

University College Dublin An Coláiste Ollscoile, Baile Átha Cliath

PHYC20080 Fields, Waves and Light

Experiment No.1 Measurement of the Focal Lengths of Lenses and a Determination of Brewster's Angle

4 February 2025

by Joana C.C. Adao (Student No. 23311051)

Tuesday 16.00-18.00 Slot Nicki (Coordinator)

Contents

Ab	stract	2
1	Theory	2
1.1	Lenses	2
	1.1.1 Focal Length	3
	1.1.2 Image Formation	3
1.2	Polarisation	4
	1.2.1 Reflection and Refraction	5
	1.2.2 Snell's Law	5
	1.2.3 Brewster's Angle	5
	1.2.4 Ratios of Intensity	6
2	Methodology	7
2.1	Determining the Focal Length	7
	2.1.1 Convex Lens Method	7
	2.1.2 Concave Lens Method	7
2.2	Determining Brewster's Angle Method	8
3	Results and Calculations	8
3.1	Determining the Focal Length	8
	3.1.1 Convex Lens	8
	3.1.2 Concave Lense	10
3.2	Determining Brewster's Angle	10
4	Conclusion	10
5	Applications of Lenses	10
5.1	Eyeglasses	10
5.2	Microscopes	10
5.3	Telescopes	10
Ref	erences	11
\mathbf{Ap}	pendix	13
List	of Figures	13
	of Tables	13
	Data	13
Coc	e	13

The aim of this experiment

1 Theory

1.1 Lenses

Lenses are a piece of transparent materials, typically glass, that are used to bend and focus rays of light onto one spot to form images [1, 2]. Lenses can either be shaped to be concave (depressed, caved) or convex (bulging, rounded), but have to have at least one curved surface [1, 2] The properties that make up a lens are: focal length (§1.1.1), focal point, optical axis, focus, principal axis, centre of curvature [3, 4]

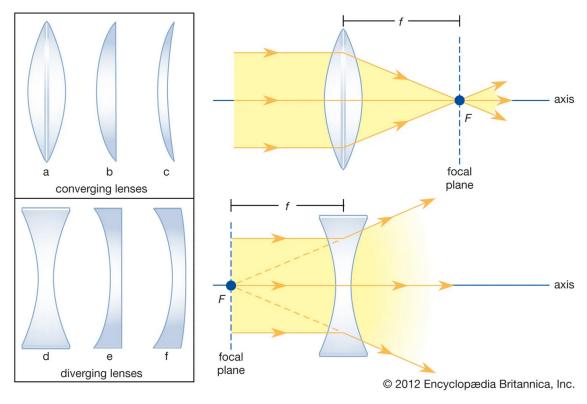


Figure 1: Diagram of converging (convex) and diverging (concave) lenses [1].

(a): biconvex, (b): plano-convex, (c): positive meniscus; (d): biconcave, (e): plano-concave, (f): negative meniscus

Convex lenses make the parallel travelling rays of light passing through it **converge** to a certain point known as the *focal point* (1.1.1) [5]. The degree at which light is bent depends on the absolute curvature of the lens [6]. The convex lens has two extra properties that do not apply to a concave lens: *radius of curvature*, and *aperture* [4]. The behaviour of ligh as it passes through a convex lens can be simulated via the interactive diagram link in *References*, §5.3 [7].

Concave lenses make the parallel travelling rays of light passing through it **refract** away from the focal point of the lens [5, 8]. The behaviour of ligh as it passes through a concave lens can be simulated via the interactive diagram link in *References*, §5.3 [9].

1.1.1 Focal Length

The focal length is the distance, typically in millimetres, of the *optical axis* (the centre of the lens) to the focal plane shown in figure 1 [10, 11]. The focal point, indicated by the point at which the focal plane and principal axis intersect, is the point at which the rays of light coincide [12]. For a concave lens, where the light diverges, there only exists an *apparent* focal point behind the lens, where a virtual image would be formed (§1.1.2) [12].

