



Game Physics

Simple Physics Engine

CS 415: Game Development

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Source: Millington, Ian. Game Physics Engine Development, Second Edition.



Newtonian Physics

Let's build a simple game physics engine!

- We will animate particles (aka point masses)
 - Position is changed by velocity
 - Velocity is changed by acceleration
 - Forces alter acceleration
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- Our physics engine will integrate to compute
 - Position
 - Velocity
 - We set the acceleration by applying forces

Force and Mass and Acceleration

- How do we update acceleration when force is applied?
- To find the acceleration due to a force we have

$$\ddot{\mathbf{p}} = \frac{1}{m} \mathbf{f}$$

- So we need to know the inverse mass of the particle
 - You can model infinite mass objects by setting this value to 0

Force: Gravity

- Law of Universal Gravitation

$$f = G \frac{m_1 m_2}{r^2}$$

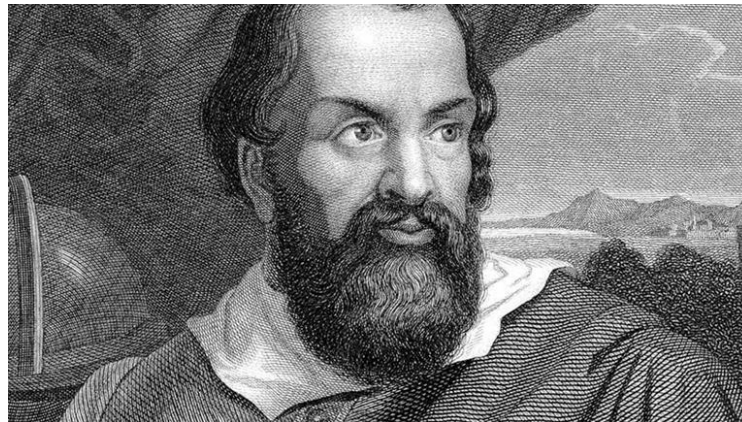
- G is a universal constant
- m_i is the mass of an object
- r is the distance between object centers
- if we care only about gravity of the Earth
 - m_1 and r are constants
 - r is about 6400 km on Earth
- We simplify to $f = mg$
 - g is about 10ms^{-2}

Acceleration due to Gravity

- If we consider acceleration due to gravity we have

$$\ddot{p} = \frac{1}{m}(mg) = g$$

- So acceleration due to gravity is independent of mass



Acceleration due to Gravity

- Typically the magnitude and direction of acceleration would be

$$\mathbf{g} = \langle 0, -g, 0 \rangle$$

- For gaming, 10ms^{-2} tends to look boring
 - Shooters often use 15ms^{-2}
 - Driving games often use 20ms^{-2}
 - Some tune g object-by-object

Force: Drag

- Drag dampens velocity
 - Caused by friction with the medium the object moves through
- Even neglecting drag, you need to dampen velocity
 - Otherwise numerical errors likely drive it higher than it should be
- A velocity update with drag can be implemented as

$$\dot{\mathbf{p}}_{new} = \dot{\mathbf{p}} d^t$$

- important to incorporate time so drag changes if the frame rate varies
- What range should d be in?

The Integrator

- The position update can found using Euler's Method:

$$p_{new} = p + \dot{p}t$$

- This is a pretty inaccurate approximation of analytical integration
 - formula gets more inaccurate as acceleration gets larger...why?
 - In general we can characterize Euler method error as $O(t)$
 - ...almost good enough for game engines...most use semi-implicit Euler
- The velocity update is computed using Euler integration as well

$$\dot{p}_{new} = \dot{p}d^t + \ddot{p}t$$

The Timestep

How does the timestep effect the accuracy of the engine?

How would you see that error in a game?

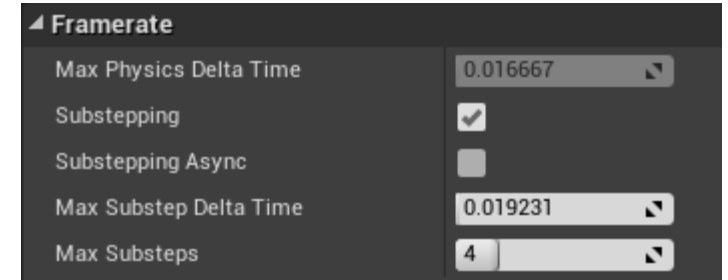
Timestep in games uses wall-clock time (sometimes a scaled version)

- Also related to framerate

If the physics timestep is tied to the framerate, what can happen?

UE Substepping

In UE look at *Project Settings > Engine > Physics*



- Substepping creates a degree of framerate independence for physics
- When framerate drops, Unreal will add extra physics iterations
- Physics timestep will not exceed the max delta time

Example:

- 16 ms Max Delta Time
- Above 60fps no substepping
- In 30 to 60 fps 2 steps