Spare of an integer must be even. Proof CI) let a E N Dedinition CII) let x = 2a+1 Definition of odl (TIL)  $x^2 = (2\alpha + 1)^2$  Algebra  $x^2 = 4\alpha^2 + 4\alpha + 1$  Definition of of  $x = 4\alpha^2 + 4\alpha + 1$ Thus if x is odd sois - x2 Thus if x is even x is even TP > to #istrac Contradiction proofs require two contradicting pieces of evidence; you need to show x^2 is

and isn't even

Proveby Induction

3. P: YNEN, JMEN, N3+2n=3M P: \( \frac{1}{2} + 2i = 3m\) (1) A Ei'tzi Primise (111) 3 definition of sub & (IV) 3.1 Math CV) 3M Substitute M=1 Conclusion

STEPS (I) - (V) show that IP is true

for M=1

Step 2: Induction Hypothesis

I at M=4 for M=1 Let M=K Jassume K (-ii3+zi)=3k Step 3: Industion step  $P_{i=2}^{m}$   $C_{i}^{2} + V_{i}^{2} = 3m$  for M = k+1  $\sum_{i=1}^{k} C_{i}^{3} + V_{i}^{2} = 3$   $C_{i}^{2} = C_{i}^{3} + V_{i}^{2} = 3m$   $C_{i}^{2} = 2m$   $C_{i}^{3} + V_{i}^{2} = 3m$   $C_{i}^{2} = 2m$   $C_{i}^{3} + V_{i}^{2} = 3m$   $C_{i}^{3} = 2m$   $C_{i}^{3} + V_{i}^{2} = 3m$   $C_{i}^{3} = 2m$   $C_{i}^{3} = 2m$  CII) K+1  $1 \times 1$   $1 \times 1$  1

K3+3K+1 + ZK+2 CIII) E Li3+2i) + (1(K+1)3+(2.(K+1)) (IV)7k+3K+ k3+1+2K+2 Induction k3+6K+2K+3 K3+8K+3 JM=K+1 False Although buse case is true the induction did Not poss because  $m \neq K+1$  thus to 1s false for all NEN and MEN

Prove by induction 4.1P: Vn EN, a = 1, a + 1, a + a + 1 -1 Let a= 2 Let n=1 17: Vn = N, a + 1, 2 a = a + 1 - 1 (1) = (2) Premise (II) E (Z) Sub n=1 (皿) 2=2 (IV) substitue 12h Stips CID-CVD proves is not true for N=1. induction fails is true. See myself or Dr. Kandel for guidance on this problem