



# Data Science & ML Course Lesson #14 Statistics Fundamentals I

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#### Agenda

- Sampling
  - Population and sampling
  - Sampling error
  - Simple random sampling (SRS)
  - Stratified sampling
  - Clustering sampling
- Variables in statistics
  - Quantitative and qualitative variables
  - Scale of measurements (nominal, ordinal, interval, ratio)



# Update from repository

git clone https://github.com/ivanovitchm/datascience2machinelearning.git

Or ....

git pull



# PREVIOUSLY ON...

- Perform basic data analysis
- Data visualization
- Fundamental statistical metrics like the mean or the median, and we plotted histograms, bar graphs or line plots.



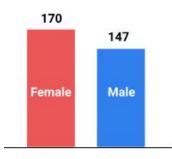
# Go much deeper into the theory



ld	Name	Salary	****	Gender	
1	Mary Ann	\$35 000		Female	
2	Marc Downey	\$55 000		Male	
 51	 Juliet Ali	\$45 000		Female	
 317	 Jane Ace	\$95 000		Female	

Understand how the data is structured and measured





Data source

Visualize the patterns

Gender	Frequency
Male	147
Female	170

Organize the data in comprehensible forms to find patterns





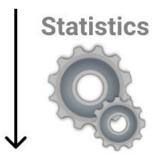
# Solving problems with Statistics

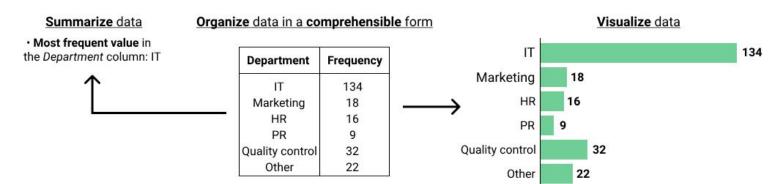
Id	Name	Salary (\$ / year)	Unexpect days of	1 210 21 1/0	rk Extra hours worked		
1 2	Macy Davidson Jake Pugh	56000 29000	6 0	Seldom Often	26 0		
3 4	Draven Whitaker Izabella Pratt	43000 35000	Id	Name	Department	Salary (\$ / year)	 Age
5 6 7	Gerardo Baker Milo Norton Fiona Benson	25000 50000 60000	1 2 3	Alec Sullivan Agustin Wang Jocelyn Pruitt	IT PR Marketing	42000 35000 41000	 26 31 32
			72	 Lainey Smith	IT	27000	  21
			231	 Lexi Wilcox	IT	 85000	  57

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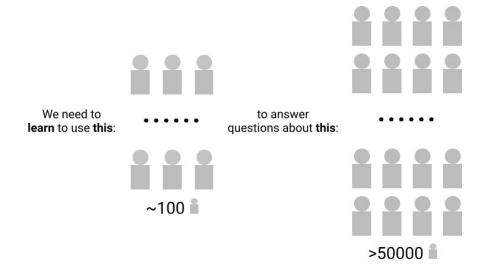
Id	Name	Department	Salary (\$ / year)	 Age
1	Alec Sullivan	IT	42000	 26
2	Agustin Wang	PR	35000	 31
3	Jocelyn Pruitt	Marketing	41000	 32
72	Lainey Smith	IT	27000	 21
	••••	****		 
231	Lexi Wilcox	IT	85000	 57





### Solving problems with statistics

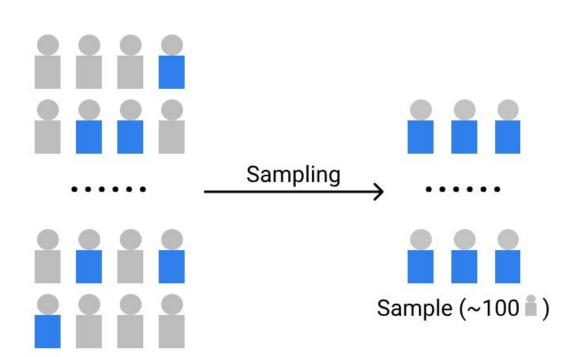
- 1. You run an international company with over **50000 employees.**
- Now you want to determine whether the employees have been impacted negatively in any significant way.







# Population and Sampling



Population (>50000 1)

Whether a set of data is a sample or a population depends on the question we're trying to answer.



### Population and Sampling

If we tried to find out whether people at international companies are satisfied at work



satisfied at work?



