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1 function spot_results = FindTrajects(image_label,start_frame,end_frame)
2 %
3 % Created by Isabel Llorente-Garcia, August 2011.
4 % If you use this code please acknowledge Isabel Llorente-Garcia in your
5 % publications.
6 %
7 % This function takes an image_label such as '513', '490', etc...
8 % which corresponds to a certain .sif image sequence in current folder,
9 % and then finds all trajectories of the bright fluorescent spots in time.
10 %
11 % Example of how to use this function:
12 % for image "Heiko_Thu Jun 24 2010_554.sif" in current folder:
13 % [numFrames2 frame_Ysize2 frame_Xsize2 image_data2] = extract_image_sequence_data('554');
14 %
15 % Reads .sif image sequence data and then for each frame:
16 % finds candidate spots,
17 % joins them to spots found and accepted on previous frame,
18 % eliminates coincidences in those candidates (points closer than 1 pixel),
19 % within all candidates, it finds actual spot centres through iterative Gaussian masking,
20 % and accepts only found spot centres with clipping flag equal to zero, constrained width and large enough SNR,
21 % eliminates coincidences from previously accepted found spot centres.
22 % Resulting final accepted spot centres are saved in the structure array spot_final.
23 % Then link spots into trajectory segments: For second frame do differently
24 % and check only spots in 1st frame and compare to spots in second frame.
25 % For rest of frames (for frame k): A) first check loose spots (TrajNumber=0) two frames
26 % ago (k-2) and compare to spots in current frame (k).
27 % B) then check all spots in previous frame (k-1) and compare to spots in
28 % current frame (k).
29 % To decide on the best assignment of pairs of spots (link), we build up
30 % matrices of pair-wise distances, ratio of intensities and ratio of sigmas
31 % of all pairs of spots in the two frames being compared, and take the
32 % winning assignment as that with the smallest pairwise distance.
33 % The intensity ratio and ratio of sigmas has to be within certain min and
34 % max bounds too.
35 %
36 % start_frame and end_frames are the frames through which the loop runs to
37 % find centres of bright spots.
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38 %
39 % Output:
40 % The output, spot_results is a cell array with two elements:
41 % spot_results = {params, spot_final};
42 % The first element in the cell array, spot_results{1}, contains all parameters used to run
43 % the function: "params" (this is a structure array itself).
44 % The second element in the cell array, spot_results{2}, contains the track
45 % results: "spot_final".
46 % "spot_final", is itself a structure array with end_frame by L elements,
47 % each of which is a structure with fields: CentreX, CentreY, IspTot,
48 % Sigma, IbgAvg, IbgTot, IinnerTot, ClipFlag, FrameNumber and SpotNumber.
49 % Along the dimension L, we have the different bright spots found on each
50 % frame (L will usually be the number of spot centres found in frame_start,
51 % or the largest number of spots ever accepted).
52 % For example, spot_final(100,8) is a structure with the above fields
53 % corresponding to the eighth found spot on frame 100.
54 %
55 % Example of params: spot_results{1}:
56 %
57 %         image_label: '498'
58 %         start_frame: 7
59 %         end_frame: 500
60 %         r: 5
61 %     max_num_candidates: 2000
62 %     subarray_halfwidth: 8
63 % inner_circle_radius: 5
64 %     gauss_mask_sigma: 2
65 %         sigmaFit_min: 2
66 %         sigmaFit_max: 4
67 %         SNR_min: 2
68 %         rsq_min: 0.2000
69 %         deflate: 1
70 %     d_coincid_cand: 1
71 %     d_coincid_found: 1
72 %         d_01_max: 5
73 %     Iratio_01_min: 0.5000
74 %     Iratio_01_max: 3
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75 %      SigmaRatio_01_min: 0.5000
76 %      SigmaRatio_01_max: 2
77 %      d_02_max: 5
78 %      Iratio_02_min: 0.5000
79 %      Iratio_02_max: 3
80 %      SigmaRatio_02_min: 0.5000
81 %      SigmaRatio_02_max: 2
82 %      rej: 10000
83 %      file_name: 'Heiko_Thu Jun 24 2010_498.sif'
84 %      numFrames: 500
85 %      frame_Ysize: 512
86 %      frame_Xsize: 512
87 %
88 % Example of how to call this function:
89 % s0 = FindTrajects('470',5,500); uses
90 % image sequence 470 and finds trajectories in it, for frames 5 to 500.
91 % Another example: s1 = FindTrajects('490',100,110);.
92 % -----
93 % Note: for reading .sif files you need 'read_sif_data_direct.m',
94 % 'GetAndorSifSize', etc. which are currently in path:
95 % 'C:\Isabel\myMatlabFiles\IO_Input\'.
96 %
97 % NOTE: before running this function you should move into the directory which
98 % contains the image sequence data (labelled by 'image_label').
99
100
101 %% DEFINITIONS and PARAMETERS:
102
103 % I have saved all parameter values in the file "paramsForFindTrajects.m"
104 % in the current directory. Just calling the name of that file loads the
105 % parameter values into the workspace:
106 paramsForFindTrajects
107 % In this way, we can save different parameter sets for different data sets
108 % in an easy manner and run two Matlabs at the same time working with different parameter sets.
109
110 % %
111 % % define data (.sif image) directory:
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112 % % dir_data = 'Z:\Leake\Heiko Data\';
113 % % dir_data = 'C:\Isabel\ExperiData\HeikoData\';
114 % % Print data directory on command window to guide user:
115 % disp(' ') % empty line
116 % disp(['The data directory (.sif images) is: ',cd]) % display current directory.
