## Data manipulations and linear regression

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This lecture is meant to supplement Chapter 2 in your textbook. We present a brief overview of linear regression.

## The dplyr package within tidyverse

dplyr provides comprehensive tools for data manipulations (or wrangling). The main "verbs" are:

- select (): choose from a subset of the columns
- filter(): choose a subset of the rows based on logical criteria
- arrange (): sort the rows based on values of the columns.
- mutate(): add or modify the definitions of the column, and create columns that are functions of existing columns.
- summarize(): collapse a data frame down to a single row (per group) by aggregating vectors into a single value. Often used in conjunction with group\_by()
- left\_join(): add columns from one data set to another, matching observations based on keys.

## The pipe operator

The pipe operator %>% allows for verbs to be strung in succession so that complicated manipulations can be combined within a single easily digestible sentence.

```
data %>%
  inner_function() %>%
  outer_function()
```

## Example: Runs differential regression

```
library (tidyverse)
library (Lahman)
data (Teams)
head (Teams, 3)
     yearID lqID teamID franchID divID Rank G Ghome
                                                       W
                                                           L DivWin WCWin LqWin
## 1
       1871
              NA
                     BS1
                              BNA
                                   <NA>
                                            3 31
                                                    NA 20 10
                                                                <NA>
                                                                      <NA>
                                                                                N
## 2
       1871
              NA
                    CH1
                              CNA
                                   <NA>
                                            2 28
                                                    NA 19
                                                                <NA>
                                                                      <NA>
                                                                                M
## 3
       1871
                    CL1
                                            8 29
                                                    NA 10 19
              NA
                              CFC
                                   <NA>
                                                                <NA>
                                                                      <NA>
                       H X2B X3B HR BB SO SB CS HBP SF
     WSWin
                 AB
                                                         RA
                                                                  ERA CG SHO
## 1
      <NA> 401 1372 426
                          70
                             37
                                  3 60 19 73 16
                                                  NA NA 303 109 3.55 22
## 2
      <NA> 302 1196 323
                         52
                              21 10 60 22 69 21
                                                  NA NA 241
                                                             77 2.76 25
      <NA> 249 1186 328
                          35
                              40
                                 7 26 25 18
                                              8
                                                  NA NA 341 116 4.11 23
     IPouts
            HA HRA BBA SOA
                               E DP
                                        FP
                                                               name
## 1
        828 367
                     42
                          23 243 24 0.834
                                              Boston Red Stockings
## 2
        753 308
                      2.8
                          22 229 16 0.829 Chicago White Stockings
## 3
        762 346
                     53
                          34 234 15 0.818
                                           Cleveland Forest Citys
##
                              park attendance BPF PPF teamIDBR teamIDlahman45
              South End Grounds I
## 1
                                            NA 103
                                                             BOS
                                                                             BS1
##
          Union Base-Ball Grounds
                                            NA 104 102
                                                             CHI
                                                                            CH1
   3 National Association Grounds
                                               96 100
                                                             CLE
                                                                            CL1
                                            NΑ
     teamIDretro
## 1
             BS1
## 2
             CH1
## 3
             CL1
```

```
Teams %>%
   select (yearID, franchID, W, L, G, AB, H, X2B, X3B, HR, BB, HBP, SF,
                HA, HRA, BBA, SOA, IPouts, FP, R, RA) %>%
   filter(vearID >= 1900) %>%
   replace na(list(HBP = 0, SF = 0)) %>%
   mutate(RD = (R - RA) / G, X1B = H - (X2B + X3B + HR)) %>%
   arrange(desc(RD)) %>%
   head (10)
     yearID franchID W L G AB
                                      H X2B X3B HR BB HBP SF
##
                                                               HA HRA BBA
                NYY 106 45 152 5300 1521 259 55 166 701
## 1
       1939
                                                         0 0 1208 85 567
## 2
       1927
                NYY 110 44 155 5347 1644 291 103 158 635
                                                       0 0 1403 42 409
## 3
      1902
               PIT 103 36 141 4926 1410 189 95 18 372
                                                       64 0 1142
                                                                   4 250
## 4
       2020
             LAD 43 17 60 2042 523 97 6 118 228
                                                       30 12 424 66 145
## 5
       1936
                NYY 102 51 155 5591 1676 315 83 182 700
                                                        0 0 1474 84 663
## 6
      1906
                CHC 116 36 154 5018 1316 181 71 20 448
                                                       45 0 1018 12 446
## 7
       2022
                LAD 111 51 162 5526 1418 325 31 212 607
                                                       56 53 1114 152 407
                NYY 94 59 155 5608 1667 277 78 155 748
## 8
      1931
                                                       0 0 1461 67 543
## 9
      1937
                NYY 102 52 157 5487 1554 282 73 174 709 0 0 1417 92 506
## 10
      1942
                NYY 103 51 154 5305 1429 223 57 108 591 0 0 1259 71 431
      SOA IPouts
##
                   FP
                         R RA
                                    RD X1R
## 1
      565
            4044 0.978 967 556 2.703947 1041
## 2
      431
           4167 0.969 975 599 2.425806 1092
           3794 0.958 775 440 2.375887 1108
## 3
      564
## 4
      517
           1616 0.982
                      349 213 2.266667 302
## 5
      624
           4200 0.973 1065 731 2.154839 1096
```

