## Data manipulations and linear regression

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This lecture is meant to supplement Chapter 2 in your textbook. We present a brief overview of linear regression.

## The dplyr package within tidyverse

```
#install.packages("tidyverse")
library(tidyverse)
```

dplyr provides comprehensive tools for data manipulations (or wrangling). The five main "verbs" are:

- select (): choose from a subset of the columns
- filter(): choose a subset of the rows based on logical criteria
- arrange (): sort the rows based on values of the columns.
- mutate(): add or modify the definitions of the column, and create columns that are functions of existing columns.
- summarize(): collapse a data frame down to a single row (per group) by aggregating vectors into a single value. Often used in conjunction with group\_by()

## The pipe operator

The pipe operator %>% allows for verbs to be strung in succession so that complicated manipulations can be combined within a single easily digestible sentence.

```
data %>%
  inner_function() %>%
  outer_function()
```

## Example: Runs differential regression

```
library (Lahman)
data (Teams)
head (Teams, 3)
     yearID lqID teamID franchID divID Rank G Ghome
                                                          L DivWin WCWin LgWin
## 1
       1871
              NA
                    BS1
                             BNA
                                 <NA>
                                           3 31
                                                   NA 20 10
                                                              <NA>
                                                                     <NA>
## 2
      1871
                    CH1
                                  <NA>
                                           2 28
                                                   NA 19 9
                                                              <NA>
              NA
                             CNA
                                                                     <NA>
                                                                              N
       1871
                    CL1
                                           8 29
              NA
                             CFC
                                  <NA>
                                                   NA 10 19
                                                              <NA>
                                                                     <NA>
                 AR
     WSWin
                      H X2B X3B HR BB SO SB CS HBP SF
                                                       RA
                                                           ER ERA CG SHO SV
      <NA> 401 1372 426
                        70
                            37 3 60 19 73 16
                                                NA NA 303 109 3.55 22
      <NA> 302 1196 323
                         52
                             21 10 60 22 69 21
                                                NA NA 241
                                                            77 2.76 25
      <NA> 249 1186 328
                         35
                             40 7 26 25 18 8
                                                 NA NA 341 116 4.11 23
     IPouts HA HRA BBA SOA
                              E DP
                                      FP
                                                             name
        828 367
                     42
                         23 243 24 0.834
                                             Boston Red Stockings
## 2
        753 308
                     28
                         22 229 16 0.829 Chicago White Stockings
## 3
        762 346
                    53
                         34 234 15 0.818 Cleveland Forest Citys
##
                             park attendance BPF PPF teamIDBR teamIDlahman45
## 1
              South End Grounds I
                                           NA 103 98
                                                           BOS
                                                                           BS1
## 2
          Union Base-Ball Grounds
                                           NA 104 102
                                                           CHI
                                                                           CH1
   3 National Association Grounds
                                          NA 96 100
                                                           CLE
##
     teamIDretro
## 1
             BS1
## 2
             CH1
## 3
```

```
Teams %>%
   select (yearID, franchID, W, L, G, AB, H, X2B, X3B, HR, BB, HBP, SF,
               HA, HRA, BBA, SOA, IPouts, FP, R, RA) %>%
   filter(vearID >= 1900) %>%
   replace na(list(HBP = 0, SF = 0)) %>%
   mutate(RD = (R - RA) / G, X1B = H - (X2B + X3B + HR)) %>%
   arrange(desc(RD)) %>%
   head (10)
                                     H X2B X3B HR BB HBP SF
##
     yearID franchID W L G AB
                                                              HA HRA BBA
## 1
       1939
                NYY 106 45 152 5300 1521 259 55 166 701
                                                      0 0 1208 85 567
## 2
       1927
               NYY 110 44 155 5347 1644 291 103 158 635
                                                      0 0 1403 42 409
## 3
      1902
            PIT 103 36 141 4926 1410 189 95 18 372
                                                      64 0 1142 4 250
## 4
       2020
            LAD 43 17 60 2042 523 97 6 118 228
                                                       30 12 424 66 145
## 5
      1936
                NYY 102 51 155 5591 1676 315 83 182 700
                                                       0 0 1474 84 663
## 6
      1906
                CHC 116 36 154 5018 1316 181 71 20 448
                                                       45 0 1018 12 446
            NYY 94 59 155 5608 1667 277 78 155 748
## 7
      1931
                                                       0 0 1461 67 543
```

