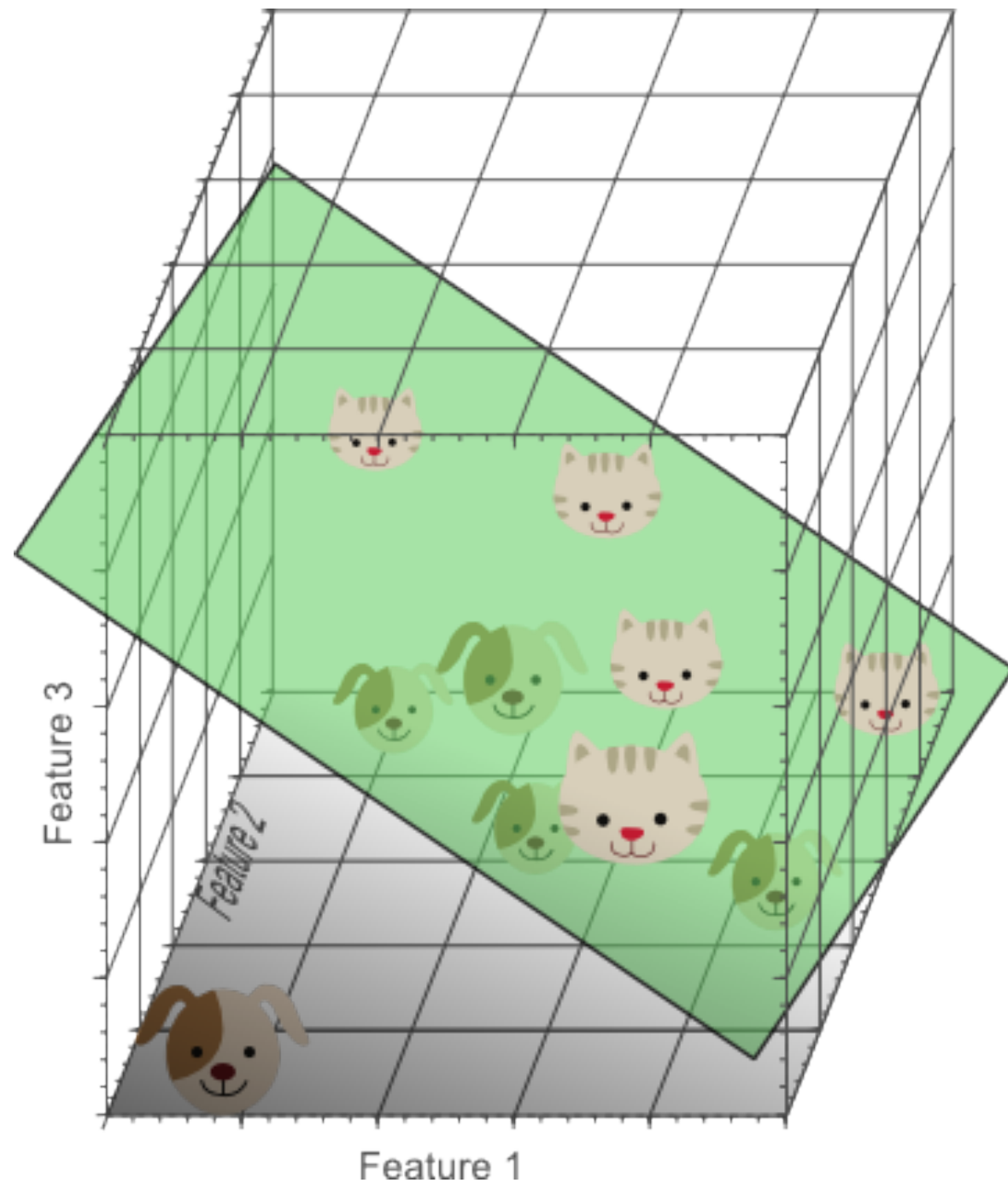
# Cats and Dogs

The good thing