4165 0.969 704 381 2.097403 1044

4354 0.986 847 513 2.061728 850

4230 0.972 1067 760 1.980645 1157

4188 0.972 979 671 1.961783 1025

4125 0.976 801 507 1.909091 1041

## 6

## 7

## 9

## 10

702

1465

686

652

558

```
dat = Teams %>%
    select (yearID, franchID, W. L. G. AB, H. X2B, X3B, HR, BB, HBP, SF,
                 HA, HRA, BBA, SOA, IPouts, FP, R, RA) %>%
    filter(yearID >= 1900) %>%
    replace na(list(HBP = 0, SF = 0)) %>%
    mutate(RD = (R - RA) / G, X1B = H - (X2B + X3B + HR)) %>%
    mutate(OBP = (H + BB + HBP) / (AB + BB + HBP + SF)) %>%
    mutate(SLG = (X1B + 2*X2B + 3*X3B + 4*HR)/AB) %>%
    mutate(OPS = OBP + SLG) %>%
    mutate(WHIP = 3*(HA + BBA)/IPouts) %>%
    mutate(FIP = 3*(13*HRA + 3*BBA - 2*SOA)/IPouts)
```

WHTP

```
head (dat, 3)
## vearID franchID W L G AB H X2B X3B HR BB HBP SF HA HRA BBA SOA
## 1 1900
              TAD 82 54 141 4860 1423 199 81 26 421 81 0 1370 30 405 300
## 2 1900
              ATT. 66 72 142 4952 1403 163 68 48 395 45 0 1263 59 463 340
## 3 1900
            CHC 65 75 146 4907 1276 202 51 33 343 65 0 1375 21 324 357
                              RD X1B
                                           OBP
## TPouts
             FP R RA
                                                    SLG
                                                             OPS
## 1 3677 0.948 816 722 0.6666667 1117 0.3590078 0.3831276 0.7421354 1.448191
## 2 3721 0.953 778 739 0.2746479 1124 0.3418027 0.3727787 0.7145813 1.391561
## 3 3813 0.933 635 751 -0.7945205 990 0.3168391 0.3421643 0.6590034 1.336743
##
         FIP
## 1 0 8199619
```

## 2 1.1900027 ## 3 0.4177813 **Note**: other packages may contain functions with the same name as those in dplyr. For example, the MASS package also contains a select function.