NYY 102 52 157 5487 1554 282 73 174 709 0 0 1417 92 506

NYY 103 51 154 5305 1429 223 57 108 591 0 0 1259 71 431

RD X1R

31 207 653 57 59 1357 156 466

NYY 114 48 162 5643 1625 290

967 556 2.703947 1041

775 440 2.375887 1108

349 213 2.266667 302

R RA

4167 0.969 975 599 2.425806 1092

4200 0.973 1065 731 2.154839 1096

4165 0.969 704 381 2.097403 1044

4230 0.972 1067 760 1.980645 1157

4188 0.972 979 671 1.961783 1025

4125 0.976 801 507 1.909091 1041

4370 0.984 965 656 1.907407 1097

## 8

## 9

## 10

##

## 1

## 2

## 3

## 4

## 5

## 6

## 7

## 8

## 9

## 10 1080

1937

1942

1998

565

431

564

517

624

702

686

652

558

SOA IPouts

FP

4044 0.978

3794 0.958

1616 0.982

```
mutate(FIP = 3*(13*HRA + 3*BBA - 2*SOA)/IPouts)
head(dat, 3)
## vearID franchID W L G AB H X2B X3B HR BB HBP SF HA HRA BBA SOA
## 1 1900
              TAD 82 54 141 4860 1423 199 81 26 421 81 0 1370 30 405 300
## 2 1900
              ATT. 66 72 142 4952 1403 163 68 48 395 45 0 1263 59 463 340
## 3 1900
            CHC 65 75 146 4907 1276 202 51 33 343 65 0 1375 21 324 357
                              RD X1B
                                           OBP
## TPouts
             FP R RA
                                                    SLG
                                                             OPS
                                                                     WHTP
## 1 3677 0.948 816 722 0.6666667 1117 0.3590078 0.3831276 0.7421354 1.448191
## 2 3721 0.953 778 739 0.2746479 1124 0.3418027 0.3727787 0.7145813 1.391561
## 3 3813 0.933 635 751 -0.7945205 990 0.3168391 0.3421643 0.6590034 1.336743
##
          FIP
## 1 0 8199619
```

## 2 1.1900027 ## 3 0.4177813 **Note**: other packages may contain functions with the same name as those in dplyr. For example, the MASS package also contains a select function.

In the event that you have both dplyr and MASS loaded in an R session, you can access dplyr's select function using dplyr::select

Baseball is a game of offense, pitching, and defense. Let's see how well runs differential per game is explained by:

- ► OPS: on base percentage plus slugging percentage
- ▶ WHIP: walks and hits allowed divided by innings pitched
- ► FP: fielding percentage

using a linear regression model

```
m \leftarrow lm(RD \sim OPS + WHIP + FP, data = dat)
```

### Regression review

Regression model:

$$y = \beta_1 x_1 + \cdots + \beta_p x_p + \varepsilon; \qquad \varepsilon \sim N(0, \sigma^2),$$

where we usually specify a model intercept by setting  $x_1 = 1$ .

Can also write in vector notation:

$$y = \mathbf{x}'\beta + \varepsilon; \qquad \varepsilon \sim N(0, \sigma^2),$$

where  $\mathbf{x}, \beta \in \mathbb{R}^p$ .

Either way, this model relies on a few assumptions:

- a linear relationship is present
- errors are independent and identically distributed
- errors are normally distributed mean 0 and common variance  $\sigma^2$

## Regression review

Remember that linear regression is about modeling a conditional expectation, the scattering of points is noise. Interest is in

$$E(y|\mathbf{x}) = \mathbf{x}'\beta,$$

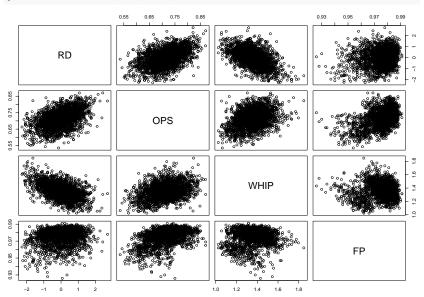
where it is important to choose the variables comprising  ${\bf x}$  and to be able to defend those choices.

#### Yes, baseball IS a game of offense, pitching, and defense.

```
summary(m)
##
## Call:
## lm(formula = RD ~ OPS + WHIP + FP, data = dat)
##
## Residuals:
## Min
               10 Median
                             30
                                        Max
## -1.46423 -0.21590 -0.00561 0.20938 1.47559
##
## Coefficients:
             Estimate Std. Error t value Pr(>|t|)
##
## (Intercept) 13.41388 0.78871 17.01 <2e-16 ***
## OPS 11.76848 0.15668 75.11 <2e-16 ***
## WHIP -5.41704 0.06472 -83.70 <2e-16 ***
## FP
           -14.84524 0.84015 -17.67 <2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.3489 on 2606 degrees of freedom
## Multiple R-squared: 0.7877, Adjusted R-squared: 0.7874
## F-statistic: 3222 on 3 and 2606 DF, p-value: < 2.2e-16
```

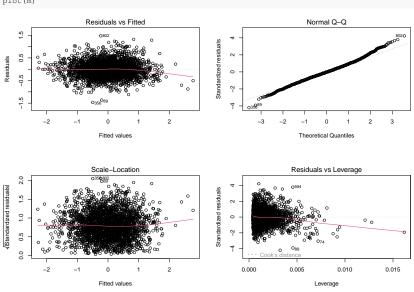
#### Linearity holds.

pairs(dat %>% select(RD, OPS, WHIP, FP))



Normality of mean-zero errors with constant variance holds. Although a slightly heavy right tail is observed in the residuals.

par(mfrow = c(2,2))
plot(m)



# The compiled fractions should be roughly 68% and 95% if errors are truly normal with common variance.

```
## # A tibble: 1 x 5

## N within_1rmse within_2rmse within_1rmse_pct within_2rmse_pct

## <int> <int> <int> <ohl> <ohl> <ohl > <ohl> <ohl> <ohl> <ohl> <ohl > <ohl
```

We will suppose that independence holds, or that any violations of this assumption that may be present in this data do not materially effect our overall conclusions.

