

Hidden Surface Removal

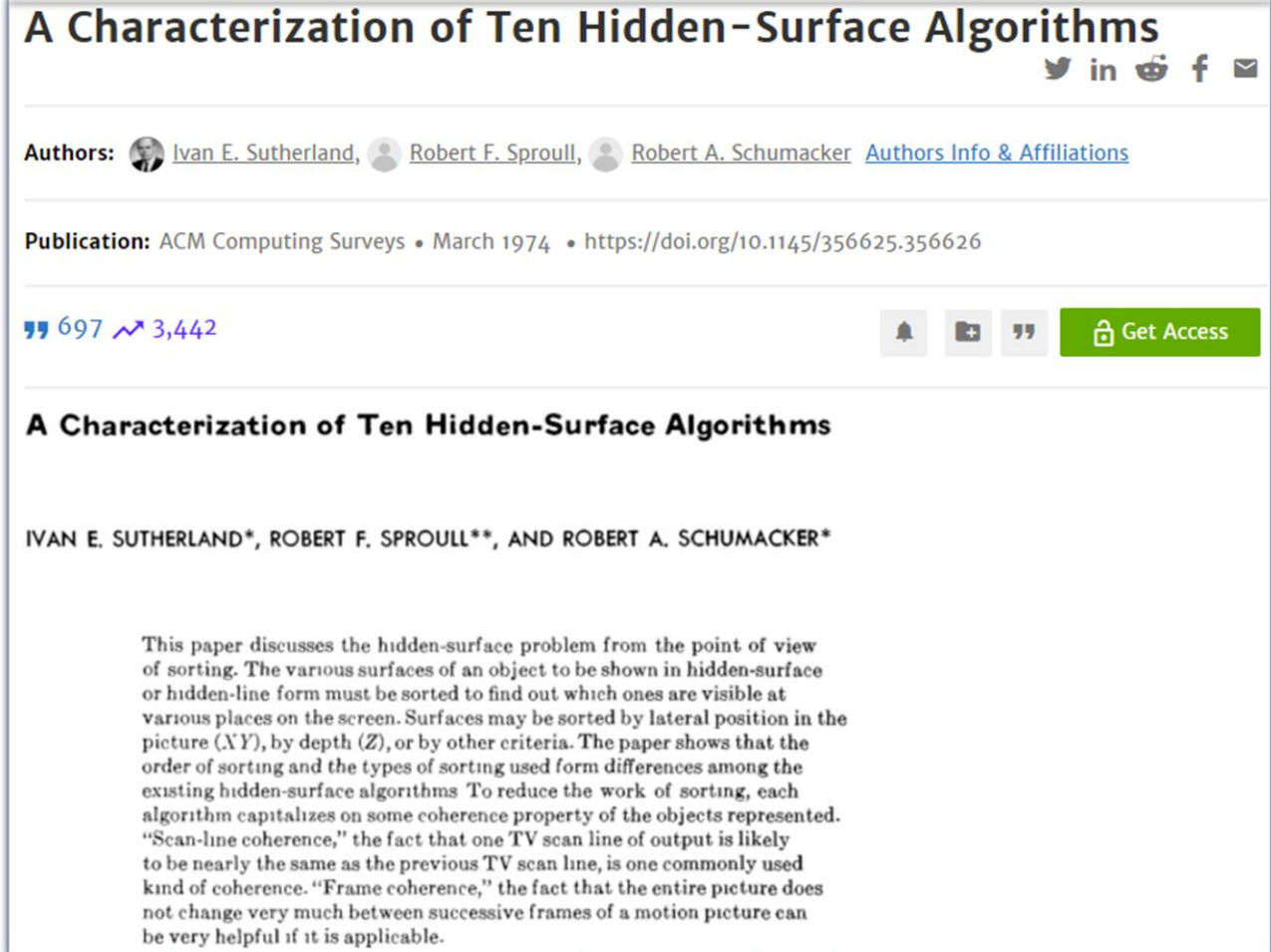


Interactive Computer Graphics
Eric Shaffer

Hidden Surface Removal

Simple problem statement:

- don't render surfaces occluded by surfaces in front
- Was a significant area of research in early days of CG
- lots of algorithms suggested