117 %
118 % % Save input parameters to "params":
119 % params.image_label = image_label;
120 % params.start_frame = start_frame;
121 % params.end_frame = end_frame;
122 %
123 % % Number of frames to average over when calculating a frame average in
124 % % order to get a Signal Mask to distinguish cell region from background
125 % % region:
126 % r = 5; % number of frames to average over, starting from start_frame. (default: 5, end_frame-start_frame)
127 % % Save parameters to results as structure "params":
128 % params.r = r;
129 %
130 % % If you don't want to use the cell mask to exclude spots found outside
131 % it, make the following parameter equal to 1 (then spots can be accepted anywhere on image):
132 % doNotUseCellMaskToTellSpotsRegion = 0;
133 % params.doNotUseCellMaskToTellSpotsRegion = doNotUseCellMaskToTellSpotsRegion;
134 %
135 % % Maximum number of candidate spots (if eg. 260000 candidate spots are
136 % % found, we get an error in function pdist: "Distance matrix has more
137 % % elements than the maximum allowed size in MATLAB"), hence, we limit the
138 % % max number of candidate spots:
139 % max_num_candidates = 2000; % should be around 200.
140 % % Save parameters to results as structure "params":
141 % params.max_num_candidates = max_num_candidates;
142 %
143 % % PARAMETERS for finding spot centres (see findSpotCentrelframe.m, inputs to the function):
144 % % The total integrated spot intensity is a bgnd corrected one, inside a
145 % % circular mask of radius inner_circle_radius.
146 % subarray_halfwidth = 8; % (Default: 8 pixels). Halfwidth of image square subarray
147 % % ROI, typically a square of size 17x17 pixels.
148 % inner_circle_radius = 5; % (Default: 5 pixels). Radius of inner circular mask that moves inside the fixed square subarray.
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149 % gauss_mask_sigma = 2; % (Default: 2 pixels). Size in pixels of the applied Gaussian mask.
150 % guess_sigma_Fit = 3; % starting guess for Gaussian fit of brightspot intensity (default = 3).
151 % % Save parameters to results as structure "params":
152 % params.subarray_halfwidth = subarray_halfwidth;
153 % params.inner_circle_radius = inner_circle_radius;
154 % params.gauss_mask_sigma = gauss_mask_sigma;
155 % params.guess_sigma_Fit = guess_sigma_Fit;
156 %
157 % % PARAMETERS for deciding if we accept a spot centre found by the function
158 % % findSpotCentrelframe or not:
159 % sigmaFit_min = -inner_circle_radius; % minimum acceptable sigma of gaussian fit to spot, in pixels (2) (-3).
160 % sigmaFit_max = inner_circle_radius; % maximum acceptable sigma of gaussian fit to spot, in pixels (4) (3).
161 % SNR_min = 1.4; % minimum acceptable signal-to-noise ratio (at least 2) (SNR as defined in findSpotCentrelframe.m).
162 % rsq_min = 0.1; % minimum acceptable r-square value (0.2) (goodness of gaussian fit to spot).
163 % % Save parameters to results as structure "params":
164 % params.sigmaFit_min = sigmaFit_min;
165 % params.sigmaFit_max = sigmaFit_max;
166 % params.SNR_min = SNR_min;
167 % params.rsq_min = rsq_min;
168 %
169 % % PARAMETER to decide if deflation method is applied or not (subtract each
170 % % found spot to allow detection of weaker spots):
171 % deflate = 1;
172 % % Save parameters to results as structure "params":
173 % params.deflate = deflate;
174 %
175 % % PARAMETERS for eliminating coincident spots:
176 % d_coincid_cand = 1; % distance (in pixels) for eliminating coincidences in spot candidates.
177 % d_coincid_found = 1; % distance for eliminating coincidences in found spot centres.
178 % % Save parameters to results as structure "params":
179 % params.d_coincid_cand = d_coincid_cand; % distance for eliminating coincidences in spot candidates.
180 % params.d_coincid_found = d_coincid_found; % distance for eliminating coincidences in found spot centres.
181 %
182 % % PARAMETERS for building trajectories:
183 % % For linking spots in current and previous frames:
184 % d_01_max = 5; % max distance in pixels between spot centres in current and previous frames, for linking them into a
trajectory (5).
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185 % Iratio_01_min = 0.5; % min ratio of total spot intensities (after bgnd subtraction) (0.5).
186 % Iratio_01_max = 3; % max ratio of total spot intensities (after bgnd subtraction) (frame k-1/frame k) (large enough value
(3) to account for blinking).
187 % SigmaRatio_01_min = 0.5; % min ratio of spot widths (sigma of Gaussian fit) (0.5).
188 % SigmaRatio_01_max = 2; % max ratio of spot width (sigma of Gaussian fit) (2).
189 % % Save parameters to results as structure "params":
190 % params.d_01_max = d_01_max;
191 % params.Iratio_01_min = Iratio_01_min;
192 % params.Iratio_01_max = Iratio_01_max;
193 % params.SigmaRatio_01_min = SigmaRatio_01_min;
194 % params.SigmaRatio_01_max = SigmaRatio_01_max;
195 %
196 % % For linking loose spots in current frame and 2 frames ago (jump of 1 frame in trajectory):
197 % d_02_max = 5; % max distance in pixels between spot centres in current frame and 2 frames ago. (default: 5)
198 % Iratio_02_min = 0.5; % min ratio of total spot intensities (after bgnd subtraction).
199 % Iratio_02_max = 3; % max ratio of total spot intensities (after bgnd subtraction).
200 % SigmaRatio_02_min = 0.5; % min ratio of spot widths (sigma of Gaussian fit).
201 % SigmaRatio_02_max = 2; % max ratio of spot width (sigma of Gaussian fit).
202 % % Save parameters to results as structure "params":
203 % params.d_02_max = d_02_max;
204 % params.Iratio_02_min = Iratio_02_min;
205 % params.Iratio_02_max = Iratio_02_max;
206 % params.SigmaRatio_02_min = SigmaRatio_02_min;
207 % params.SigmaRatio_02_max = SigmaRatio_02_max;
208 %
209 % % Use a very large number (larger than image size in pixels) for rejected asignments:
210 % rej = 10000;
211 % params.rej = rej; % Save parameters to results as structure "params".
212 %
213 % % Parameter to exclude a region from accepting spots (see later on, lines 322 and 507):
214 % exclude_region = 0;
215 % % Note that when exclude_region is 1, at the moment is it set for an image
216 % % with two channels, where spots are excluded also from around a horizontal
217 % % line centred on the image.
