Suppose you have a 2D Bezier curve defined by the control points b₀, b₁, and b₂. Which of the follow is NOT true of that curve? (a) It will be a cubic polynomial curve. (b) It will be completely contained within the triangle formed by b₀, b₁, and b₂. (c) Changing the order of the control points to be b₂, b₁, and b₀ will result in the same curve. (d) It will pass through the points b₀ and b₂. Save & Grade Save only

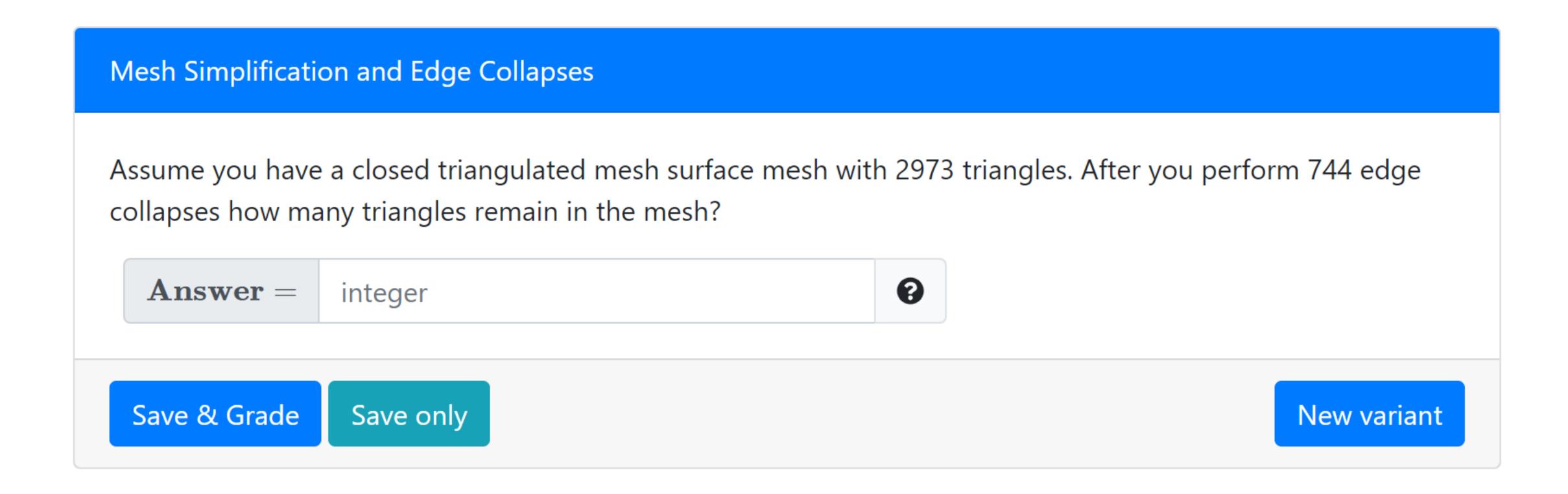
See the lecture Bezier Curves pages 7-13

Bezier Patches 1	
Suppose we have a cubic Bezier patch in 3D space defined by the control net of points $b_{0,0}$,, of points does the patch interpolate?	b _{3,3} . Which set
 (a) All the control points on the boundary of the patch (b) The corner points b_{0,0} b_{3,0} b_{0,3} and b_{3,3} (c) A Bezier patch does not interpolate any of the points in the control net. (d) All the boundary points of the patch 	
Save & Grade Save only	New variant

