



Indoor Air Quality (IAQ) modelling, application to COVID-19 transmission

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From June 7th 2021 to July 30th 2021

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Introduction

- ▶ The air quality within and around buildings.
- ▶ Responsible for 1.5 million to 2 million deaths in 2000.



Indoor air quality facts¹

- ▶ COVID-19 consequences.

1. <https://www.pinterest.fr/pin/534661787013453107/>

- ▶ Cemosis : Strasbourg Center for Modelling and Simulation .
- ▶ Cemosis² created in January 2013 by Christophe Prud'homme.
- ▶ Cemosis and Synapse-Concept project 4fastsim-ibat³.
- ▶ Reduce and control energy consumption in buildings.
- ▶ Air quality of indoor spaces and its consequences⁴.

2. <https://www.cemosis.fr/>

3. <https://www.cemosis.fr/projects/4fastsim-ibat/>

4. <http://agrohome.com.br/wp-content/uploads/2020/12/DINAMARCA-Produtividade.pdf>

Objectives

- ▶ Proceed the model of the airborne transmission of COVID-19.
- ▶ Modelling indoor air quality (IAQ) applied to COVID-19's transmission .
- ▶ Couple the IAQ model with the zero-equation turbulence model.

I. Indoor Air Quality (IAQ)



Indoor air quality⁵

5. <https://catalysts.basf.com/products-and-industries/indoor-air-quality>

Different pollutants

- ▶ Principal pollutants of indoor air :
 - Chemical pollutants : volatile organic compounds (VOCs), nitrogen oxides (NO_x), carbon monoxide (CO)...
 - Biological contaminants : moulds, pets , pollens ...
 - Particles and fibers : asbestos, artificial mineral fibers...
- ▶ Main sources of residential buildings :
 - Mold,
 - Tobacco smoke,
 - Household Products,
 - Carpet,
 - Pet Dander...

Effects of nefarious IAQ

- ▶ Major effects on comfort and health,
- ▶ Simple discomforts :
 - drowsiness
 - eye and skin irritation
 - lost productivity at work.
- ▶ Severe pathologies :
 - respiratory allergies,
 - asthma,
 - cancer,
 - poisoning...
- ▶ Sick Building Syndrome (SBS).
- ▶ Causes and solutions.

Recommendations to enhance IAQ

- ▶ Indoor Air Quality top 5 most urgent environmental risks to public health.
- ▶ Major recommendations :
 - eliminate individual sources of pollution or to reduce their emissions.
 - increase the amount of outdoor air coming indoors.
 - air cleaners collecting pollutants from indoor air.

Modeling IAQ

- ▶ Three principal categories of models.
- ▶ Statistical :
 - estimate the distribution of indoor pollutant exposures,
 - using Monte Carlo techniques to combine the databases.
- ▶ Mass balance :
 - estimate the impacts of sources, sinks and IAQ control options on pollutant concentrations.
- ▶ Computational fluid dynamics (CFD) :
 - room air movement and contaminant transport application.
 - incompressible, inviscid, irrotational fluid.

ARD Equation

- ▶ The **advection**–**reaction**–**diffusion** equation :

$$\frac{\partial C}{\partial t} = \nabla \cdot (K \nabla C) - \nabla \cdot (\vec{v} C) + S.$$

- ▶ C = concentration of airborne infectious particles (*particles/m²*)
 t = time(s)
 ∇ = two-dimensional gradient operator
 K = isotropic eddy diffusion coefficient (turbulent diffusion)
 \vec{v} = advection velocity of the air(*m.s⁻¹*)
 S = sum of sources and sinks of viral particles.

II. COVID-19 transmission

- ▶ The COVID-19 virus since december 2019.
- ▶ Pandemic declared on 11th March 2020.
- ▶ Overs 200 million confirmed cases and 4.36 milion deaths.
- ▶ 81% moderate symptoms, 14% severe and 5% critical symptoms.
- ▶ 4.45 billion vaccine doses administered.

Transmission's modes

Coronavirus COVID-19

Transmission and infection

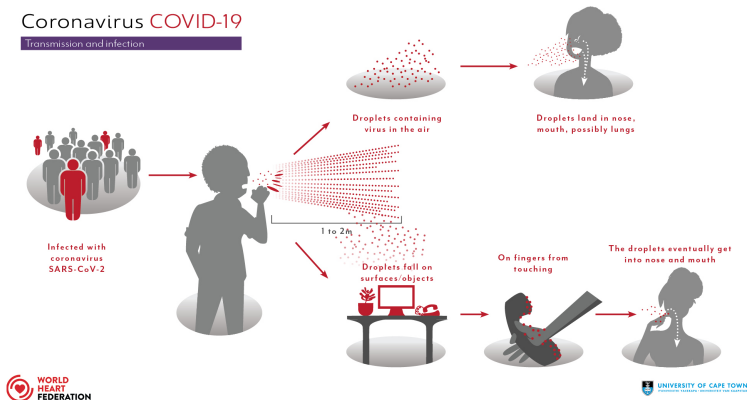


Figure – Transmission and the infection of COVID-19.