# Cats and Dogs

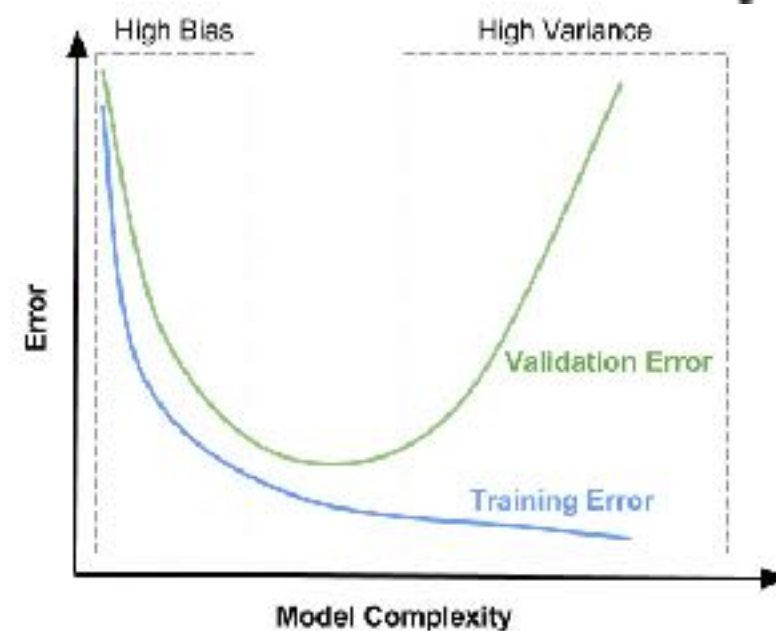
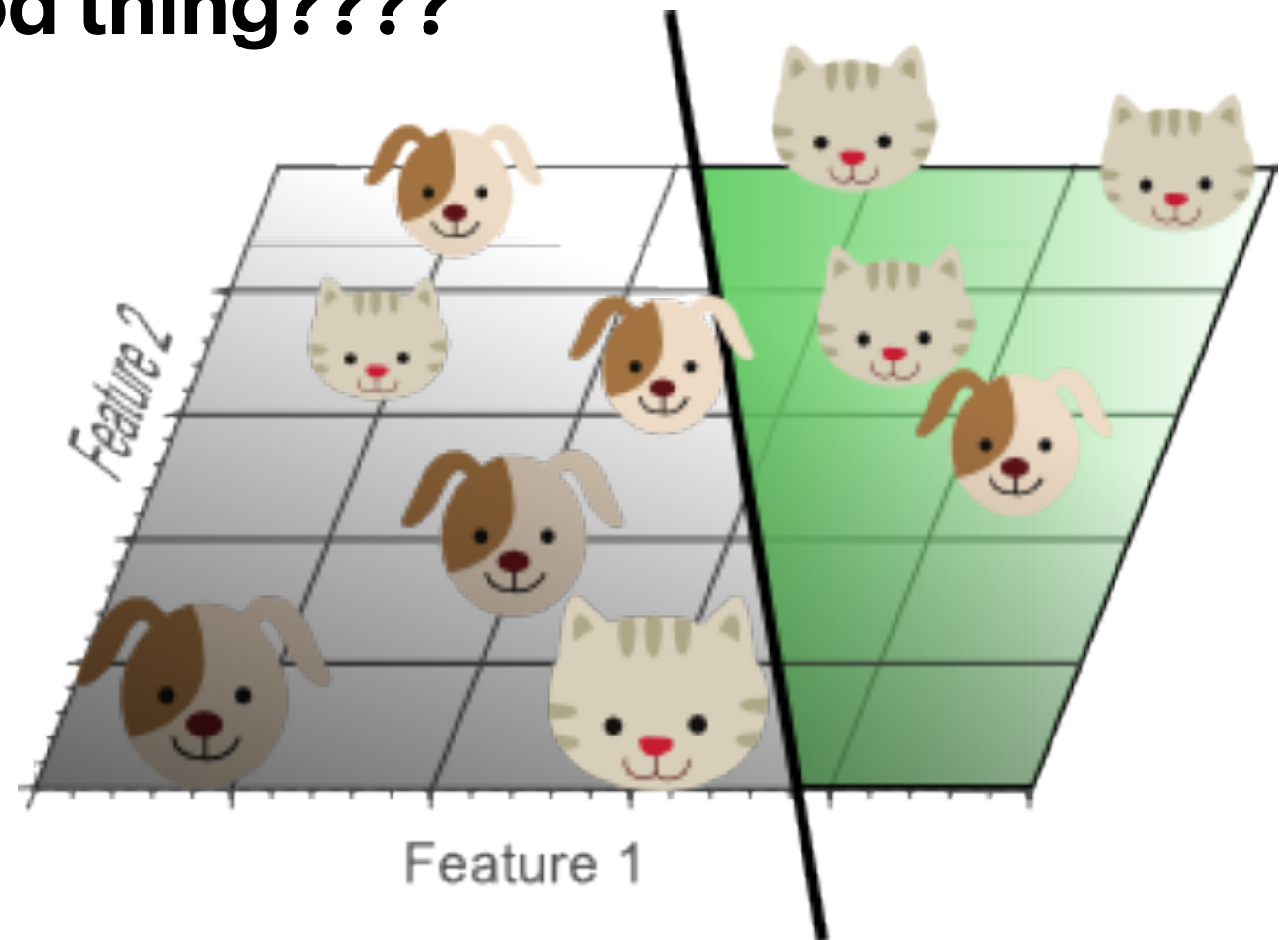
