

11_1 Recursion Basics

Recursive void Methods

- A recursive method
 - A method that includes a call to itself
 - Problem solving technique of breaking down a task into subtasks
 - Used when a subtask is a smaller version of the original task

Example: Vertical Numbers

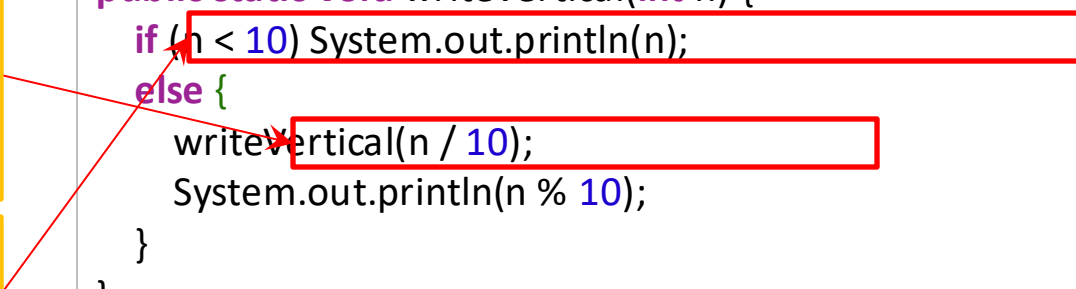
```
public class VerticalNumbersRecursion {  
    public static void main(String[] args) {  
        System.out.println("writeVertical(3):");  
        writeVertical(3);  
        System.out.println("writeVertical(12):");  
        writeVertical(12);  
        System.out.println("writeVertical(123):");  
        writeVertical(123);  
    }  
    public static void writeVertical(int n) {  
        if (n < 10) System.out.println(n);  
        else { // n is two or more digits long  
            writeVertical(n / 10);  
            System.out.println(n % 10);  
        }  
    }  
}
```

```
writeVertical(3):  
3  
writeVertical(12):  
1  
2  
writeVertical(123):  
1  
2  
3
```

Subtasks

- Subtasks
 - Subtask 1: Recursive case
 - Smaller version of the original task
 - Implemented with a recursive call
 - Subtask 2: Stopping case
 - The simple case

```
public static void writeVertical(int n) {  
    if (n < 10) System.out.println(n);  
    else {  
        writeVertical(n / 10);  
        System.out.println(n % 10);  
    }  
}
```



Tracing a Recursive Call

```
writeVertical(123);  
    writeVertical(12);    // writeVertical(123/10);  
        writeVertical(1); // writeVertical(12/10); stopping case  
            System.out.println(1); // print(1)  
        System.out.println(2);    // n % 10 = 12 % 10 = 2, print(2)  
    System.out.println(3);    // n % 10 = 123 % 10 = 3, print(3)
```

Infinite Recursion

- An alternative version of `writeVertical`
 - Note: No stopping (simple) case!

```
public static void newWriteVertical(int n)
{
    newWriteVertical(n/10);
    System.out.println(n%10);
}
```

```
newWriteVertical(123);
    newWriteVertical(12); // newWriteVertical(123/10);
        newWriteVertical(1); // newWriteVertical(12/10);
            newWriteVertical(0); // newWriteVertical(1/10);
                newWriteVertical(0); // newWriteVertical(0/10);
                    ...
```

Stacks for Recursion (1/2)

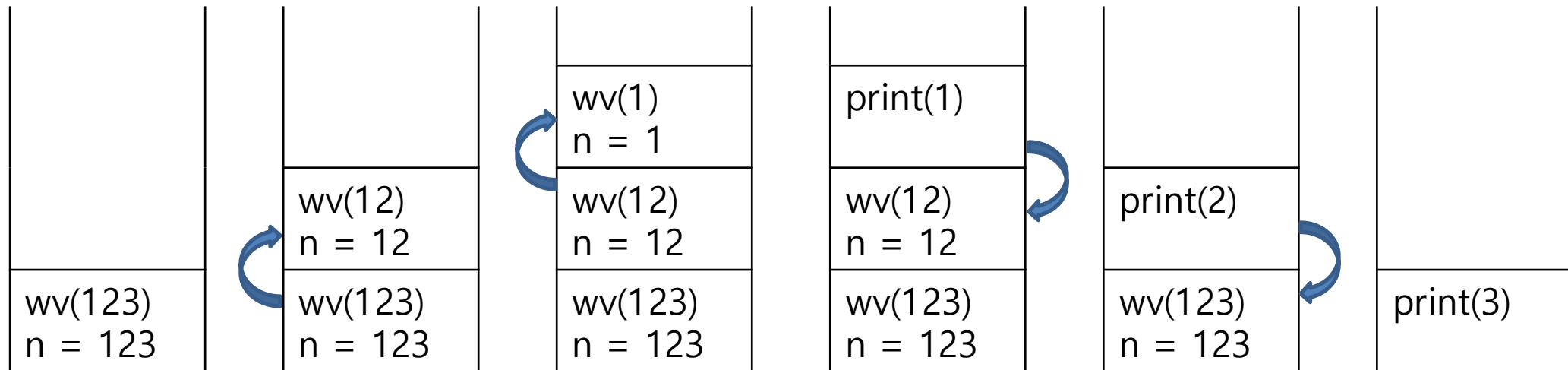
- To keep track of recursion
 - Most computer systems use a stack
 - Stack
 - Specialized kind of data structure
 - Analogous to a stack of paper
 - New paper is placed on top of the stack
 - A paper on the top removed first
 - LIFO: Last In First Out



Stacks for Recursion (2/2)

```
public static void wv(int n) {  
    if (n < 10) {  
        print(n);  
    }  
    else {  
        wv(n / 10);  
        print(n % 10);  
    }  
}
```

Stack of the activation records of called methods



Recursion Versus Iteration

- Recursion is not absolutely necessary
 - Any task using recursion can also be done in a non-recursive manner
 - A non-recursive version of a method is called an **iterative** version
- A recursive version
 - simpler, but usually run slower than iterative version
 - spend more storage than iterative version

Iterative version of writeVertical

```
public static void writeVertical(int n) {  
    int nsTens = 1;  
    int left = n;  
    while (left > 9) {  
        left = left / 10;  
        nsTens = nsTens * 10;  
    }  
  
    // nsTens: power of 10 having the same number  
    // of digits as n. ex) if n=2345, nsTen=1000.  
  
    for (int pt = nsTens; pt > 0; pt = pt/10) {  
        System.out.println(n/pt);  
        n = n % pt;  
    }  
}
```

left	nsTens
2345	1
234	10
23	100
2	1000

pt	n	print
1000	2345	2
100	345	3
10	45	4
1	5	5