218 % exclude_region_width = subarray_halfwidth; % exclude edges of image, only look at spots with a centre far enough from image
edges.
219 % params.exclude_region = exclude_region;
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220 % params.exclude_region_width = exclude_region_width;
221
222 % Alternative way of selecting image sequence file:
223 % uigetfile opens a file dialog box to choose data file:
224 % [file_data,path_data] = uigetfile({'*.sif'}, 'Chose image data sequence:');
225 % strcat('data (.sif image):',' ',path_data,file_data)
226 % open a file dialog box to choose analysis file:
227 % [file_analysis,path_analysis] = uigetfile({'*.xls'}, 'Chose analysis file (trajectory):');
228 % strcat('analysis file (.xls trajectory):',' ',path_analysis,file_analysis)
229
230 disp(' ') % empty line
231 disp(['The start frame for finding bright spot trajectories will be ',num2str(start_frame)]) % start_frame is an input.
232 disp(['The end frame for finding bright spot trajectories will be ',num2str(end_frame)]) % end_frame is an input.
233 % -----
234
235
236 %% Read in the image-sequence data:
237
238 % Read image-sequence file:
239 [numFrames frame_Ysize frame_Xsize image_data image_path] = extract_image_sequence_data(image_label);
240 % See "extract_image_sequence_data.m".
241 % numFrames is the number of frames in the image sequence.
242 % To get frame number "p" do: image_data(p).frame_data.
243 % Frame dimensions are frame_Ysize and frame_Xsize.
244 % -----
245
246 % Save to parameters:
247 params.file_name = image_path;
248 params.numFrames = numFrames;
249 params.frame_Ysize = frame_Ysize;
250 params.frame_Xsize = frame_Xsize;
251
252
253 %% Calculate Signal Mask to distinguish cell region from background region:
254 % Use frame average (of first frames only) to calculate signal mask.
255
256 % Initialise frame accumulation in order to later calculate a frame average:
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257 frame_accumul = zeros(frame_Ysize,frame_Xsize);
258
259 % r is the number of frames to average over, starting from start_frame.
260 % See PARAMETERS section.
261
262 for k = start_frame:start_frame+r % loop through frames.
263     % Get frame data:
264     frame = image_data(k).frame_data; % extract frame data, stored in the field 'frame_data'.
265     frame = double(frame);
266     % Accumulate frames to then calculate frame average:
267     frame_accumul = frame_accumul + frame;
268 end
269
270 % Calculate frame average as the accumulation of all frames divided by the number of frames:
271 frame_avg = frame_accumul/(r+1);
272
273 frame_avg_Gray = mat2gray(frame_avg); % The input to function "getCellMaskAndBoundary" needs to be a grayscale image:
274
275 % Get SignalMask to know where cells are, to distinguish cells from background:
276 [SignalMask CellBoundaryMask] = getCellMaskAndBoundary(frame_avg_Gray);
277 % SignalMask is a matrix with 1 at positions where cells are and 0 at background.
278
279 % Or use getCellMaskAndBoundary2(frame,local_region),
280 % with local_region = [xleft xright ytop ybottom].
281 % [SignalMask CellBoundaryMask] = getCellMaskAndBoundary2(frame_avg_Gray,[1 frame_Xsize round(frame_Ysize/2) frame_Ysize]); % Use bottom half of image only.
282 % Using a local region for thresholding and finding the cell mask, makes this function much faster,
283 % since only spots within that cell mask will be considered.
284
285 % CHECK: uncomment the following line if you don't want to use a signal
286 % mask. Detected spots don't need to be within a signal mask:
287
288 if doNotUseCellMaskToTellSpotsRegion ==1
289     SignalMask = ones(size(frame_avg_Gray,1),size(frame_avg_Gray,2));
290 end
291
292 %% Obtain candidate bright spots for start_frame (first frame), and find spot centres for those:
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293
294 frame = image_data(start_frame).frame_data; % extract matrix data for first frame.
295 frame = double(frame);
296
297 disp(['frame number: ',num2str(start_frame)]) % print frame number to Command Window.
298
299 % Xpos is a matrix of the same size as frame, containing x values for all
300 % pixels and similarly for Ypos (used in future sections):
301 [Xpos,Ypos] = meshgrid(1:frame_Xsize,1:frame_Ysize);
302 % Note that the image thresholding occurs in two halves: separating top and bottom halves.
303 % Find candidate-bright-spots on first frame:
304 frame_Gray = mat2gray(frame); % The input to function "findCandidateSpots" needs to be a grayscale image:
305
306 [candidate_spotsX_00 candidate_spotsY_00] = findCandidateSpots(frame_Gray,2); % Second input: use method 2, which seems to
work better.
307 % See C:\Isabel\myMatlabFiles\findCandidateSpots.m.
308 % candidate_spotsX and candidate_spotsY are two column vectors of the same
309 % length containing the x and y coordinates of the candidate bright spots found on the image.
310 % They contain integer numbers: coordinates or pixel numbers which give
311 % position on image plane.
312
313 % Reject candidate spots outside cell region (to speed up algorithm):
314 candidate_spotsX_0 = []; % initialise empty vectors before loop.
315 candidate_spotsY_0 = [];
316 for nn = 1:length(candidate_spotsX_00)
317     % Only use candidates for which there is a 1 in the SignalMask image:
318     if SignalMask(candidate_spotsY_00(nn),candidate_spotsX_00(nn))==1
319         candidate_spotsX_0 = [candidate_spotsX_0; candidate_spotsX_00(nn)];
320         candidate_spotsY_0 = [candidate_spotsY_0; candidate_spotsY_00(nn)];
321     end
322 end
323
324 disp(['no. of new candidate spots on start frame: ',num2str(length(candidate_spotsX_0))])
325
326 % Error control:
327     % Limit the max number of candidate spots (if eg. 260000 candidate spots are
328     % found, we will get an error in function pdist: "Distance matrix has more
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329 % elements than the maximum allowed size in MATLAB").
330 % Select only the first max_num_candidates then.
