

CSc 600-01 (SECTION 1)
Homework 1 - Syntax
prepared by Ilya Kopyl

CSC 600 HOMEWORK 1 - SYNTAX

February 14, 2018

Homework is prepared by: Ilya Kopyl.

It is formatted in LaTeX, using TeXShop editor (under GNU GPL license).

Syntax diagrams are created in LucidChart online editor (lucidchart.com).

1. Using BNF write the syntax definitions of the following objects:

a) Natural number (1, 2, 3, ...). The answer:

$$\begin{aligned}\langle \textit{natural number} \rangle &::= \langle \textit{non-zero digit} \rangle \mid \langle \textit{natural number} \rangle \langle \textit{digit} \rangle \\ \langle \textit{digit} \rangle &::= 0 \mid \langle \textit{non-zero digit} \rangle \\ \langle \textit{non-zero digit} \rangle &::= 1 \mid 2 \mid 3 \mid 4 \mid 5 \mid 6 \mid 7 \mid 8 \mid 9\end{aligned}$$

b) Unsigned integer (0, 1, 2, 3, ...). The answer:

$$\begin{aligned}\langle \textit{unsigned integer} \rangle &::= \langle \textit{digits} \rangle \\ \langle \textit{digits} \rangle &::= \langle \textit{digit} \rangle \mid \langle \textit{digits} \rangle \langle \textit{digit} \rangle \\ \langle \textit{digit} \rangle &::= 0 \mid \langle \textit{non-zero digit} \rangle \\ \langle \textit{non-zero digit} \rangle &::= 1 \mid 2 \mid 3 \mid 4 \mid 5 \mid 6 \mid 7 \mid 8 \mid 9\end{aligned}$$

The BNF definition of unsigned integer in languages that do not support leading zeroes (e.g. Python):

$$\begin{aligned}\langle \textit{unsigned integer} \rangle &::= 0 \mid \langle \textit{natural number} \rangle \\ \langle \textit{natural number} \rangle &::= \langle \textit{non-zero digit} \rangle \mid \langle \textit{natural number} \rangle \langle \textit{digit} \rangle \\ \langle \textit{digit} \rangle &::= 0 \mid \langle \textit{non-zero digit} \rangle \\ \langle \textit{non-zero digit} \rangle &::= 1 \mid 2 \mid 3 \mid 4 \mid 5 \mid 6 \mid 7 \mid 8 \mid 9\end{aligned}$$

c) Integer (... , -2, -1, 0, 1, 2, ...). The answer:

$\langle integer \rangle$	$::= \langle sign \rangle \langle unsigned integer \rangle$
$\langle sign \rangle$	$::= + \mid - \mid \langle empty \rangle$
$\langle empty \rangle$	$::=$
$\langle unsigned integer \rangle$	$::= 0 \mid \langle natural number \rangle$
$\langle natural number \rangle$	$::= \langle non-zero digit \rangle \mid \langle natural number \rangle \langle digit \rangle$
$\langle digit \rangle$	$::= 0 \mid \langle non-zero digit \rangle$
$\langle non-zero digit \rangle$	$::= 1 \mid 2 \mid 3 \mid 4 \mid 5 \mid 6 \mid 7 \mid 8 \mid 9$

d) Odd number (... , -3, -1, 1, 3, ..., 101, ..., 2047, ...). The answer:

$\langle odd number \rangle$	$::= \langle sign \rangle \langle unsigned odd number \rangle$
$\langle sign \rangle$	$::= + \mid - \mid \langle empty \rangle$
$\langle empty \rangle$	$::=$
$\langle unsigned odd number \rangle$	$::= \langle odd digit \rangle \mid \langle natural number \rangle \langle odd digit \rangle$
$\langle natural number \rangle$	$::= \langle non-zero digit \rangle \mid \langle natural number \rangle \langle digit \rangle$
$\langle digit \rangle$	$::= 0 \mid \langle non-zero digit \rangle$
$\langle non-zero digit \rangle$	$::= 2 \mid 4 \mid 6 \mid 8 \mid \langle odd digit \rangle$
$\langle odd digit \rangle$	$::= 1 \mid 3 \mid 5 \mid 7 \mid 9$

