



## Assignment 6 Solution

Probability and statistics (National University of Computer and Emerging Sciences)

# Assignment 6

## Solution

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Marks Distribution :

Q1 :	5
Q2 :	5
Q3 :	8
Q4 :	6
Q5 :	12
Q6 :	5
Q7 :	10
Q8 :	9
Presentation :	10
Total :	70

Q1

$$P(I) = 0.8$$
$$P(S/I) = 0.85$$

$$P(II) = 0.2$$
$$P(S/II) = 0.65$$

$$P(S) = P(I \cap S) + P(II \cap S)$$

$$P(S) = P(I) \cdot P(S/I) + P(II) \cdot P(S/II)$$

$$P(S) = (0.8)(0.85) + (0.2)(0.65)$$

$$= 0.81$$

$$P(II/S) = \frac{P(II \cap S)}{P(S)} = \frac{0.65}{0.81} = 0.802$$

Q2 i)

$$P(X=4) = \frac{{}^6C_4 \times {}^{48}C_2}{{}^{54}C_6} = 0.000655$$

$$ii) P(X=0,1) = \left( \frac{{}^6C_0 \times {}^{48}C_6}{{}^{54}C_6} \right) + \left( \frac{{}^6C_1 \times {}^{48}C_5}{{}^{54}C_6} \right)$$

$$= 0.873$$

Q3

$$a) P\left(\frac{P_r}{B}\right) = \frac{P(P_r \cap B)}{P(B)} = \frac{36/450}{116/450} = 0.310$$

$$b) P\left(\frac{P_r}{G}\right) = \frac{P(P_r \cap G)}{P(G)} = \frac{14/450}{334/450} = 0.042$$

$$c) P(P_r' \cap G) = P(P_r') \cdot P(G)$$

$$\frac{320}{450} = \frac{400}{450} \cdot \frac{334}{450}$$

$$0.71 \neq 0.66$$

$\therefore$  Not Independent

Q4

<u>X</u>	<u>P(X)</u>	
0	0.3	$(3c_2 \times 2c_0)/5c_2$
1	0.6	$(3c_1 \times 2c_1)/5c_2$
2	0.1	$(3c_0 \times 2c_2)/5c_2$

Q5

<u>X</u>	<u>f(z)</u>	<u>z = -6X</u>	<u>z.f(z)</u>	<u>z<sup>2</sup>f(z)</u>
0	0.35	0	0	0
1	0.30	-6	-1.8	10.8
2	0.10	-12	-1.2	14.4
3	0.15	-18	-2.7	48.6
4	0.10	-24	-2.4	57.6
			<u>E(z) = -8.1</u>	<u>E(z<sup>2</sup>) = 131.4</u>

i)  $\text{Var}(-6X)$   
 $= 36 \text{Var}(X)$   
 $= 36 (E(z^2)) - (E(z))^2$   
 $= 36 (131.4 - (-8.1)^2)$   
 $= 2368.44$

ii)

<u>X</u>	<u>z = 4X - 3</u>	<u>f(z)</u>	<u>z.f(z)</u>
0	-3	0.35	-1.05
1	1	0.30	0.30
2	5	0.10	0.5
3	9	0.15	1.35
4	13	0.10	1.3
			<u>E(z) = 2.4</u>

$\therefore E(4X - 3) = 2.4$

$$\text{iii)} \quad E(x) = (1 \times 0.3) + (2 \times 0.1) + (3 \times 0.15) + (4 \times 0.1) \\ = 1.35$$

$$E(4x-3) \equiv 4(E(x)) - 3$$

$$2.4 \equiv 4(1.35) - 3$$

$$2.4 \equiv 2.4$$

$$\textcircled{Q6} \quad P(A \cup B) = P(A) + P(B) - P(A \cap B)$$

$$P(A \cap B) = P(A) + P(B) - P(A \cup B)$$

$$= \frac{1}{3} + \frac{3}{4} - \frac{11}{12}$$

$$= \frac{1}{6}$$

$$P(B|A) = \frac{P(A \cap B)}{P(A)} = \frac{\frac{1}{6}}{\frac{1}{3}} = \frac{1}{2}$$

$\textcircled{Q7}$

$$P(1) = 0.3$$

$$P(2) = 0.2$$

$$P(3) = 0.5$$

$$\begin{array}{cc} \swarrow & \searrow \\ P(D|P1) = 0.01 & P(D|P1)' = 0.99 \end{array}$$

$$\begin{array}{cc} \swarrow & \searrow \\ P(D|P2) = 0.03 & P(D|P2)' = 0.97 \end{array}$$

$$\begin{array}{cc} \swarrow & \searrow \\ P(D|P3) = 0.02 & P(D|P3)' = 0.98 \end{array}$$

$$P(D) = P(1 \cap D) + P(2 \cap D) + P(3 \cap D)$$

$$= P(1) \cdot P(D|1) + P(2) \cdot P(D|2) + P(3) \cdot P(D|3)$$

$$= (0.3 \times 0.01) + (0.2 \times 0.03) + (0.5 \times 0.02)$$

$$= 0.019$$

$$P(1|D) = \frac{P(1 \cap D)}{P(D)} = \frac{P(1) \cdot P(D|1)}{P(D)} = \frac{0.3 \times 0.01}{0.019} = 0.158$$

Q8

<u>X</u>	<u>f(x)</u>
80	0.2
200	0.5
220	0.3

$$\begin{aligned} \text{i) Mean} = E(X) &= (80 \times 0.2) + (200 \times 0.5) + (220 \times 0.3) \\ &= 182 \end{aligned}$$

$$\begin{aligned} E^2(X) &= (80^2 \times 0.2) + (200^2 \times 0.5) + (220^2 \times 0.3) \\ &= 35,800 \end{aligned}$$

$$\begin{aligned} \text{Var}(X) &= E^2(X) - (E(X))^2 \\ &= 35,800 - (182)^2 \\ &= 2676 \end{aligned}$$

$$\begin{aligned} \text{C.O.V} &= \frac{\text{st. dev}}{\text{Mean}} \times 100 \\ &= \frac{\sqrt{2676}}{182} \times 100 \\ &= 28.42\% \end{aligned}$$

$$\text{ii) Mean} = \frac{182 - 200}{20} = -0.9$$

$$\text{Variance} = \frac{\text{Var}(X)}{400} = \frac{2676}{400} = 6.69$$

$$\begin{aligned} \text{C.O.V} &= \frac{\sqrt{6.69}}{-0.9} \times 100 \\ &= -287\% \end{aligned}$$