331 if length(candidate_spotsX_0) > max_num_candidates
332     candidate_spotsX_0 = candidate_spotsX_0(1:max_num_candidates);
333     candidate_spotsY_0 = candidate_spotsY_0(1:max_num_candidates);
334     disp(['NOTE!! no. of candidate spots has been limited to ',num2str(max_num_candidates)])
335 end
336
337 % % Check graphically:
338 % imshow(frame_Gray,[]);
339 % hold on;
340 % plot(candidate_spotsX_0,candidate_spotsY_0,'*');
341 % figure;
342
343 % Find spot centres and decide if we accept them or not:
344 n =1; % Initialise index n (index for accepted spot centres which have a clipping flag equal to zero):
345 frame_to_search = frame; % Initialise frame to search for spot centres.
346
347 % Find spot centre through iterative masking:
348 for m = 1:size(candidate_spotsX_0,1) % loop through all candidate spots.
349     % Now find centre of bright spot using function findSpotCentrelframe:
350     % use candidate spots as initial estimates and then iterate to find spot centre.
351     % Image subarray ROI is a square of size 17x17 pixels (halfwidth is
352     % 8 pixels), inner circular mask that moves inside the fixed 17x17
353     % square has a radius of 5 pixels and the applied Gaussian
354     % mask has a sigma of 2 pixels:
355     spot_result = findSpotCentrelframe(frame_to_search,candidate_spotsX_0(m),candidate_spotsY_0(m),subarray_halfwidth,inner_circle_radius,gauss_mask_sigma,guess_sigma_Fit);
356     spot_result.FrameNumber = start_frame; % Add new field containing frame number (time) to result structure.
357
358
359 if (spot_result.ClipFlag == 0 && spot_result.noConverge == 0 && ...
360     spot_result.SigmaFit <= sigmaFit_max && ...
361     spot_result.SigmaFit >= sigmaFit_min && ...
362     spot_result.SNR >= SNR_min &&...
363     spot_result.rsqFit >= rsq_min) &&...
364     (exclude_region == 0 || (exclude_region ==1 && (spot_result.CentreY <(frame_Ysize/2-exclude_region_width) ||
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spot_result.CentreY > (frame_Ysize/2+exclude_region_width)))
365         % Only accept and save result of found spot if clipping flag =0 and if values of sigmaFit, signal to noise and
rsquare of fit are acceptable.
366         spot_result.SpotNumber = n; % Add new field containing spot number to result structure.
367         spot_final(start_frame,n) = spot_result; % store "good" found spots.
368         % This is also saved in the final result spot_final, structure array.
369         % first index is for frame number, second index is for spot number.
370
371         %-----
372         if deflate==1 % see parameter section at the beginning.
373             % "Deflation" process: subtract from raw frame image the corresponding
374             % Gaussian fit of each found and accepted spot before finding next spot centre (enables acceptance of dimmer
spots).
375             %
376             % Matrices containing the x and y positions in the image frame: Xpos and Ypos
377             % Xpos is a matrix of the same size as frame, containing x values for all pixels and similarly for Ypos.
378             % Calculate Xpos, Ypos at the beginning: [Xpos,Ypos] = meshgrid(1:frame_Xsize,1:frame_Ysize);
379             % Parameters of Gaussian fit of previously accepted spot:
380             x_fit = spot_final(start_frame,n).CentreX;
381             y_fit = spot_final(start_frame,n).CentreY;
382             I_fit = spot_final(start_frame,n).I0Fit;
383             sigma_fit = spot_final(start_frame,n).SigmaFit;
384             % deflated frame (frame with found spot subtracted):
385             deflated_frame = frame_to_search - I_fit*exp(-((Xpos-x_fit).^2+(Ypos-y_fit).^2)/(2*sigma_fit^2));
386             frame_to_search = deflated_frame; % update frame to search for finding next spot-centre.
387             % % Graphical check of deflated frames:
388             % subplot(1,2,1); imshow(frame,[]); % frame is the original frame (always the same).
389             % subplot(1,2,2); imshow(deflated_frame,[]);
390         end
391         %-----
392
393         n = n+1; % advance index n for accepted spot centres.
394     end
395 end
396
397 % % display the number of accepted spot-centres for this frame:
398 disp(['no. of accepted spot centres in first frame: ',num2str(n-1)])
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399
400 % convert results of found spot-centre positions to a useful form that can
401 % be used as input candidate-spots on the following frame:
402 if (n-1) == 0 % error control: if no spots were accepted.
403     found_spot_CentreX = [];
404     found_spot_CentreY = [];
405     % I need to create the whole spot_final structure with all its fields
406     % here, just in case the number of accepted spots in the first frame is
407     % zero, in order not to get error: "Subscripted assignment between
408     % dissimilar structures".
409     % Save empty spot (we need this, otherwise if in the last frame the no. of accepted spots is 0, there will be no result
spot_final(end_frame,:) and the following functions will fail).
410     spot_final(start_frame,n).CentreX = [];
411     spot_final(start_frame,n).CentreY = [];
412     spot_final(start_frame,n).IspTot = [];
413     spot_final(start_frame,n).rsqFit = [];
414     spot_final(start_frame,n).SigmaFit = [];
415     spot_final(start_frame,n).IOFit = [];
416     spot_final(start_frame,n).bg_noise_offset_afterBGsubtract = [];
417     spot_final(start_frame,n).BgNoiseStd = [];
418     spot_final(start_frame,n).IbgAvg = [];
419     spot_final(start_frame,n).IbgTot = [];
420     spot_final(start_frame,n).SNR = [];
421     spot_final(start_frame,n).IinnerTot = [];
422     spot_final(start_frame,n).ClipFlag = [];
423     spot_final(start_frame,n).noConverge = [];
424     spot_final(start_frame,n).TrajNumber = [];
425     spot_final(start_frame,n).FrameNumber = [];
426     spot_final(start_frame,n).SpotNumber = [];
427 else
428     found_spot_CentreX = [spot_final(start_frame,:).CentreX]'; % column vector with found CentreX positions of all candidate
spots.
