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Sec : 08

1) For person,

velocity of the person  $V_p = u_0 + gt = 0 + (-9.8)0.5$   
 $= -4.9 \text{ ms}^{-1} \hat{j}$

Displacement of the person  $y'_p = -\frac{1}{2}gt^2$   
 $= -1.225 \text{ m} \hat{j}$

$\therefore$  Displacement from the axis (as it is measured from the ground) so  $y_p = h - |y'_p|$   
 $= (11.5 - 1.225) \hat{j}$   
 $= 10.275 \hat{j}$

For the ball,

Velocity of the ball  $V_B = u - gt = (9.8 - 4.9) \text{ m/s} = 4.9 \text{ m/s}$

Displacement of the ball  $y_B = ut - \frac{1}{2}gt^2$   
 $= 10 \times 1 - \frac{1}{2} \times 9.8 \times 1^2$   
 $= 3.675 \text{ m}$

Both of the person got some displacement

towards  $x \rightarrow$  axis

Displacement of the person from  $x$ -axis  
 $x_p = 5 \text{ m}$

Displacement of the Ball from  $x$ -axis  
 $x_B = 20 \text{ m}$

Position of the center of mass

$$r_{cm} = \frac{m_p (x_p \hat{i} + y_p \hat{j}) + m_B (x_B \hat{i} + y_B \hat{j})}{m_p + m_B}$$

$$r_{cm} =$$

$$= \frac{60 (5 \hat{i} + 10.275 \hat{j}) + 0.2 (20 \hat{i} + 3.675 \hat{j})}{60 + 0.2}$$

$$= 5.03 \hat{i} + 10.25 \hat{j}$$

Velocity of the center of mass,

$$v_{cm} = \frac{m_p (v_p \hat{j}) + m_B (v_B \hat{j})}{m_p + m_B}$$

$$= \frac{60 (-4.9 \hat{j}) + 0.2 (4.9 \hat{j})}{60 + 0.2}$$

$$= -4.87 \text{ m s}^{-1} \hat{j}$$

b) ~~Let~~ Final velocity of the person when he hits the ground

$$V = \sqrt{2gh}$$
$$= \sqrt{2 \times 9.8 \times 10}$$
$$= 14 \text{ ms}^{-1}$$

magnitude of impulse  $J = m \Delta V$

$$= 60 \times 14$$

momentum of person  $= 840 \text{ kg ms}^{-1}$

$$\text{Average force} = m \frac{\Delta V}{\Delta t} = \frac{840}{0.02} = 84000 \text{ kgms}^{-2}$$

Average force acting on the person

is  $84 \times 10^3 \text{ kgms}^{-2}$  (Ans)

$$= 84 \times 10^3 \text{ N (Ans)}$$



From (b) we get  $v = 14 \text{ ms}^{-1}$

we can say in  $0.15 \text{ m}$  the person decelerates to  $0 \text{ ms}^{-1}$

$$\therefore a = \frac{v^2 - u^2}{2s} = \frac{(14)^2 - 0^2}{2 \times 0.15} = 653.33 \text{ ms}^{-2}$$

we know,

$$F = ma$$

in  $0.15 \text{ m}$  the person will be decelerated and the normal force acting on the person

$$\text{will be } F = ma = 60 \times 653.33$$

$$= 39200 \text{ N}$$

As when the person travels ~~for~~ 0.15 m then the gravitational force still acts on that person ~~is~~ along with the deceleration,

$$a = \frac{v^2 - u^2}{2s} = \frac{5^2 - 0}{2 \times 0.15} = \frac{25}{0.3} = 83.33 \text{ m/s}^2$$

So, the normal force will be

$$F_N = mg + F$$

$$= 60 \times 9.8 + 39200 \text{ N}$$

$$= 39788 \text{ N}$$

$$\text{As, } F_N < 50000 \text{ N}$$

His legs can withstand the force and

it will not break his legs.

2) a) Given that,

$$\text{Last velocity } v = \frac{50}{3.6} = 13.89 \text{ m s}^{-1}$$

$$\text{past velocity } v_0 = \frac{90}{3.6} = 25 \text{ m s}^{-1}$$

we know,

$$v = v_0 + at$$

$$\therefore a = \frac{v - v_0}{t} = \frac{13.89 - 25}{15} = -0.74074 \text{ m s}^{-2}$$

$\therefore$  Magnitude of the tangential acceleration

is  $-0.74074 \text{ m s}^{-2}$ .

$\therefore$  Direction of tangential acceleration

is in opposite direction of the velocity of the train,



b) Given,

$$V = \frac{50}{3.6} = 13.89 \text{ ms}^{-1}$$

$$\text{Radius } r = 150 \text{ m}$$

$$\therefore \text{Radial acceleration } a_c = \frac{V^2}{r}$$

$$= \frac{(13.89)^2}{150}$$

$$= 1.286 \text{ ms}^{-2}$$

The magnitude of radial acceleration is  $1.286 \text{ ms}^{-2}$

The direction of radial acceleration is directed towards center.

c) From a, b we get,

tangential acceleration  $a_t = -0.74074 \text{ m s}^{-2}$

radial acceleration  $a_c = 1.286 \text{ m s}^{-2}$

$\therefore$  Magnitude of total acceleration

$$= \sqrt{(a_t)^2 + (a_c)^2}$$

$$= \sqrt{(1.286)^2 + (0.74074)^2}$$

$$= 1.484 \text{ m s}^{-2}$$

Direction of acceleration  $\theta = \tan^{-1} \left( \frac{|a_c|}{|a_t|} \right)$   
 $= \tan^{-1} \left( \frac{1.286}{0.74047} \right)$

$$= 60.067^\circ$$

Magnitude of the acceleration  $1.484 \text{ ms}^{-2}$

Direction of the acceleration ~~from~~  
is  $60.067^\circ$  and it is relative to the  
direction of tangential acceleration.