

1 | Exercise

I started by creating a data type for interpreting *Stlc* terms that rightfully covers the type checking patterns of lambda-calculus.

The `evaluation` function takes a *Stlc* term, an integer (or gas) and returns a new type: `String | (Stlc, Int)`. To this effect, I instantiated the following data type:

```
data MaybeTerm = Message String | Term (Stlc, Int)
```

1.1 Type Checking

The type checking is done over the `eval` function that has the following type:

```
eval :: [Context] -> Stlc -> Maybe Type
```

The *typing contexts* Γ is captured as a list of `CONTEXTs`, where each of the latter corresponds to a character being associated with a `TYPE`.

```
data Context = Env Char Type
```

To implement the types described in the assignment, which are needed for typed abstractions, I defined the following data type:

```
data Type = TypeInt | TypeFloat | TypeUnit | TypeFunction Type Type
```

1.2 Reduction

The most valued function in *Stlc* reduction is the β -reduction, that tries to replace a variable x from an abstraction for the term under a `TAPP`.

1.3 Notes

To implement floating values, I added an *Stlc* term to refer to those: the `TFLOAT` constructor, which requires a value of type `float`. Adding `(T-ADD)` directly a `TFLOAT` to a `TINT` will cause an exception (*Maybe* type); however, I created additional type constructors, that allows the conversion between `TFLOAT` and `TINT`:

```
TFromFloat Stlc | TFromInt Stlc
```

The *call-by-value* for these terms use functions to allow conversion between types `INT` and `FLOAT`, that are then wrapped in either the `TINT` or `TFLOAT` constructor, respectively. For instance, the type checking for `TFROMINT` is as follows:

```
eval c (TFromInt term) =  
  case eval c term of  
    Just TypeInt -> Just TypeFloat  
    -             -> Nothing
```

The most intriguing task was to understand how to use the *call-by-value* within `CONTEXT`. I was not quite sure on how `T-APP` and `T-ADD` would work on such situations.