In the event that you have both dplyr and MASS loaded in an R session, you can access dplyr's select function using dplyr::select

Baseball is a game of offense, pitching, and defense. Let's see how well runs differential per game is explained by:

- ► OPS: on base percentage plus slugging percentage
- ▶ WHIP: walks and hits allowed divided by innings pitched
- ► FP: fielding percentage

using a linear regression model

```
m = 1m(RD \sim OPS + WHIP + FP, data = dat)
```

## Regression review

Regression model:

$$y = \beta_1 x_1 + \cdots + \beta_p x_p + \varepsilon; \qquad \varepsilon \sim N(0, \sigma^2),$$

where we usually specify a model intercept by setting  $x_1 = 1$ .

Can also write in vector notation:

$$y = \mathbf{x}'\beta + \varepsilon; \qquad \varepsilon \sim N(0, \sigma^2),$$

where  $\mathbf{x}, \beta \in \mathbb{R}^p$ .

Either way, this model relies on a few assumptions:

- a linear relationship is present
- errors are independent and identically distributed
- errors are normally distributed mean 0 and common variance  $\sigma^2$

## Regression review

Remember that linear regression is about modeling a conditional expectation, the scattering of points is noise. Interest is in

$$E(y|\mathbf{x}) = \mathbf{x}'\beta,$$

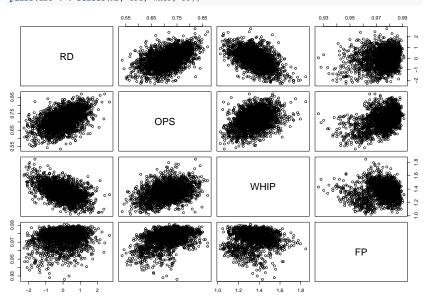
where it is important to choose the variables comprising  ${\bf x}$  and to be able to defend those choices.

#### Yes, baseball IS a game of offense, pitching, and defense.

```
summary (m)
##
## Call:
## lm(formula = RD ~ OPS + WHIP + FP, data = dat)
##
## Residuals:
## Min 10 Median 30
                                   Max
## -1.4707 -0.2169 -0.0061 0.2103 1.4758
##
## Coefficients:
             Estimate Std. Error t value Pr(>|t|)
##
## (Intercept) 13.71282 0.78206 17.53 <2e-16 ***
        11.79734 0.15538 75.92 <2e-16 ***
## OPS
## WHIP -5.40521 0.06403 -84.42 <2e-16 ***
## FP
           -15.19191 0.83208 -18.26 <2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.3484 on 2636 degrees of freedom
## Multiple R-squared: 0.7891, Adjusted R-squared: 0.7889
## F-statistic: 3288 on 3 and 2636 DF, p-value: < 2.2e-16
```

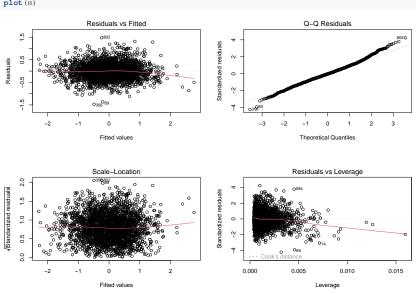
### Linearity holds.

pairs(dat %>% select(RD, OPS, WHIP, FP))



# Normality of mean-zero errors with constant variance holds. Although a slightly heavy right tail is observed in the residuals.

par(mfrow = c(2,2))
plot(m)



# The compiled fractions should be roughly 68% and 95% if errors are truly normal with common variance.

We will suppose that independence holds, or that any violations of this assumption that may be present in this data do not materially effect our overall conclusions.

A saturated model (one parameter per observation) does not fit the data better than our model with three variables and an intercept.

```
# likelihood ratio test of fitted model vs a saturated model
m_glm = glm(RD ~ OPS + WHIP + FP, data = dat)
pchisq(m_glm$deviance, m_glm$df.residual, lower = FALSE)
## [1] 1
```

Thus we have a well-fitting simple and useful model that provides satisfactory dimension reduction.