Focus on models

- ▶ Data-driven models.
- ▶ Exemple of Italy.
- ▶ Importance of strong social-distancing strategies.

Our model

- ▶ Based on ADR equation.
- ▶ An infectious person talking or breathing with or without a mask S_{inf} .
- ▶ The room contains an air-conditioning unit.
- ▶ The airborne particles transported by advection caused by the airflow.
- ▶ The infectious particles are removed due to three factors :
 - the ventilation system (S_{vent}), - biological deactivation of the virus (S_{deact}),
 - gravitational settling of the virus (S_{set}).

$$\frac{\partial C}{\partial t} + \nabla \cdot (\vec{v}C) - \nabla \cdot (K \nabla C) = S_{inf} - S_{vent} - S_{deact} - S_{set}$$

- ▶ The eddy diffusion coefficient $K(m^2/s)$:

$$K = c_v Q (2c_\epsilon V N^2)^{1/3}$$

Modelling environment and tools

- ▶ Using Feel++ finite library.
- ▶ Coefficient Form PDEs described by⁷

$$d \frac{\partial u}{\partial t} + \nabla \cdot (-c \nabla u - \alpha u + \gamma) + \beta \cdot \nabla u + a u = f \quad \text{in } \Omega$$

- ▶ d : damping or mass coefficient
- ▶ c : diffusion coefficient
- ▶ α : conservative flux convection coefficient
- ▶ γ : conservative flux source term
- ▶ β : convection coefficient
- ▶ a : absorption or reaction coefficient
- ▶ f : source term

7. <https://docs.feelpp.org/toolboxes/0.109/cfpdes/introduction.html>

Application

Assumptions :

- ▶ the advection–diffusion–reaction equation governs the concentration of the virus.
- ▶ particles released with zero initial velocity.
- ▶ only one infectious person in the room.

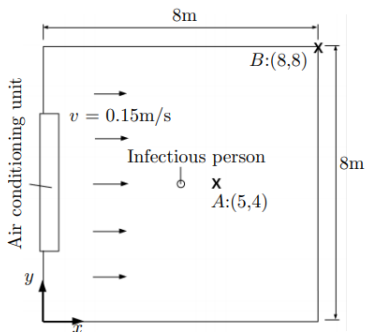
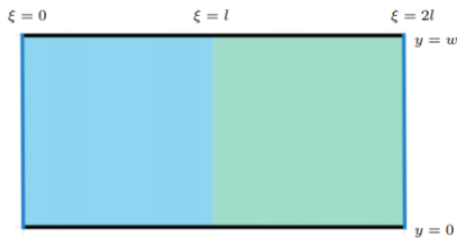


Figure – Schematic of the modelled room. One infectious person is located at the centre of the room.

Application(follow-up)

- Unwrapping the loop surface of the airflow to the two-dimensional domain $(\xi, y) \in [0, 2l] \times [0, w]$.



- Boundary conditions :
 - $C(0, y, t) = C(2l, y, t)$ at the wall $\xi = 0$.
 - $\frac{\partial C}{\partial \xi}(0, y, t) = \frac{\partial C}{\partial \xi}(2l, y, t)$ at $\xi = 2l$.
 - $\frac{\partial C}{\partial y}(\xi, 0, t) = \frac{\partial C}{\partial y}(\xi, w, t) = 0$ at $y = 0, w$.

References

- ▶ Coronavirus disease(COVID-19)
update[https://www.who.int/bangladesh/emergencies/coronavirus-disease-\(covid-19\)-update](https://www.who.int/bangladesh/emergencies/coronavirus-disease-(covid-19)-update)
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- ▶ Z. Lau, K. Kaouri, I. Griffiths. Modelling Airborne Transmission of COVID-19 in Indoor Spaces Using an Advection–Diffusion–Reaction Equation. School of Mathematics, Cardiff University and Mathematical Institute, University of Oxford.
- ▶ B. Zhao and X. Li. A simplified system for indoor airflow simulation. Building and Environment © April 2003
- ▶ Zohra Djatouti, Christophe Prud'homme, Vincent Chabannes, Romain Hild, 4FastSim-IBat
- ▶ https://twitter.com/T_Fiolet/status/1378989583682179075?s=09