

# Path Tracing



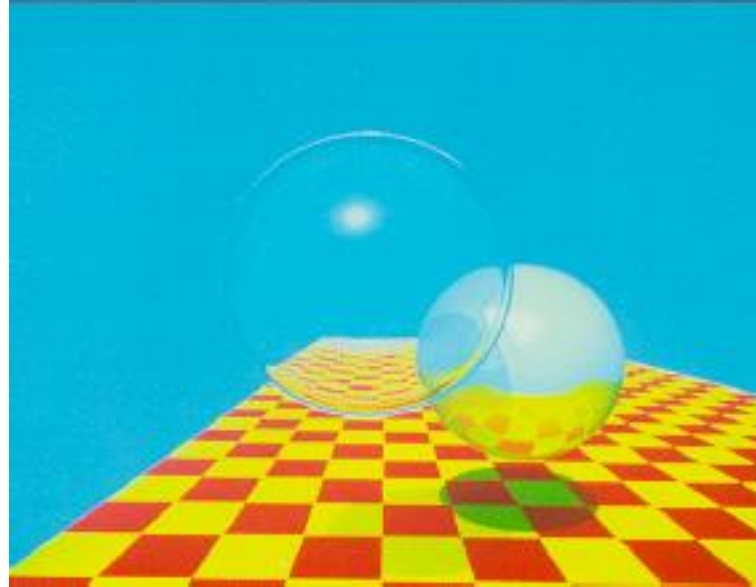
Production Computer Graphics  
Eric Shaffer

# A Brief History of Path Tracing

- Path tracing  $\approx$  recursive ray-tracing
- Turner Whitted [1979]: perfect specular reflection and refraction
- Cook et al [1984]: stochastic ray-tracing
  - glossy effects
  - motion blur
  - depth of field
- Kajiya [1986]: rendering equation, full global illumination
- Lafortune [1993]: Bidirectional path-tracing
- Jensen [1995]: Photon mapping

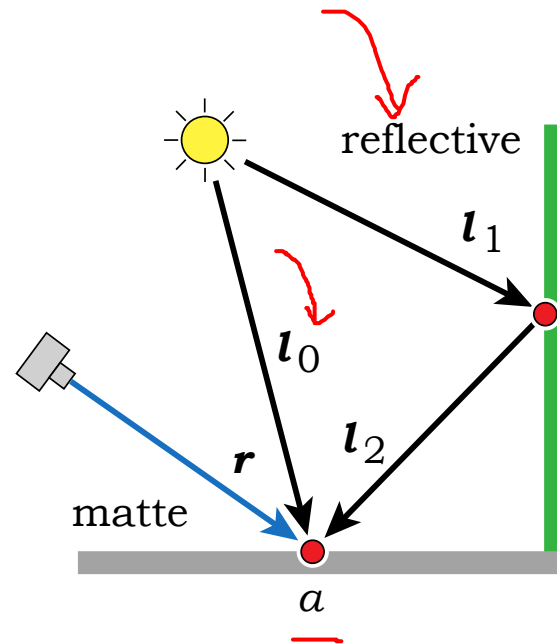
# Whitted Ray-Tracing

- 1979, Turner Whitted
- As an aside:
  - 74 minutes at 640x480
  - By Moore's Law we should now have 1024x1024 at 16 f.p.s.



# Global Illumination

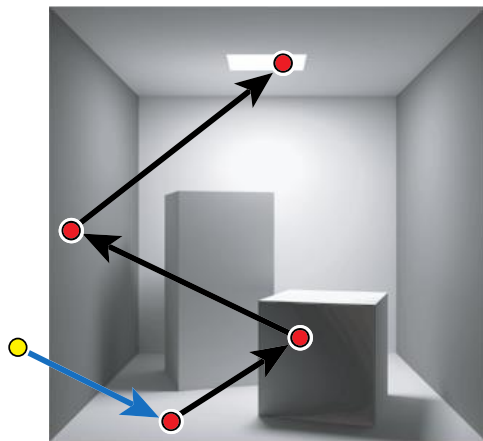
- Whitted ray-tracing can't discover certain light paths
- The  $l_1$  to  $l_2$  path below wouldn't be discovered