429     found_spot_CentreY = [spot_final(start_frame,:).CentreY]'; % column vector with found CentreY positions of all candidate
spots.
430 end
431
432 % Check graphically:
```

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433 figure;
434 imshow(frame_Gray,[]);
435 hold on;
436 plot(found_spot_CentreX,found_spot_CentreY,'o','Color','g','MarkerSize',10) % plot accepted spot centres in green.
437 pause(0.1); % this pause is needed to give time for the plot to appear
438 hold off;
439 % -----
440
441
442 %% Loop through selected frames:
443
444 tr =1; % initialise trajectory index.
445
446 for k = (start_frame+1):end_frame
447     % to go through all frames do instead: for k = 1:length(sifData)
448
449     frame = image_data(k).frame_data; % extract frame data which is stored in field 'frame_data'.
450     frame = double(frame);
451
452     imshow(frame,[],'Border','tight','InitialMagnification',150); % show image scaled between its min and max values ([]).
453     hold on;
454
455     disp(['frame number: ',num2str(k)]) % print frame number to Command Window.
456
457     %-----
458     % Find new candidate spots for this frame:
459     frame_Gray = mat2gray(frame); % The input to function "findCandidateSpots" needs to be a grayscale image:
460
461     [candidate_spotsX_00 candidate_spotsY_00] = findCandidateSpots(frame_Gray,2); % Second input: use method 2, which seems
to work better.
462     % the subindex "_00" in candidate_spotsX_00 indicates newly found spot
463     % candidates for the current frame. On the other hand, found_spot_CentreX and found_spot_CentreY are the
464     % accepted spot-centre positions coming from the previous frame.
465
466     % Reject candidate spots outside cell region (SignalMask) (to speed up algorithm):
467     candidate_spotsX_0 = []; % initialise empty vectors before loop.
468     candidate_spotsY_0 = [];
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```
469     for nn = 1:length(candidate_spotsX_00)
470         % Only use candidates for which there is a 1 in the SignalMask image:
471         if SignalMask(candidate_spotsY_00(nn),candidate_spotsX_00(nn))==1
472             candidate_spotsX_0 = [candidate_spotsX_0; candidate_spotsX_00(nn)];
473             candidate_spotsY_0 = [candidate_spotsY_0; candidate_spotsY_00(nn)];
474         end
475     end
476
477     disp(['no. of new candidate spots: ',num2str(length(candidate_spotsX_0))])
478     %-----
479
480     % Join accepted spot-centre positions from previous frame with
481     % candidate spots for this frame to use them as new candidates for this frame:
482     candidate_spotsX = [found_spot_CentreX; candidate_spotsX_0];
483     candidate_spotsY = [found_spot_CentreY; candidate_spotsY_0];
484
485     % Plot new candidate spots in yellow and found spot centres from
486     % previous frame in cyan
487     % plot(candidate_spotsX_0,candidate_spotsY_0,'+','Color','y','MarkerSize',3);
488     % pause(0.5);
489     % plot(found_spot_CentreX,found_spot_CentreY,'+','Color','c','MarkerSize',3);
490     % pause(0.5);
491
492     disp(['no. of initial total candidate spots: ',num2str(length(candidate_spotsX))])
493
494     % Error control:
495     % Limit the max number of candidate spots (if eg. 260000 candidate spots are
496     % found, we get an error in function pdist: "Distance matrix has more
497     % elements than the maximum allowed size in MATLAB").
498     % Select only the first max_num_candidates then.
499     if length(candidate_spotsX) > max_num_candidates
500         candidate_spotsX = candidate_spotsX(1:max_num_candidates);
501         candidate_spotsY = candidate_spotsY(1:max_num_candidates);
502         disp(['NOTE!! no. of initial total candidate spots has been limited to ',num2str(max_num_candidates)])
503     end
504
505     %-----
```

```
506 % Eliminate coincidences in spot candidates:
507
508 [candidate_spotsX candidate_spotsY pos] = eliminateCoincidentSpots(candidate_spotsX,candidate_spotsY,d_coincid_cand);
509 % see C:\Isabel\myMatlabFiles\eliminateCoincidentSpots.m
510 % The function checks the distances between all pairs of points with x
511 % and y coordinates candidate_spotsX and candidate_spotsY respectively,
512 % and removes those points (x,y) which are closer than one pixel (distance<1) to
513 % another point in the list.
514
515 % % for debugging:
516 % x2 = candidate_spotsX;
517 % y2 = candidate_spotsY;
518
519 disp(['no. of total candidate spots after eliminating coincidences: ',num2str(length(candidate_spotsX))])
520
521 % % Plot all candidate spots in magenta after removing coincidences:
522 % plot(candidate_spotsX,candidate_spotsY,'+','Color','m','MarkerSize',3);
523 % pause(0.5);
524 %-----
525
526
527 n =1; % Initialise index n (index for accepted spot centres which have a clipping flag equal to zero):
528 frame_to_search = frame; % Initialise frame to search for spot centres.
529
530 for m = 1:size(candidate_spotsX,1) % for each frame, loop throuh all the candidate spots.
531 % Now find centre of bright spot using function findSpotCentreIframe:
532 % use candidate spots as initial estimates and then iterate to find spot centre.
533 % Image subarray ROI is a square of size 17x17 pixels (halfwidth is
534 % 8 pixels), inner circular mask that moves inside the fixed 17x17
535 % square has a radius of 5 pixels and the applied Gaussian
536 % mask has a sigma of 2 pixels:
537 spot_result = findSpotCentreIframe(frame_to_search,candidate_spotsX(m),candidate_spotsY(m),subarray_halfwidth,inner_circle_radius,gauss_mask_sigma,guess_sigma_Fit);
538 % index k is for frame number, index m is for spot number
539 spot_result.FrameNumber = k; % Add new field containing frame number (time) to result structure.
540
541 % accepted spot centres:
```

```

542     if (spot_result.ClipFlag == 0 && spot_result.noConverge == 0 && ...
