

## CS 332, M02.3: Finite State Machines, Practice Problems

1. Use this to practice making FSM's. Given  $\Sigma = \{ a, b \}$ , create the machine  $M$  for:

- (a)  $L_1 = a^*$
- (b)  $L_2 = (aba)^*$
- (c)  $L_3 = (bb)^*$
- (d)  $L_4 = (bb)^*aa(bb)^*$
- (e)  $L_5 = aaaaaa^*b^*bb$
- (f)  $L_6 = a^* + b^*$
- (g)  $L_7 = a^*b^* + b^*a^*$
- (h)  $L_8 = a^+b^+a^+$
- (i)  $L_9 = a(a+b)^*a$
- (j)  $L_{10} = (a+b)^+bbb$
- (k)  $L_{11} = a(a+b)^*a(a+b)^*a$
- (l)  $L_{12} = (a+b)^*aa + (a+b)^*bb$

2. Let  $L$  be the language of strings containing only pairs of  $a$ 's or  $b$ 's for alphabet  $\Sigma = \{a, b\}$ . For example,  $aabbaabbaa$ ,  $bbbbbb$ ,  $aaaabb$  and  $bbbbaa$  are all in  $L$ , while  $aba$ , and  $bbbaa$  are not in  $L$ .  $L$  does not include zero length strings, so at least one  $aa$  or  $bb$  pair must be present. The regular expression for  $L = (aa \text{ OR } bb)^+$ , which is more correctly written as  $L = (aa + bb)^+$ .

- (a) (10) Draw the machine,  $M$ , that corresponds to  $L$ .
- (b) (10) Define the machine  $M$  in terms of  $S$ ,  $\Sigma$ ,  $q_0$ ,  $\delta$ , and  $F$ .