The formula below, equation 1, is used to calculate the focal length of a thin converging lens [13, 12], where \mathbf{u} is the distance between the *object* and the centre of the lens, and \mathbf{v} is the distance between the *image* and the centre of the lens:

$$\frac{1}{f} = \frac{1}{u} + \frac{1}{v} \tag{1}$$

Since a concave lens does not form a real image (§1.1.2) one must add a convex lens to overcome this issue. Therefore equation 1 becomes invalid (individually) for calculating the focal length. Instead, equation 2 below can be used to find the focal length of the combined lenses, where f_{convex} (focal length of the convex lens) and $f_{concave}$ (focal length of the concave lens) can be calculated individually using equation 1 [13]:

$$\frac{1}{f} = \frac{1}{f_{convex}} + \frac{1}{f_{concave}} \tag{2}$$

Concave lenses have *negative* focal length, as opposed to convex lenses, since the focal point is on the same side as the incident (incoming) light [3].

1.1.2 Image Formation

Two types of images can be formed when looking at a mirror or through a lens:

- Real image: an image formed when light converges at a point; inverted in nature [14].
- Virtual image: an image formed when light diverges away from a point; appears to be produced but is not actually present [14].

Standard image properties of convex lenses is that what is produced is a real image that is inverted and enlarged [4], but virtual images can also be formed. The image produced depends on the object position at the time of measurement. The types of images convex lenses can form are illustrated in figure 2 and described in table 1 (sourced directly from Geeksforgeeks [4]).

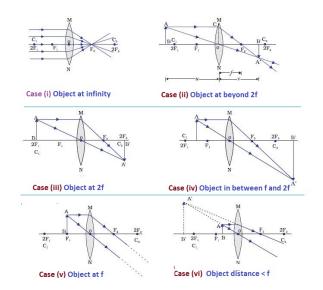


Figure 2:	Ray diagram o	f the cases	of convex	lens
	image form	ation $[15]$.		

Object	Image	Image	Image
Position	Position	Size	Nature
Beyond 2F	Between	Smaller	Real,
Beyond 2F	F and 2F		Inverted
At 2F	At 2F	Same size	Real,
At 2F			Inverted
Between	Beyond 2F	Larger	Real,
F and 2F		Larger	Inverted
	Infinity	Infinite	Real,
At F			Inverted
			(Highly Diminished)
Between	Beyond 2F	Larger	Virtual,
F and lens		Larger	Upright
At lens	At lens	Larger	Virtual,
At icis			Upright
Object inside	Between	Larger	Virtual,
lens	lens and F		Upright

Table 1: Table of the different cases of convex lens image formation [4, 15].

Standard image properties of concave lenses is that what is produced is a virtual image that is upright and diminished [3]. Concave lenses cannot produce real images. The only thing that changes between the virtual images that are produced is the magnitude at which they're diminished [15, 3].

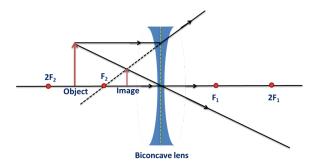


Figure 3: Ray diagram of concave lens image formation [15].

	Object	Image	Image	Image
	Position	Position	Size	Nature
	At infinity	At F_2	Highly Diminished,	Virtual,
		At F2	Point-Sized	Upright
	Object inside	Between	Diminished	Virtual,
	lens	lens and F_2	Diminished	Upright

Table 2: Table of the different cases of concave lens image formation [3, 15]

1.2 Polarisation

Since light, electromagnetic radiation, has both particle and (transverse) wave properties, it can be restricted to propagating in one direction, shown in figure 4 [16, 17]. Light can be polarised by passing through certain materials, like crystals, that act as a filter [17].

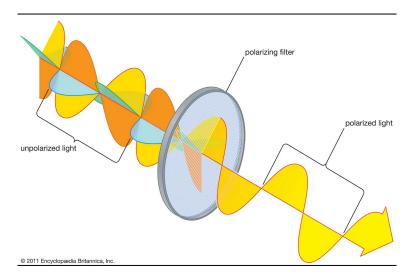


Figure 4: Visual representation of polarisation of light [17].

