## Data manipulations and linear regression

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This lecture is meant to supplement Chapter 2 in your textbook. We present a brief overview of linear regression.

## The dplyr package within tidyverse

```
#install.packages("tidyverse")
library(tidyverse)
```

dplyr provides comprehensive tools for data manipulations (or wrangling). The five main "verbs" are:

- select (): choose from a subset of the columns
- filter(): choose a subset of the rows based on logical criteria
- arrange (): sort the rows based on values of the columns.
- mutate(): add or modify the definitions of the column, and create columns that are functions of existing columns.
- summarize(): collapse a data frame down to a single row (per group) by aggregating vectors into a single value. Often used in conjunction with group\_by()

## The pipe operator

The pipe operator %>% allows for verbs to be strung in succession so that complicated manipulations can be combined within a single easily digestible sentence.

```
data %>%
  inner_function() %>%
  outer_function()
```

## Example: Runs differential regression

```
library (Lahman)
data (Teams)
head (Teams, 3)
     yearID lqID teamID franchID divID Rank G Ghome
                                                          L DivWin WCWin LgWin
## 1
       1871
              NA
                    BS1
                             BNA
                                 <NA>
                                           3 31
                                                   NA 20 10
                                                              <NA>
                                                                     <NA>
## 2
      1871
                    CH1
                                  <NA>
                                           2 28
                                                   NA 19 9
                                                              <NA>
              NA
                             CNA
                                                                     <NA>
                                                                              Ν
       1871
                    CL1
                                           8 29
              NA
                             CFC
                                  <NA>
                                                   NA 10 19
                                                              <NA>
                                                                     <NA>
                 AR
     WSWin
                      H X2B X3B HR BB SO SB CS HBP SF
                                                       RA
                                                           ER ERA CG SHO SV
      <NA> 401 1372 426
                        70
                            37 3 60 19 73 16
                                                NA NA 303 109 3.55 22
      <NA> 302 1196 323
                         52
                             21 10 60 22 69 21
                                                NA NA 241
                                                            77 2.76 25
      <NA> 249 1186 328
                         35
                             40 7 26 25 18 8
                                                 NA NA 341 116 4.11 23
     IPouts HA HRA BBA SOA
                              E DP
                                      FP
                                                             name
        828 367
                     42
                         23 243 24 0.834
                                             Boston Red Stockings
## 2
        753 308
                     28
                         22 229 16 0.829 Chicago White Stockings
## 3
        762 346
                    53
                         34 234 15 0.818 Cleveland Forest Citys
##
                             park attendance BPF PPF teamIDBR teamIDlahman45
## 1
              South End Grounds I
                                           NA 103 98
                                                           BOS
                                                                           BS1
## 2
          Union Base-Ball Grounds
                                           NA 104 102
                                                           CHI
                                                                           CH1
   3 National Association Grounds
                                          NA 96 100
                                                           CLE
##
     teamIDretro
## 1
             BS1
## 2
             CH1
## 3
```

```
Teams %>%
    select (yearID, franchID, W, L, AB, H, X2B, X3B, HR, BB, HBP, SF,
                 HA, HRA, BBA, SOA, IPouts, FP, R, RA) %>%
    filter(vearID >= 1900) %>%
    replace na(list(HBP = 0, SF = 0)) %>%
    \text{mutate}(RD = (R - RA) / (W + L), X1B = H - (X2B + X3B + HR))  %>%
    arrange(desc(RD)) %>%
    head (10)
```