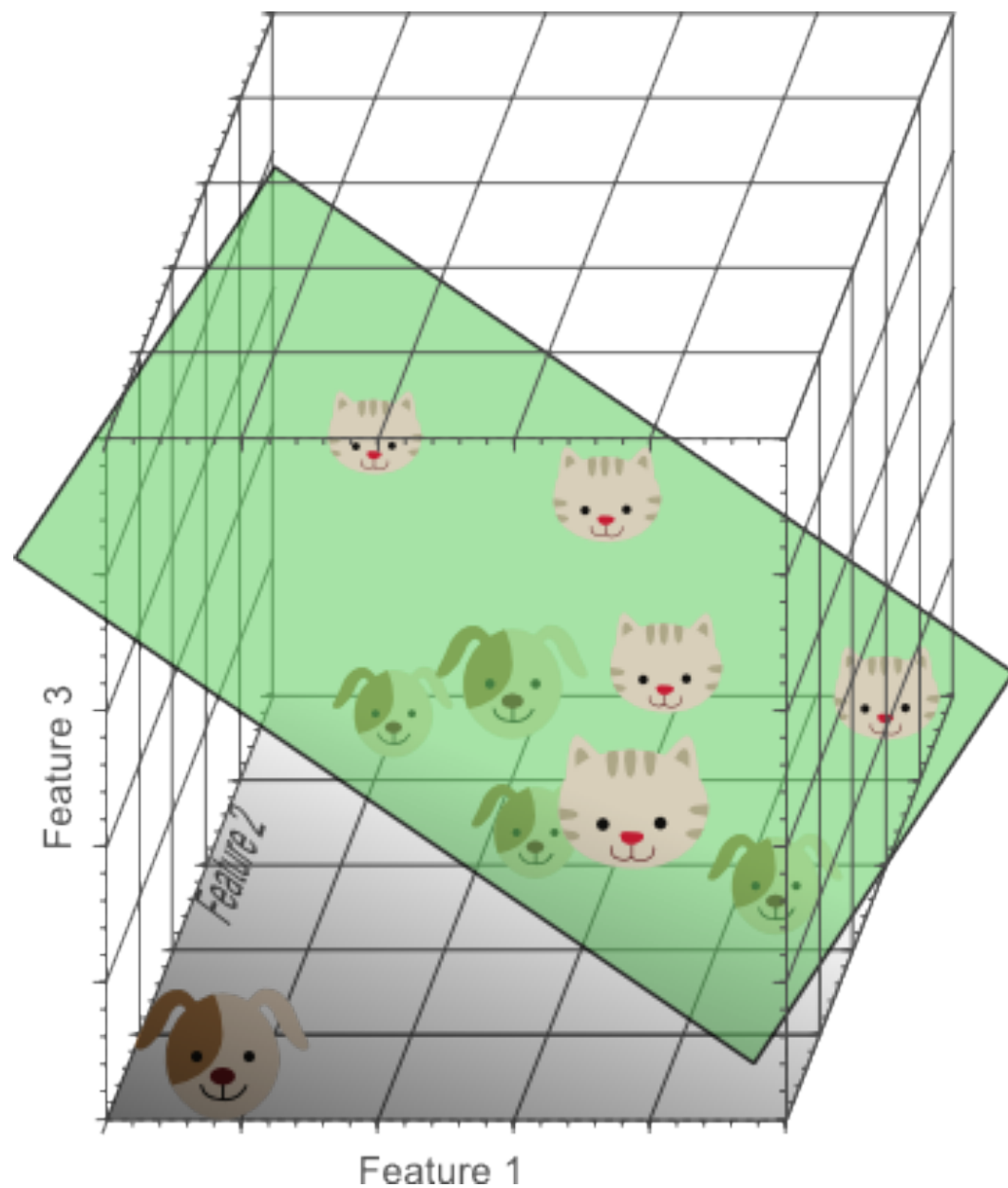
The good thing