>50000

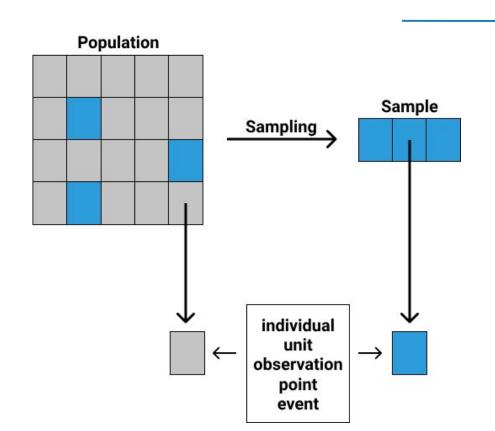


Are people working at international companies satisified at work?





## Population and Sampling



You'll often see this terminology used interchangeably: sample unit, sample point, sample individual, or sample observation.



### Sampling error

For instance, let's say we know that the average salary in our company is **U\$ 34500**, and the **proportion of women is 60%**.

#### Sample 1

Average salary = \$31000

Proportion of women = 70%

#### Sample 2

Average salary = \$35000

Proportion of women = 61%

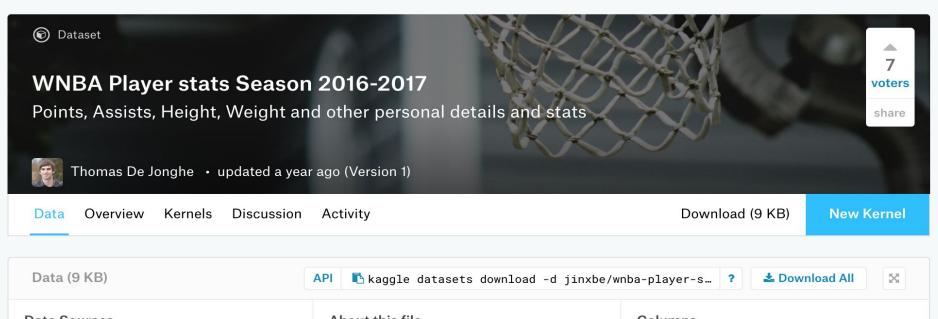
Population

Sampling



sampling error = parameters - statistics





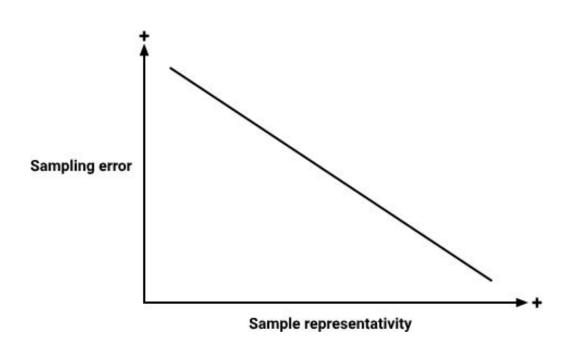


#### Dataset

	Name	Team	Pos	Height	Weight	вмі	Birth_Place	Birthdate	Age	College	Experience	Games Played	MIN	FGM	FGA
0	Aerial Powers	DAL	F	183	71.0	21.200991	US	January 17, 1994	23	Michigan State	2	8	173	30	85
1	Alana Beard	LA	G/F	185	73.0	21.329438	US	May 14, 1982	35	Duke	12	30	947	90	177
2	Alex Bentley	CON	G	170	69.0	23.875433	US	October 27, 1990	26	Penn State	4	26	617	82	218
3	Alex Montgomery	SAN	G/F	185	84.0	24.543462	US	December 11, 1988	28	Georgia Tech	6	31	721	75	195
4	Alexis Jones	MIN	G	175	78.0	25.469388	US	August 5, 1994	23	Baylor	R	24	137	16	50



## Simple Random Sampling (SRS)







# Simple Random Sampling (SRS)

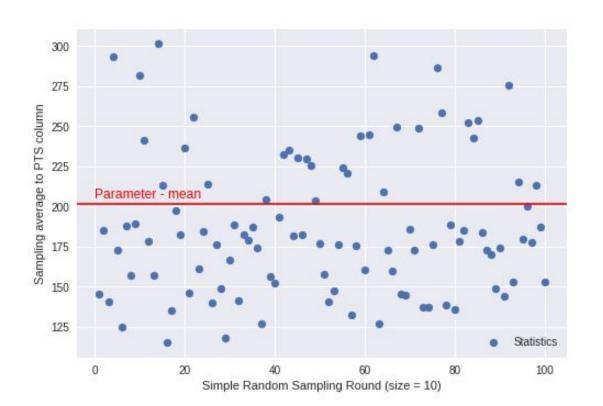
1	2	3	Simple <b>random</b> sampling	3	5
4	5	6	$x 2 \longrightarrow 3, 5$	San	nple

