

# DIGITAL LOGIC DESIGN

CSE - 260

LAB Report - 6

GROUP - 4

## GROUP MEMBERS:

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Name of the experiment: Implementation of  
4 bit magnitude comparator.

Objective:

- ① To get the idea of how comparator works
- ② To gain experience working with comparator
- ③ To <sup>understand</sup> simplify the complexity of comparator

Required components and Equipments:

- |                  |                 |
|------------------|-----------------|
| ① Bread Board    | ⑤ OR (IC-7432)  |
| ② Trainer Board, | ⑥ NOT (IC-7404) |
| ③ Jumper wires   | ⑦ XOR (IC-7486) |
| ④ AND (IC-7408)  |                 |

## Experimental setup:

Let us think of the numbers as,

1st number  $\rightarrow A_3 A_2 A_1 A_0$

2nd number  $\rightarrow B_3 B_2 B_1 B_0$

For  $A=B$  the equations for the magnitude comparator will be,

if  $A_3 = B_3 \therefore K_3 : A_3' B_3' + A_3 B_3$

if  $A_2 = B_2 \therefore K_2 : A_2' B_2' + A_2 B_2$

if  $A_1 = B_1 \therefore K_1 : A_1' B_1' + A_1 B_1$

if  $A_0 = B_0 \therefore K_0 : A_0' B_0' + A_0 B_0$

The final equation  $\therefore K_3 \cdot K_2 \cdot K_1 \cdot K_0$

To do this practically, we need to take a XOR gate and place it on to Bread board.

After that we need connect ground to pin 7,  
Vcc to pin 7 ~~and~~ of the IC. Then, I need  
to connect  $A_3, B_3$  input to the XOR IC's  
pin 1 and pin 2. The out ~~will~~ will be in  
pin 3. We need to place a NOT Gate below  
the XOR IC and connect ~~to~~ GND and Vcc  
as like XOR Gate. We will take input  
~~from~~ from pin 3 of XOR IC and connect  
it with NOT Gate's pin 1. Out-put of  
NOT gate will generate at pin 2. We  
will place an AND Gate in the Breadboard  
and connect Vcc and GND to pin 14, pin  
7 of the IC. After that we will take  
input from pin 2 of NOT Gate and



connect it to pin 1 of AND gate. Furthermore, we will take input  $A_2, B_2$  to pin 4, pin 5 of XOR IC. The output will be generated in pin 6 of XOR IC. This output we will take as an input of pin 3 of Not gate. The output in the Not gate will be generated in pin 4. This output of Not gate will be taken as an input of pin 2 of the AND gate. The output will be generated in pin 3 of AND gate. This pin 3 will be taken as an input in pin 13 of AND gate. After 7. Moreover, we will take  $A_1, B_1$  as the input in XOR gate pin 10, 9. The output will be generated in pin 8.

We will take ~~pin 8~~ connect pin 8 with the

Not gate's pin 5 and the output of

NOT gate will generate in pin 6. We will

take this output and take it as an

input to the AND gates IC pin 9. Lastly

we will take A<sub>0</sub>, B<sub>0</sub> as an input and

connect it to pin 12, 13 of XOR gate IC.

The output of XOR gate will generate

in pin 11 of the XOR gate IC. We will

connect pin 11 of XOR gate with pin 9 of

NOT gate. The Not gate's output

will generate in pin 8. We will take

pin 8's output and connect it

to the pin 10 of AND gate IC. The output will generate in pin 8 of AND gate IC. We will take this output as an input to the pin 12 of the AND gate. By this we will get the final output of equal comparator. ~~If we get 1~~ we will connect this output to the display of trainer board.

## Results and Discussion:

For all 3 of these comparators we need to define  $X_3, X_2, X_1, X_0$ .