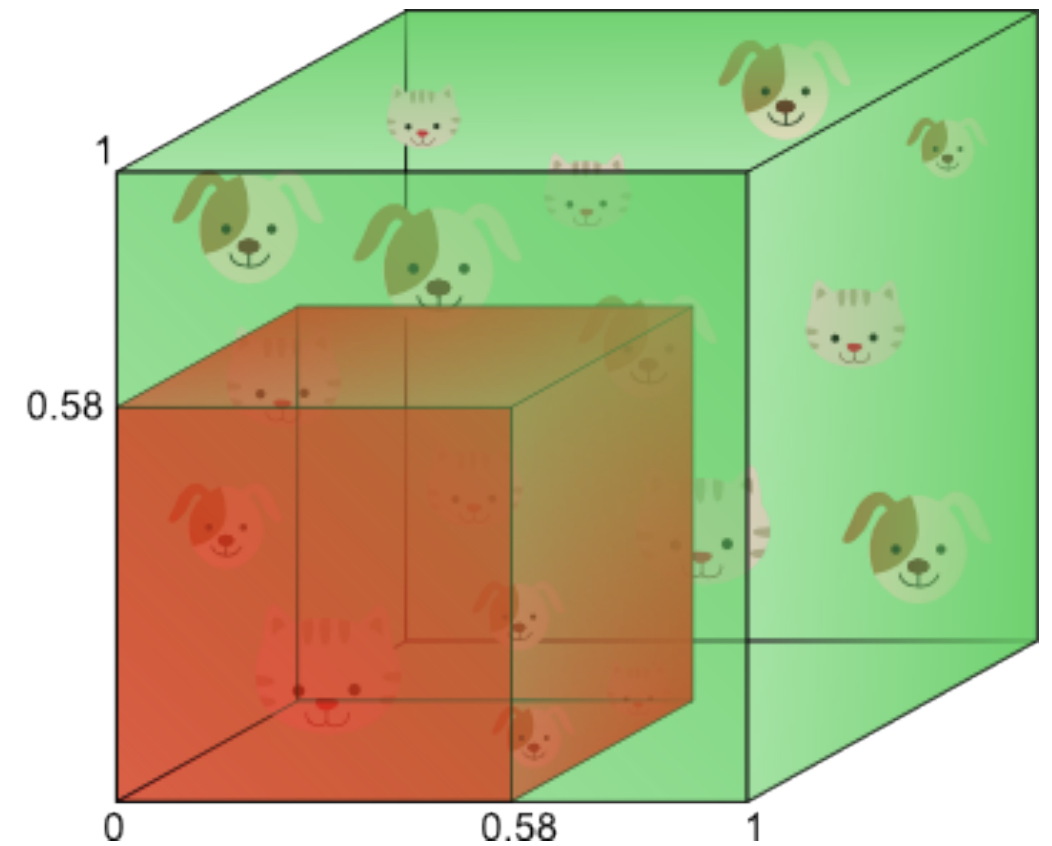
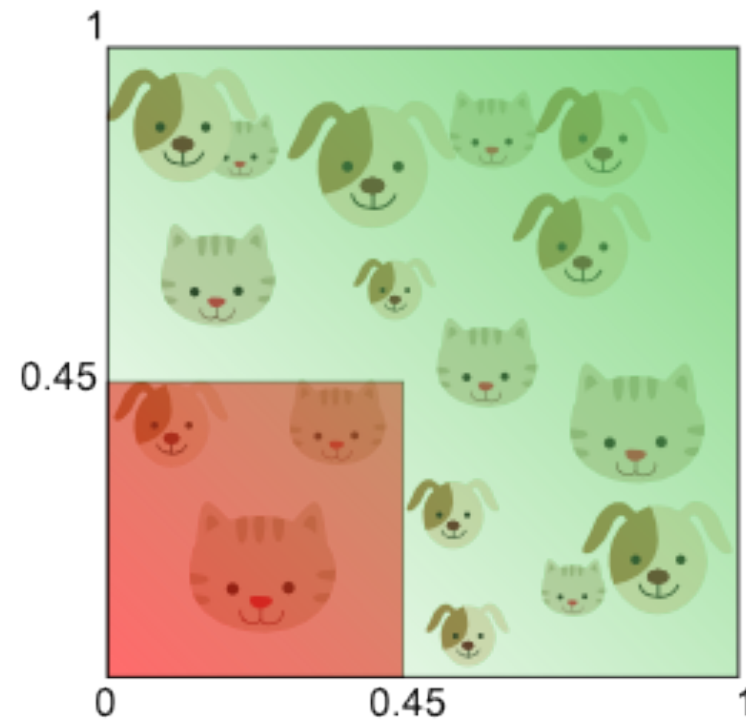
# Cats and Dogs