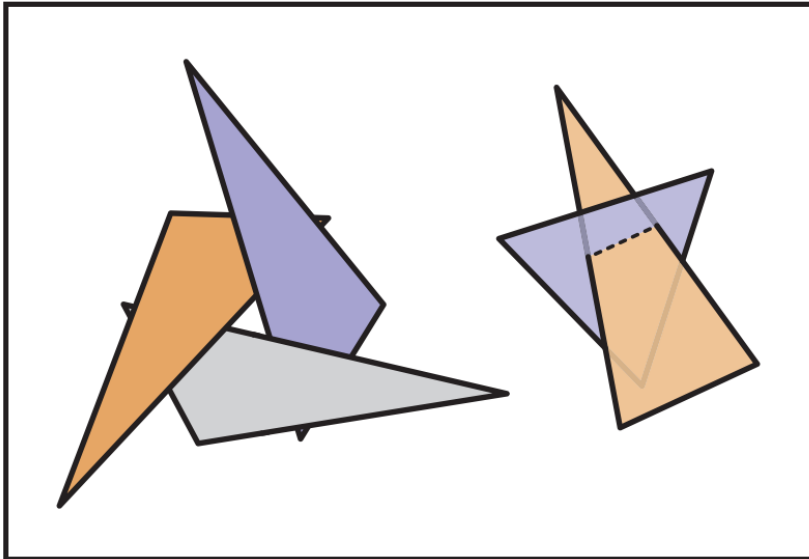


Hidden Surface Removal

- Hidden Surface Removal
 - ...don't render surfaces occluded by surfaces in front of them
- Was a significant area of research in early days of CG
 - ...lots of algorithms suggested
- Painter's Algorithm
 - Render objects in order from back to front
 - i.e. sort your triangles by depth and render deepest first
 - Can anyone imagine any problems with this approach?

Problems with the Painter's Algorithm

- No correct rendering order for
 - intersecting triangle
 - occlusion cycles



- Sorting is slow...too slow for interactivity in complex scenes

Hidden Surface Removal: Z-Buffer

Key Observation:

Each pixel displays color of only one triangle,
Ignores everything behind it

Don't need to sort triangles, just find, for each pixel, the closest triangle

Z-buffer: one fixed or floating point value per pixel

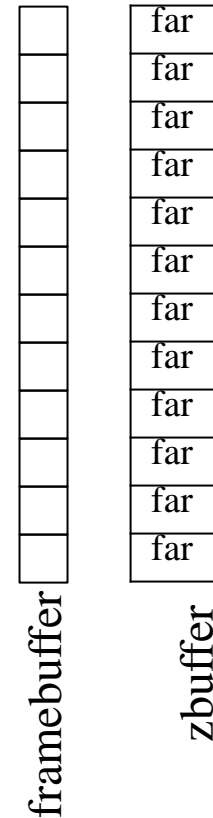
Algorithm:

For each rasterized fragment (x,y)

If $z < \text{zbuffer}(x,y)$ then

$\text{framebuffer}(x,y) = \text{fragment color}$

$\text{zbuffer}(x,y) = z$



Frame Buffer: buffer that stores the colors for the pixels we will render

Z-Buffer

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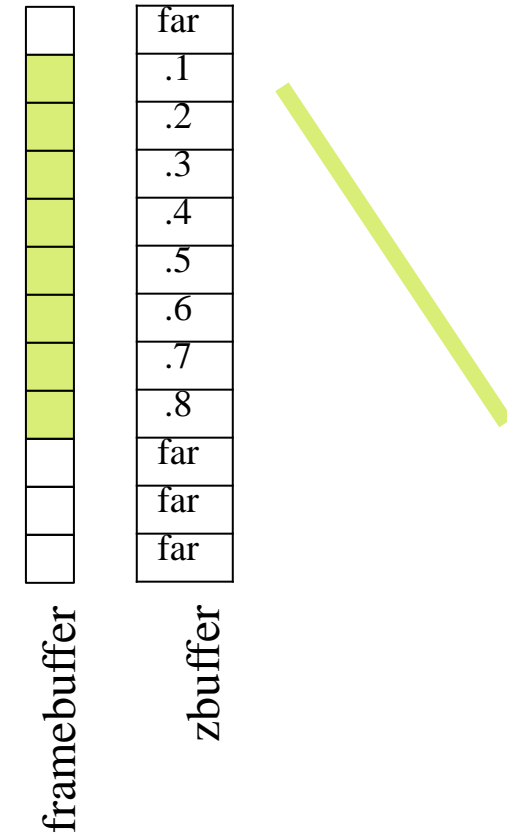
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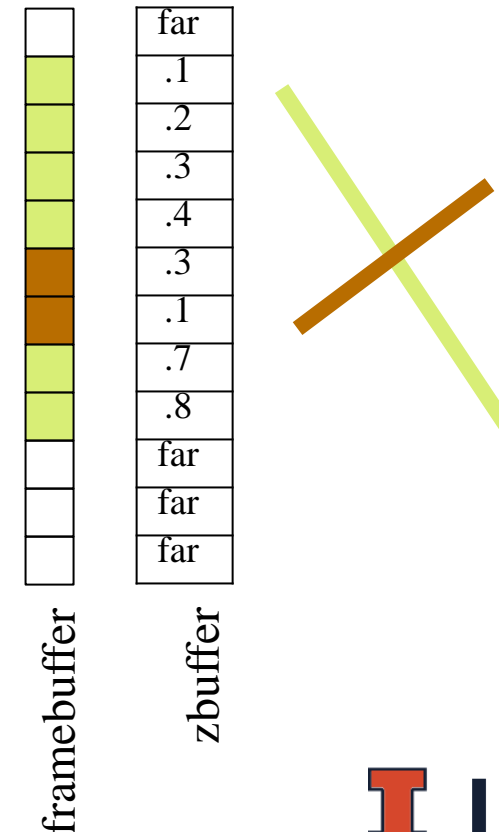
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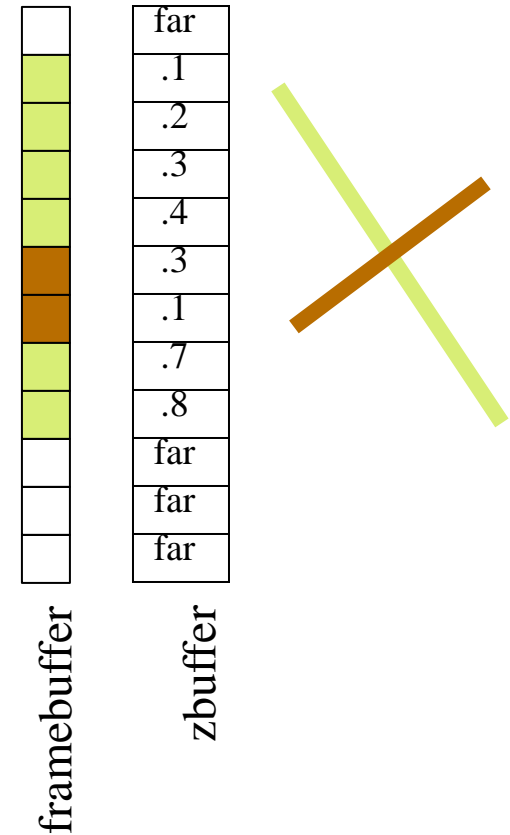