1.2.1 Reflection and Refraction

Reflection is when the light rays change direction as they hit a surface, or travel through a medium that has a different chemical composition to the original medium [18, 19]. For reflection to take place, the angle of incidence (θ_i) must equal the angle of reflection (θ_r) , of which are measured with respect to the normal (perpendicular) to the surface. This is known as the law of reflection [18, 19]. Diffusion is a type of reflection on a rough surface, so the light rays reflect in many different directions [18].

Refraction occurs when light travelling through a transparent medium encounters another transparent medium [19]. The variations in the matter of the medium causes the light to "bend" (change directions) as it is transmitted through the new medium [18]. The law of refraction is more commonly known as Snell's Law, §1.2.2.

1.2.2 Snell's Law

A ray of light changes directions when it passes from a medium of specificied refractive index (number indicating the magnitude of refraction of a medium) through another medium of different refractive index [18].

The below equation, equation 3, is the mathematical description of Snell's Law, with $n_{1,2}$ as the refractive index of the two mediums, θ_i as the incident angle, and θ_r as the refractive angle:

$$n_1 \sin \theta_i = n_2 \sin \theta_r \implies \frac{n_2}{n_1} = \frac{\sin \theta_i}{\sin \theta_r}$$
 (3)

The angle at which the light is refracted is dependent on the refractive index of the medium, $\sin \theta \propto n$, so if the refractive index of the second medium is greater than the first medium the angle of refraction will be smaller [20].

1.2.3 Brewster's Angle

Light can be polarised by reflection and refraction, as seen in figure 5, where majority of the light will be reflected off the medium and the rest of the light will be refracted through the medium. In doing so, the reflected ray gets partially polarised parallel to the medium's surface and the refracted ray get partially polarised perpendicular to the surface of the medium [21].

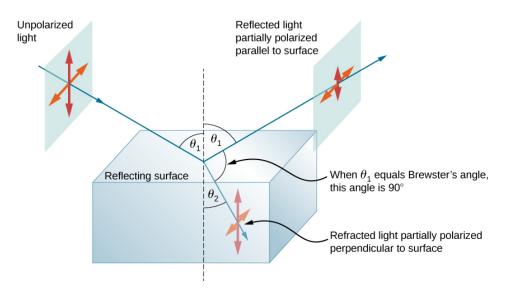


Figure 5: Diagram of light polarisation with Brewster's angle [22].

Brewster's angle is also known as the *polarisation angle*, which is the incident angle at which unpolarised light is seperated into its vertical (perpendicular) and horizontal (parallel) components when that light is transmitted through a medium such that the angle between the reflected and refracted ray is 90°, Brewster's angle (θ_B) [23, 24].

Brewster's angle can be derived from Snell's law [13, 23]:

$$n_1 \sin \theta_i = n_2 \sin \theta_t \qquad \theta_i = \theta_B , \ \theta_i + \theta_t$$
 (4)

$$\implies n_1 \sin \theta_B = n_2 \sin(90^\circ - \theta_B) = n_2 \cos(\theta_B) \tag{5}$$

$$\implies \frac{\sin \theta_B}{\cos \theta_B} = \tan \theta_B = \frac{n_2}{n_1} = n \qquad \therefore n = \tan \theta_B$$
 (6)

This equation (6) can be used to both calculate the polarisation angle (θ_B) or the refractive index (n) of a material, depending on the values previously known.

1.2.4 Ratios of Intensity

By manipulation of Snell's law, equation 3, ratios of the intensities of the reflected to the incident light of the polarised light can be found [13]:

$$R_{parallel} = \frac{\tan^2(\theta_i - \theta_t)}{\tan^2(\theta_i + \theta_t)}$$
 (7)
$$R_{perpendicular} = \frac{\sin^2(\theta_i - \theta_t)}{\sin^2(\theta_i + \theta_t)}$$
 (8)

This is such that if R = 0, light is fully transmitted through the medium (no reflection), and if R = 1, all the light is reflected (no polarisation) [13].

2 Methodology

2.1 Determining the Focal Length

A similar equipment setup to the one used for this section of the experiment is shown in figure 6 below:



Figure 6: Experiment setup to determine the focal point of a convex lens [25].