SOA

565

431

564

517

624

702

686

652

558

```
##
     yearID franchID W L AB
                                H X2B X3B HR BB HBP SF HA HRA BBA
## 1
       1939
                NYY 106 45 5300 1521 259 55 166 701
                                                   0 0 1208
                                                            85 567
## 2
      1927
              NYY 110 44 5347 1644 291 103 158 635 0 0 1403
                                                            42 409
## 3
      1902
            PIT 103 36 4926 1410 189 95 18 372 64 0 1142
                                                            4 250
## 4
       2020
            LAD 43 17 2042 523 97
                                      6 118 228 30 12 424
                                                            66 145
## 5
      1936
            NYY 102 51 5591 1676 315 83 182 700
                                                   0 0 1474
                                                            84 663
## 6
      1906
            CHC 116 36 5018 1316 181
                                      71 20 448 45 0 1018
                                                            12 446
            NYY 94 59 5608 1667 277
                                      78 155 748
## 7
     1931
                                                   0 0 1461
                                                            67 543
                                      73 174 709
## 8
     1937
            NYY 102 52 5487 1554 282
                                                   0 0 1417
                                                            92 506
## 9
      1942
            NYY 103 51 5305 1429 223
                                      57 108 591 0 0 1259 71 431
## 10
       1998
            NYY 114 48 5643 1625 290
                                      31 207 653 57 59 1357 156 466 1080
##
     IPouts
            FP R RA
                              RD X1B
## 1
       4044 0.978 967 556 2.721854 1041
## 2
       4167 0.969 975 599 2.441558 1092
## 3
       3794 0.958 775 440 2.410072 1108
## 4
      1616 0.982 349 213 2.266667 302
## 5
       4200 0.973 1065 731 2.183007 1096
## 6
     4165 0.969 704 381 2.125000 1044
## 7
       4230 0.972 1067 760 2.006536 1157
## 8
     4188 0.972 979 671 2.000000 1025
## 9
      4125 0.976 801 507 1.909091 1041
```

4370 0.984 965 656 1.907407 1097

## 10

```
dat <- Teams %>%
    select (yearID, franchID, W. L. AB, H. X2B, X3B, HR, BB, HBP, SF,
                 HA, HRA, BBA, SOA, IPouts, FP, R, RA) %>%
    filter(yearID >= 1900) %>%
    replace na(list(HBP = 0, SF = 0)) %>%
    mutate(RD = (R - RA) / (W + L), X1B = H - (X2B + X3B + HR)) %>%
    mutate(OBP = (H + BB + HBP)/(AB + BB + HBP + SF)) %>%
    mutate(SLG = (X1B + 2*X2B + 3*X3B + 4*HR)/AB) %>%
    mutate(OPS = OBP + SLG) %>%
    mutate(WHTP = 3*(HA + BBA)/TPouts) %>%
    mutate(FIP = 3*(13*HRA + 3*BBA - 2*SOA)/IPouts)
```

3677

3721

3813

```
head(dat, 3)
## vearID franchID W L AB H X2B X3B HR BB HBP SF HA HRA BBA SOA IPouts
## 1 1900
              TAD 82 54 4860 1423 199 81 26 421 81 0 1370 30 405 300
## 2 1900
               ATT. 66 72 4952 1403 163 68 48 395 45 0 1263 59 463 340
## 3 1900
              CHC 65 75 4907 1276 202 51 33 343 65 0 1375 21 324 357
##
                        RD X1B
     FP R RA
                                     OBP
                                              SLG
                                                       OPS
                                                              WHTP
## 1 0.948 816 722 0.6911765 1117 0.3590078 0.3831276 0.7421354 1.448191
## 2 0.953 778 739 0.2826087 1124 0.3418027 0.3727787 0.7145813 1.391561
```

## 3 0.933 635 751 -0.8285714 990 0.3168391 0.3421643 0.6590034 1.336743

##

FIP

## 1 0 8199619 ## 2 1.1900027 ## 3 0.4177813

**Note**: other packages may contain functions with the same name as those in dplyr. For example, the MASS package also contains a select function.