Z-Buffer

Get fragment z-values by interpolating z-values at vertices during rasterization

True perspective projection destroys z-values, setting them all to $-d$

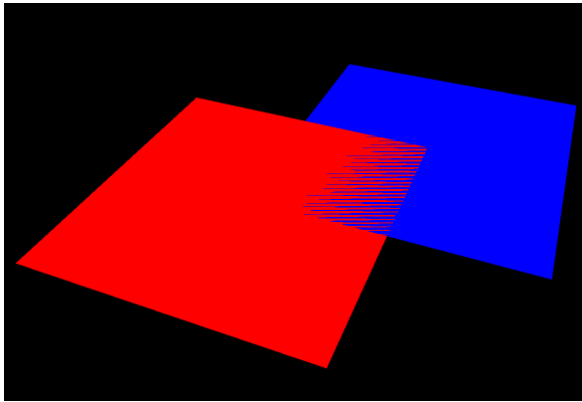
The perspective distortion we use preserves at least the ordering of z-values



Precision Issues with Z-Buffering

- In practice, depths values are typically converted to non-negative integers
 - Comparison operation needs to be fast...
- Imagine having depth values of $\{0, 1, \dots, B-1\}$
 - $0 \rightarrow$ near clipping plane distance
 - $B-1 \rightarrow$ far clipping plane distance
- Depths occur discretely in “buckets”
 - Each bucket covers a range of length $\Delta z = \frac{f-n}{B}$
- If we use b bits for the z-buffer values, $B = 2^b$
 - You usually can't change the value b
 - To maximize z-buffer effectiveness, **need to minimize $f-n$**

Z-Fighting



How can you fix z-fighting?

1. Move co-planar polygons slightly away from each other
2. Move near and far clipping planes as close together as you feasibly can

Actually, It's Worse Than That....

Post-projection depth value does NOT vary linearly with input depth p_z

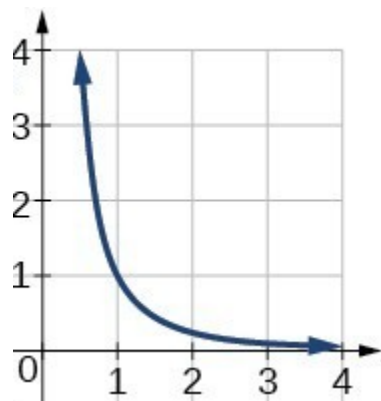
$$\mathbf{P}_{\text{OpenGL}} = \begin{pmatrix} \frac{2n'}{r-l} & 0 & \frac{r+l}{r-l} & 0 \\ 0 & \frac{2n'}{t-b} & \frac{t+b}{t-b} & 0 \\ 0 & 0 & -\frac{f'+n'}{f'-n'} & -\frac{2f'n'}{f'-n'} \\ 0 & 0 & -1 & 0 \end{pmatrix}$$