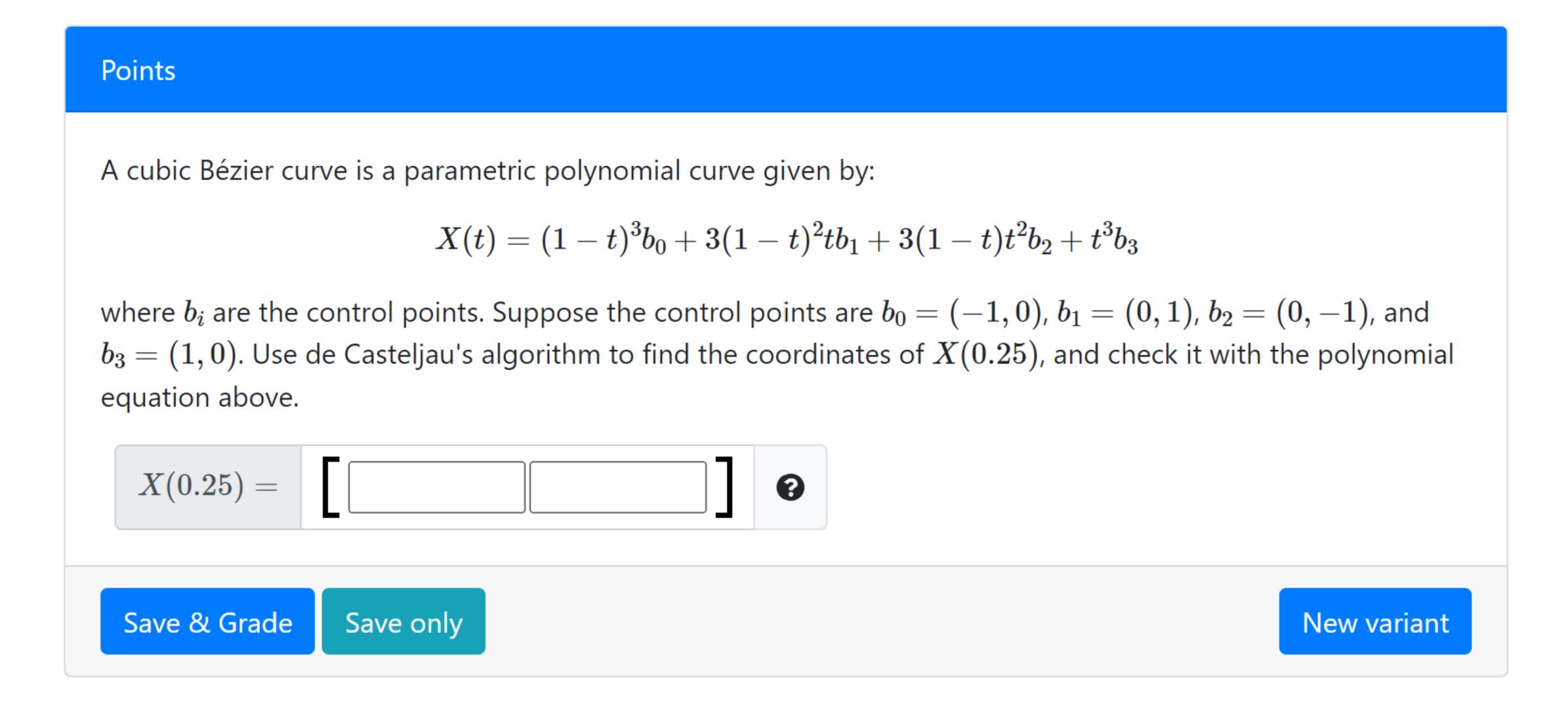
See the lecture Bezier Patches page 15

Suppose we have a quadratic Bezier patch in 3D. We wish to render the patch using a set of triangles. What is the maximum resolution at which the patch can be rendered in terms of the number of triangles? (a) We can render the patch using a grid with 16 vertices, generating 18 triangles. (b) We can render the patch using a grid with 16 vertices, generating 32 triangles. (c) We can render the patch using a grid with 9 vertices, generating 8 triangles. (d) We can render the patch using a grid with 9 vertices, generating 18 triangles. (e) A Bezier patch can only be used to generate quadrilaterals. (f) We can render the patch using as many triangles as we wish; there is no inherent limit to the resolution at which you can approximate a Bezier patch.