In the event that you have both dplyr and MASS loaded in an R session, you can access dplyr's select function using dplyr::select

Baseball is a game of offense, pitching, and defense. Let's see how well runs differential per game is explained by:

- ► OPS: on base percentage plus slugging percentage
- ▶ WHIP: walks and hits allowed divided by innings pitched
- ► FP: fielding percentage

using a linear regression model

```
m \leftarrow lm(RD \sim OPS + WHIP + FP, data = dat)
```

### Regression review

Regression model:

$$y = \beta_1 x_1 + \cdots + \beta_p x_p + \varepsilon; \qquad \varepsilon \sim N(0, \sigma^2),$$

where we usually specify a model intercept by setting  $x_1 = 1$ .

Can also write in vector notation:

$$y = \mathbf{x}'\beta + \varepsilon; \qquad \varepsilon \sim N(0, \sigma^2),$$

where  $\mathbf{x}, \beta \in \mathbb{R}^p$ .

Either way, this model relies on a few assumptions:

- a linear relationship is present
- errors are independent and identically distributed
- errors are normally distributed mean 0 and common variance  $\sigma^2$

## Regression review

Remember that linear regression is about modeling a conditional expectation, the scattering of points is noise. Interest is in

$$E(y|\mathbf{x}) = \mathbf{x}'\beta,$$

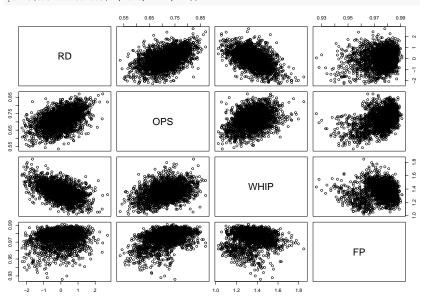
where it is important to choose the variables comprising  ${\bf x}$  and to be able to defend those choices.

#### Yes, baseball IS a game of offense, pitching, and defense.

```
summary(m)
##
## Call:
## lm(formula = RD ~ OPS + WHIP + FP, data = dat)
##
## Residuals:
##
       Min
               10 Median
                             30
                                        Max
## -1.46029 -0.21779 -0.00699 0.20934 1.48506
##
## Coefficients:
             Estimate Std. Error t value Pr(>|t|)
##
## (Intercept) 13.41760 0.79402 16.90 <2e-16 ***
## OPS 11.81943 0.15773 74.93 <2e-16 ***
## WHIP -5.44368 0.06515 -83.55 <2e-16 ***
## FP
           -14.84942 0.84580 -17.56 <2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.3513 on 2606 degrees of freedom
## Multiple R-squared: 0.787, Adjusted R-squared: 0.7868
## F-statistic: 3210 on 3 and 2606 DF, p-value: < 2.2e-16
```

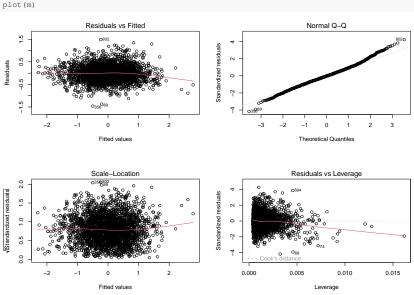
#### Linearity holds.

pairs(dat %>% select(RD, OPS, WHIP, FP))



Normality of mean-zero errors with constant variance holds. Although a slightly heavy right tail is observed in the residuals.

par(mfrow = c(2,2))
plot(m)



# The compiled fractions should be roughly 68% and 95% if errors are truly normal with common variance.

```
## # A tibble: 1 x 5

## N within_1rmse within_2rmse within_1rmse_pct within_2rmse_pct

## <int> <int> <int> <dbl> <dbl> 

481 2610 1844 2469 0.707 0.946
```

We will suppose that independence holds, or that any violations of this assumption that may be present in this data do not materially effect our overall conclusions.

A saturated model (one parameter per observation) does not fit the data better than our model with three variables and an intercept.

```
# likelihood ratio test of fitted model vs a saturated model
m_glm <- glm(RD ~ OPS + WHIP + FF, data = dat)
pchisq(m_glm$deviance, m_glm$df.residual, lower = FALSE)</pre>
```

## [1] 1

Thus we have a well-fitting simple and useful model that provides satisfactory dimension reduction.