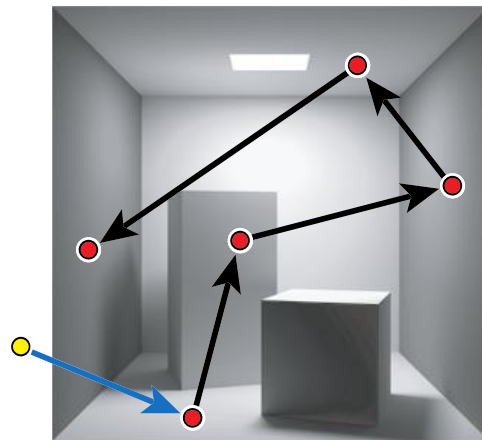
# Path Tracing

Path Tracing: more completely approximates the rendering equation

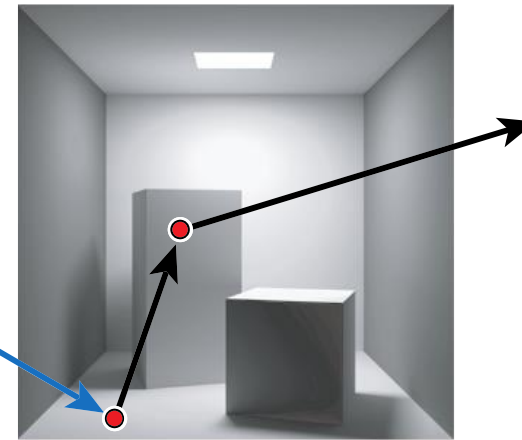
- Each ray is followed in a scene until:
  - It hits a light (a)
  - Maximum recursion depth is reached (b)
  - The ray leaves the scene (c)



(a)



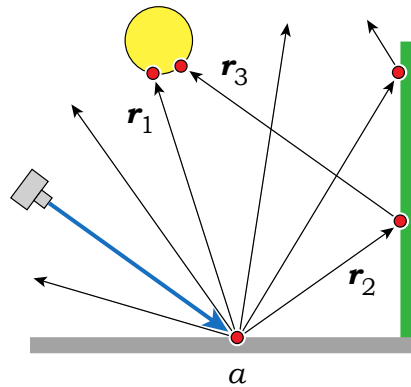
(b)



(c)

# Path Tracing

- Shoot multiple rays per pixel
- A primary ray and its reflected rays are a *ray path*
- At each hit point, a PDF is determines reflected ray direction
- In pure Path Tracing radiance only comes from area lights
  - no point or directional lighting



The blue ray represents multiple primary rays!

Each primary ray generates a single path.

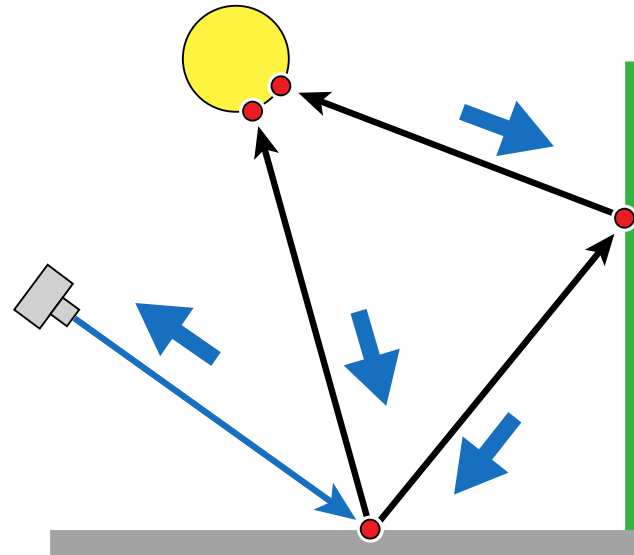
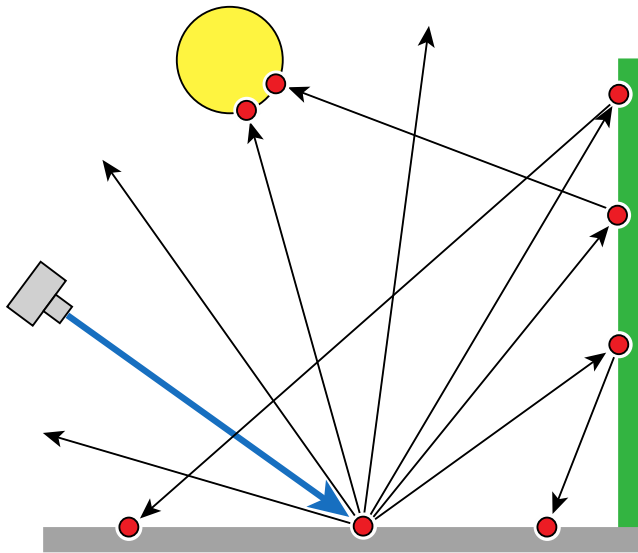
# Path Tracing