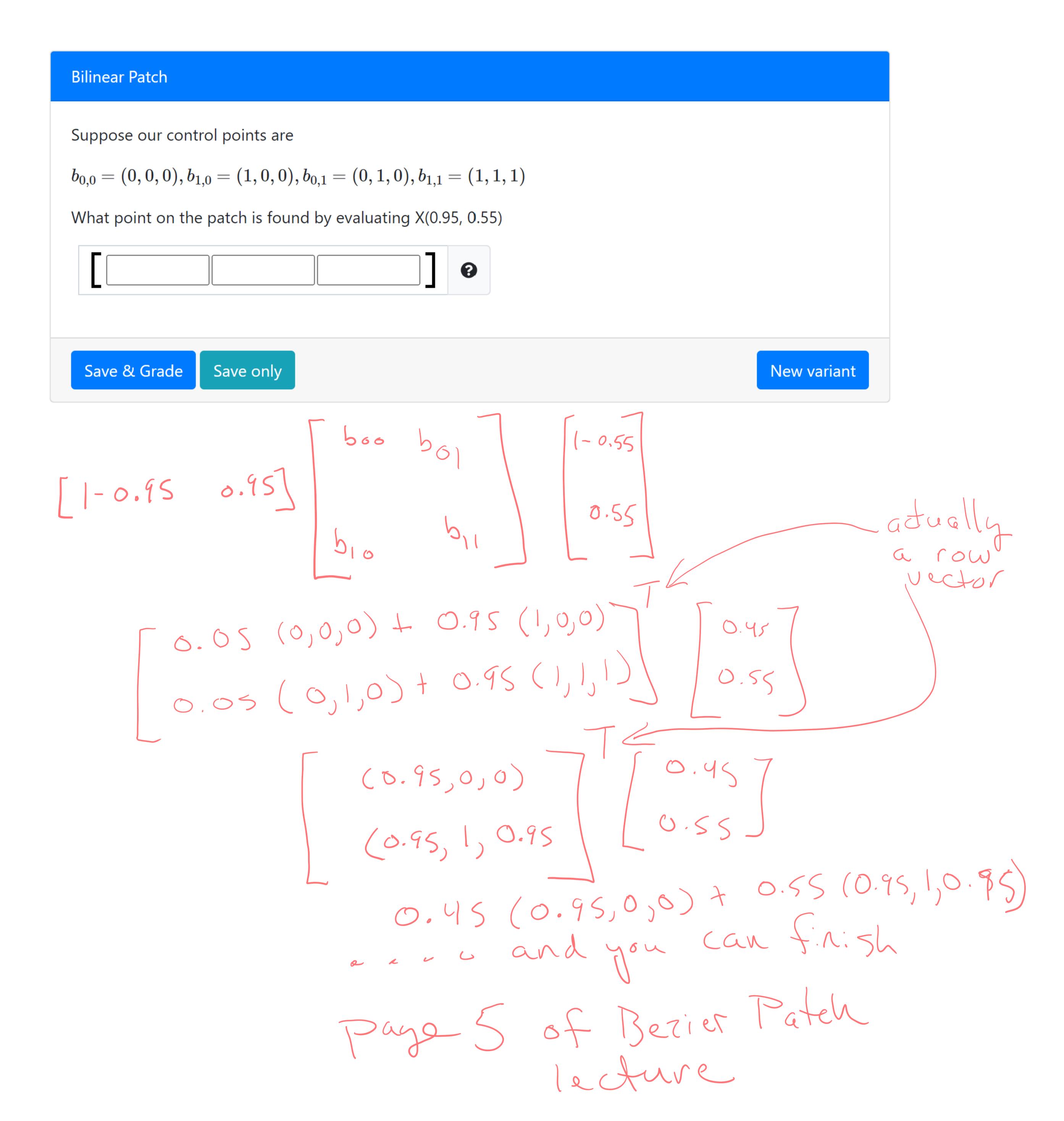
We can generate any number of points on the patch the we wish...imagine we want to generate a grid of n by n points we simply generate a point B(u,v) where u and v go from 0 to 1 using a stepsize of 1/(n-1). This grid consists of quadrilateral cells, each of which can be broken into 2 triangles. So...how many triangles can we generate?