#### Investigate large residuals

```
dat_aug %>% filter(abs(.resid) >= 1) %>%
  select(yearID, franchID, W, RD, OPS, WHIP, FP, .resid, .fitted) %>%
  mutate(across(4.9, round, 3)) %>%
  arrange(desc(.resid))
```

```
## # A tibble: 27 x 9
   vearID franchID
                                        FP .resid .fitted
##
                      W
                           RD OPS WHIP
##
     <int> <fct> <int> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl>
                                                    <dbl>
## 1 1949 NYY
                     97 1.25 0.758 1.49 0.977 1.48 -0.238
## 2
     1936 NYY
                   102 2.18 0.861 1.53 0.973
                                              1.34 0.838
     1939 NYY
                    106 2.72 0.821
                                   1.32 0.978
                                               1.29 1.43
##
##
  4
     1950 BOS
                     94 1.45 0.846 1.59 0.981
                                               1.24
                                                   0.211
##
  5
     1949 BOS
                     96 1.49 0.8
                                   1.48 0.98
                                               1.22
                                                   0.27
## 6
     1935 DET
                     93 1.68 0.798 1.44 0.979
                                               1.20 0.487
## 7 1948 BOS
                     96 1.21 0.779 1.48 0.981
                                               1.19 0.021
## 8
     1950 NYY
                     98 1.45 0.804 1.48 0.979
                                               1.12
                                                   0.329
## 9
     1943 CIN
                     87 0.422 0.653 1.34 0.98
                                               1.12 - 0.694
## 10 1914 OAK
                     99 1.45 0.693 1.27 0.966
                                               1.10
                                                   0.349
## # with 17 more rows
```

#### Investigate large fitted values

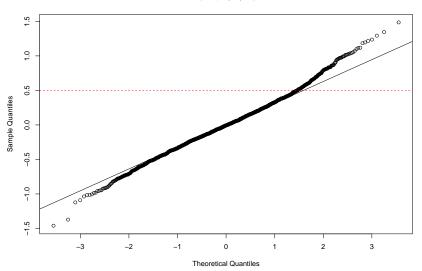
```
dat_aug %>% filter(.fitted >= 2) %>%
    select(yearID, franchID, W, RD, OPS, WHIP, FP, .resid, .fitted)
```

```
## # A tibble: 4 x 9
  yearID franchID
                                           FP .resid .fitted
                           RD
                               OPS
                                    WHIP
##
     <int> <fct>
                  <int> <dbl> <dbl> <dbl> <dbl> <dbl>
                                                     <dbl>
## 1 1927 NYY
                                                      2.21
                    110 2.44 0.870 1.30 0.969 0.231
    2019 HOU
                    107 1.73 0.848 1.13 0.988 -0.886
## 2
                                                      2.61
## 3 2019 TAD
                    106 1.69 0.810 1.10 0.982 -0.722
                                                      2.41
## 4 2020 LAD
                    43 2.27 0.821 1.06 0.982 -0.518
                                                      2.79
```

#### A closer look at problems with fit

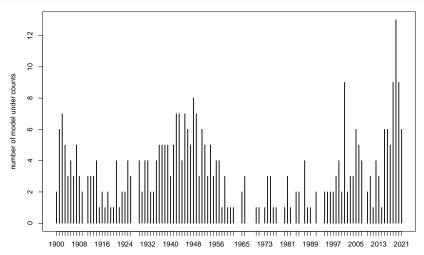
```
qqnorm(resid(m)); qqline(resid(m))
abline(a=0.5, b=0, lty = 2, col = "red")
```

Normal Q-Q Plot



#### A closer look at problems with fit

```
plot(table(dat_aug %>% filter(abs(.resid) >= 0.5) %>%
  pull(yearID)), ylab = "number of model under counts")
```



#### League conditions change over time