543         spot_result.SigmaFit <= sigmaFit_max && ...
544         spot_result.SigmaFit >= sigmaFit_min && ...
545         spot_result.SNR >= SNR_min &&...
546         spot_result.rsqFit >= rsq_min)&&...
547         (exclude_region == 0 || (exclude_region ==1 && (spot_result.CentreY <(frame_Ysize/2-exclude_region_width) ||
spot_result.CentreY >(frame_Ysize/2+exclude_region_width))))
548         % Only accept and save result of found spot if clipping flag =0 and if values of sigmaFit, signal to noise and
rsquare of fit are acceptable.
549         spot(k,n) = spot_result; % store accepted found spots in this preliminary result.
550         % first index is for frame number, second index is for spot number.
551         % -----
552         %         plot(spot(k,n).CentreX,spot(k,n).CentreY,'o','Color','r','MarkerSize',10); % Plot found centre spots
in red
553         % -----
554         if deflate==1 % see parameter section at the beginning.
555             % "Deflation" process: subtract from raw frame image the corresponding
556             % Gaussian fit of each found and accepted spot before finding
557             % next spot centre (enables acceptance of dimmer spots).
558             % Xpos and Ypos are matrices of x and y positions on image frame.
559             % Parameters of Gaussian fit of previously accepted spot:
560             x_fit = spot(k,n).CentreX;
561             y_fit = spot(k,n).CentreY;
562             I_fit = spot(k,n).IOFit;
563             sigma_fit = spot(k,n).SigmaFit;
564             % deflated frame (frame with found spot subtracted):
565             deflated_frame = frame_to_search - I_fit*exp(-((Xpos-x_fit).^2+(Ypos-y_fit).^2)/(2*sigma_fit^2));
566             frame_to_search = deflated_frame; % update frame for finding next spot-centre.
567             % % Graphical check of deflated frames:
568             % subplot(1,2,1); imshow(frame,[]); % frame is the original frame (always the same).
569             % subplot(1,2,2); imshow(deflated_frame,[]);
570         end
571         %-----
572
573         n = n+1; % and advance index n for accepted spot centres.
574     end
575

```



```
576     end
577
578     % display the number of accepted spot-centres for each frame:
579     disp(['no. of accepted spot centres: ',num2str(n-1)])
580
581     % % The following two lines are used together with the previous two
582     % "plot" and "imshow" (commented off) lines:
583     pause(0.1); % this pause is needed to give time for the plot to appear
584     %     hold off;
585
586     % convert results of found spot-centre positions to a useful form that can
587     % be used as input candidate-spots on the following frame:
588     if (n-1) == 0 % error control: if no spots were accepted.
589         found_spot_CentreX = [];
590         found_spot_CentreY = [];
591         spot_final(k,n).SpotNumber = []; % Save empty spot (we need this, otherwise if in the last frame the no. of accepted
spots is 0, there will be no result spot_final(end_frame,:) and the following functions will fail).
592     else
593         found_spot_CentreX = [spot(k,:).CentreX]'; % column vector with found CentreX positions of all candidate spots.
594         found_spot_CentreY = [spot(k,:).CentreY]'; % column vector with found CentreY positions of all candidate spots.
595
596         %-----
597         % Eliminate coincidences in result of last found spots for a given frame (for distance <1):
598         [found_spot_CentreX found_spot_CentreY pos_final] = eliminateCoincidentSpots(found_spot_CentreX,found_spot_CentreY,
d_coincid_found);
599         % see C:\Isabel\myMatlabFiles\eliminateCoincidentSpots.m
600         % pos_final contains positions of selected, kept spot centres.
601         %-----
602
603         % Save final spots to variable final_spots:
604         n=1; % index for final kept spot.
605         for ii = 1:length(pos_final)
606             mientras = spot(k,pos_final(ii)); % intermediate result.
607             mientras.SpotNumber = n; % Add new field containing spot number to result structure.
608             spot_final(k,n)=mientras; % final result structure of accepted spot centres.
609             n = n+1;
610         end
```

```
611     % Plot found spot centres:
612     pause(0.5);
613     plot(found_spot_CentreX,found_spot_CentreY,'o','Color','g','MarkerSize',10) % plot final accepted spot centres in
green.
614     pause(0.1); % this pause is needed to give time for the plot to appear
615     hold off;
616
617     disp(['no. of final found spot centres after eliminating coincidences: ',num2str(length(found_spot_CentreX))])
618 end
619
620
621
622 %-----
623 % LINKING SPOTS INTO TRAJECTORY SEGMENTS:
624
625 % Link found and accepted spots into trajectory segments:
626
627 % Trajectory index tr is initialised to 1 outside the loop through frames (k loop).
628
629 % Do differently FOR SECOND FRAME (k == start_frame+1): compare only accepted spots in
630 % previous and current frames:
631 if k == start_frame+1 && ... % If second frame and
632     (n-1)~=0 && ... % if the number of accepted spot centres is not zero and
633     isempty([spot_final(k-1,:).SpotNumber])==0 && ... % at least 1 accepted spot in previous frame and
634     isempty([spot_final(k,:).SpotNumber])==0 % at least 1 accepted spot in current frame.
635     % There are no trajectories yet, so compare accepted spots in previous and current frames:
636     N0 = max(cat(1,spot_final(k-1,:).SpotNumber)); % no. of accepted spots in previous frame.
637     % Note: cat(1,spot_final(k-1,:).SpotNumber) gives a column vector with the values of SpotNumber for all non-empty
accepted spots in frame k-1.
638     N1 = max(cat(1,spot_final(k,:).SpotNumber)); % no. of accepted spots in current frame.
639
640     % Create cell arrays with empty elements to pre-assign sizes:
641     d01 = cell(N0,N1); % Note: d01 is a cell array (matrix) but d_01 below is a scalar.
642     Iratio01 = cell(N0,N1); % Note: Iratio01 is a cell array (matrix) but Iratio_01 below is a scalar.
643     SigmaRatio01 = cell(N0,N1); % Note: SigmaRatio01 is a cell array (matrix) but SigmaRatio_01 below is a scalar.
644
645     for q0 = 1:N0 % loop though accepted spots in previous frame.