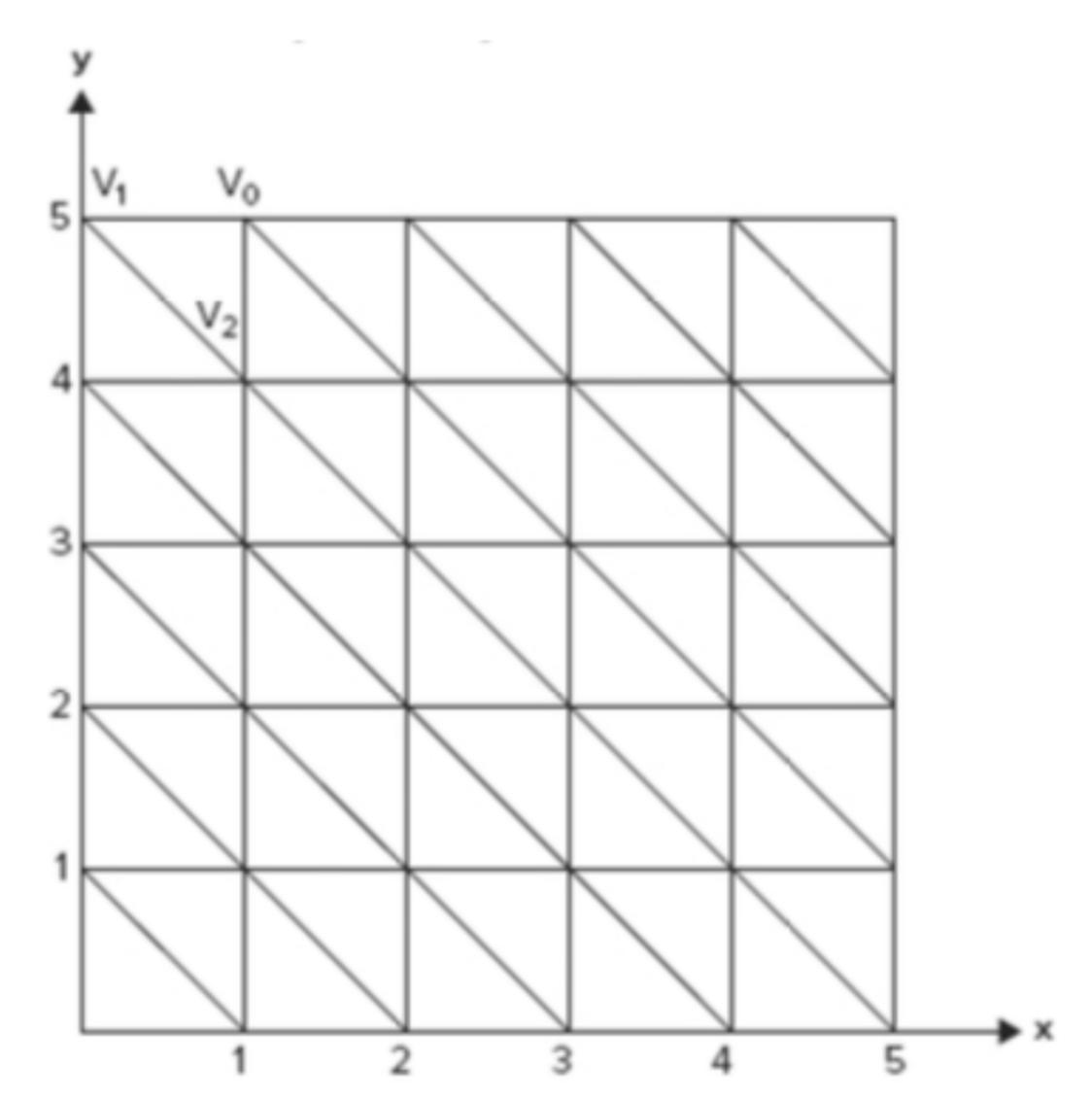
How many triangles are removed by an edge collapse?
See the lecture LOD Generation and Mesh Simplification page 13.



See the lecture Bezier Curves page 18, example on page 20



Indexed Face Format for Meshes



Imagine we generate a rectangular mesh with a boundary using an n+1 by n+1 grid of vertices. In the example above, it is using n=5. We have (5+1)*(5+1) grid of vertices and 5*5*2 triangles. Triangles are generated as shown, cutting each grid square into 2 triangles.

The mesh is stored using an **indexed face format** (like an OBJ file, for example). Assuming:

- 1. each vertex is specified by 3 floating point coordinates (the image doesn't show z-axis)
- 2. floating point numbers use **4 bytes** of space
- 3. integer indices use **2 bytes** of space.

Suppose you need to store a mesh with n=15. How much space is used by the mesh?

bytes = integer

For n=15

162 vertices each needing 3 woords x 4 bytes

152 guads in grid each spirit into 2 triangles

2 x 152 x 3 indices x 2 bytes

50 12 x 162 + 6 x 152 bytes

Quadric Error Metric 1

We saw that the squared distance from a point p to a plane q in 3D space can be found in the following manner:

$$p = (x, y, z, 1)^T, q = (a, b, c, d)^T$$

$$\operatorname{dist}(q,p)^2 = (q^Tp)^2 = p^T(qq^T)p =: p^TQ_qp$$

$$Q_q = egin{bmatrix} a^2 & ab & ac & ad \ ab & b^2 & bc & bd \ ac & bc & c^2 & cd \ ad & bd & cd & d^2 \ \end{pmatrix}$$

Suppose we wish to find the sum of the squared distances from p to a set of N planes $q_1,...,q_n$ and we already have access to the matrices $Q_1,...,Q_n$. How many scalar multiplications would need to be performed to find the sum? Disregard any addition operations.

