Bezier Curves

Cubic Bezier Curves

A Bezier curve is a parametric polynomial curve given by:

$$X(t) = (1-t)^3b_0 + 3(1-t)^2tb_1 + 3(1-t)t^2b_2 + t^3b_3$$

where b_i are the control points.

The tangent vector of the curve can be found by

$$X(t) = 3(b_1 - b_0)(1 - t)^2 + 6(\dot{b}_2 - b_1)(1 - t)t + 3(b_3 - b_2)t^2$$

1. The de Casteljau Algorithm

Suppose our control points are

$$b_0 = (-1,0)$$
 $b_1 = (0,1)$ $b_2 = (0,-1)$ $b_3 = (1,0)$

Use the de Casteljau algorithm to find the coordinates of X(1/4). Check that you get the same answer from using the parametric expression given above.

2. Tangents to a Bezier Curve

a. What are the tangents at the controls b₀ and b₃? Give the answer as a pair of parameterized functions.

b. What is the tangent vector at *t*=0.25 for the curve given in question one?