```

```

646     for q1 = 1:N1 % loop though accepted spots in current frame.
647         % d_01: distance between spot centres in previous and current frames:
648         d_01 = sqrt((spot_final(k-1,q0).CentreX-spot_final(k,q1).CentreX)^2+(spot_final(k-1,q0).CentreY-spot_final(k,
q1).CentreY)^2);
649         % Iratio_01: ratio of intensities of spot centre in previous and current frames:
650         Iratio_01 = spot_final(k-1,q0).IspTot/spot_final(k,q1).IspTot;
651         % SigmaRatio_01: ratio of widths of spots (Gaussian fits) in previous and current frames:
652         SigmaRatio_01 = spot_final(k-1,q0).SigmaFit/spot_final(k,q1).SigmaFit;
653
654         %           d_01
655         %           Iratio_01
656         %           SigmaRatio_01
657
658         % Accept and save trajectory if spots in previous and
659         % current frames fulfill the following conditions:
660         if d_01 < d_01_max && ... % see PARAMETERS at start of this function.
661             Iratio_01_min <= Iratio_01 && Iratio_01 <= Iratio_01_max && ...
662             SigmaRatio_01_min <= SigmaRatio_01 && SigmaRatio_01 <= SigmaRatio_01_max
663             % Assign accepted values to cell array elements to store them:
664             d01{q0,q1} = d_01; % use {} for cell arrays.
665             Iratio01{q0,q1} = Iratio_01;
666             SigmaRatio01{q0,q1} = SigmaRatio_01;
667         else % rejected assignments:
668             d01{q0,q1} = rej; % Use rej for assignments not accepted (images usually 512x512arrays, so rej pix is an
impossibly large distance, this is why it is chosen here).
669             Iratio01{q0,q1} = rej; % Use rej for assignments not accepted.
670             SigmaRatio01{q0,q1} = rej; % Use rej for rejected assignments.
671         end
672     end
673
674     %           d01
675     %           [d01{q0,:}]
676     % Note that [d01{q0,:}] gives only non-empty elements of row q0
677     % in the cell array d01 as a row vector, that's why we had to
678     % give a numeric value rej to non-accepted assignments.
679
680     % Note that if all assignments in previous step are rejected,

```

```

681     % [d01{q0,:}] will be a list of rej values, and its minimum will
682     % be rej.
683     % If list of "linkable" spots, [d01{q0,:}], has no accepted
684     % assignments (all values are rej):
685     if min([d01{q0,:}]) == rej
686         % Assign trajectory number 0 to the spot in the previous frame only:
687         spot_final(k-1,q0).TrajNumber = 0;
688     else % if there is at least one accepted assignment for a given spot in the previous frame:
689
690         % Decide of all possible accepted spots (in current frame)
691         % that could be linked to spot q0 in previous frame, which one is the best:
692         % We take the best as the closest one to spot q0:
693         q1_chosen = find([d01{q0,:}] == min([d01{q0,:}]))); % find position of the minimum pair-wise distance.
694
695         %
696         % Check if there is a better competing assignment for a given spot q1 in the current
697         % frame from another spot in the previous frame.
698         % Hence, check also column-wise in matrix d01 to avoid assigning a traj
699         % number to a spot q1 in the current frame that had already
700         % had a traj number assigned to it linking it to a different spot q0 in
701         % the previous frame, which might be at a shorter distance
702         % from it than the current one.
703
704         %
705         % [d01{:,q1_chosen}] % chosen column of d01 matrix of distances.
706
707         % Assign trajectory numbers to structure spot_final:
708         % If the found distance in that column is not the minimum one:
709         if q0 ~= find([d01{:,q1_chosen}] == min([d01{:,q1_chosen}])));
710             spot_final(k-1,q0).TrajNumber = 0; % assign trajectory number 0 to spot in previous frame.
711         else
712             spot_final(k-1,q0).TrajNumber = tr; % assign trajectory number to spot in previous frame, to spot_final
713             structure.
714             spot_final(k,q1_chosen).TrajNumber = tr; % assign same trajectory number to spot in current frame.
715             tr = tr+1; % advance trajectory-number index.
716         end
717     end

```



```

752
753     % Accept and save trajectory if spots in previous and
754     % current frames fulfill the following conditions:
755     if d_02 < d_02_max && ... % see PARAMETERS at start of this function.
756         Iratio_02_min <= Iratio_02 && Iratio_02 <= Iratio_02_max && ...
757         SigmaRatio_02_min <= SigmaRatio_02 && SigmaRatio_02 <= SigmaRatio_02_max
758         % Assign accepted values to cell array elements to store them:
759         d02{q0,q1} = d_02; % use {} for cell arrays.
760         Iratio02{q0,q1} = Iratio_02;
761         SigmaRatio02{q0,q1} = SigmaRatio_02;
762     else % rejected assignments:
763         d02{q0,q1} = rej; % Use rej for assignments not accepted (images usually 512x512arrays, so rej pix
764         % is an impossibly large distance, this is why it is chosen here).
765         Iratio02{q0,q1} = rej; % Use rej for assignments not accepted.
766         SigmaRatio02{q0,q1} = rej; % Use rej for rejected assignments.
767     end
768 end
769 %
770 %           d02
771 %           [d02{q0,:}]
772 % Note that [d02{q0,:}] gives only non-empty elements of the cell array d01 as a row vector.
773
774 % Note that if all assignments in previous step are rejected,
775 % [d02{q0,:}] will be a list of rej values, and its minimum will be rej.
776 % If list of "linkable" spots, [d02{q0,:}], has no accepted assignments (all values are rej):
777 if min([d02{q0,:}]) == rej
778     % Assign trajectory number 0 to the spot two frames ago only:
779     spot_final(k-2,q0).TrajNumber = 0; % point stays loose (unlinked).