Series.sample(2, random\_state = 1)

**Population** 

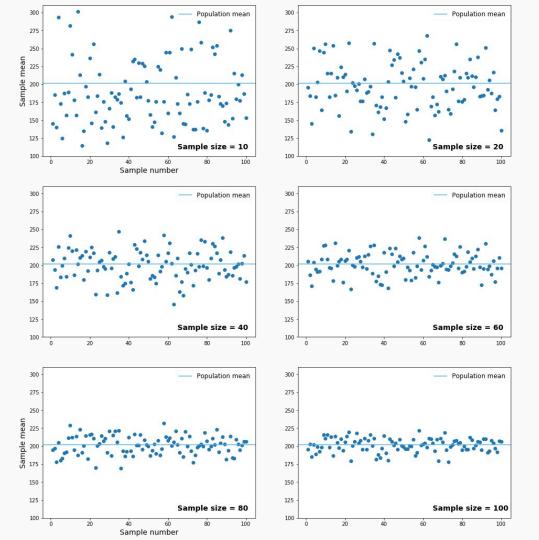


### Discrepancy between parameter and statistics







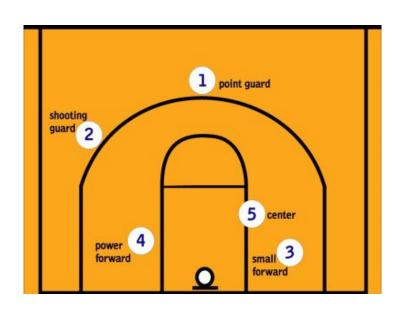


# The Importance of Sample Size

Simple random sampling is not a reliable sampling method when the sample size is small.



# **Stratified Sampling**



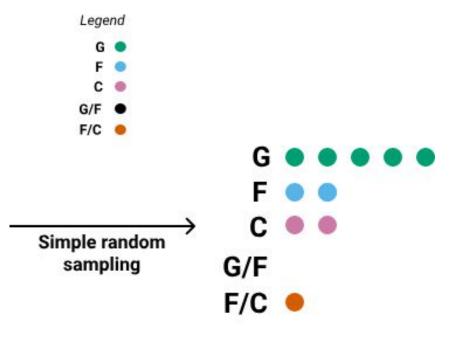
Abbreviation	Full name
F	Forward
G	Guard
С	Center
G/F	Guard/Forward
F/C	Forward/Center



#### Stratified Sampling (SRS problem)

The downside of simple random sampling is that it can leave out individuals playing in a certain position on the field



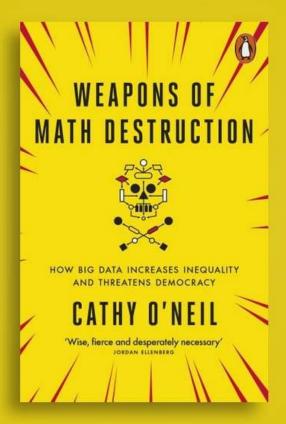


Population (25 players)

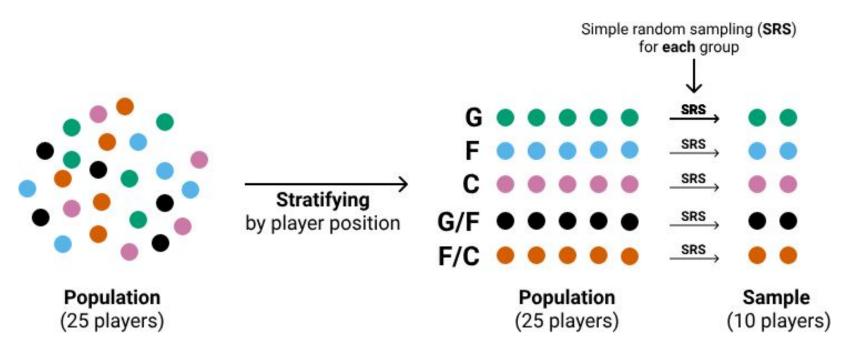
Sample (10 players)