The good thing????



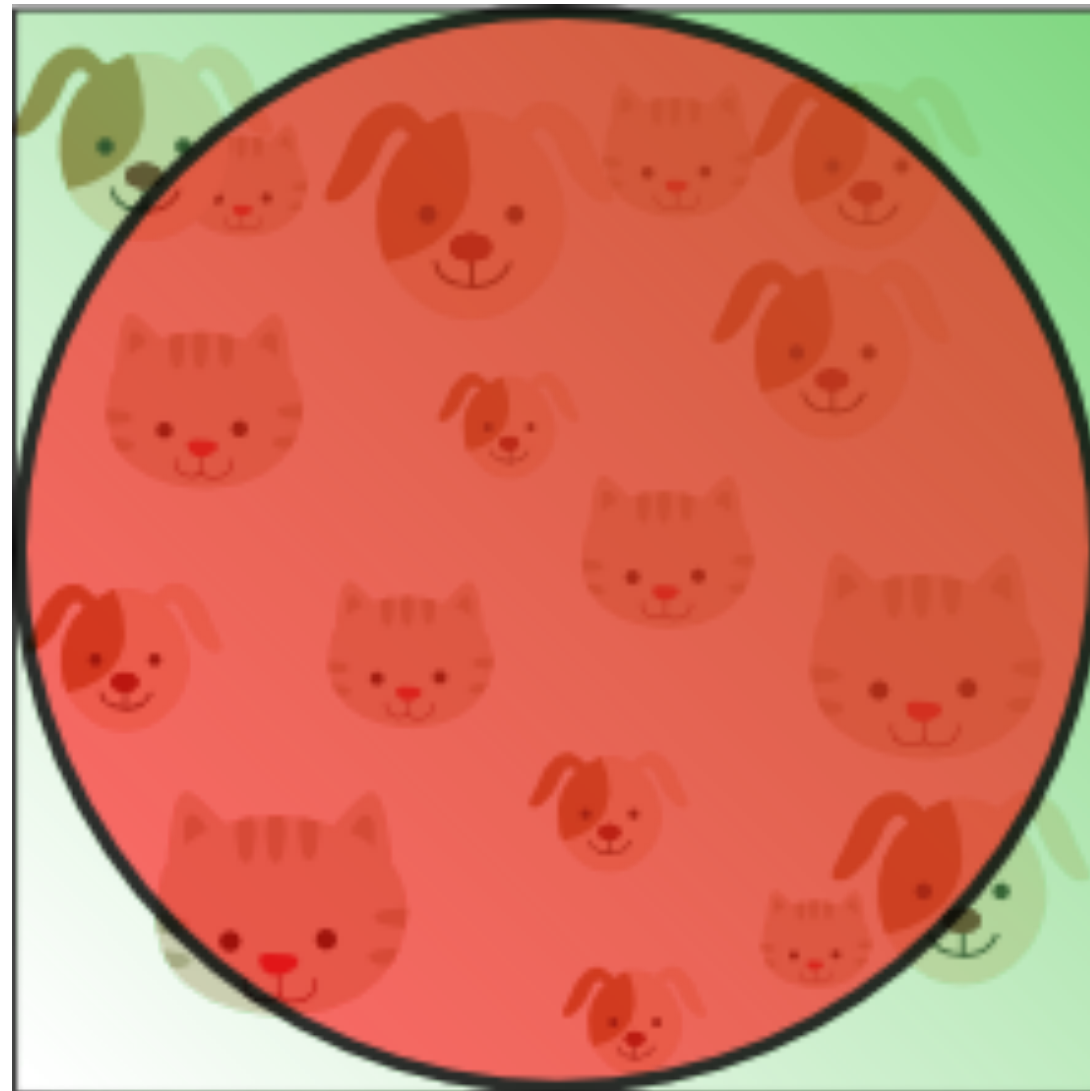
# Cats and Dogs

**The 20% is the 60% of features in 3D**



# Cats and Dogs

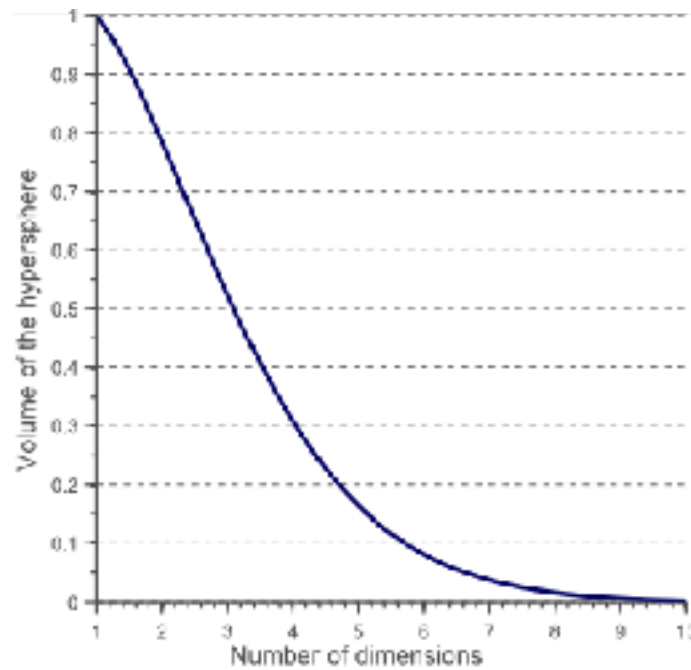
