

Tracking and Collision Detection

1. Correcting Drift

When tracking orientation, drift correction can be accomplished by a complementary filter:

$$\hat{\theta}_c[k] = \alpha \hat{\theta}_d[k] + (1 - \alpha) \hat{\theta}[k]$$

Here, k is the current timestep. The function $\hat{\theta}[k]$ is orientation determined by integrating a gyroscope reading. The function $\hat{\theta}_d[k]$ provides orientation through a lower sampling rate sensor like a camera. The parameter $\alpha \in [0,1]$ is called the *gain*. Approximately where in the interval $[0,1]$ should the gain be set? Provide two reasons supporting your choice for the gain.

2. Orientation Drift in 3D

Suppose the true orientation is given by the quaternion q and the estimated orientation measured by the quaternion \hat{q} .

- Derive a formula for the drift error.
- If the accelerometer produces a vector \mathbf{a} in body coordinates, how can it be converted into world coordinates?

3. Using a BVH for Collision Detection

We have two objects **a** and **b**, each with their own BVH as shown below. Each node a bounding volume associated with it. Only the geometry in nodes a_3 and b_8 are in collision. What is the minimal number of bounding volume intersections that might be needed to determine this? What would be the maximal number?