#### Stratified Sampling (solution)





#### **Proportional Stratified Sampling**

(1.969, 12.0]

```
1 wnba['Games Played'].value counts()
       30
      25
30
28
      10
22
26
18
16
15
```

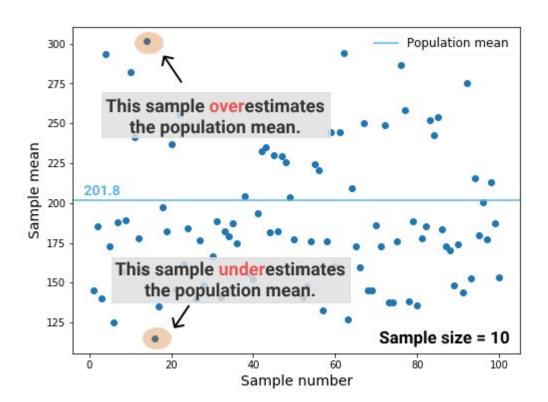
```
wnba['Games Played'].value counts(bins=3)
 (22.0, 32.0]
                    104
 (12.0, 22.0)
                     26
 (1.969, 12.0)
                     13
 1 wnba['Games Played'].value_counts(bins=3,
                                   normalize=True)
(22.0, 32.0]
                0.727273
(12.0, 22.0]
                0.181818
```

72.72% players who played more than 23 games

0.090909



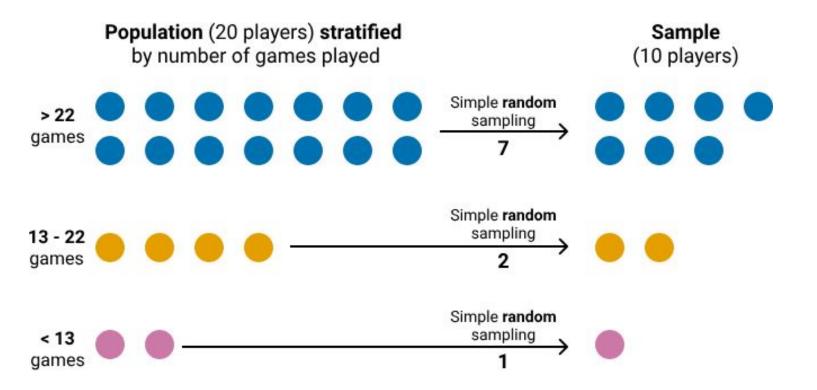
#### **Proportional Stratified Sampling**







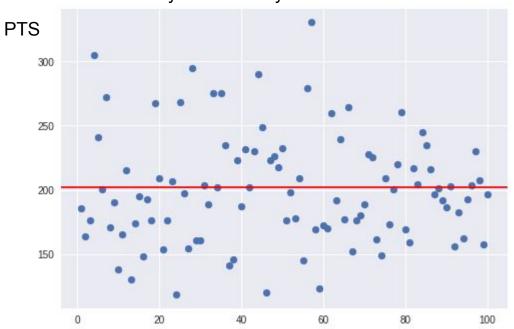
#### Proportional Stratified Sampling (solution)