Material type determines ray orientation

- Pure Lambertian surfaces reflect rays in a random direction

Relying only on hitting lights leads to long convergence times

- Few paths will hit lights in the recursion depth limit

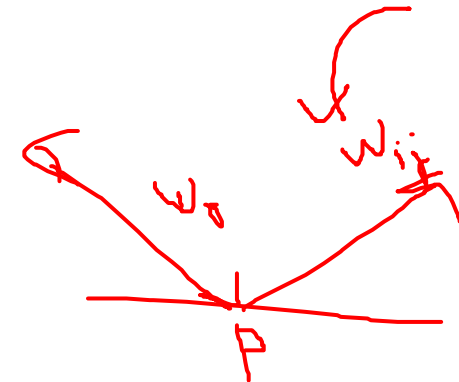


# A Monte Carlo Estimator for Path Tracing

Note: subscript  $i$  refers to incoming irradiance...not an index

- To evaluate the radiance at **each pixel**:

$$\langle L_r(p, w_o) \rangle = \frac{1}{n_s} \sum_{j=1}^{n_s} \frac{f_r(p, w_{i,j}, w_o) L_i(p, w_{i,j}) \cos q_{i,j}}{p(w_{i,j})} + \epsilon$$



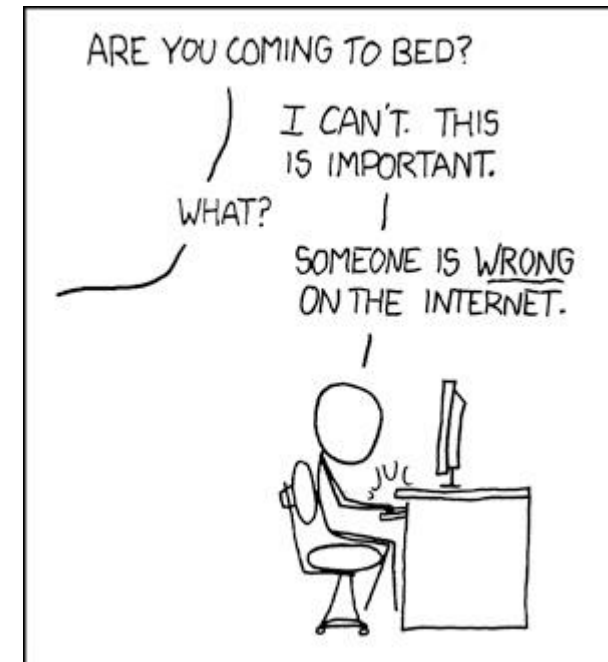
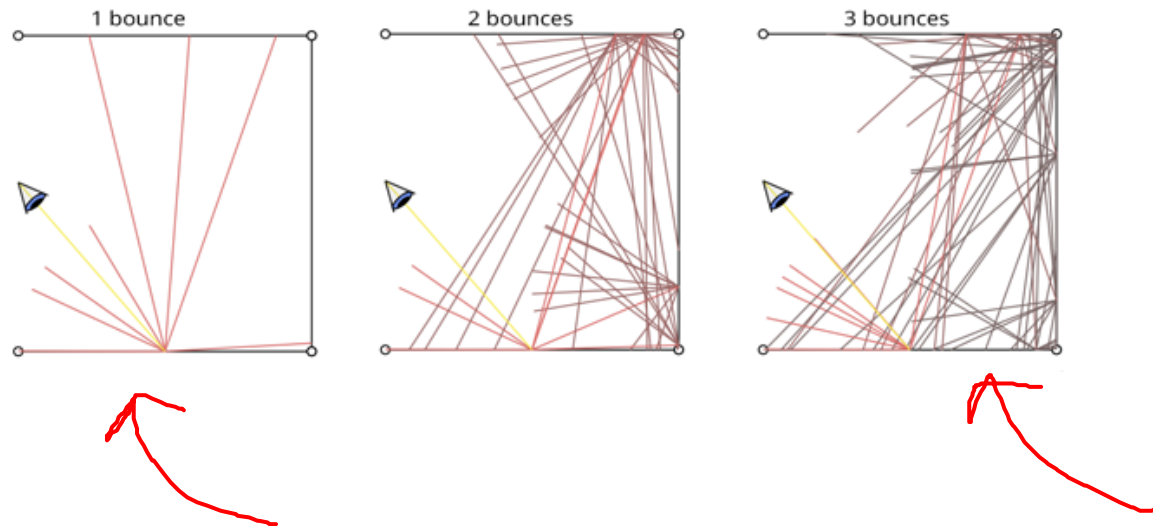
- We are generating  $n_s$  rays per pixel
  - The expression inside the summation computes radiance from first hit
  - But, of course, it's recursive



# Things that are wrong on the internet

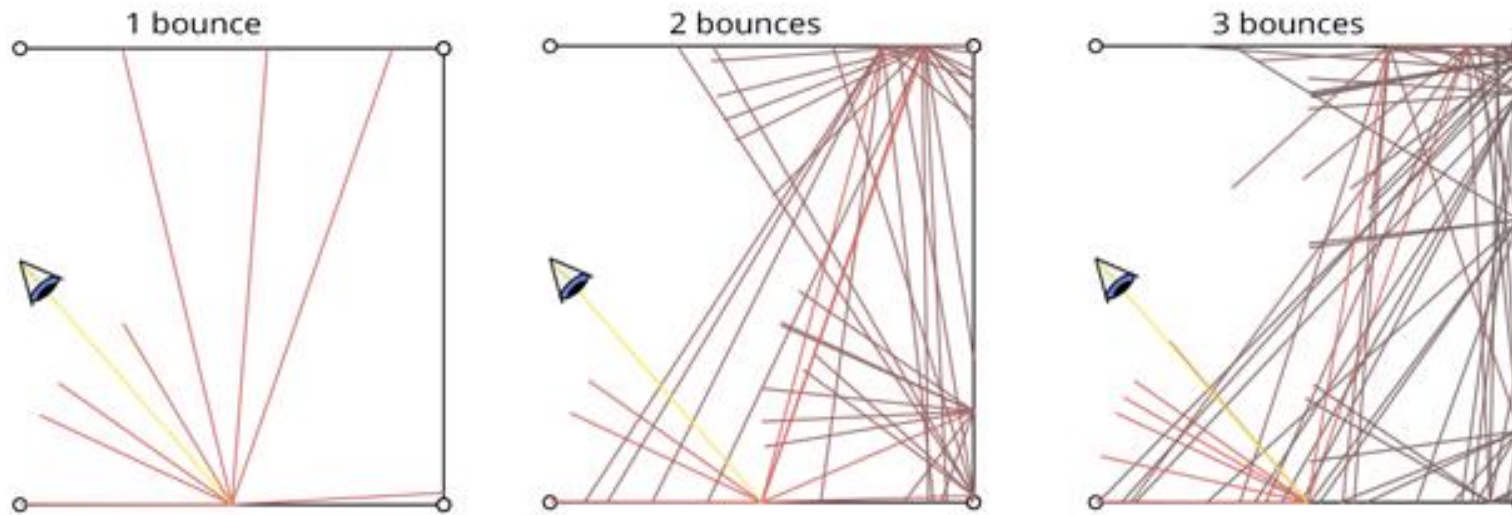
## Path tracing does not branch...and yet