2.1.1 Convex Lens Method

The apparatus was setup as in $\S 2.1$ with a convex lens in the holder. The image drawn in front of the light was a cross rather than the car shown in the figure. The light source was placed first 50cm away from the lens and the screen was adjusted until the image shown was at its sharpest. Five measurements at different \mathbf{u} and \mathbf{v} were taken and inserted into the table in $\S 3.1.1$.

For each pair of measurements the focal length was then calculated using equation 1 in §1.1.1 and added to the table. The mean of the focal lengths provided the rough estimate of the true focal length for the convex lens and the uncertainty on it.

2.1.2 Concave Lens Method

A similar method is used as for the convex lens (§2.1.1) with the addition of a concave lens placed behind the convex lens. Since light diverges when travelling through a concave lens and only forms a virtual image, a convex lens is needed in front of it to correct the light direction for a real image to be formed, which is measurable, as discussed in §1.1.2.

The procedure then follows the same as before, first the light source is placed 50cm away from the source and the screen is adjusted until the sharpest image forms. Five measurements are taken and a table similar to the one is §3.1.1 is made.

To calculate the focal length of the *concave* lens, equation 2 must be adjusted:

$$\frac{1}{f_{concave}} = \frac{1}{f} - \frac{1}{f_{convex}} \tag{9}$$

Since f_{convex} was calculated in §2.1.1 and f is what is found (through equation 1) by doing the above procedure, the individual focal length of the concave lens can be found through subtraction.

2.2 Determining Brewster's Angle Method

The apparatus is first setup in a similar fashion as to what is shown below in figure 7:



Figure 7: Experiment setup to determing Brewster's angle [26].

The two arms, one holding the light source (laser) and the other holding the photoresistor, are free to move around the table which holds the lens with the polaroid filter set in front of the laser light source. A multimeter was connected to the photoresistor and set to read up to 200mV. The arm holding the photoresistor is adjusted such that it is in the position to be able to read the **reflected** light, not the transmitted light.

Once the plane of incidence is found the polaroid, and thus the plane of polarisation, is adjusted such that it is perpendicular to the plane of incidence. The angle of incidence is varied and read from the table, and the intensity of the reflected light is measured, with each value being recorded in a table. This procedure is repeated for the polaroid perpendicular and parallel to the plane of incidence.

Equation 6 can then be used to calculate the refractive index of the lens material when the value for Brewster's angle is found.

3 Results and Calculations

3.1 Determining the Focal Length

3.1.1 Convex Lens

The values gathered for the convex lens are represented in the table, table 4, below:

u (cm)	$\Delta u \text{ (cm)}$	v (cm)	$\Delta v \text{ (cm)}$	f (cm)
60	± 0.05	12.7	± 0.05	10.48
50	± 0.05	13.4	± 0.05	10.57
40	± 0.05	12.1	± 0.05	9.29
30	± 0.05	15.3	± 0.05	10.13
20	± 0.05	21.6	± 0.05	10.38

Table 3: Table of the values gathered for the convex lens, with the focal length calculated using equation 1.

The average of the focal lengths for the convex lens with the standard deviation uncertainty is found to be:

$$10.17 \pm 0.464 \,\mathrm{cm}$$

The inverse of \mathbf{u} , the object-lens distance, and the inverse of \mathbf{v} , the screen-lens distance, were then plotted against each other in figure 8 where the relationship between both values can be seen.

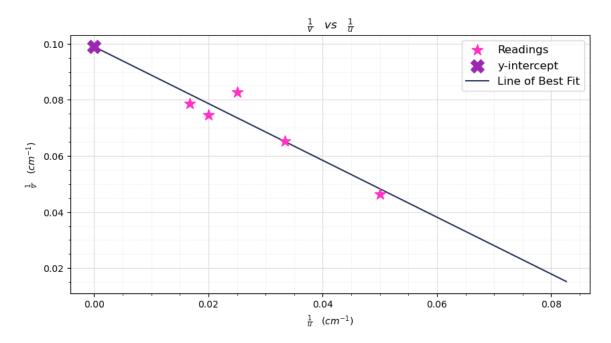


Figure 8: Graph of $\frac{1}{v}$ vs $\frac{1}{u}$ with y-intercept marked.