780
781 else % if there is at least one accepted assignment for a given spot two frames ago:
782
783     % Decide of all possible accepted/saved spots (in current frame)
784     % that could be linked to spot q0 in previous frame (of all possible assignments), which one is the
785     best:
786     % We take the best as the closest one to spot q0:
787     q1_chosen = find([d02{q0,:}] == min([d02{q0,:}])); % find position of the minimum pair-wise distance.

```



```

822     N1 = max(cat(1,spot_final(k,:).SpotNumber)); % no. of accepted spots in current frame.
823
824     % Create cell arrays with empty elements to pre-assign sizes.
825     d01 = cell(N0,N1);
826     Iratio01 = cell(N0,N1);
827     SigmaRatio01 = cell(N0,N1);
828
829     for q0 = 1:N0 % loop though accepted spots in previous frame.
830         for q1 = 1:N1 % loop though accepted spots in current frame.
831             % d_01: distance between spot centres in previous and current frames:
832             d_01 = sqrt((spot_final(k-1,q0).CentreX-spot_final(k,q1).CentreX)^2+(spot_final(k-1,q0).CentreY-
spot_final(k,q1).CentreY)^2);
833             % Iratio_01: ratio of intensities of spot centre in previous and current frames:
834             Iratio_01 = spot_final(k-1,q0).IspTot/spot_final(k,q1).IspTot;
835             % SigmaRatio_01: ratio of widths of spots (Gaussian fits) in previous and current frames:
836             SigmaRatio_01 = spot_final(k-1,q0).SigmaFit/spot_final(k,q1).SigmaFit;
837
838             %           d_01
839             %           Iratio_01
840             %           SigmaRatio_01
841
842             % Accept and save trajectory if spots in previous and
843             % current frames fulfill the following conditions:
844             if d_01 < d_01_max && ... % see PARAMETERS at start of this function.
845                 Iratio_01_min <= Iratio_01 && Iratio_01 <= Iratio_01_max && ...
846                 SigmaRatio_01_min <= SigmaRatio_01 && SigmaRatio_01 <= SigmaRatio_01_max
847                 % Assign accepted values to cell array elements to store them:
848                 d01{q0,q1} = d_01; % use {} for cell arrays.
849                 Iratio01{q0,q1} = Iratio_01;
850                 SigmaRatio01{q0,q1} = SigmaRatio_01;
851             else % rejected assignments:
852                 d01{q0,q1} = rej; % Use rej for assignments not accepted (images usually 512x512arrays, so rej pix is
an impossibly large distance, this is why it is chosen here).
853                 Iratio01{q0,q1} = rej; % Use rej for assignments not accepted.
854                 SigmaRatio01{q0,q1} = rej; % Use rej for rejected assignments.
855             end
856         end

```



```
857
858 %                               d01
859 %                               [d01{q0,:}] % last row of d01 matrix of distances.
860 % Note that [d01{q0,:}] gives only non-empty elements
861 % of row q0 in the cell array d01, as a row vector.
862
863 % Note that if all asignments in previous step are rejected,
864 % [d01{q0,:}] will be a list of rej values, and its minimum will
865 % be rej.
866 % If list of "linkable" spots, [d01{q0,:}], has no accepted
867 % asignments (all values are rej):
868 if min([d01{q0,:}]) == rej
869
870     if isempty(spot_final(k-1,q0).TrajNumber) % if point in previous frame was not part of a trajectory ✓
871         (TrajNumber=[]):
872             % Assign trajectory number 0 to the spot in the previous frame only:
873             spot_final(k-1,q0).TrajNumber = 0;
874         end
875     else % if there is at least one accepted assignment for a given spot two frames ago:
876
877         % Decide of all possible accepted/saved spots (in current frame)
878         % that could be linked to spot q0 in previous frame, which one is the best:
879         % We take the best as the closest one to spot q0:
880         q1_chosen = find([d01{q0,:}] == min([d01{q0,:}])); % find position of the minimum pair-wise distance.
881
882 %                               q1_chosen
883
884 % Check if there is a better competing asignment for a given spot q1 in the current
885 % frame from another spot q0 in the previous frame.
886 % Hence, check also column-wise in d01 to avoid assigning a traj
887 % number to a spot q1 in the current frame that had already
888 % had a traj number assigned to it linking it to a different spot q0 in
889 % the previous frame which might be at a shorter distance
890 % from it than the current one.
891
892 %                               [d01{:,q1_chosen}] % chosen column of d01 matrix of distances.
```



```
928 % each of which is a structure with fields:
929 %     'CentreX'
930 %     'CentreY'
931 %     'IspTot'
932 %     'rsqFit'
933 %     'SigmaFit'
934 %     'I0Fit'
935 %     'BgNoiseStd'
936 %     'IbgAvg'
937 %     'IbgTot'
938 %     'SNR'
939 %     'IinnerTot'
940 %     'ClipFlag'
941 %     'TrajNumber'
942 %     'FrameNumber'
943 %     'SpotNumber'
944 %
945 % Along the dimension L, we have the different bright spots found on each
946 % frame (L will often be the number of spot centres found in frame_start,
947 % it is always the largest number of spots ever accepted on one frame).
948 % For example, spot_final(100,8) is a structure with the above fields
949 % corresponding to the eighth found spot on frame 100.
950 %
951 % Note that even if we only analyse from start_frame to end_frame,
952 % spot_final is a list containing empty structure arrays from index 1 to
953 % index start_frame, and then the found spots for the analysed frames start_frame to end_frame.
954 %
955 % The result is padded to a fixed number of spot structures for reach
956 % frame (the maximum no. of accepted found spots of all frames), so that for a given
957 % frame in which less found spots have been accepted, the remaining
958 % elements are padded with empty structures with empty fields [].
959 % To check if a given spot is empty: isempty(spot_final(101,10).CentreX)
960 % gives 1 if field "CentreX" of tenth spot found and accepted in frame 101
961 % is empty (equal to []).
962 %
963 % e.g. cat(1,spot_final(100,:).SigmaFit) gives a vector column with all the
964 % non-empty SigmaFit values for all spot centres accepted in frame 100.
```

965