## Proportional Stratified Sampling (solution)

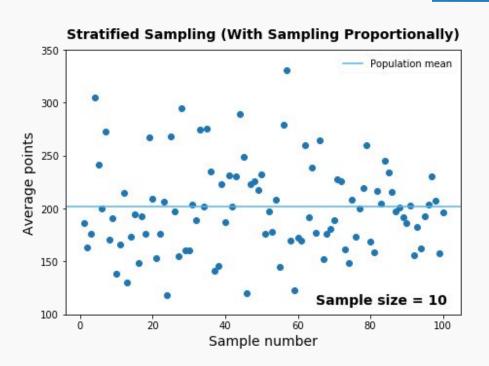
#### Stratified by Games Played

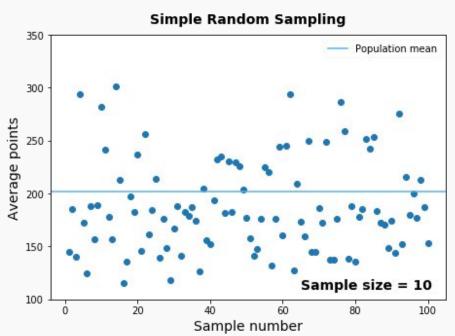






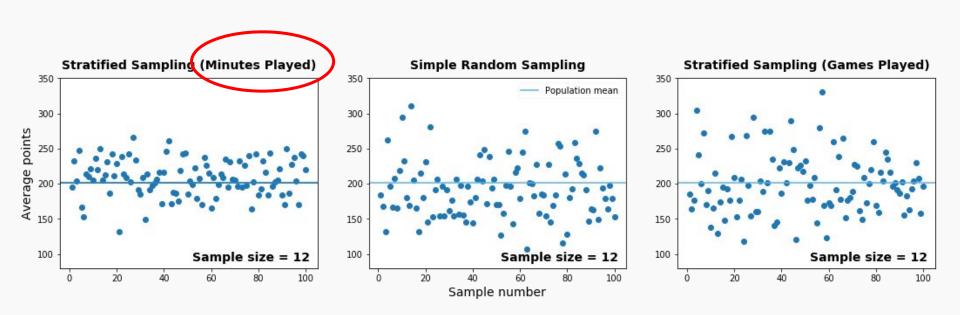
#### Choosing right strata







### Choosing right strata



Minimize the variability within each stratum.

Maximize the variability between strata.

The stratification criterion should be strongly correlated with the property you're trying to measure.



#### **Cluster Sampling**







### Sampling in Data Science

#### e-commerce



- Company that has a table in a database with more than 10 million rows of online transactions.
- The marketing team asks you to analyze the data and find categories of customers with a low buying rate, so that they can target their marketing campaigns at the right people
- Instead of working with more than 10 million rows at each step of your analysis, you can save a lot of code running time by sampling several hundred rows



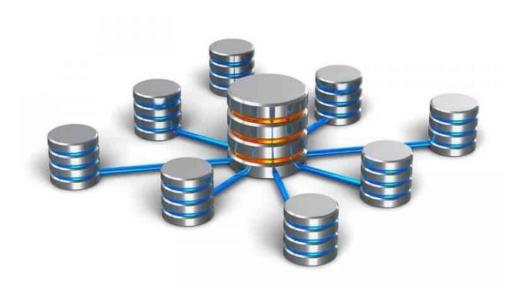
## Sampling in Data Science



- 1. It could be that you need to collect data from an API that either has usage limit, or is not free.
- In this case, you are more or less forced to sample. Knowing how and what to sample can be of great use.



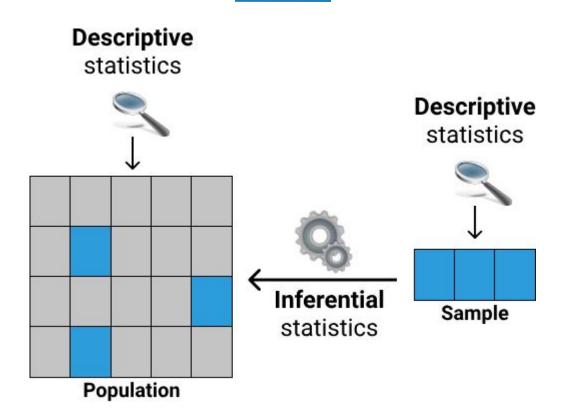
#### Sampling in Data Science



- Another common use case of sampling is when the data is scattered across different locations (different websites, different databases, different companies, etc.).
- 2. As we've discussed in the previous screen, cluster sampling would be a great choice in such a scenario.



#### Descriptive & Inferential Statistics

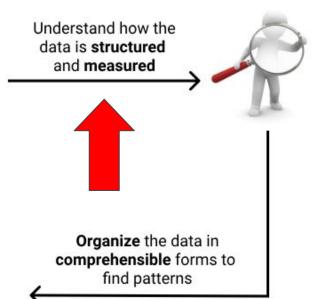




### Next Steps



Id	Name	Salary	 Gender	
1	Mary Ann	\$35 000	 Female	
2	Marc Downey	\$55 000	 Male	
 51	 Juliet Ali	\$45 000	 Female	
 317	 Jane Ace	\$95 000	  Female	