### Investigate large residuals

```
dat aug %>% filter(abs(.resid) >= 1) %>%
   select(yearID, franchID, W, RD, OPS, WHIP, FP, .resid, .fitted) %>%
   mutate(across(4:9, round, 3)) %>%
   arrange (desc (.resid))
## Warning: There was 1 warning in `mutate()`.
## i In argument: `across(4:9, round, 3)`.
## Caused by warning:
## ! The `...` argument of `across()` is deprecated as of dplyr 1.1.0.
## Supply arguments directly to `.fns` through an anonymous function instead.
##
    # Previously
##
##
   across(a:b, mean, na.rm = TRUE)
##
##
    # Now
## across(a:b, \(x) mean(x, na.rm = TRUE))
## # A tibble: 26 x 9
## vearID franchID
                      W RD OPS WHIP FP .resid .fitted
##
    <int> <fct> <int> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl>
## 1 1949 NYY
                    97 1.24 0.758 1.49 0.977 1.48 -0.237
## 2 1936 NYY 102 2.15 0.861 1.53 0.973 1.32 0.84
## 3 1939 NYY 106 2.70 0.821 1.32 0.978 1.28 1.42
                     94 1.45 0.846 1.59 0.981 1.24 0.213
## 4 1950 BOS
## 5 1949 BOS
                     96 1.48 0.8 1.48 0.98 1.21 0.269
## 6 1948 BOS
                     96 1.21 0.779 1.48 0.981 1.19 0.02
## 7 1935 DET
                     93 1.67 0.798 1.44 0.979
                                               1.19 0.485
## 8 1943 CIN 87 0.419 0.653 1.34 0.98 1.12 -0.697
## 9 1950 NYY
                     98 1.44 0.804 1.48 0.979 1.11 0.328
## 10 1938 DET
                     84 0.432 0.768 1.59 0.976
                                               1.07 - 0.634
## # i 16 more rows
```

### Investigate large fitted values

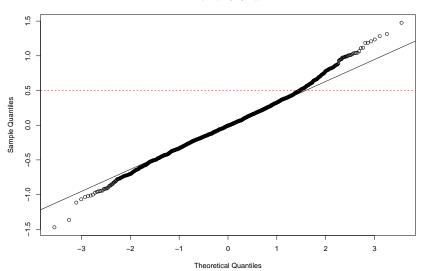
```
dat_aug %>% filter(.fitted >= 2) %>%
    select(yearID, franchID, W, RD, OPS, WHIP, FP, .resid, .fitted)
## # A tibble: 5 x 9
## vearID franchID W RD OPS WHIP FP .resid .fitted
```

```
yearID franchID
                            RD
                                 OPS
                                     WHIP
                                             FP .resid .fitted
##
     <int> <fct>
                   <int> <dbl> <dbl> <dbl> <dbl> <dbl>
                                                <dbl>
                                                         <dbl>
## 1
     1927 NYY
                     110 2.43 0.870 1.30 0.969 0.221
                                                         2.20
## 2
     2019 HOU
                     107 1.73 0.848 1.13 0.988 -0.868
                                                        2.60
## 3
     2019 LAD
                     106 1.69 0.810 1.10 0.982 -0.705
                                                        2.39
## 4 2020 LAD
                     43 2.27 0.821 1.06 0.982 -0.500
                                                        2.77
## 5 2022 LAD
                     111 2.06 0.775 1.05 0.986 -0.152
                                                        2.21
```

### A closer look at problems with fit

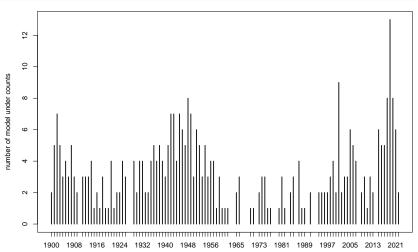
```
qqnorm(resid(m)); qqline(resid(m))
abline(a=0.5, b=0, lty = 2, col = "red")
```

Normal Q-Q Plot



### A closer look at problems with fit

```
plot(table(dat_aug %>% filter(abs(.resid) >= 0.5) %>%
  pull(yearID)), ylab = "number of model under counts")
```



### League conditions change over time