$$\mathbf{v} = \mathbf{P}\mathbf{p} = \begin{pmatrix} \dots \\ \dots \\ dp_z + e \\ \pm p_z \end{pmatrix}$$

$$d = -(f' + n') / (f' - n')$$

$$e = -2f'n' / (f' - n')$$

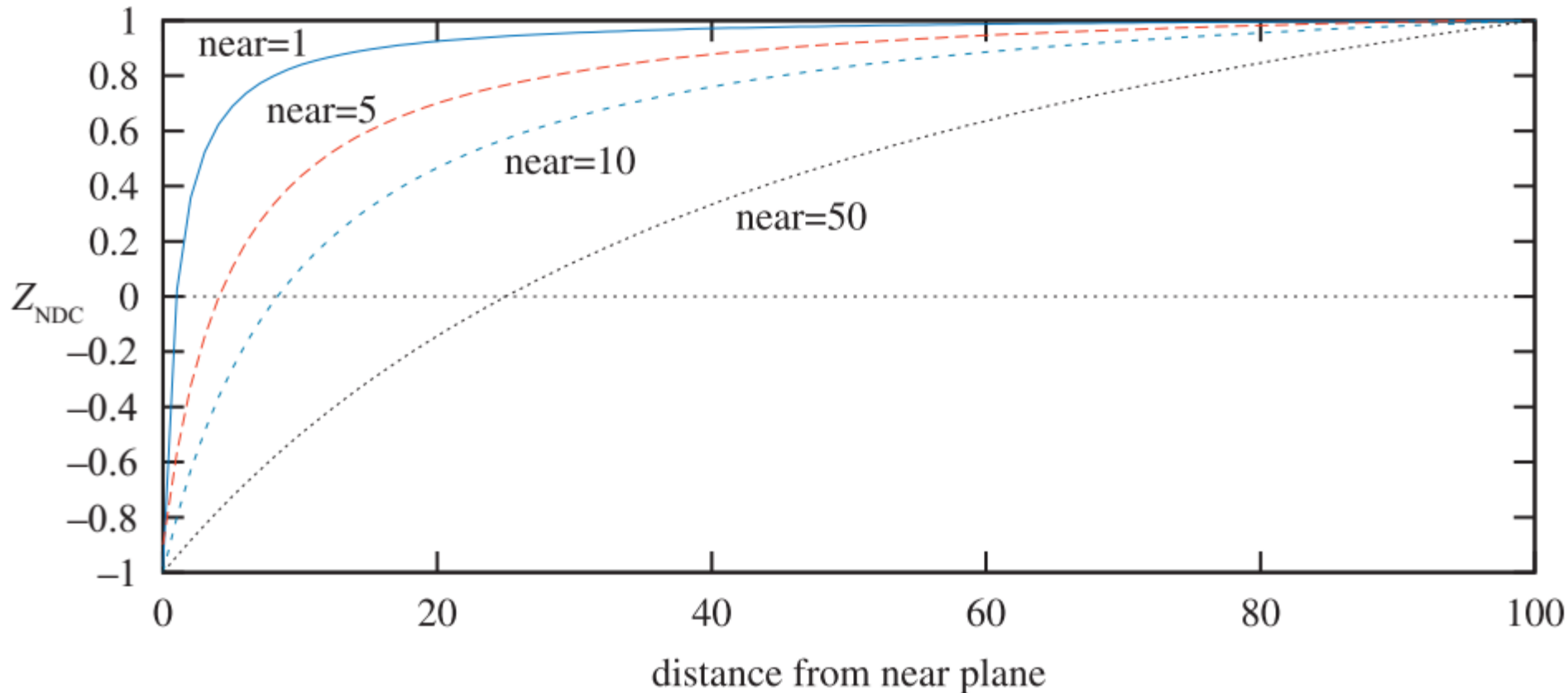
Output depth is inversely proportional to the input depth



$$z_{\text{NDC}} = \frac{dp_z + e}{-p_z} = d - \frac{e}{p_z}$$

$$z_{\text{NDC}} \in [-1, +1]$$

...More Precision Issues with Z-Buffering



The effect of varying the distance of the near plane from the origin. The distance $f-n$ is kept constant at 100. As the near plane becomes closer to the origin, points nearer the far plane use a smaller range of the normalized device coordinate (NDC) depth space. This has the effect of making the z-buffer less accurate at greater distances.

WebGL Hidden Surface Removal

At Startup:

```
gl.enable(gl.DEPTH_TEST);    // use depth test for hidden surface remove  
gl.depthFunc(gl.LESS);      //this is the default
```

Each frame:

```
gl.clear(gl.DEPTH_BUFFER_BIT); // clear depth values form previous frame
```

Hidden surface removal uses the depth buffer (z-buffer)

Happens after the fragment shader