repeat the same process again: the process is recursive. After 3 bounces, this is already  $16 * 16 * 16 = 4096$  rays cast into the scene (assuming all rays intersect geometry). This number increases exponentially as the number of bounces increases. For this reason, as in the case of mirror reflections, we stop casting rays after a certain number of bounces (for example 3) which in the code above is controlled by the `maxDepth` variable once again



# What is a good argument against branching?

Consider the relative contribution of rays cast at different depths



# Path Tracer Example



How does this code deviate from pure path tracing?

Why does it do that?

```
// global illumination algorithm
// stochastic ray tracing
computeImage(eye)
  for each pixel
    radiance = 0;
    H = integral(h(p));
    for each sample // Np viewing rays
      pick sample point p within support of h;
      construct ray at eye, direction p-eye;
      radiance = radiance + rad(ray)*h(p);
      radiance = radiance/(#samples*H);

rad(ray)
  find closest intersection point x of ray with scene;
  return(Le(x,eye-x) + computeRadiance(x, eye-x));

computeRadiance(x, dir)
  estimatedRadiance += directIllumination(x, dir);
  estimatedRadiance += indirectIllumination(x, dir);
  return(estimatedRadiance);

directIllumination (x, theta)
  estimatedRadiance = 0;
  for all shadow rays // Nd shadow rays
    select light source k;
    sample point y on light source k;
    estimated radiance +=
      Le * BRDF * radianceTransfer(x,y)/(pdf(k)pdf(y|k));
  estimatedRadiance = estimatedRadiance / #paths;
  return(estimatedRadiance);

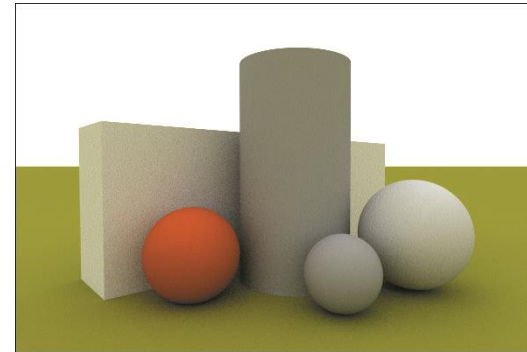
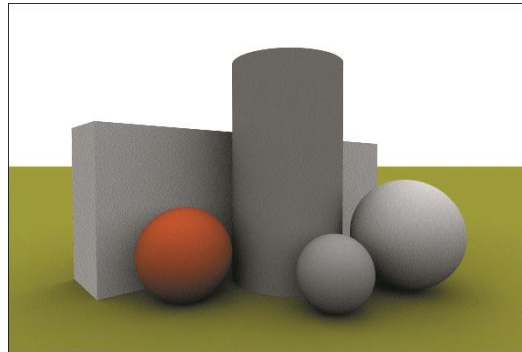
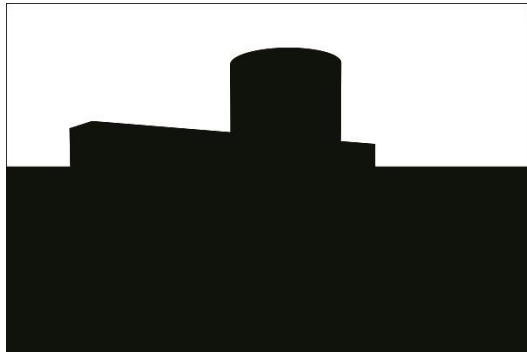
indirectIllumination (x, theta)
  estimatedRadiance = 0;
  if (no absorption) // Russian roulette
    for all indirect paths // Ni indirect rays
      sample direction psi on hemisphere;
      y = trace(x, psi);
      estimatedRadiance +=
        compute_radiance(y, -psi) * BRDF *
        cos(Nx, psi)/pdf(psi);
  estimatedRadiance = estimatedRadiance / #paths;
  return(estimatedRadiance/(1-absorption));

radianceTransfer(x,y)
  transfer = G(x,y)*V(x,y);
  return(transfer);
```



