

# # A Priori Analysis

1/5<sup>2k</sup>

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## 1 Assignment.

1)  $i = n$

while  $i > 2$ ;  
 $i = i^{1/25}$

print(i)

Find Time Complexity = ?

2)  $i = 29$

while  $i < n$ ;  
 $i = i^{23}$

Find Time Complexity = ?

3)  $i = 1$

while  $i < n$ ;

$i = 2 \times i$

$i = 3 \times i$

Find Time Complexity = ?

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①  $i = n$

while  $i > 2$ ;

$i = i^{1/25}$

print(i)

$i = n$

$n^{1/25}$

$n^{1/25^2}$

$n^{1/25^3}$

$i \rightarrow k \text{ times}$

$n^{1/25^k} = 2$

$\Rightarrow n^{1/25^k} = 2$

$\log_2 n^{1/25^k} = \log_2 2$

$\frac{1}{25^k} \log_2 n = 1$

$\log_2 n = 25^k$

$\log_{25}(\log_2 n) = \log_{25} 25^k$

$$\log_{25} (\log_2 n) = k \log_{25} 25$$

$$\Rightarrow \log_{25} (\log_2 n) = k \quad [\because \log_{25} 25 = 1]$$

$$\text{Time Complexity} = O(\log(\log n))$$

2.

$$i = 29$$

$$\text{while } i < n;$$

$$i = i^{23}$$

$$\Rightarrow (29)^{23^1}$$

$$\Rightarrow (29)^{23^2}$$

$$\Rightarrow (29)^{23^k} = n$$

$$29^{23^k} = n$$

$$\log_n (29)^{23^k} = \log_n n$$

$$\log_n (29)^{23^k}$$

$$23^k \log_n 29 = 1$$

$$\log_n 29 = \frac{1}{23^k}$$

$$\log_{23} \log_n 29 = \log_{23} \frac{1}{23^k}$$



③  $i = 1$

while  $i < n$ ;

$\begin{cases} i = 2 * i \\ i = 3 * i \end{cases}$

$\rightarrow i = 6 * i$

$1 < 50$

$i = 2 \times 1 = 2 \Rightarrow i = 6 \times 1$

$i = 3 \times 2 = 6 = 6$

$6 < 50$

$i = 2 \times 6 = 12 \quad i = 6 \times 6$

$i = 3 \times 12 = 36 = 36$

Whenever we multiplying  $i$  by any value, the time complexity will be  $\Rightarrow \log_n$  (multiplicative)

here we are multiplying by 6 so the time complexity will be.

$\Rightarrow \log_6 n$