The value of the slope of the line of best fit is calculated to be -1.013 and the y-intercept to be 0.0989. Therefore to be able to compute best value of the focal length from the graph the mean of the x- and y-intercepts are found:

$$0 = mx + c \implies x = \frac{-b}{m} = \frac{-0.0989}{-1.013} = 0.0976$$

Thus the mean focal length from the graph can be calculated,

$$<\frac{1}{f}> = \frac{0.0976 + 0.0989}{2} = 0.09825 \,\mathrm{cm}^{-1}$$

So therefore the average value of the focal length and its uncertainty as per the graph would be $10.178 \pm 3.24 \times 10^{-4}$ cm⁻¹.

3.1.2 Concave Lense

The values gathered for the combined lenses are represented in the table, table 4, below:

u (cm)	$\Delta u \text{ (cm)}$	v (cm)	$\Delta v \text{ (cm)}$	f (cm)
60	± 0.05	17.2	± 0.05	13.37
50	± 0.05	18.4	± 0.05	13.45
40	± 0.05	20.2	± 0.05	13.42
30	± 0.05	25.9	± 0.05	13.90
20	± 0.05	48.7	± 0.05	14.18

Table 4: Table of the values gathered for the concave + convex lens, with the focal length calculated using equation 1.

3.2 Determining Brewster's Angle

4 Conclusion

5 Applications of Lenses

- 5.1 Eyeglasses
- 5.2 Microscopes
- 5.3 Telescopes

References

- [1] A. Tikkanen. (2025, January) lens. [Accessed 9 January 2025]. [Online]. Available: https://www.britannica.com/technology/lens-optics/Manufacturing-optical-lenses
- [2] N. Khan. (n.d.) Types of Lenses in Physics. [Accessed 9 February 2025]. [Online]. Available: https://www.vedantu.com/evs/types-of-lenses-in-physics
- [3] Anon. (2024, July) Concave lens. [Accessed 9 February 2025]. [Online]. Available: https://www.geeksforgeeks.org/concave-lens/
- [4] —. (2024, July) Convex lens. [Accessed 9 February 2025]. [Online]. Available: https://www.geeksforgeeks.org/convex-lens/
- [5] M. Fuchs and В. Chesnutt. (2023,November) Convex Lens. Accessed February 2025]. [Online]. Available: https://study.com/academy/lesson/ convex-lens-definition-equation-examples.html
- [6] Anon. (n.d.) What is a Convex Lens? [Accessed 9 February 2025]. [Online]. Available: https://www.shanghai-optics.com/about-us/resources/technical-articles/what-is-a-convex-lens/
- [7] —. (n.d.) Convex lens. [Accessed 9 February 2025]. [Online]. Available: https://g.co/kgs/dNsvwpT
- [8] R. Enrera and J. Corbat. (2023, November) Concave Lens. [Accessed 9 February 2025]. [Online]. Available: https://study.com/academy/lesson/concave-lens-definition-uses.html
- [9] Anon. (n.d.) Concave lens. [Accessed 9 February 2025]. [Online]. Available: https://g.co/kgs/ES3287p
- [10] A. Nicholson and A. Summersby. (n.d.) Understanding focal length in photography. [Accessed 9 February 2025]. [Online]. Available: https://www.canon.ie/pro/infobank/understanding-focal-length/
- [11] R. Ν. Milelr. Enrera and (2023,November) Focal Length. Accessed February 2025]. [Online]. Available: https://study.com/academy/lesson/ focal-length-definition-equation-examples.html
- [12] Anon. (n.d.) Lenses. [Accessed 9 February 2025]. [Online]. Available: https://isaacphysics.org/concepts/cp_lenses
- [13] UCD. Measurement Focal Lengths of (2025)of the Lenses and Determination of Brewster's Angle. Accessed 9 February 2025]. [Online]. Available: https://brightspace.ucd.ie/content/enforced/299908-PHYC20080-2024-SPR/ phyc20080_Lenses_Spring%202025.pdf
- [14] Anon. (2024, April) Difference between Real and Virtual Images. [Accessed 9 February 2025]. [Online]. Available: https://www.geeksforgeeks.org/difference-between-real-image-and-virtual-image/?ref=header_search
- [15] —. (n.d.) Images Formed by Lenses. [Accessed 9 February 2025]. [Online]. Available: https://www.toppr.com/guides/science/light/images-formed-by-lenses/
- [16] —. (n.d.) Polarisation. [Accessed 9 February 2025]. [Online]. Available: https://isaacphysics.org/concepts/cp_polarisation