A saturated model (one parameter per observation) does not fit the data better than our model with three variables and an intercept.

```
# likelihood ratio test of fitted model vs a saturated model
m_glm <- glm(RD ~ OPS + WHIP + FF, data = dat)
pchisq(m_glm$deviance, m_glm$df.residual, lower = FALSE)</pre>
```

## [1] 1

Thus we have a well-fitting simple and useful model that provides satisfactory dimension reduction.

#### Investigate large residuals

```
dat_aug %>% filter(abs(.resid) >= 1) %>%
  select(yearID, franchID, W, RD, OPS, WHIP, FP, .resid, .fitted) %>%
  mutate(across(4.9, round, 3)) %>%
  arrange(desc(.resid))
```

```
## # A tibble: 27 x 9
   vearID franchID
                                        FP .resid .fitted
##
                      W
                           RD OPS WHIP
##
     <int> <fct> <int> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl>
                                                    <dbl>
## 1 1949 NYY
                      97 1.24 0.758 1.49 0.977
                                               1.48 -0.237
## 2
     1936 NYY
                    102 2.15 0.861 1.53 0.973
                                               1.32 0.835
     1939 NYY
                    106 2.70 0.821
                                   1.32 0.978
                                               1.28 1.42
##
##
  4
     1950 BOS
                     94 1.45 0.846 1.59 0.981
                                               1.24 0.211
##
  5
     1949 BOS
                     96 1.48 0.8
                                   1.48 0.98
                                               1.21 0.269
## 6
     1935 DET
                      93 1.67 0.798 1.44 0.979
                                               1.19 0.485
## 7 1948 BOS
                      96 1.21 0.779 1.48 0.981
                                               1.18 0.021
## 8
     1943 CIN
                      87 0.419 0.653 1.34 0.98
                                               1.11 -0.691
## 9
     1950 NYY
                      98 1.44 0.804
                                   1.48 0.979
                                               1.11
                                                    0.327
## 10 1938 DET
                      84 0.432 0.768
                                   1.59 0.976
                                               1.07 -0.636
## # with 17 more rows
```

#### Investigate large fitted values

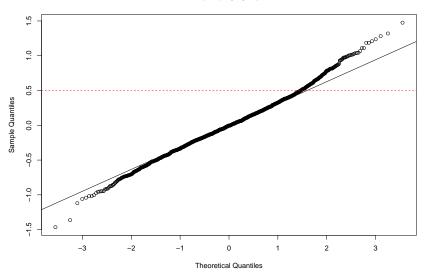
```
dat_aug %>% filter(.fitted >= 2) %>%
    select(yearID, franchID, W, RD, OPS, WHIP, FP, .resid, .fitted)
```

```
## # A tibble: 4 x 9
  yearID franchID
                                           FP .resid .fitted
                           RD
                               OPS
                                    WHIP
##
     <int> <fct>
                  <int> <dbl> <dbl> <dbl> <dbl> <dbl>
                                                     <dbl>
## 1 1927 NYY
                                                      2.20
                    110 2.43 0.870 1.30 0.969 0.225
    2019 HOU
                    107 1.73 0.848 1.13 0.988 -0.874
## 2
                                                     2.60
## 3 2019 TAD
                    106 1.69 0.810 1.10 0.982 -0.710
                                                     2.40
## 4 2020 LAD
                    43 2.27 0.821 1.06 0.982 -0.505
                                                      2.77
```

#### A closer look at problems with fit

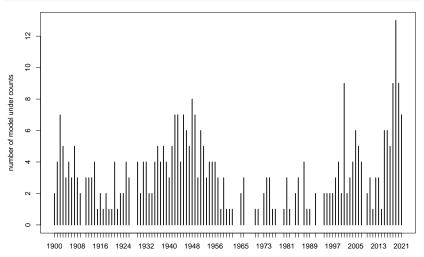
```
qqnorm(resid(m)); qqline(resid(m))
abline(a=0.5, b=0, lty = 2, col = "red")
```

Normal Q-Q Plot



#### A closer look at problems with fit

```
plot(table(dat_aug %>% filter(abs(.resid) >= 0.5) %>%
  pull(yearID)), ylab = "number of model under counts")
```



#### League conditions change over time

