

Homework is prepared by: Ilya Kopyl  
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**1. Using BNF write the syntax definitions of the following objects:**

a) Natural number (1, 2, 3, ...). The answer:

$$\begin{aligned} \langle \textit{natural number} \rangle &::= \langle \textit{non-zero digit} \rangle \mid \langle \textit{natural number} \rangle \langle \textit{digit} \rangle \\ \langle \textit{digit} \rangle &::= 0 \mid \langle \textit{non-zero digit} \rangle \\ \langle \textit{non-zero digit} \rangle &::= 1 \mid 2 \mid 3 \mid 4 \mid 5 \mid 6 \mid 7 \mid 8 \mid 9 \end{aligned}$$

b) Unsigned integer (0, 1, 2, 3, ...). The answer:

$$\begin{aligned} \langle \textit{unsigned integer} \rangle &::= 0 \mid \langle \textit{non-zero digit} \rangle \langle \textit{digits} \rangle \\ \langle \textit{digits} \rangle &::= \langle \textit{digit} \rangle \mid \langle \textit{digits} \rangle \langle \textit{digit} \rangle \\ \langle \textit{digit} \rangle &::= 0 \mid \langle \textit{non-zero digit} \rangle \\ \langle \textit{non-zero digit} \rangle &::= 1 \mid 2 \mid 3 \mid 4 \mid 5 \mid 6 \mid 7 \mid 8 \mid 9 \end{aligned}$$

c) Integer (... , -2, -1, 0, 1, 2, ...). The answer:

$$\begin{aligned} \langle \textit{integer} \rangle &::= \langle \textit{sign} \rangle \langle \textit{unsigned integer} \rangle \\ \langle \textit{sign} \rangle &::= + \mid - \mid \langle \textit{empty} \rangle \\ \langle \textit{empty} \rangle &::= \\ \langle \textit{unsigned integer} \rangle &::= 0 \mid \langle \textit{non-zero digit} \rangle \langle \textit{digit} \rangle \\ \langle \textit{digits} \rangle &::= \langle \textit{digit} \rangle \mid \langle \textit{digits} \rangle \langle \textit{digit} \rangle \\ \langle \textit{digit} \rangle &::= 0 \mid \langle \textit{non-zero digit} \rangle \\ \langle \textit{non-zero digit} \rangle &::= 1 \mid 2 \mid 3 \mid 4 \mid 5 \mid 6 \mid 7 \mid 8 \mid 9 \end{aligned}$$

d) Odd number (... , -3, -1, 1, 3, ...). The answer:

$$\begin{aligned} \langle \textit{add number} \rangle &::= \langle \textit{sign} \rangle \langle \textit{unsigned odd num} \rangle \\ \langle \textit{sign} \rangle &::= + \mid - \mid \langle \textit{empty} \rangle \\ \langle \textit{empty} \rangle &::= \\ \langle \textit{unsigned odd num} \rangle &::= \langle \textit{odd digit} \rangle \mid \langle \textit{number} \rangle \langle \textit{unsigned odd num} \rangle \\ \langle \textit{number} \rangle &::= \langle \textit{non-zero digit} \rangle \mid \langle \textit{number} \rangle \langle \textit{digit} \rangle \\ \langle \textit{digit} \rangle &::= 0 \mid \langle \textit{non-zero digit} \rangle \\ \langle \textit{non-zero digit} \rangle &::= 2 \mid 4 \mid 6 \mid 8 \mid \langle \textit{odd digit} \rangle \\ \langle \textit{odd digit} \rangle &::= 1 \mid 3 \mid 5 \mid 7 \mid 9 \end{aligned}$$