Here,

$$X_3 = A_3' B_3' + \cancel{A_3 B_3} A_3 B_3$$

$$X_2 = A_2' B_2' + A_2 B_2$$

$$X_1 = A_1' B_1' + A_1 B_1$$

$$X_0 = A_0' B_0' + A_0 B_0$$

Here,  $A_3, A_2, A_1, A_0$  are the digits of a binary number  $A$ . same goes for  $B_3, B_2, B_1, B_0$ . If 1011 is a binary

number then  $A_3=1, A_2=0, A_1=1, A_0=1$

Moreover, for  $X_3$  will provide 1 if

both  $A_3$  and  $B_3$  are equal. If both

are not equal  $X_3$  will provide 0 in

the output. ~~so~~



① Comparator for  $A=B$

As we want to make a 4 bit comparator where it will show 1 if both of number  $A=B$  and give output 0 if  $A \neq B$ .

$A_3, A_2, A_1, A_0$  all of them gives output 1 if a single digit from two number is equal.

As, we have 4 bit or 4 digits we need to give output 1 if all of the sequential digits are same. If 1 digit does not match with the other number than it will give output

0. So, the "Equal <sup>comparator</sup> ~~converter~~" equation will be,

$$A_3 \cdot A_2 \cdot A_1 \cdot A_0 \leftarrow \text{Equal comparator,}$$

Let's assume two numbers,

$$A = 1101$$

$$B = 1100$$

Here,

$$A_3 = 1, A_2 = 1, A_1 = 0, A_0 = 1$$

$$B_3 = 1, B_2 = 1, B_1 = 0, B_0 = 0$$

$$X_3 = A_3' B_3' + A_3 B_3 = 1$$

$$X_2 = A_2' B_2' + A_2 B_2 = 1$$

$$X_1 = A_1' B_1' + A_1 B_1 = 1$$

$$X_0 = A_0' B_0' + A_0 B_0 = 0 \quad [ \text{As } A_0 \neq B_0 ]$$

$$\therefore \cancel{N_3} N_3 \cdot N_2 \cdot N_1 \cdot N_0 = 0$$

So, the numbers are not equal.

$$\text{If } A = 1011$$

$$B = 1011,$$

Here,

$$N_3 = 1$$

$$N_2 = 1$$

$$N_1 = 1$$

$$N_0 = 1$$

$$\therefore N_3 N_2 N_1 N_0 = 1$$

As the output is 1, which means both numbers are equal.

⑪  $A > B$  comparator, and  $B_3 B_2 B_1 B_0$

same, as equal comparator  $A_3, A_2, A_1, A_0$  are the digits or bits of <sup>two</sup> binary number,  $A, B$ .

As we ~~gonna count~~ are going to count from MSB, the steps will be.

Step 1  $\rightarrow A_3 > B_3$  for it we need to write the equation  $A_3 B_3'$ . This equation is only going to provide 1 if  $A_3 = 1, B_3 = 0$ .

Step 2  $\rightarrow$  We need to go to step 2 from step 1 if in step 1  $A_3 = B_3$ , which will provide 0 in step 1. So the equation we will need in this step is  ~~$A_3 A_2 B_2$~~   $A_3 A_2 B_2'$

As  $n_3$  means  $A_3 = B_3$  and,  $n_3$  is only 1 if  $A_3$  and  $B_3$  equal, also  $A_2 B_2'$  only provide 1 if  $A_2 = 1, B_2 = 0$ ,

Step 3  $\Rightarrow$  If previous step is false, we need to come to this step, Equation of this step is  $n_3 n_2 A_1 B_1'$ . This step will provide 1 only if  $A_3 = B_3, A_2 = B_2$  and  $A_1 = 1, B_1 = 0$ ,

Step 4  $\Rightarrow$  If previous steps are false, then we need to come to this step. Equation of this step is  $n_3 n_2 n_1 A_0 B_0'$ . This step is only going to provide 1 if  $A_3 = B_3, A_2 = B_2, A_1 = B_1$  and  $A_0 = 1, B_0 = 0$ .