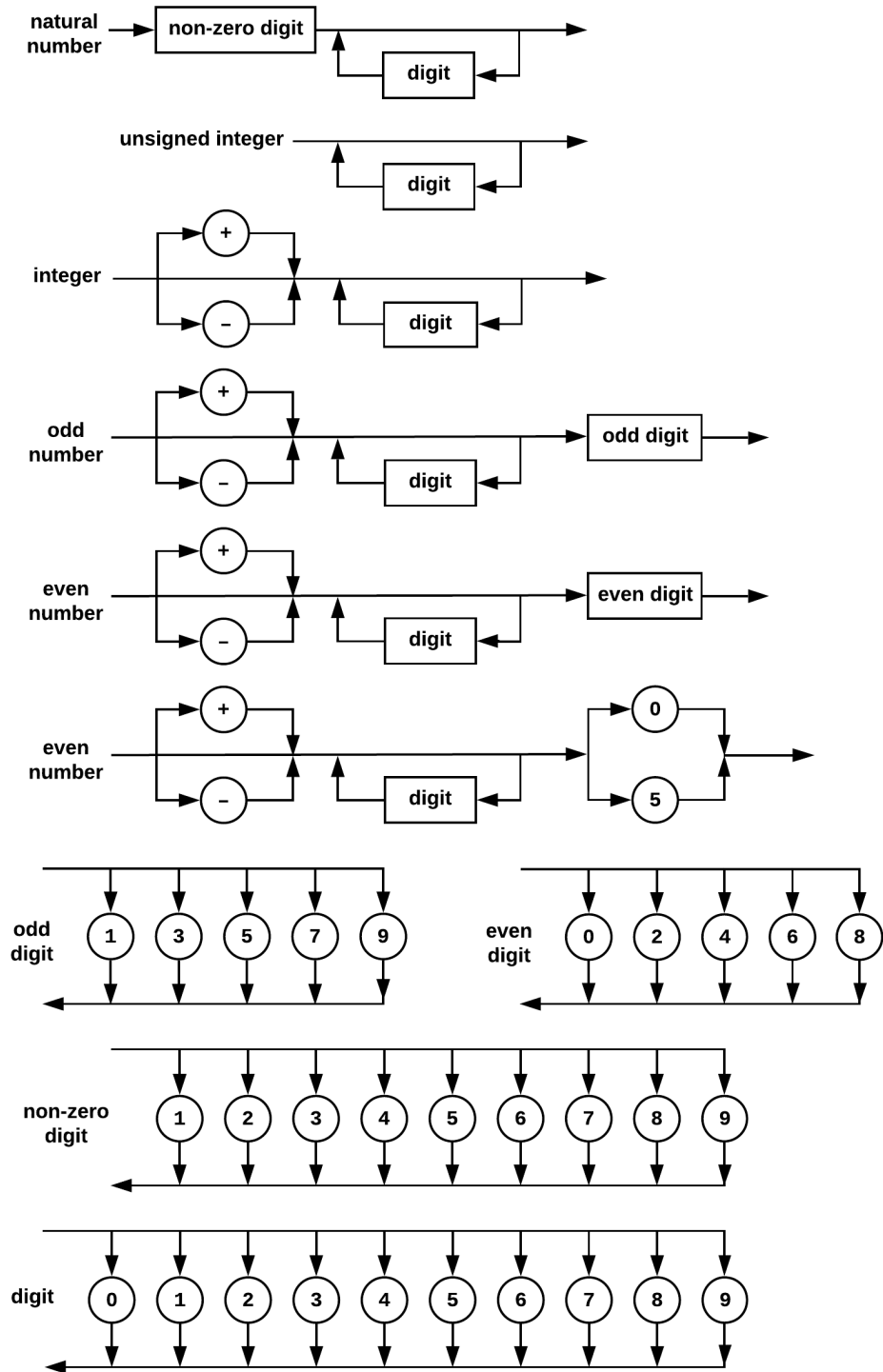
e) Even number (... , -4, -2, 0, 2, 4, ..., 332, ..., 1022, ...). The answer:

$\langle even number \rangle$	$::= \langle sign \rangle \langle unsigned even number \rangle$
$\langle sign \rangle$	$::= + \mid - \mid \langle empty \rangle$
$\langle empty \rangle$	$::=$
$\langle unsigned even number \rangle$	$::= \langle even digit \rangle \mid \langle natural number \rangle \langle even digit \rangle$
$\langle natural number \rangle$	$::= \langle non-zero digit \rangle \mid \langle natural number \rangle \langle digit \rangle$
$\langle digit \rangle$	$::= 0 \mid \langle non-zero digit \rangle$
$\langle non-zero digit \rangle$	$::= 1 \mid 2 \mid 3 \mid 4 \mid 5 \mid 6 \mid 7 \mid 8 \mid 9$
$\langle even digit \rangle$	$::= 0 \mid 2 \mid 4 \mid 6 \mid 8$

f) Integer divisible by five (... , -10, 5, 0, 5, 10, ...). The answer:

$\langle \text{integer div-by-5} \rangle$	$::= \langle \text{sign} \rangle \langle \text{unsigned int div-by-5} \rangle$
$\langle \text{sign} \rangle$	$::= + \mid - \mid \langle \text{empty} \rangle$
$\langle \text{empty} \rangle$	$::=$
$\langle \text{unsigned int div-by-5} \rangle$	$::= \langle \text{div-by-5 suffix} \rangle \mid \langle \text{natural number} \rangle \langle \text{div-by-5 suffix} \rangle$
$\langle \text{natural number} \rangle$	$::= \langle \text{non-zero digit} \rangle \mid \langle \text{natural number} \rangle \langle \text{digit} \rangle$
$\langle \text{div-by-5 suffix} \rangle$	$::= 0 \mid 5$
$\langle \text{digit} \rangle$	$::= 0 \mid \langle \text{non-zero digit} \rangle$
$\langle \text{non-zero digit} \rangle$	$::= 1 \mid 2 \mid 3 \mid 4 \mid 5 \mid 6 \mid 7 \mid 8 \mid 9$

2. Show syntax diagrams for questions (a), ..., (f) of problem 1.



Example of syntax diagrams for integers with no support of leading zeroes.