- O (a) 20
- O (b) 32N
- O (c) 16N
- O (d) 32
- O (e) 20N

Save & Grade

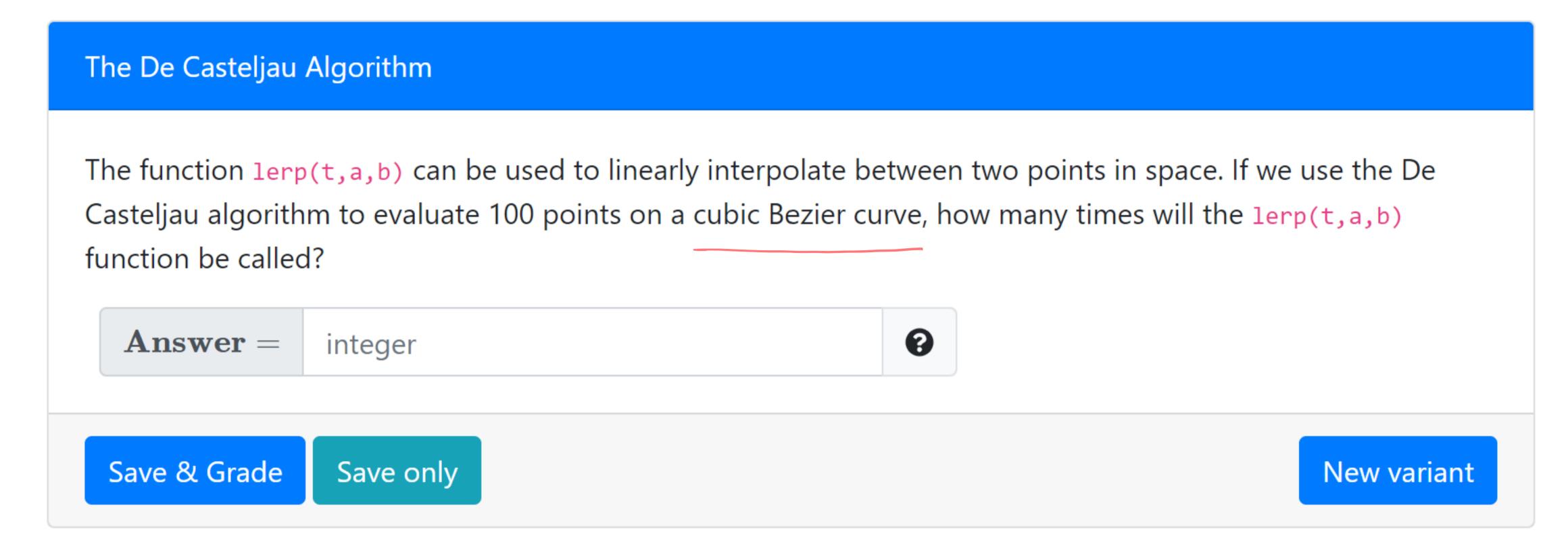
Save only

New variant

Can sum all n Q; matrices to a single matrix using only addition

T Qg P = [x,y,z,1] [900 ... - 903] [x]

[250 ... 823] [7]



Each point reguires 6 Zerps, for cubics

Evaluating Bezier Curves

Suppose we have a 2D quadratic Bezier curve with control points

$$b_0 = (-3, -2) \ b_1 = (0, -1)$$

$$b_1=(0,-1)$$

$${\color{red} \digamma}b_2=(2,4)$$

Recall that the Berstein polynomials for a quadratic Bezier curve are:

$$B_0^2(t) = (1-t)^2$$
 $B_1^2(t) = (1-t)2t$ $B_2^2(t) = t^2$

$$B_1^2(t) = (1-t)2t$$

$$B_2^2(t) = t^2$$

What is the y coordinate of the point on the curve at $t=0.1\,$ Your answer is expected to be correct to 2 significant digits.

number (2 significant figures)



Save & Grade Save only New variant

Using only y coords we have $(1-0.1)^2 (-2) + (1-0.1)(2 \times 0.1) (-1) + (0.1)^2 (-2)$