We need the output 1 if one of the



following step is true, so, the equation will be,

$$A_3 B_3' + K_3 A_2 B_2' + K_3 K_2 A_1 B_1' + K_3 K_2 K_1 A_0 B_0'$$

This equation is going to only provide 0 if all of the steps are false.

For number,  $A = 1101$   
 $B = 1110$

Hence,

$$A_3 B_3' = 0 \quad [A_3 = B_3]$$

$$K_3 A_2 B_2' = 0 \quad [A_2 = B_2]$$

$$K_3 K_2 A_1 B_1' = 0 \quad [A_1 < B_1]$$

$$K_3 K_2 K_1 A_0 B_0' = 0 \quad [K_1 = 0]$$

$$\therefore A < B$$

For number,

$$A = 1110$$

$$B = 1011$$

Hence,

$$A_3 B_3' = 0 \quad [A_3 = B_3]$$

$$K_3 A_2 B_2' = 1 \quad [A_2 > B_2]$$

$$K_3 K_2 A_1 B_1' = 0 \quad [K_2 = 0]$$

$$K_3 K_2 K_1 A_0 B_0' = 0 \quad [K_2 = 0]$$

$$\therefore A > B$$

### ③ (A < B) comparator

As like  $A > B$  comparator this equation will have kind of same but opposite equation.

For this comparator we need to consider some steps:

Step 1  $\rightarrow$  We need to give output 1 if  $A_3 < B_3$ ,

so, equation of this step is,

$A_3' B_3$ . This equation is only going

to generate 1 if  $A_3 = 0, B_3 = 1$ ,

Step 2  $\rightarrow$  If step 1 is false, then we need

to consider this step. Equation of

this step is  $A_3 A_2' B_2$ . This equation

only going to provide 1 if

$A_3 = B_3$  and  $A_2 = 0, B_2 = 1$ .

Step 3  $\rightarrow$  We need to consider this step, if previous steps are false. The equation of this step is  $\kappa_3 \kappa_2 A_1' B_1$ . This step only going to provide 1 if  $A_3 = B_3$ ,  $A_2 = B_2$  and  $A_1 = 0$ ,  $B_1 = 1$ .

Step 4  $\rightarrow$  If previous steps are false we need to consider this step. The equation of this step is  $\kappa_3 \kappa_2 \kappa_1 A_0' B_0$ . This equation is only going to provide 1 if  $A_3 = B_3$ ,  $A_2 = B_2$ ,  $A_1 = B_1$  and  $A_0 = 0$ ,  $B_0 = 1$ .

As, we want to give the comparator output 1 only if one of these following steps are true.

So, the equation will be

$$A_3' B_3 + \kappa_3 A_2' B_2 + \kappa_3 \kappa_2 A_1' B_1 + \kappa_3 \kappa_2 \kappa_1 A_0' B_0$$



The following equation will only give output 0 if all of the steps are false.

For number,

$$A = 1011$$

$$B = 1100$$

Here,

$$A_3' B_3 = 0 \quad [A_3 = B_3]$$

$$K_3 A_2' B_2 = 1 \quad [B_2 > A_2]$$

$$K_3 K_2 A_1' B_1 = 0 \quad [K_2 = 0]$$

$$K_3 K_2 K_1 A_0' B_0 = 0 \quad [K_2 = 0]$$

$$A < B$$

For number,

$$A = 1110$$

$$B = 1101$$

Here,

$$A_3' B_3 = 0 \quad [A_3 = B_3]$$

$$K_3 A_2' B_2 = 0 \quad [A_2 = B_2]$$

$$K_3 K_2 A_1' B_1 = 0 \quad [A_1 > B_1]$$

$$K_3 K_2 K_1 A_0' B_0 = 1 \quad [K_1 = 0]$$

$$K_3 K_2 K_1 A_0' B_0 = 1$$

$$A \neq B$$