- [17] E. Gregersen. (2025, January) polarization. [Accessed 9 February 2025]. [Online]. Available: https://www.britannica.com/science/polarization-physics
- [18] Anon. (n.d.) Reflection, Refraction, and Dispersion. [Accessed 9 February 2025]. [Online]. Available: https://phys.libretexts.org/Bookshelves/University_Physics/Physics_(Boundless)/24%3A_Geometric_Optics/24.2%3A_Reflection_Refraction_and_Dispersion
- [19] G. Stark. (2025, February) Reflection and Refraction. [Accessed 9 February 2025]. [Online]. Available: https://www.britannica.com/science/light/Reflection-and-refraction
- [20] Anon. (n.d.) Snell's Law. [Accessed 9 February 2025]. [Online]. Available: https://eng.libretexts.org/Bookshelves/Materials_Science/Supplemental_Modules_(Materials_Science)/Optical_Properties/Snell%27s_Law
- [21] —. (2024, June) Polarization of Light. [Accessed 9 February 2025]. [Online]. Available: https://www.geeksforgeeks.org/polarization-of-light/
- [22] S. J. Ling, J. Sanny, and W. Moebbs. (n.d.) Polarization. [Accessed 9 February 2025]. [Online]. Available: https://pressbooks.online.ucf.edu/osuniversityphysics3/chapter/polarization/
- [23] W. Emery and A. Camps, "Chapter 2 Basic Electromagnetic Concepts and Applications to Optical Sensors," in *Introduction to Satellite Remote Sensing*, W. Emery and A. Camps, Eds. Elsevier, 2017, pp. 43–83. [Online]. Available: https://www.sciencedirect.com/science/article/pii/B9780128092545000026
- [24] Anon. (n.d.) Brewster's angle. [Accessed 9 February 2025]. [Online]. Available: http://physics.bu.edu/~duffy/semester2/c27_brewster.html
- [25] -Determining (n.d.) the focal point a convex lens. Accessed 9 February 2025]. [Online]. https://www.leybold-shop.com/physics/demonstration-experiments-physics/ optics/formation-of-images-by-lenses-and-mirrors.html
- [26] —. (n.d.) Brewster's angle apparatus. [Accessed 9 February 2025]. [Online]. Available: https://www.holmarc.com/brewster_angle.php

Appendix

List of Figures

1	Diagram of converging (convex) and diverging (concave) lenses [1].	
	(a): biconvex, (b): plano-convex, (c): positive meniscus; (d): biconcave, (e): plano-concave, (f): negative	
	meniscus	2
2	Ray diagram of the cases of convex lens image formation [15]	4
3	Ray diagram of concave lens image formation [15]	4
4	Visual representation of polarisation of light [17]	5
5	Diagram of light polarisation with Brewster's angle [22]	6
6	Experiment setup to determine the focal point of a convex lens [25]	7
7	Experiment setup to determing Brewster's angle [26]	8
8	Graph of $\frac{1}{v}$ vs $\frac{1}{u}$ with y-intercept marked	9
List	of Tables	
1	Table of the different cases of convex lens image formation [4, 15]	4
2	Table of the different cases of concave lens image formation [3, 15]	4
3	Table of the values gathered for the convex lens, with the focal length calculated	
	using equation 1	9
4	Table of the values gathered for the concave + convex lens, with the focal length	
	calculated using equation 1	10
	<u> </u>	

Raw Data

\mathbf{Code}