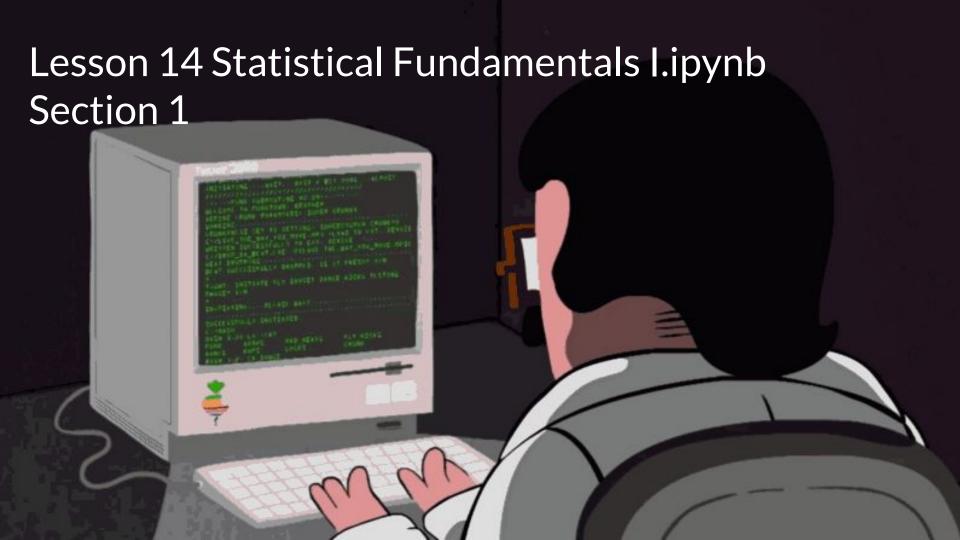


170	147	
Female	Male	<b>✓ Visualize</b> the patterns

Gender	Frequency
Male	147
Female	170







#### Variables in Statistics

	Name	Team	Pos	Height	Weight	ВМІ	Birth_Place	Birthdate
39	Crystal Langhorne	SEA	F/C	188	84.0	23.766410	US	October 27, 1986
52	Érika de Souza	SAN	С	196	86.0	22.386506	BR	September 3, 1982
102	Nia Coffey	SAN	F	185	77.0	22.498174	US	May 21, 1995

The properties with varying values we call variables



# Quantitative and Qualitative Variables

	<b>Quantitative</b> variables	<b>Qualitative</b> variables
Describe <b>quantities</b>	YES	NO
Describe <b>qualities</b>	NO	YES
Use <b>numbers</b>	YES	YES
The numbers are actual quantities	YES	NO
Use <b>words</b>	YES	YES
The words express a <b>quantity</b>	YES	NO

Height	Name
ВМІ	Team
Age	Pos
Birth_Data	Birth_Place
Weight	College



### Scale of Measurements

The system of rules that define how each variable is measured is called **scale** of measurement

	Team	Height
We can tell whether two individuals are <b>different</b>	YES	YES
We can tell <b>the size</b> of the difference	NO	YES
We can tell the <b>direction</b> of the difference	NO	YES

- Nominal
- Ordinal
- Interval
- Ratio



## **Nominal Scale**

	Nominal
We can tell whether two individuals are different	YES
We can tell the <b>direction</b> of the difference	NO
We can tell <b>the size</b> of the difference	NO
We can measure quantitative variables	NO
We can measure qualitative variables	YES

	Name	Team	Pos	Birth_Place	College
0	Aerial Powers	DAL	F	US	Michigan State
1	Alana Beard	LA	G/F	US	Duke
2	Alex Bentley	CON	G	US	Penn State
3	Alex Montgomery	SAN	G/F	US	Georgia Tech
4	Alexis Jones	MIN	G	US	Baylor



# Ordinal Scale (ranking)

	Nominal	Ordinal
We can tell whether two individuals are different	YES	YES
We can tell the <b>direction</b> of the difference	NO	YES
We can tell <b>the size</b> of the difference	NO	NO
We can measure quantitative variables	NO	YES
We can measure qualitative variables	YES	NO

	Height	Height_labels
0	183	tall
1	185	tall
2	170	short
3	185	tall
4	175	medium





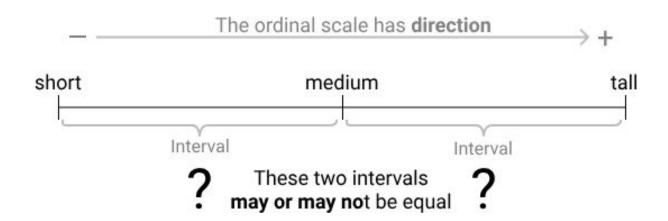
### Nominal or Ordinal??