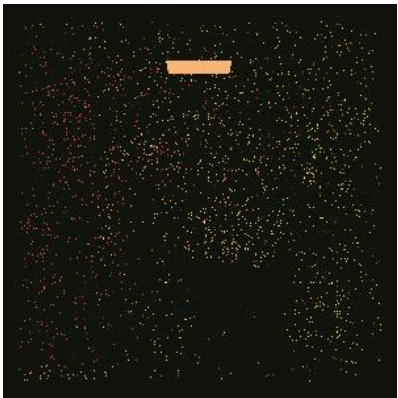
# Path Tracing with an Environment Light

Zero bounces...one bounce....five bounces

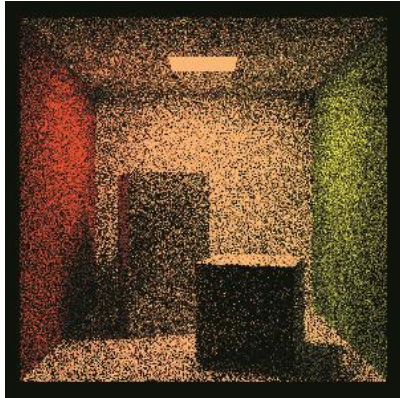


# Path Tracing with an Area Light

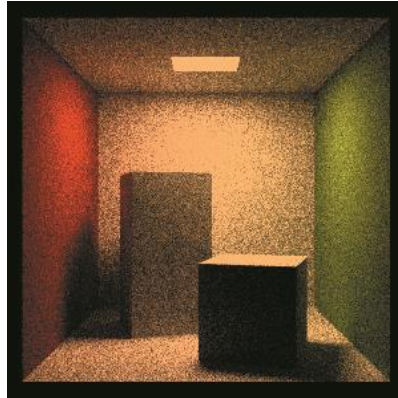
1 sample per pixel



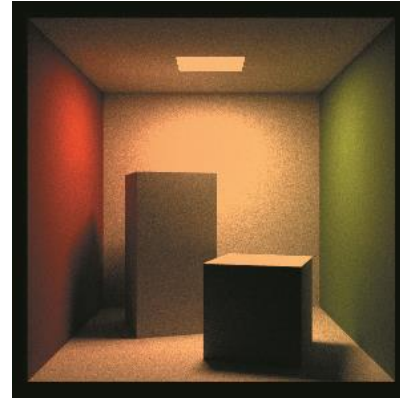
100



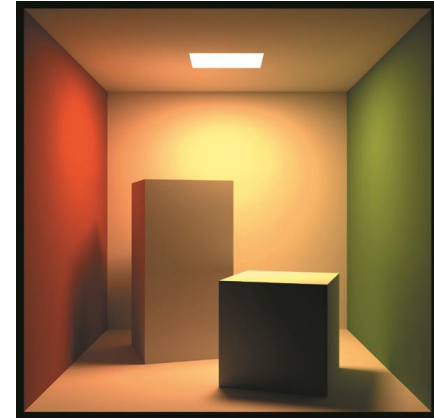
1024



10,000



100,000





# Path Tracing : Speedup through Light Sampling

Can employ a hybrid approach

- Direct illumination computed by sampling lights
- Indirect illumination computed by path tracing

Must take care not to render direct illumination twice

- Sample direct illumination with a shadow ray
- Indirect illumination as before
  - Hit on a light returns radiance if ray depth  $\neq 1$