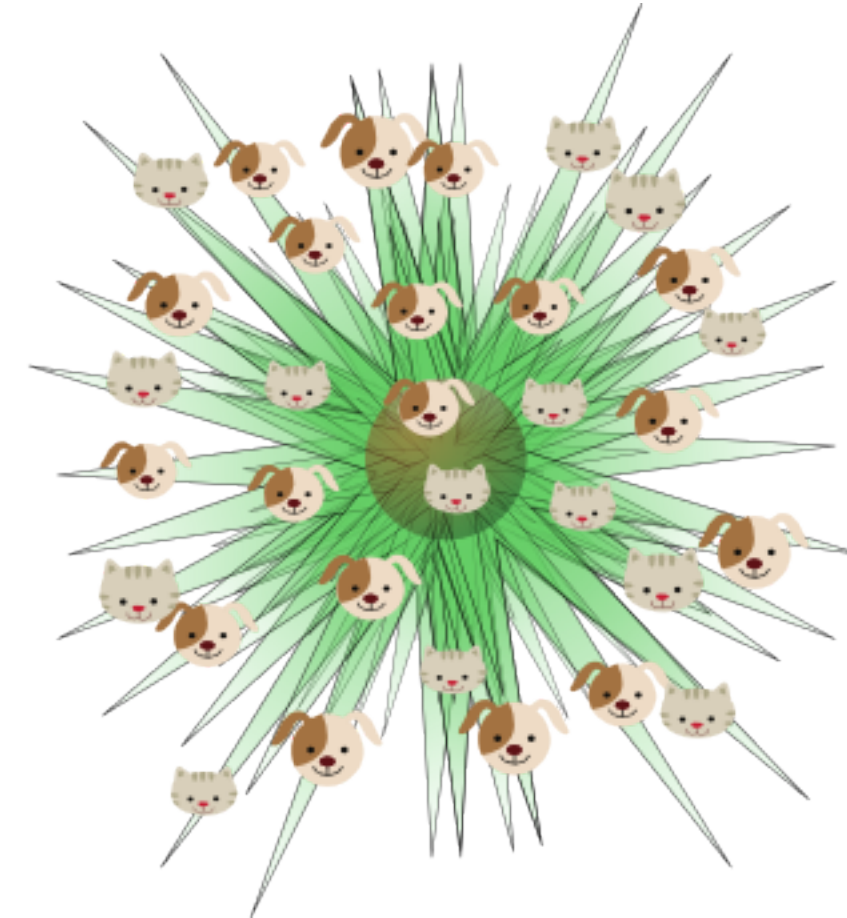
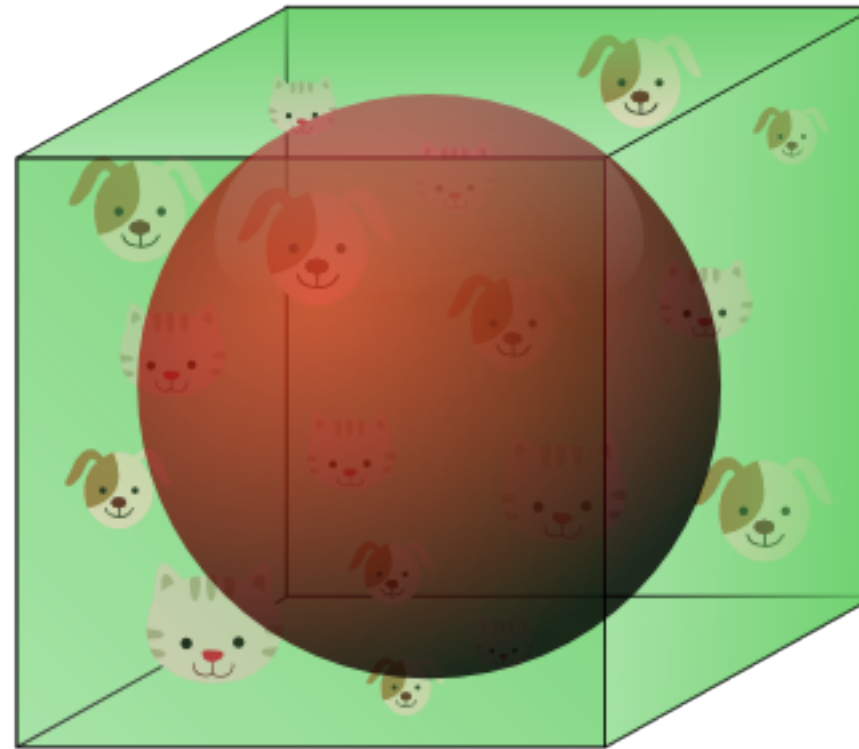
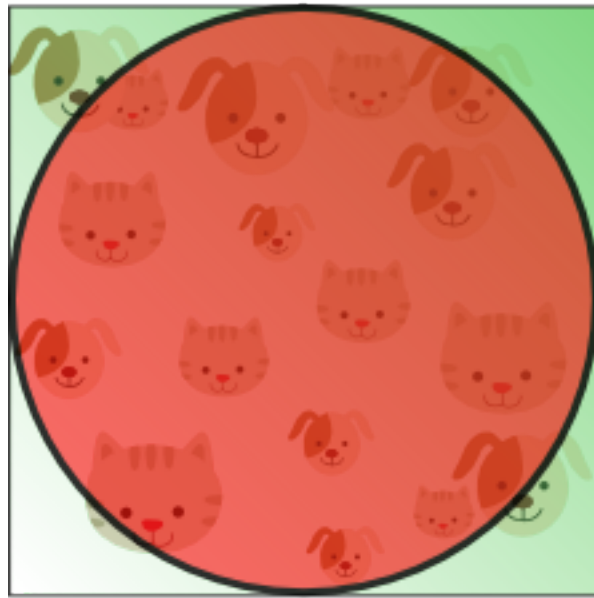
## Circle in a Square





# Cats and Dogs

## Hypersphere in a Hypercube



# « Gaussian egg »

$$X = (X_1, \dots, X_M) \quad X_i \sim N(0,1)$$

estimation for  $P(X \approx (r, \dots, r)^T)$

$$E(r^2) = \frac{1}{M} M = 1 \quad V(r^2) = \frac{2M}{M^2} = \frac{2}{M}$$