	<pre>Height_labels</pre>	College	Games Played	Experience
0	tall	Michigan State	8	2
1	tall	Duke	30	12
2	short	Penn State	26	4
3	tall	Georgia Tech	31	6
4	medium	Baylor	24	R



### The interval and ratio scales

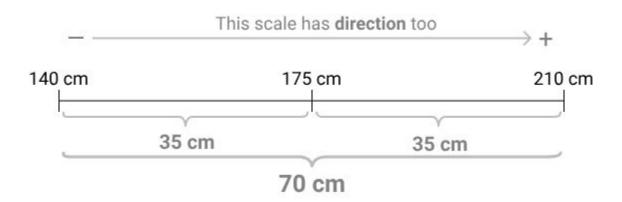
# The height variable measured on an **ordinal scale**





### The interval and ratio scales

The height variable measured on a scale that uses **real numbers** 



We know the value of each interval, which means we can compute the size of the difference between any two points.



	Nominal	Ordinal	Interval	Ratio
We can tell whether two individuals are <b>different</b>	YES	YES	YES	YES
We can tell the <b>direction</b> of the difference	NO	YES	YES	YES
We can tell <b>the size</b> of the difference	NO	NO	YES	YES
We can measure quantitative variables	NO	YES	YES	YES
We can measure qualitative variables	YES	NO	NO	NO



### The difference between ratio and interval scales

What sets apart ratio scales from interval scales is the nature of the zero point.

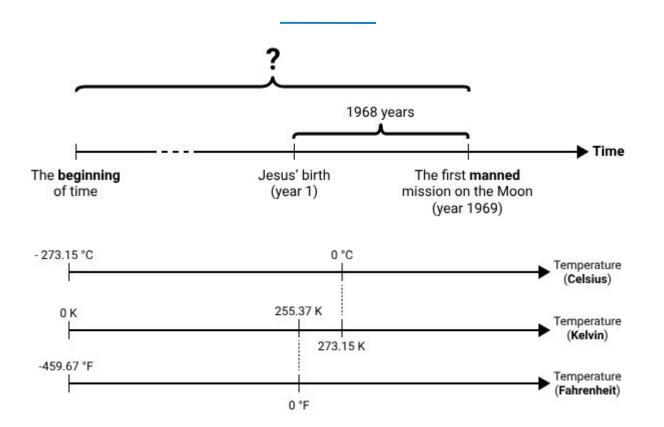
Name	Weight	Weight_deviation
Clarissa dos Santos	89.0	10.021127
Alex Montgomery	84.0	5.021127
Renee Montgomery	63.0	-15.978873
Layshia Clarendon	64.0	-14.978873
Sugar Rodgers	75.0	-3.978873
	Clarissa dos Santos Alex Montgomery Renee Montgomery Layshia Clarendon	Clarissa dos Santos 89.0 Alex Montgomery 84.0 Renee Montgomery 63.0 Layshia Clarendon 64.0

	Interval	Ratio
Well-defined intervals	YES	YES
The zero point indicates the absence of a quantity	NO	YES
Difference measured in terms of <b>distance</b>	YES	YES
Difference measured in terms of <b>ratios</b>	NO	YES





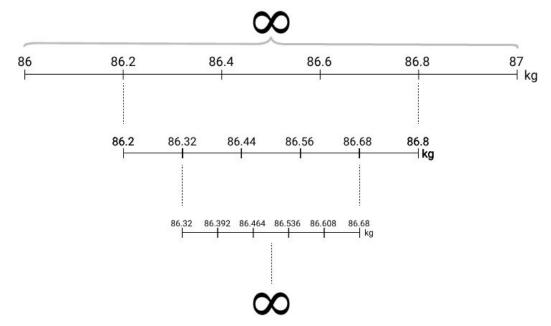
## Common Examples of Interval Scales





### Discrete and Continuous Variable

_	Name	Weight	PTS
77	Kayla Thornton	86.0	32
16	Asia Taylor	76.0	31
80	Kia Vaughn	90.0	134
137	Tierra Ruffin-Pratt	83.0	225
12	Amanda Zahui B.	113.0	51







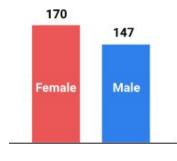


Id	Name	Salary	 Gender
1	Mary Ann	\$35 000	 Female
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Understand how the data is **structured** and **measured** 







Visualize the patterns

Gender	Frequency
Male	147
Female	170

Organize the data in comprehensible forms to find patterns





